

## Problem I

# Rectangular Pool

You are the owner of a land that can be represented as a grid  $G$  of size  $N \times M$ , with rows numbered from 1 to  $N$ , and columns numbered from 1 to  $M$ . Define  $G_{i,j}$  as the cell of the grid on the row  $i$  and column  $j$ . Each cell of  $G$  has either of the following terrains: puddle represented as  $.$  and dirt represented as  $\#$ . A connected component of puddles are defined as a **pool**. A connected component is a set of cells such that any two cells in the set are connected by traversing between cells that share a side.

Your land is very bizarre that, for the next  $Q$  days, exactly one cell will change its type. Formally, suppose cell at row  $R$  and column  $C$  change its type. If the cell  $G_{R,C}$  is a puddle, it will transform into dirt; if the cell is dirt, it will transform into a puddle.

You have an abnormal obsession to rectangles, so you will get sick if a pool is not rectangular. A rectangular pool is defined as follows: let  $r_{min}$ ,  $r_{max}$ ,  $c_{min}$ , and  $c_{max}$  as the minimum row number, maximum row number, minimum column number, and maximum column number of all puddles in the pool respectively, then there are exactly  $(r_{max} - r_{min} + 1) \times (c_{max} - c_{min} + 1)$  puddles in the pool.

At the end of each day, determine if there exists any non-rectangular pool in your land!

### Input

The first line contains two integers  $N$  and  $M$  ( $1 \leq N \leq M \leq 1000$ ). Each of the next  $N$  lines contains  $M$  characters of either  $.$  or  $\#$ , where the character at  $i$ -th row and  $j$ -th column represents the type of cell  $G_{i,j}$ .

The next line contains an integer  $Q$  ( $1 \leq Q \leq 300\,000$ ). Each of the next  $Q$  lines contains two integers  $R$  and  $C$  ( $1 \leq R \leq N$ ;  $1 \leq C \leq M$ ) meaning that the cell  $G_{R,C}$  change its type.

### Output

Output  $Q$  lines representing the existence of non-rectangle pool at the end of each day. Each of the lines contains either **RECTANGLES** if all pools are rectangular, or **NO** if there exists a non-rectangular pool.

#### Sample Input 1

```
5 5
#...#
#...#
#####
#...#
#####
3
4 3
1 3
2 3
```

#### Sample Output 1

```
RECTANGLES
NO
RECTANGLES
```

*Explanation of Sample 1:* The following are the states of the land after each day:

```
# . . #   # . # . #   # . # . #
# . . #   # . . #   # . # . #
#####   #####   #####
# . # . #   # . # . #   # . # . #
#####   #####   #####
```

After the first day, all three pools are rectangular pools. After the second day, the pool formed by cells (1, 2), (1, 4), (2, 2), (2, 3), (2, 4) is not rectangular. All pools are rectangular again after the third day.

#### Sample Input 2

```
3 4
####
# . ##
####
1
2 2
```

#### Sample Output 2

```
RECTANGLES
```