TABLE 3.2 RANGANATHAN'S GENERATING FUNCTION FOR $u_{v_{W_{\approx_{1}}}}$

| Θ_{*} | Σ | х | у |
|--------------------------------------|------------------------|------------------|------------------|
| 180 | 7 1 | 0 1 | 1 |
| 150.07 123.75 102.56 86.18 | 15 9 23 15 | 1 2 3 4 | 1 1 1 1 |
| 164.78 150.07 136.31 123.75 | 57 15 65 9 | 1 2 3 4 | 2 2 2 2 |
| 169.82 159.79 150.07 140.77 | 127 65 135 71 | 1 2 3 4 | 3 3 3 |
| 172.35 164.78 157.33 150.07 | 225 57 233 15 | 1 2 3 4 | 4 4 4 |

TABLE 3.3

| | | A 11 | | | - 5.5 | | | | |
|-----|-----------------|------------------------------------|-----|------------------------------|--------------------------------------|-----|----------------------|----------------------------|--|
| | Σ | All values of θ/UVW for Σ up to 31 | | | | | | | |
| 100 | 5 13a 17a | 36.9 22.6 | 110 | Σ | θ " | | Σ | θ | |
| | 25a 29b | 28.1 16.3 43.6 | | 9 11 17b 19a 27h | 70.5 38.9 50.5 86.6 26.5 | 111 | 3 7 13b 19b | 60 38.2 27.8 46.6 | |

27b

31.6

21a

31a

21.8

17.9

Table 3.3 (continued)

| 210 | 3 | 131.8 | 211 | 3 | 180 | 221 | 5 | 143.1 |
|-----|-----|-------|---------------------------------------|------------|-------|---------|------|-------|
| | 5 | 180 | | 5 | 101.5 | | 9 | 90 |
| | 7 | 73.4 | | 7 | 135.6 | | 9 | 180 |
| | 9 | 96.4 | | 11 | 63.0 | | 13b | 112.2 |
| | 15 | 48.2 | | 15 | 78.5 | | 17b | 61.9 |
| | 21b | 58.4 | | 21b | 44.4 | | 25b | 73.7 |
| | 23 | 163.0 | | 25b | 156.9 | | 29a | 46.4 |
| | 27a | 35.4 | | 29a | 149.6 | | | |
| | 29a | 112.3 | | 31b | 52.2 | | | |
| | ZJa | 112.5 | | 310 | 32.2 | | | |
| 310 | 5 | 180 | 311 | 3 | 146.4 | 320 | PC 7 | 149.0 |
| 310 | 7 | 115.4 | 511 | 5 | 95.7 | 020 | 11 | 100.5 |
| | 11 | 144.9 | | 9 | 67.1 | | 13a | 180 |
| | 13b | 76.7 | | 11 | 180 | And the | 17b | 122.0 |
| | 19a | 93.0 | | 15 | 50.7 | , | 19b | 71.6 |
| | 23 | 55.6 | | 15 | 117.8 | (| 29a | 84.1 |
| | 23 | 33.0 | | 23 | 40.5 | | 31b | 54.5 |
| | | | | 25b | 168.3 | | 310 | 31.5 |
| | | | | 230 27a | 79.3 | | | |
| | | | | 31b | 126.6 | | 141 | |
| | | | * | 310 | 120.0 | | | |
| 321 | 7 | 180 | 322 | 9 | 152.7 | 410 | . 9 | 152.7 |
| | 9 | 123.8 | , , , , , , , , , , , , , , , , , , , | 13a | 107.9 | | 13b | 107.9 |
| | 15 | 86.2 | | 17b | 180 | | 17a | 180 |
| | 15 | 150.1 | | 21a | 128.3 | | 21a | 79.0 |
| - 1 | 23 | 102.6 | | 21b | 79.0 | | 21b | 128.3 |
| | 25b | 63.9 | | , | , - | | A | 120.0 |
| | | | | | | | | |
| 411 | 9 | 180 | 331 | 5 | 154.2 | 421 | 11 | 155.4 |
| | 11 | 129.5 | | 7 | 110.9 | | 15 | 113.6 |
| | 17a | 93.4 | | 11 | 82.2 | | 21b | 180 |
| | 19b | 153.5 | | 17b | 63.8 | | 23 | 85.0 |
| | 27a | 109.5 | | 19a | 180 | | 25b | 132.8 |
| | 27b | 70.5 | | 23 | 130.7 | | 250 | 132.0 |
| | -/ | , , , | - | 25b | 51.7 | | | |
| | | | | 1 , | 1. | | | |
| 332 | 11 | 180 | 430 | 13b | 157.4 | 431 | 13b | 180 |
| | 13a | 133.8 | | 17b | 118.1 | 1.0 | 15 | 137.2 |
| | 19a | 99.1 | | 25a | 180 | | 21b | 103.8 |
| | 23 | 155.9 | | 25b | 90 | | 27a | 157.8 |
| | 29a | 76.0 | | 29a | 136.4 | | 31b | 80.7 |
| | 31a | 114.8 | | | | | 510 | 80.7 |
| | | | | | | | | |

Table 3.3 (continued)

| 510 | 13a 15 21a 27b 31a | 180 137.2 103.8 157.8 80.7 | 511 | 7 9 13a 19a 27a 27b 31b | 158.2 120.0 92.2 73.2 60 180 137.9 | 432 | 15 19a 27a 29a | 94.3 |
|-----|--------------------------------|--|-----|---|--|-----|-------------------------|---------------------------------|
| 520 | 15 19b 27b 29b | 159.0 121.8 94.3 180 | 521 | 15 17b 23 31b | 180 139.9 107.7 159.3 | 441 | 17a 21b 29a | 160.3 124.9 97.9 |
| 522 | 17b 21b 29b | 160.3 124.9 97.9 | 433 | 17b 19a 25a | 180 142.1 111.1 | 530 | 17a 19b 25b | 180 142.1 111.1 |
| 610 | 19a 23 31a | 161.3 127.5 101.2 | 532 | 19b 21b 27a | 180 144.1 114.0 | 611 | 19a 21b 27b | 180 144.1 114.0 |
| 443 | 21b 25a | 162.3 129.8 | 540 | 21a 25b | 162.3 129.8 | 621 | 21b 25b | 162.3 129.8 |
| 531 | 9 11 15 21b 29a | 160.8 126.2 99.6 80.4 66.6 | 533 | 11 13b 17a 23 31b | 162.7 130.8 105.3 86.3 72.2 | 551 | 13a 15 19b 25b | 164.1 134.4 110.0 91.2 |
| 541 | 21a 23 29a | 180 145.7 116.6 | 542 | 23 27a | 163 131.8 | 631 | 23 25b 31b | 180 147.1 118.9 |
| 632 | 25b 29a | 163.7 133.6 | 543 | 25b 27a | 180 148.4 | 710 | 25a 27a | 180 148.4 |
| 711 | 13b 15 19a 25a | 164.1 134.4 110.0 91.2 | 553 | 15 17a 21a 27b | 165.2 137.3 113.9 95.3 | 731 | 15 17b 21b 27a | 165.2 137.3 113.9 95.3 |

Table 3.3 (continued)

| 641 | 27b | 164.4 | 720 | 27a | 164.4 | 552 | 27b | 180 |
|-----|-----|-------|-----|-----|-------|--------|-----|-------|
| | 31b | 135.2 | | 31b | 135.2 | | 29b | 149.6 |
| 721 | 27a | 180 | 544 | 29a | 164.9 | 730 | 29b | 180 |
| | 29a | 149.6 | 722 | 29a | 164.9 | | 31b | 150.6 |
| 733 | 17b | 166.1 | 751 | 19a | 166.8 | 753 | 21b | 167.5 |
| | 19b | 139.7 | | 21b | 141.8 | | 23 | 143.6 |
| | 23 | 117.2 | | 25b | 120 | | 27b | 122.5 |
| t | 29b | 98.9 | | 31b | 102.1 | | | |
| 911 | 21a | 167.5 | 931 | 23 | 168.0 | 755 | 25b | 168.5 |
| | 23 | 143.6 | | 25b | 145.1 | | 27b | 146.4 |
| | 27a | 122.5 | | 29a | 124.7 | | 31a | 126.6 |
| | | | | | | | | |
| 771 | 25a | 168.5 | 773 | 27a | 169.0 | 951 | 27a | 169.0 |
| | 27a | 146.4 | | 29b | 147.7 | | 29a | 147.7 |
| | 31b | 126.6 | 645 | 31b | 165.4 | 650 | 31a | 165.4 |
| | | | | | | | | |
| 953 | 29a | 169.4 | 775 | 31b | 169.7 | 11,1,1 | 31a | 169.7 |
| | 31b | 148.7 | 732 | 31b | 180 | 651 | 31a | 180 |

The significance of the letters which occur in Tables 3.1, 3.3 and 3.4 are that more than one misorientation can generate geometrically independent CSLs with a particular Σ -value. For example a $\Sigma = 39$ CSL arises from the disorientation 32.21°/111 ($\Sigma = 39a$) and also 50.13°/123 ($\Sigma = 39b$). A full list of all 24 variants of $\Sigma = 39b$ were given in Table 2.1. The letters which distinguish identical Σ -values are designated according to increasing Θ .

In analogy to equation 2.6 the misorientation matrix for a CSL is given by

$$\mathbf{M}_{\text{CSL}} = 1/\Sigma \begin{bmatrix} A_{11} & A_{12} & A_{13} \\ A_{21} & A_{22} & A_{23} \\ A_{31} & A_{32} & A_{33} \end{bmatrix}$$
(3.2)

Hence the misorientation matrix in equation 2.7, which refers to a $\Sigma = 3$ CSL, could be rewritten: