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Assignment #2

CS 302 – 1004

1. Formal definitions:

- a. Big Oh – Notation for upper bound (worst case) to its growth rate of $f(n)$

$T(N) = O(f(N))$, if there are positive constant C and no Such that

$$T(N) \leq C.$$

- b. Big Ω - Notation for lower bound (best case) to its growth rate of $f(n)$

$T(N) = \Omega(g(N))$, if there are positive constants C and no such that

$$T(N) \leq C \cdot g(N), \text{ when } N \geq n$$

- c. Big Θ - Notation for, when the upper bound and lower bound are the same within a constant factor.

$$T(N) = \Theta(n(N)), \text{ if and only if } T(N) = O(h(N))$$

$$\text{when } T(N) = \Omega(h(N))$$

2. Shor informal description:

- a. Big Oh – Notation for upper bound (worst case) to its growth rate of $f(n)$

- b. Big Ω - Notation for lower bound (best case) to its growth rate of $f(n)$

- c. Big Θ - Notation for, when the upper bound and lower bound are the same within a constant factor.

3. Growth rate order: $\frac{2}{n}, \log n, \sqrt{n}, n \log n, 2n, 2^{\frac{n}{2}}, n^2 \log n, 2^n, n^3, 4n^2, 730$

4.

- a. Big O analysis for binary search for finding an element in sorted array is $O(\log n)$

- b. Because in Binary search there are $O(\log n)$ comparisons, where n is the number of elements in the array. For sequential search Big-Oh is $O(n)$, where n is the number of elements.

5. Big-Oh for inserting a new element in an unsorted linked list is $O(1)$

6. Big-Oh for inserting a new element in sorted linked list is $O(1)$

7. Big-Oh of an algorithm to find if a number is prime is $O(N)$

8. –

- a. $O(n^2)$
- b. $O(n^2)$

9. –

- a. $O(n \log n)$
- b. $O(n)$

10. –

- a. $O(n^2)$
- b. $O(n \log n)$
- c. $O(n)$
- d. $O(n^2)$
- e. $O(n)$
- f. $O(n^3)$
- g. $O(n^4)$
- h. $O(n^3)$
- i. $O(n^2)$

11. –

- a. Algorithm 1 - $O(n)$
- b. Algorithm 2 - $O(n)$

12. –

- a. Algorithm 1 - $O(n)$
- b. Algorithm 2 - $O(2^n)$

13. –

- a. Algorithm 1 - $O(2^n)$
- b. Algorithm 2 - $O(n)$

14. –

- a. The space/time tradeoff principle says that one can often achieve a reduction in time if one is willing to sacrifice space or vice versa.
- b. Example of space/time tradeoff is a lookup table.

15. –

- a. Big-Oh for recursive algorithm in assignment #1 was, $O(2^n)$
- b. Big-Oh for dynamic algorithm in assignment #1 was, $O(n^2)$