

## Problem B

# Construct BFS Graph

You are currently researching a graph traversal algorithm called the Breadth First Search (BFS). Suppose there is a graph of  $N$  nodes, numbered from 1 to  $N$ , and an adjacency matrix  $A$ , for which node  $u$  can traverse to node  $v$  if  $A_{u,v}$  is 1, otherwise it is 0. The following pseudocode will output the order the nodes that are visited in a BFS algorithm.

```
BFS(A[1..N] [1..N]):  
    let U be an empty array  
    let Q be an empty queue  
  
    append 1 to U  
    push 1 to Q  
  
    while Q is not empty:  
        pop the front element of Q into u  
        for v = 1 to N:  
            if A[u][v] == 1 and v is not in U:  
                append v to U  
                push v to Q  
  
    return U
```

Suppose now you have an integer  $N$ ,  $M$ , and an array  $U$  of  $N$  integers. You wonder whether there exists a simple undirected graph with  $N$  nodes and  $M$  edges such that the output of the pseudocode above is the array  $U$ . Construct such graph if it exists.

A simple undirected graph with  $M$  edges has an adjacency matrix  $A$  that satisfies the following.

- $A_{u,u} = 0$  for all  $1 \leq u \leq N$ .
- Exactly  $M$  pairs  $(u,v)$  satisfies  $1 \leq u < v \leq N$  and  $A_{u,v} = 1$ , meaning that there is an edge connecting node  $u$  and  $v$ .
- $A_{u,v} = A_{v,u}$  for all  $1 \leq u < v \leq N$ .

### Input

The first line contains two integers  $N$  and  $M$  ( $1 \leq N, M \leq 200\,000$ ). The second line contains  $N$  integers representing  $U$ , which is a permutation of  $(1, 2, \dots, N)$ . You are guaranteed that the first element of  $U$  is always 1.

### Output

If such a graph exists, output  $M$  lines, each containing two integers  $u$  and  $v$  representing an edge that connects node  $u$  and  $v$ .



If there is no such graphs, output -1 -1 in a single line.

**Sample Input 1**

5 6 1 5 2 3 4	1 5 2 3 5 2 4 3 3 5 4 5
------------------	--

**Sample Output 1**

*Explanation of Sample 1:* You can also output the following edges and get a correct answer:  
(1, 5), (5, 2), (2, 3), (3, 5), (2, 4), (5, 4).

**Sample Input 2**

5 10 1 5 2 3 4	-1 -1
-------------------	-------

**Sample Output 2**