

1. Consider the poset as shown in Figure-b (Hasse diagram). Find the following:
 - a. Find the maximal elements.
 - b. Find the minimal elements.
 - c. Is there a greatest element?
 - d. Is there a least element?
 - e. Find all upper bounds of $\{a, b, c\}$.
 - f. Find the least upper bound of $\{a, b, c\}$, if exists.
 - g. Find the lower bounds of $\{f, g, h\}$.
 - h. Find the greatest lower bound of $\{f, g, h\}$, if it exists.

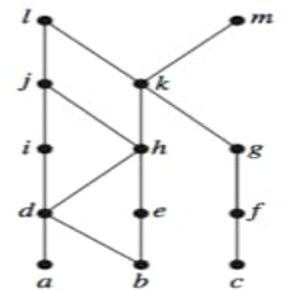


Figure-b

2. How many four-digit numbers can be formed using the digits 0, 3, 4, 5, 6, 7 if
 - (i) Repetition of digits is not allowed ?
 - (ii) Repetition of digits is allowed ?
3. State the converse, contrapositive, and Inverse of the proposition, "If 7 is greater than 5, then 8 is greater than 6".
4. Prove by constructing truth table, $\neg (p \vee q) \equiv \neg p \wedge \neg q$ are logically equivalent.
5. Prove that if n is an integer and $3n + 2$ is odd, then n is odd.
6. Prove that the sum of two rational numbers is a rational number.
7. Use mathematical induction to prove

$$1^2 + 3^2 + 5^2 + \dots + (2n - 1)^2 = \frac{n(2n - 1)(2n + 1)}{3}.$$
8. Find if the following is a tautology, contradiction or contingency:

$$(p \rightarrow (q \rightarrow r)) \rightarrow ((p \rightarrow q) \rightarrow (p \rightarrow r)).$$

9. a) Show that $\neg p \leftrightarrow q$ and $p \leftrightarrow \neg q$ are logically equivalent.

b) Show that $\neg(p \oplus q)$ and $p \leftrightarrow q$ are logically equivalent.

10. Construct a truth table for each of these compound propositions.

a) $((p \rightarrow q) \rightarrow r) \rightarrow s$

b) $(p \wedge q) \rightarrow (p \vee q)$