#### CS 302 – Assignment #10

Purpose: Learn concepts regarding basic graph data structures and shortest path algorithms.

Due: Wednesday  $(11/14) \rightarrow$  Must be submitted on-line before class.

Points: Part A  $\rightarrow$  75 pts, Part B  $\rightarrow$  50 pts

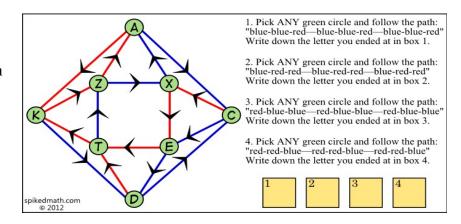
### Assignment:

#### Part A:

Design and implement a C++ class, *graphAlgoritms*, to implement a topological sort<sup>1</sup> using Kahn's algorithm and Dijkstra's single source shortest path algorithm<sup>2</sup>. *Note*, this class may be expanded and updated on future assignments.

In addition, Dijkstra's single source shortest path algorithm will use the priority queue object from a previous assignment.

A main will be provided that performs a series of tests. Refer to the UML descriptions for implementation details.



#### Part B:

Create and submit a brief write-up including the following:

- Name, Assignment, Section.
- Summary of adjacency list and adjacency matrix data structures. Include the trade-offs associated with dense and sparse matrices.
- Note some applications for the topological sort shortest and shortest path algorithms.
- Big-O for the topological sort and Dijkstra's single source shortest path algorithms.

#### **Submission:**

- Submit a compressed zip file of the program source files, header files, and makefile via the on-line submission by 23:50.
- Submit a copy of the write-up (PDF format).

All necessary files must be included in the ZIP file. The grader will download, uncompress, and type **make**. You must have a valid, working *makefile*.

It should be noted that there are many variations on both these algorithms. These are the algorithms that must be implemented. Copying code from the net or another student will result in a zero for the assignment and referral to the Office of Student Conduct.

- 1 For more information, refer to: http://en.wikipedia.org/wiki/Topological\_sorting
- 2 For more information, refer to: http://en.wikipedia.org/wiki/Dijkstra's\_algorithm

### **Class Descriptions**

• <u>Graph Algorithms Class</u> The graph algorithms class will implement functions specified below.

```
graphAlgorithms
-vertexCount: int
-title: string
-graphMatrix: **int
-dist: *int
-prev: *int
-topoNodes: *int
-topoCount: int
+graphAlgorithms(int=5)
+~graphAlgorithms()
+newGraph(int): void
+addEdge(int, int, int): void
+readGraph(const string): bool
+getVertexCount() const: int
+printMatrix() const: void
+topoSort(): void
+dijkstraSP(int): void
+printPath(const int, const int) const: void
-showPath(const int) const: void
+getGraphTitle() const: string
+setGraphTitle(const string): void
+printDistances(const int) const: void
-destroyGraph(): void
+getArgs(int, char *[], bool &, string &, int &,
                                    int &, bool &): bool
```

#### **Function Descriptions**

- The *graphAlgorithms()* constructor should initialize the class variables (0, "", or NULL as appropriate). If a vertex count is passed, it must be  $\geq 5$ . If not, an error should be displayed (and no memory allocated). If the vertex count is  $\geq 5$ , the *newGraph()* function should be called to allocate and initialize the adjacency matrix.
- The ~*graphAlgorithms()* destructor should call the *destroyGraph()* function to delete the dynamically allocated memory. This includes the adjacency matrix, distances array, previous array, and the topological sort array. Additionally, reset all variables.
- The *newGraph()* function should allocate and initialize the adjacency matrix to all 0's. This function should call the *destroyGraph()* function before allocating memory to ensure there are no memory leaks.
- The *getGraphTitle()* function should return the current graph title.
- The *setGraphTitle()* function should set the graph title, over-writing any previous title.
- The *printMatrix()* function should print the current adjacency matrix in a formatted manner. This is primarily used for testing. See example output for formatting.
- The *getVertexCount()* function should return the current vertex count.

- The *getArgs()* function accept and validate the command line arguments. The arguments include the testing flag ("-t", bool), the graph file name ("-gf <fileName>" string), the source node ("-sn" <sourceNode>, integer), destination nodes ("-dn" <destNode>, integer), and optionally the show matrix flag ("-sm", bool). If no arguments are entered, a basic usage message should be displayed. The function should accept "-t" as the only argument which should set the testing flag to true (false otherwise). If the "-t" is not included the "-gf", "-sn", and "-dn" are required. The "-sm" is optional. Refer to the example executions for argument handling.
- The *addEdge()* function should add an edge to the adjacency matrix. The function will expect the *from* vertex, the *to* vertex, and the weight (in that order). The function must ensure the two passed vertexes are valid (≤ *vertexCount*) and not equal. If not valid, an error should be displayed and nothing changed in the adjacency matrix. Refer to the example execution for output formatting.
- The *readGraph()* function should read a formatted graph file. The file will include a title, the vertex count, and a series of lines for the edges. The edge lines will include the *from* vertex, the *to* vertex, and the weight (in that order). The function must verify that the vertex count is ≥ 5. If not, an error message should be displayed and no memory allocated. Otherwise, the function should create a new graph by calling the *newGraph()* function and adding each edge to the adjacency matrix by calling the *addEdge()* function.
- The *topoSort()* function should perform a topological sort on the current graph. The function should implement Kahn's algorithm which stores the nodes in the *topoNodes[]* array and updates the *topoCount*. The algorithm is outlined in the topological sort section. When completed, the function should display the *topoNodes[]* array contents.
- The *dijkstraSP()* function should implement Dijkstr's Algorithm to find the shortest path from the passed source node to each node in the graph. The function should ensure the passed source node is valid, and if not display an error message and return. The results should be placed in the dynamically allocated *dist[]* array and the *prev[]* array updated. The distance from a node to itself is 0 by definition. The function should use the Dijkstra's Shortest Path with adjacency matrix and priority queue algorithm as outlined in the assignment and in class. The last step would be to call the *printDistances()* function to display the final results.
- The *printDistances()* function should print the shortest paths from the passed source node to each node as contained in the distances array (as set in the *dijkstraSP()* function) and the previous node. Each field should be a size of 10 (i.e., **setw(10)**) If the distances array is not set, the function should display an error. See example output for formatting. The function should display "not reachable" if that vertex is not reachable in the graph from the source node.
- The *printPath()* function should print the path from source node (1<sup>st</sup> argument) to the destination node (2<sup>nd</sup> argument). *Note*, this function can only be called after the *dijkstraSP()* function with a matching source node (which is addressed in the provided main). The function should verify that the destination node is reachable, and if not display an appropriate error message. Otherwise, the function should display a header (see example output) and call the private *showPath()* function.
- The *showPath()* function should recursively print the path from the source node to the destination node. Only the destination node is passed. Must be recursive.
- The *destroyGraph()* function should delete all dynamically allocated memory and reinitialize the class variables as appropriate.

Refer to the example executions for output formatting. Make sure your program includes the appropriate documentation. See Program Evaluation Criteria for CS 302 for additional information. *Note, points will be deducted for especially poor style or inefficient coding.* 

#### Limits

The correct way to access the maximum integer is to use the C++ max() function as follows:

```
maxIntOnThisMachine = std::numeric limits<int>::max()
```

This requires the **#include <limits>**.

## **Dijkstra's Shortest Path Algorithm**

The following is the Dijkstra's Single Source Shortest Path Algorithm using an adjacency matrix and a minimum priority queue.

- Distances / Previous Nodes
  - dynamically create a distances array of vertex count size
  - dynamically create a previous nodes array of vertex count size
  - initialize all distances to infinite
  - initialize all elements of previous array to -1
- Priority Queue → create empty priority queue
  - value = vertex number
  - key = distance
- Insert source node
  - insert source node into priority queue
    - value = source node, key = 0
  - set distance array of source node to 0
- While priority queue is not empty
  - extract minimum distance element from priority queue
    - u = value of minimum distance element
  - iterate thought all vertexes, v, adjacent to u
    - new distance is; dist[u] + distance between u and v
    - if there is a shorter path distance to *v* from *u* (e.g., if current distance, new distance is < *dist*[*v*])
      - update dist[v] to new distance
      - set prev[v] to u
      - insert  $\mathbf{v}$  into priority queue (even if it is already there), key = new distance
- Print distance array *dist*[] and array *prev*[] to show all the shortest paths.

*Note*, the minHeap can be modified to accommodate both the vertex and the distance.

#### **Topological Sort:**

The following algorithm outlines a depth first search approach for performing a topological sort on a graph. The topological sort algorithm is as follows:

- Perform initializations
  - create in-degree array and initialize all elements to 0
  - create topo[] nodes array and initialize all elements to 0
  - initialize topo count to 0
- Compute in-degree for each vertex in graph
- En-queue each vertex with an in-degree of 0
- While queue is not empty
  - remove a vertex from queue
    - decrease in-degree by 1 for all of it neighbors
    - if in-degree of a neighbor is reduced to 0, add to queue.

The topo[] nodes array holds the topological sort.

## **Example:**

For example, given graph1.txt

## Graph 0 Simple Example

1 4 10 1 3 3 3 4 2

3 6 4

3 5 8 3 2 2

2 5 5

2 6 4 4 6 6

6 5 1

The adjacency matrix would be as follows:

## Graph Adjacency Matrix:

Graph Title: Graph 0 Simple Example

	0	1	2	3	4	5	6
0	0	2		1			
1		0		3	10		
2			0			5	4
3			2	0	2	8	4
0   1   2   3   4   5   6					0		6
5						0	
6						1	0

The adjacency matrix would be as follows:

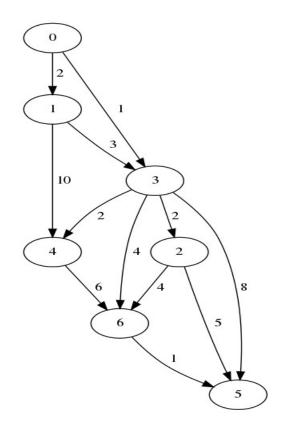
The shortest-paths would be as follows:

# Shortest Paths: From Node: 0 to:

From Node:	U to:	
Vertex	Dist	From
0	0	-
1	2	0
2	3	3
3	1	0
4	3	3
5	6	6
6	5	3

-----

Path from 0 to 5 0 - 3 - 6 - 5



#### **Example Execution:**

ed-vm%

Below is an example output for the main with the testing option selected.

```
ed-vm% ./paths -t
______
Error testing:
graphAlgorithms: Error, invalid graph size.
graphAlgorithms: Error, invalid graph size.
newGraph: Error, invalid graph size.
newGraph: Error, invalid graph size.
addEdge: error, invalid vertex.
addEdge: error, invalid vertex.
addEdge: error, invalid vertex.
addEdge: error, vertex to and from can not be the same.
topoSort: Error, no graph data.
printMatrix: Error, no graph data.
dijkstra: Error, no graph data.
dijkstra: error, invalid source.
*************************
Game Over, thank you for playing.
ed-vm%
Below are some example outputs for the main using several different graph input files.
ed-vm% ./paths -gf graph1.txt -sn 0 -dn 5 -sm
CS 302 - Assignment #10
Graph Algorithms
Graph Adjacency Matrix:
   Graph Title: Graph 0 Simple Example (0 - 5)
        0 1 2 3 4 5 6
           2 -- 1 -- -- --
0 -- 3 10 -- --
  1
       -- -- 0 -- -- 5 4
  2
       -- -- 2 0 2 8 4
-- -- -- -- 0 -- 6
-- -- -- -- 0 --
  3
  4
  5 |
  6
Topological Sort:
0 1 3 2 4 6 5
Shortest Paths:
From Node: 0 to:
   m Node: 0 to:
Vertex Dist From
0 0 0 -
1 2 0
2 3 3
3 1 0
4 3 3
5 6 6 6
6 5 3
Path from 0 to 5
  0 - 3 - 6 - 5
***********************
Game Over, thank you for playing.
ed-vm%
ed-vm%
```

```
ed-vm% ./paths -gf test/graph1.txt -sn 0 -dn 5
CS 302 - Assignment #10
______
Graph Algorithms
Topological Sort:
0 1 3 2 4 6 5
Shortest Paths:
From Node: 0 to:
   Vertex Dist From
           0
2
3
1
3
                     0 3 0
      0
       1
       2
       3
              6
5
       5
                        6
       6
                        3
Path from 0 to 5
 0 - 3 - 6 - 5
********************
Game Over, thank you for playing.
ed-vm%
ed-vm% ./paths -gf graph3.txt -sn 0 -dn 9 -sm
************************************
CS 302 - Assignment #10
______
Graph Algorithms
Graph Adjacency Matrix:
  Graph Title: Graph 3 (0 - 9)
         1 2 3 4 5 6 7 8 9
     -- 0 8 -- 6 11 -- -- -- --

-- 0 0 -- 8 4 2 7 -- --

-- -- 0 -- 7 14 9 -- --
 1
 3
      -- -- -- 0 10 --
 5
     -- -- -- 0 2 4 10 --

-- -- -- 0 1 6 --

-- -- -- -- 0 7 1
  6
 7
  8
 9 İ
Topological Sort:
0 1 3 2 4 5 6 7 8 9
Shortest Paths:
From Node: 0 to:
  Vertex Dist
            0
4
      0
      1 4
2 12
3 8
4 10
5 15
6 14
7 15
8 19
9 16
                    0
1
0
                        4
```

Path from 0 to 9

0 - 1 - 2 - 6 - 7 - 9

Game Over, thank you for playing. ed-vm%

Graph Algorithms

Graph Adjacency Matrix:

Graph Title: Larger Graph (0 - 49)

#### Topological Sort:

0 1 3 4 8 9 25 2 11 42 6 10 16 5 12 13 19 20 7 21 26 22 24 17 14 23 29 27 34 15 28 30 36 18 33 40 31 32 45 35 41 37 38 39 43 44 46 48 47 49

## Shortest Paths:

From Node: 0 to:

Houe.	•		
<i>l</i> ertex		Dist	From
0		0	_
1		not	reachable
2		3	0
3		not	reachable
4		not	reachable
5		38	2
6		not	reachable
7		1	0
8		not	reachable
9		not	reachable
10		not	reachable
11		not	reachable
12		6	2
13		not	reachable
14		19	7
15		34	14
16		not	reachable
17		not	reachable
18		34	14
19		not	reachable
20		not	reachable
21		19	12
22		not	
23		42	21
24		77	5
25		not	reachable
26		23	12
27		110	24
28		95	29
29		50	26
30		80	29
31		46	21
32		53	18
33		90	23
34		68	21
35		86	32
36		83	34

```
37
        86
       93
38
                 30
       92
121
39
                 32
40
                 36
      92
41
                 32
       not reachable
42
       134
43
                 37
44
       143
                 38
            38
34
39
46
33
46
45
       118
46
       109
47
       130
48
       124
49
       116
```

-----

Path from 0 to 49 0 - 7 - 14 - 18 - 32 - 39 - 46 - 49

\*

Game Over, thank you for playing. ed-vm% ed-vm%

*Note*, the font size was changed on the matrix output only on this PDF for formatting purposes.