

## Problem J

### Mediation

You are the mayor of a tree-structured city with  $N$  districts, numbered from 1 to  $N$ , connected by  $N - 1$  roads, numbered from 1 to  $N - 1$ . Road  $i$  connects district  $U_i$  and district  $V_i$  bidirectionally with weight  $W_i$ . Two districts  $S_1$  and  $S_2$  have been marked as **mediator districts**. The travel cost between district  $x$  and district  $y$ , denoted by  $d(x, y)$ , is the minimum sum of weights of the roads you need to pass through.

Whenever a conflict arise between any two districts, the mediator districts are required to travel to the conflicting districts. The **mediation cost** for two conflicting districts  $u$  and  $v$ , denoted by  $M(u, v)$ , is the maximum travel cost of the mediator districts to the nearest conflicting district. Formally,  $M(x, y)$  can be calculated as follows.

$$M(u, v) = \max(\min(d(u, S_1), d(v, S_1)), \min(d(u, S_2), d(v, S_2)))$$

Calculate the sum of mediation cost  $M(u, v)$  over all  $1 \leq u < v \leq N$ .

#### Input

The first line contains three integers:  $N$ ,  $S_1$ , and  $S_2$  ( $2 \leq N \leq 200\,000$ ;  $1 \leq S_1 < S_2 \leq N$ ).

The next  $N - 1$  lines contains integers  $U_i$ ,  $V_i$ , and  $W_i$  ( $1 \leq U_i < V_i \leq N$ ;  $1 \leq W_i \leq 100$ ) describing an edge.

#### Output

Output the sum of mediation cost in a single line.

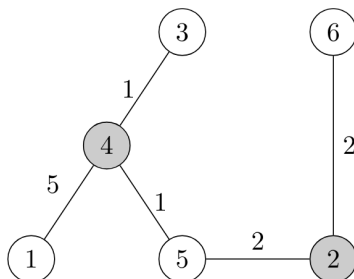
#### Sample Input 1

```
6 2 4
1 4 5
3 4 1
4 5 1
2 5 2
2 6 2
```

#### Sample Output 1

```
35
```

*Explanation of Sample 1:* The city is illustrated as follows.



The values of  $M(u, v)$  over all  $1 \leq u < v \leq N$  are presented as follows.

$u \setminus v$	1	2	3	4	5	6
1		3	4	3	2	5
2			1	0	1	3
3				3	2	2
4					2	2
5						2

The sum of all  $M(u, v)$  is 35.