Reinforcement Learning

Dr. P. Kuppusamy Prof / CSE

Reinforcement learning

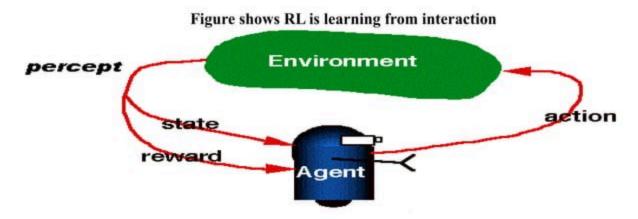
- Reinforcement Learning is the agent must sense the environment, learns to behave (act) in a environment by performing actions (reinforcement) and seeing the results.
- Task
 - Learn how to behave successfully to achieve a goal while interacting with an external environment.
 - The goal of the agent is to learn an action policy that maximizes the total reward it will receive from any starting state.
- Examples
 - Game playing: player knows whether it win or lose, but not know how to move at each step

Applications

- A robot cleaning the room and recharging its battery
- Robot-soccer
- invest in shares
- Modeling the economy through rational agents
- · Learning how to fly a helicopter
- Scheduling planes to their destinations

Reinforcement Learning Process

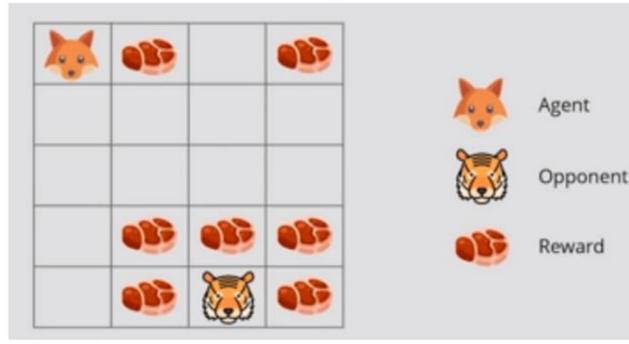
- · RL contains two primary components:
 - 1. Agent (A) RL algorithm that learns from trial and error
 - 2. Environment World Space in which the agent moves (interact and take action)
- State (S) Current situation returned by the environment
- Reward (R) An immediate return from the environment to appraise the last action
- Policy (π) –Agent uses this approach to decide the next action based on the current state
- Value (V) Expected long-term return with discount. Oppose to the short-term reward (R)
- Action-Value (Q) Similar to value except it contains an additional parameter, the current action (A)



RL Approaches

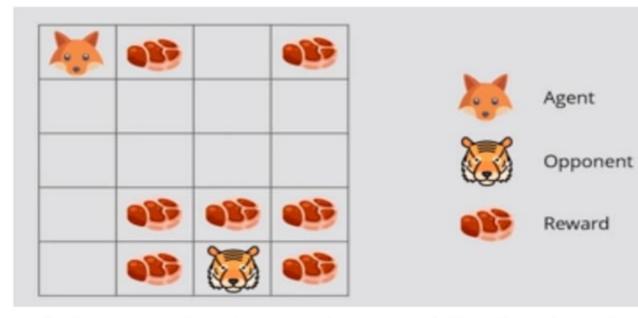
- Two approaches
 - Model based approach RL:
 - learn the model, and use it to derive the optimal policy.
 e.g Adaptive dynamic learning(ADP) approach
 - Model free approach RL:
 - derive the optimal policy without learning the model.
 - e.g LMS and Temporal difference approach
- Passive learning
 - The agent imply watches the world during transition and tries to learn the utilities in various states
- Active learning
 - The agent not simply watches, but also acts on the environment

Example



- Immediate reward is worth more than future reward.
- Reward Maximization Agent is trained to take best (optimal) action to get maximum reward

Reward Maximization



- Exploration Search and capture more information about the environment
- Exploitation Use the already known information to maximize the rewards

Reinforcement learning model

- Each percept(e) is enough to determine the State(the state is accessible)
- Agent's task: Find a optimal policy by mapping states of environment to actions of the agent, that maximize long-run measure of the reward (reinforcement)
- It can be modeled as Markov Decision Process (MDP) model.
 - Markov decision process (MDP) is a a mathematical framework for modeling decision making i.e mapping a solution in reinforcement learning.

MDP model

MDP model <S,T,A,R>



$$s_0 \stackrel{a_0}{\longrightarrow} s_1 \stackrel{a1}{\longrightarrow} s2 \stackrel{a2}{\longrightarrow} s3$$

- · S- set of states
- A set of actions
- Transition Function: T(s,a,s') = P(s'|s,a) – the probability of transition from s to s' given action a

$$T(s,a) \rightarrow s'$$

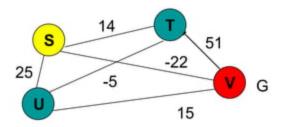
 Reward Function: r(s,a) → r the expected reward for taking action a in state s

$$R(s,a) = \sum_{s'} P(s'|s,a)r(s,a,s')$$

$$R(s,a) = \sum_{s'} T(s,a,s')r(s,a,s')$$

MDP - Example I

- Consider the graph, and find the shortest path from a node S to a goal node G.
- Set of states {S, T, U, V}
- Action Traversal from one state to another state
- Reward Traversing an edge provides "length edge" in dollars.
- Policy Path considered to reach the destination {S→T→V}



Q - Learning

values (action values) to iteratively improve the behavior of the learning agent.Goal is to maximize the Q value to find the optimal action-selection policy.

Q-Learning is a value-based reinforcement learning algorithm uses Q-

The Q table helps to find the best action for each state and maximize the expected reward.
 Q-Values / Action-Values: Q-values are defined for states and actions.

This estimation of Q(s, a) will be iteratively computed using the **TD**-

states i.e. there are no further transition possible is called **completion of an**

• Q(s, a) denotes an estimation of the action a at the state s.

episode.

Update rule.
Reward: At every transition, the agent observes a reward for every action from the environment, and then transits to another state.
Episode: If at any point of time the agent ends up in one of the terminating

Q-Learning

- Initially agent explore the environment and update the Q-Table. When the Q-Table is ready, the agent will start to exploit the environment and taking better actions.
- It is an off-policy control algorithm i.e. the updated policy is different from the behavior policy. It estimates the reward for future actions and appends a value to the new state without any greedy policy

Temporal Difference or TD-Update:

Estimate the value of Q is applied at every time step of the agents interaction with the environment
 Q(S,A) ← Q(S,A) + α(R + γQ(S',A') – Q(S,A))

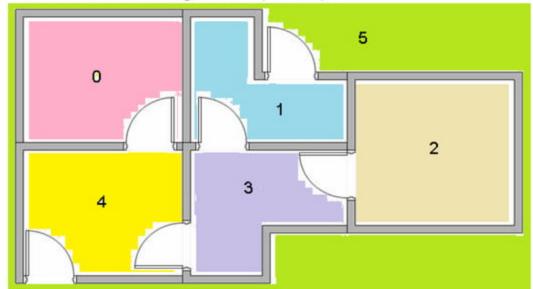
Advantage:

 Converges to an optimal policy in both deterministic and nondeterministic MDPs.

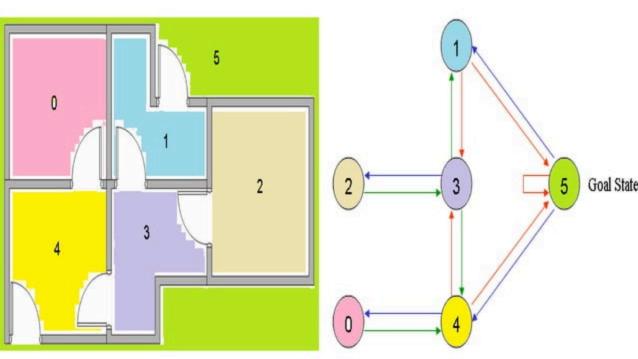
Disadvantage:

· Suitable for small problems.

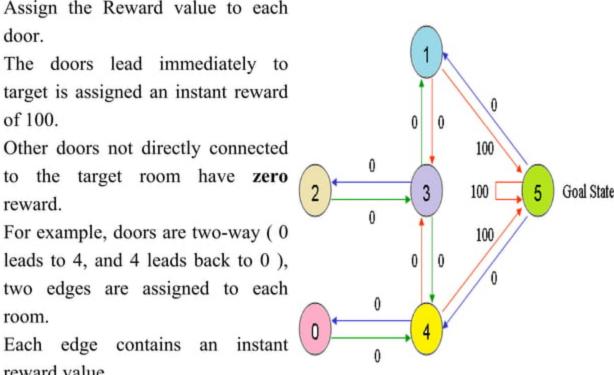
- Building Environment contains 5 rooms that are connected with doors.
- Each room is numbered from 0 to 4. The building outside is numbered as 5.
- Doors from room 1 and 4 leads to the building outside 5.
- Problem: Agent can place at any one of the rooms (0, 1, 2, 3, 4). Agent's goal is to reach the building outside (room 5).



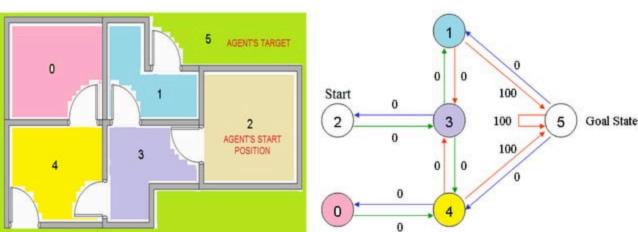
- · Represent the room in the graph.
- Room number is the state and door is the edge.



- Assign the Reward value to each door.
- The doors lead immediately to target is assigned an instant reward of 100.
- Other doors not directly connected to the target room have zero reward.
 - leads to 4, and 4 leads back to 0), two edges are assigned to each room.
- Each edge contains instant an reward value

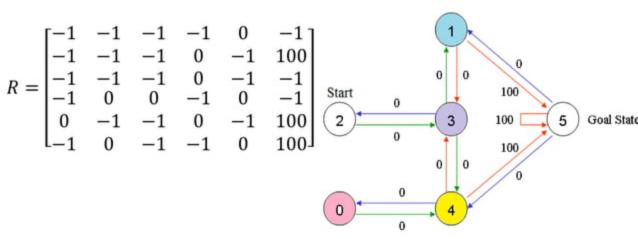


- Let consider agent starts from state s (Room) 2.
- Agent's movement from one state to another state is action a.
- Agent is traversing from state 2 to state 5 (Target).
 - Initial state = current state i.e. state 2
 - Transition State 2 → State 3
 - Transition State 3 → State (2, 1, 4)
 - Transition State 4 → State 5



Prepare rewards table R (matrix)

- · -1 denotes the no edge between the states
- · 0 represents the indirect edge to the target



Understanding the Q – Learning: Prepare matrix Q Matrix Q is the memory of the agent in which learned information

- from experience is stored.

 Row denotes the current state of the agent
- Column denotes the possible actions leading to the next state

rewards with higher edge weights.

Compute Q matrix:

Gamma is discounting factor for future rewards. Its range is 0 to 1.
 i.e. 0 < Gamma <1.

Q(state, action) = R(state, action) + Gamma * max[Q(next state, all actions)]

- Future rewards are less valuable than current rewards so they must be discounted.
 If Gamma is closer to 0, the agent will tend to consider only the
- immediate rewards.
 If Gamma is closer to 1, the agent will tend to consider only future

Q – Learning Algorithm

- Set the gamma parameter
- Set environment rewards in matrix R
- Initialize matrix Q as Zero
 - Select random initial (source) state
 - Set initial state *s* = current state
 - Select one action a among all possible actions using exploratory policy
 - Take this possible action a, going to the next state s'.
 - Observe reward r
 - Get maximum Q value to go to next state based on all possible actions
- Compute:
- -Q(state, action) = R(state, action) + Gamma * max[Q(next state, all actions)]
- Repeat the above steps until reach the goal state i.e current state = goal state

Example: Q - Learning

Matrix Q:

- Set the Gamma value = 0.8
- Initialize the matrix Q to zero matrix

| | | | | | | _ | | Action | | | | | |
|-------------------|-------|---|---|---|---|----|--|--------|----|----|----|------|--|
| | 0 | 1 | 2 | 3 | 4 | 5 | State 0 | 1 | 2 | 3 | 4 | 5 | |
| 0 | L_0 | 0 | 0 | 0 | 0 | 07 | <mark>0</mark> | -1 | -1 | -1 | 0 | -17 | |
| 1 | 0 | 0 | 0 | 0 | 0 | 0 | $\begin{bmatrix} 0 & -1 \\ 1 & -1 \end{bmatrix}$ | -1 | -1 | 0 | -1 | 100 | |
| $Q=\frac{2}{3}$ | 0 | 0 | 0 | 0 | 0 | 0 | $R = \frac{2}{3} \begin{bmatrix} -1 \\ -1 \end{bmatrix}$ | -1 | -1 | 0 | -1 | -1 | |
| $Q - \frac{3}{3}$ | 0 | 0 | 0 | 0 | 0 | 0 | x - 3 - 1 | 0 | 0 | -1 | 0 | -1 | |
| 4 | 0 | 0 | 0 | 0 | 0 | 0 | $\begin{array}{c c} 4 & 0 \\ 5 & -1 \end{array}$ | -1 | -1 | 0 | -1 | 100 | |
| 5 | I٨ | 0 | n | n | Λ | ۸l | 5L-1 | 0 | -1 | -1 | 0 | 1001 | |

Example: Q – Learning

5

- From state 1, agent can go to either state 3 or 5.
- Let's choose 5.
- From 5, Compute Max Q value to go to
- Next state based on all possible actions

$$Q(state, action) = R(state, action) + Gamma * max[Q(next state, all actions)]$$
• $Q(1,5) = R(1,5) + 0.8 * max[Q(5,1), Q(5,4), Q(5,5)]$

Update the Matrix Q.

= 100 + 0.8 * max[0, 0, 0] = 100 + 0 = 100

- For next episode, choose next state 3 randomly that becomes current state.
- State 3 contains 3 choices i.e. state 1, 2 or 4.

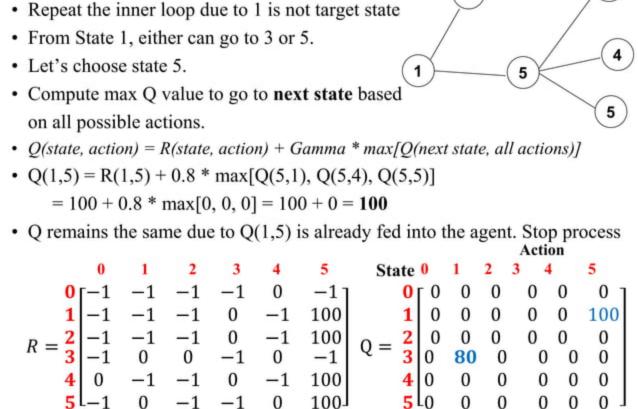
Compute max Q value to go to next state based

- Let's choose state 1.
 - on all possible actions.

$$Q(state, action) = R(state, action) + Gamma * max[Q(next state, all actions)]$$

 $Q(3,1) = R(3,1) + 0.8 * max[Q(1,3), Q(1,5)]$

- = 0 + 0.8 * max[0, 100] = 0 + 80 = 80• Update the Matrix Q.



For next episode, next state 1 becomes current state

References

- Tom Markiewicz& Josh Zheng, Getting started with Artificial Intelligence, Published by O'Reilly Media, 2017
- Stuart J. Russell and Peter Norvig, Artificial Intelligence A Modern Approach
- Richard Szeliski, Computer Vision: Algorithms and Applications, Springer 2010