

# EN 312 - Controls and Instrumentation

## Tutorial II - Signal Flow Graph

Draw the signal Flow Graphs for the tutorial block diagrams of the first tutorial and find out transfer function  $C(s)/R(s)$  using Mason's Gain Formula.

**Answers:**

Note: Answers should be the same for both block diagram reduction and signal flow graph approaches!

### PRACTICE PROBLEMS - SIGNAL FLOW GRAPH

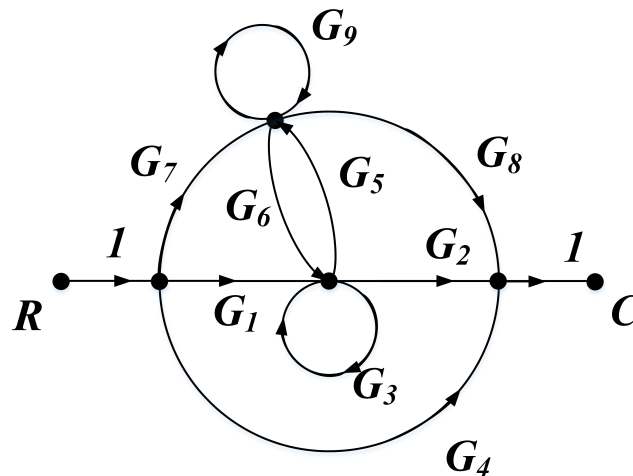
1) Draw the signal flow graph for the system of equations given below and obtain the overall transfer function  $\frac{X_6}{X_1}$  using the Masons gain formula:

$$X_2 = G_1 X_1 - H_1 X_2 - H_2 X_3 - H_6 X_6, \quad X_3 = G_1 X_1 + G_2 X_2 - H_3 X_3,$$

$$X_4 = G_2 X_2 + G_3 X_3 - H_4 X_5, \quad X_5 = G_4 X_4 - H_5 X_6$$

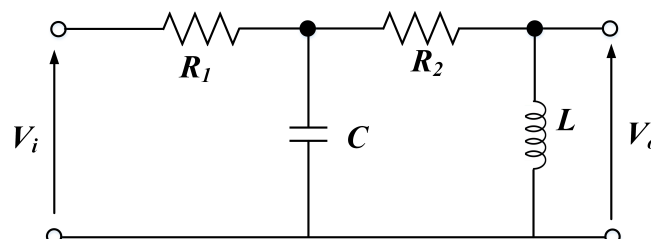
$$X_6 = G_5 X_5.$$

2) Obtain  $C(s)/R(s)$  using Mason's Gain formula (MGF):

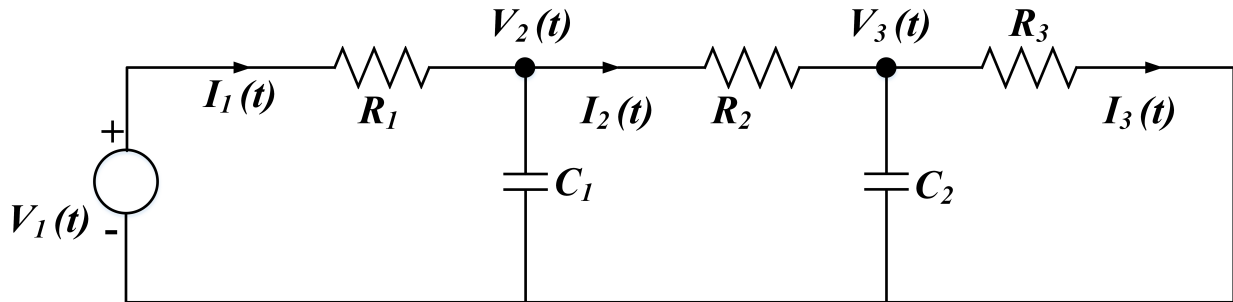


3) Find the  $T(s)$  for the given network using MGF approach:

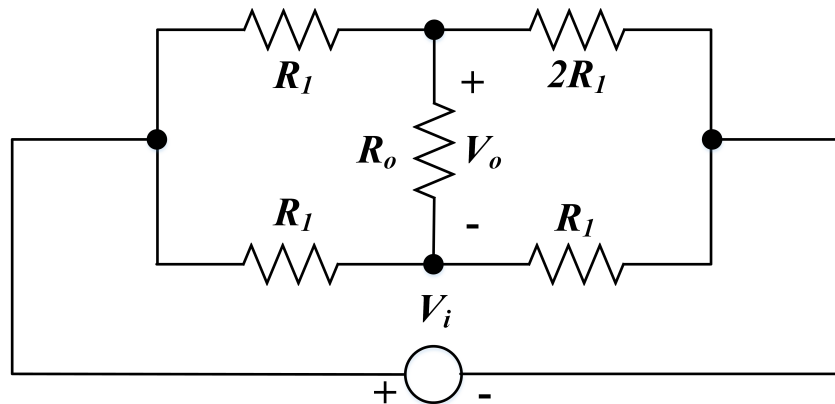
$$T(s) = V_o(s)/V_i(s).$$



4) Use MGF to determine  $I_3(s)/V_1(s)$  for the circuit, given  $R_1 = 100k\Omega$ ,  $R_2 = 50k\Omega$ ,  $R_3 = 40k\Omega$ ,  $C_1 = 10\mu F$  and  $C_2 = 5\mu F$ :



5) For the network given below obtain the transfer function  $V_o/V_i$  using Mason's gain formula (MGF):



**Answers for practice problems:**

1)  $X_6/X_1 = A/B$

where  $A = (G_1G_2G_3G_4G_5 + G_1G_3G_4G_5(1 + H_1) + G_1G_2G_4G_5(1 + H_3) - G_1G_2G_4G_5H_2)$  and  $B = 1 + G_2H_2 + G_4H_4 + G_5H_5 + G_2G_3G_4G_5H_6 + G_2G_4G_5G_6 + H_1 + H_3 + G_2G_4H_2H_4 + G_2G_5H_2H_5 + H_1G_4H_4 + G_4H_4H_3 + G_5H_1H_5 + G_5H_3H_5 + H_1H_3 + G_4H_1H_3H_4 + G_5H_1H_3H_5 + G_2G_4G_5H_3H_6$ .

2)  $C(s)/R(s) = (G_1G_2(1 - G_9) + G_4(1 - G_3 - G_6G_5 - G_9 + G_3G_9) + G_7G_8(1 - G_3) + G_7G_6G_2 + G_1G_5G_8) / (1 - G_3 - G_6G_5 - G_9 + G_3G_9)$ .

3)  $V_o(s)/V_i(s) = sL / (s^2LR_1C + S(L + R_1R_2C) + R_1 + R_2)$ .

4)  $I_3(s)/V_1(s) = 10^{-4} / (s^2 + 12s + 19)$ .

5)  $V_o(s)/V_i(s) = R_o / (6R_o + 7R_1)$ .

Please note that we (the teaching assistants) may have made a calculation error or a mistake, please feel free to get back to us if you find any discrepancy.

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