

Construct a B+ tree for the set of key values.

(2, 3, 5, 7, 11, 17, 19, 23, 29, 32)

Assume that the tree is initially empty and values are added in ascending order. Construct B+ tree for the case where the number of pointers that will fit in one node is four. Also show the form of the tree after deletion of 23. [PU: 2015 Spring].

Soln:

Construction of B+ tree for order $n=4$:

As we know,

→ Internal nodes (non-leaf nodes) must hold at least $\lceil n/2 \rceil$ and at most n children. (Pointers to children)

Here,

for order $n=4$

minimum ~~pointers~~ in internal nodes $= (4/2)$
 $= 2$

maximum ~~pointers~~ in internal nodes $= 4$

Similarly, each leaf node must hold between $\lceil (n-1)/2 \rceil$ and $(n-1)$ value.

Now, Minimum number of search key values

$$= \frac{(4-1)}{2} = \frac{3}{2} = \text{ceiling}(1.5)$$

$= 2$

{Node gets merged if count goes below in particular node}

∴ maximum number of search key

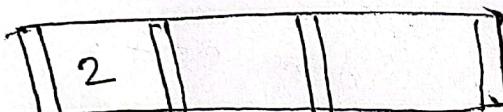
values = 3

(Here, Nodes get split when number of search key values reaches 4 in particular node.)

→ If root node is not a leaf it has at least 2 children.

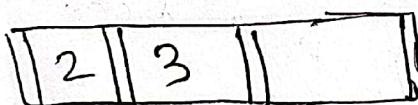
Step 1

Insert key value 2



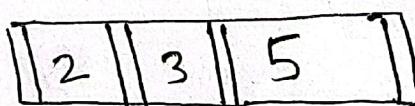
Step 2

Insert key value 3



Step 3

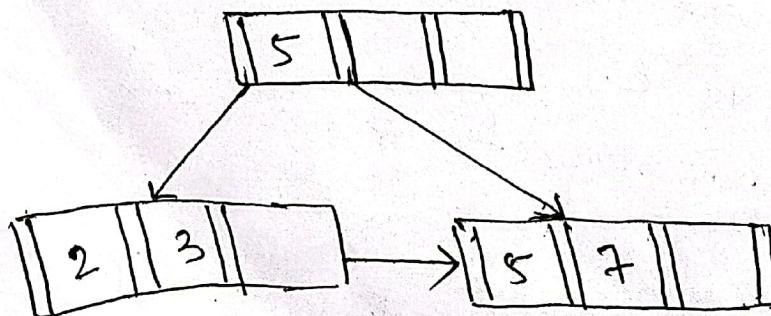
Insert key value 5



Step 4

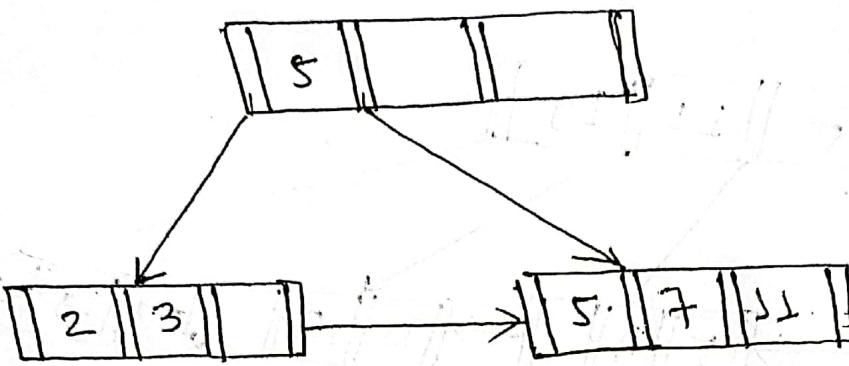
Insert key value 7.

Now, Node becomes full, splitting the nodes



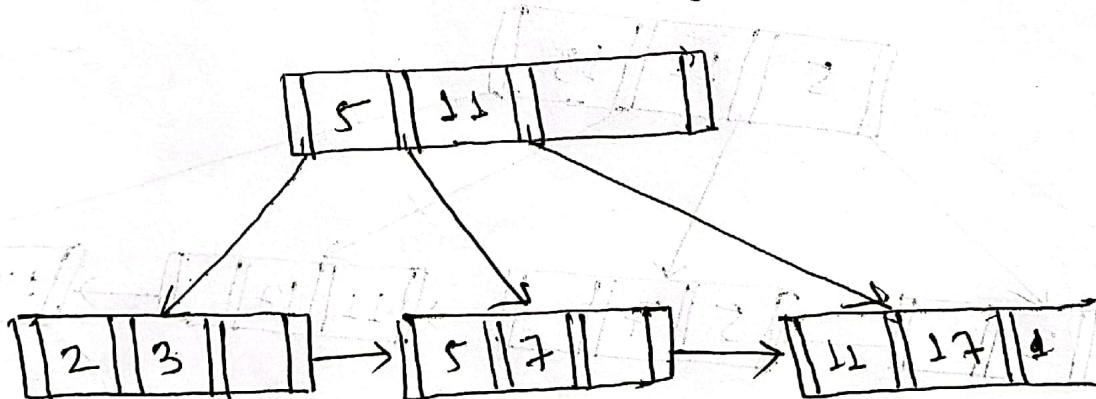
Step-5

Insert key value 11



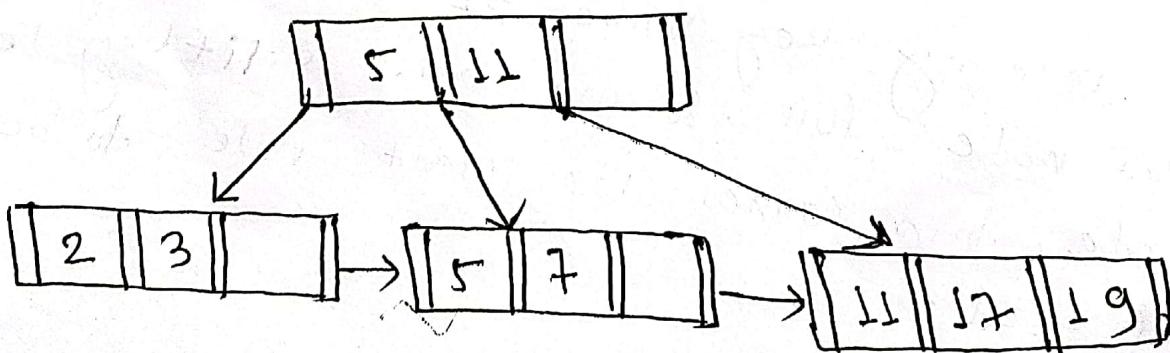
Step-6

Insert key value 17, Here second leaf node becomes full, Now splitting leaf node



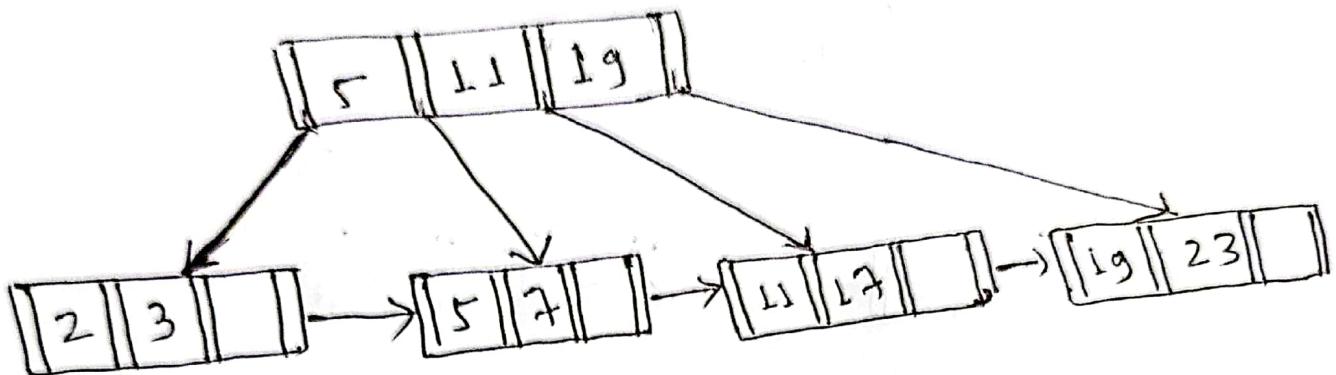
Step-7

Insert key value 19



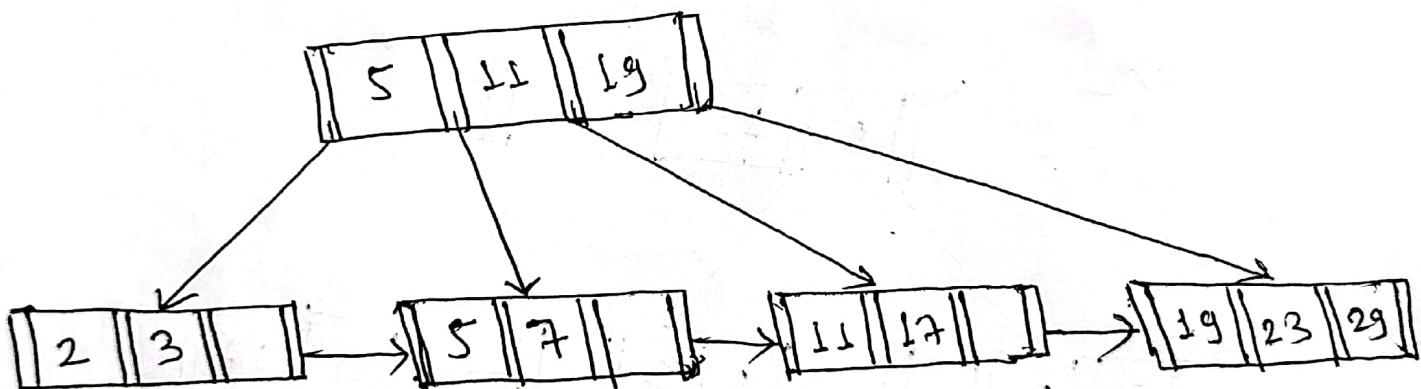
Step - 8

Insert key value 23, Here Third leaf node is full, Now splitting leaf node



Step - 9

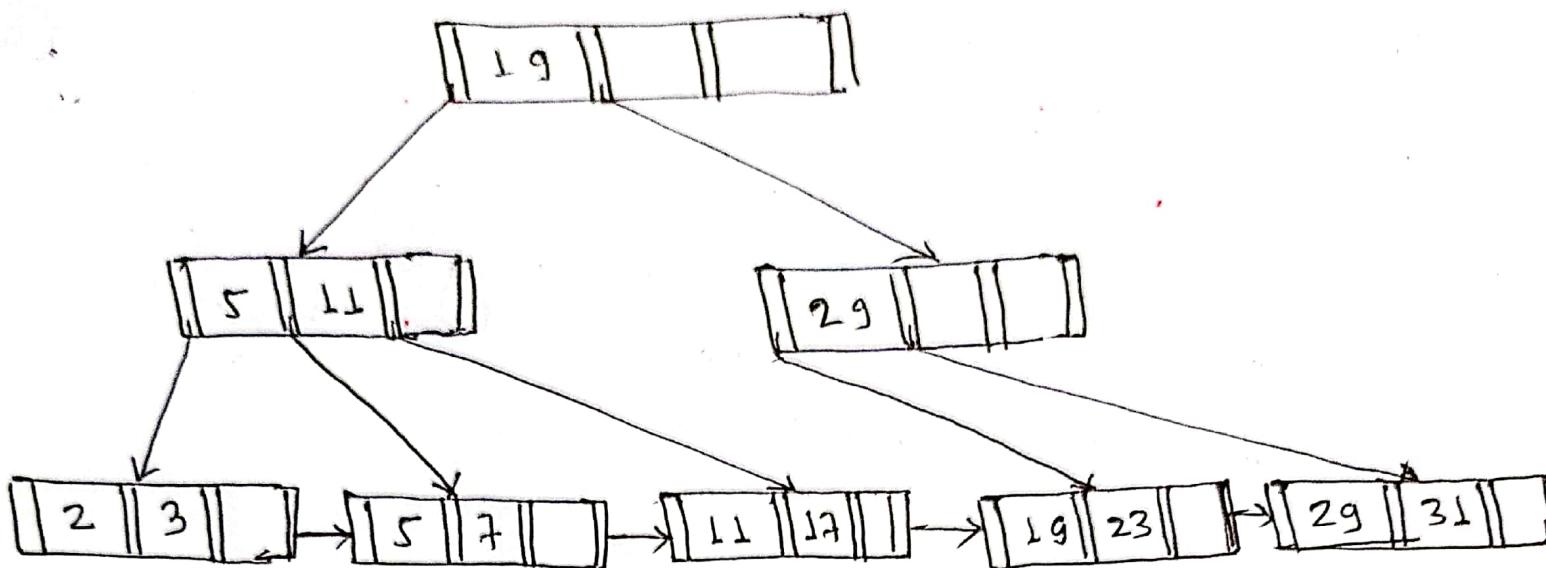
Insert key value 29



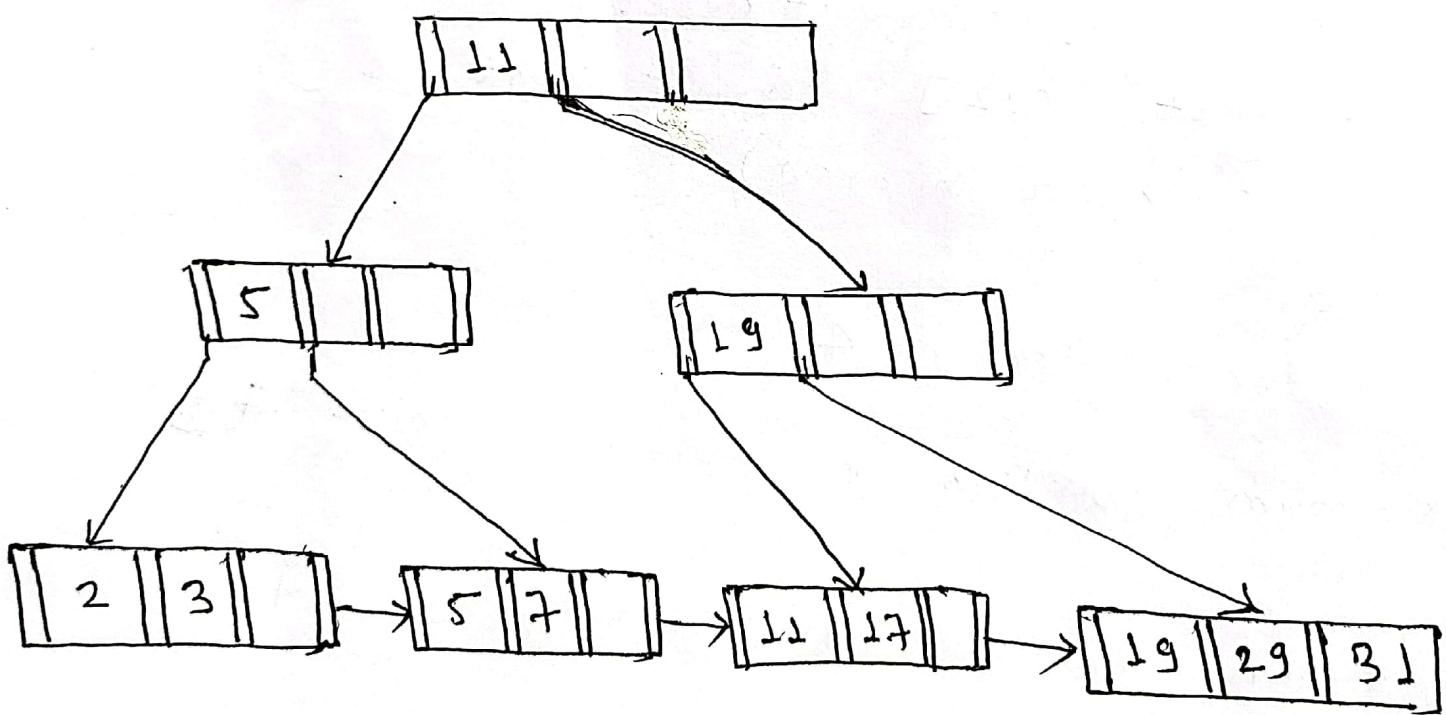
Step - 10

Insert key value 31.

Here inserting key value.. 31 causes rightmost leaf node full, so we must splitting leaf node, this causes its parent node to be splitted.



Add or deletion 23



Create B+ tree for order 4
with following data.

(4, 9, 16, 25, 3, 20, 13, 15, 20, 11, 12)

of order 4. Assume that tree is initially
empty and values are added in ascending
order. Also show formation of tree after
deletion of 16. [CU: 2019 Spring]

→ Soln:

Construction of B+ tree for order $n=4$.

As we know,

→ Internal nodes (non-leaf nodes) must hold
at least $\lceil n/2 \rceil$ and at most n children -
(pointers to children)

Here,

for order $n=4$,

$$\text{Maximum pointers in internal nodes} = \left(\frac{4-1}{2}\right) \\ = 2$$

$$\text{Maximum pointers in internal nodes} = 4$$

Similarly,

→ Each leaf node must hold between $\lceil (n-1)/2 \rceil$
and $(n-1)$ value

Now, minimum number of search key
values = $\left(\frac{4-1}{2}\right)$

$$= \text{ceiling}(1.5)$$

Node gets merged if count goes below in particular node.

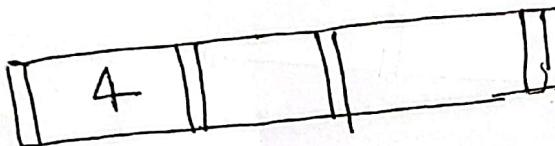
i. maximum number of search key values = 3

(Node gets split when number of search key values reaches 4 in particular node)

→ If the root node is not a leaf, it has at least 2 children.

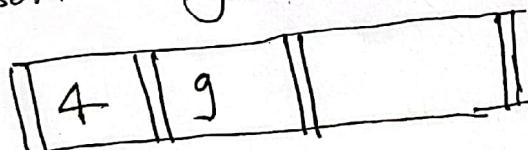
Step 1:

Insert key value 4



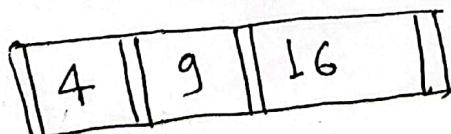
Step 2

Insert key value 9



Step 3

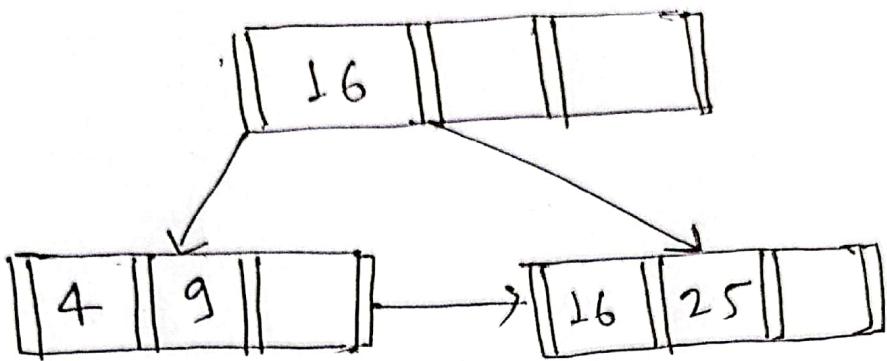
Insert key value 16



Step 4

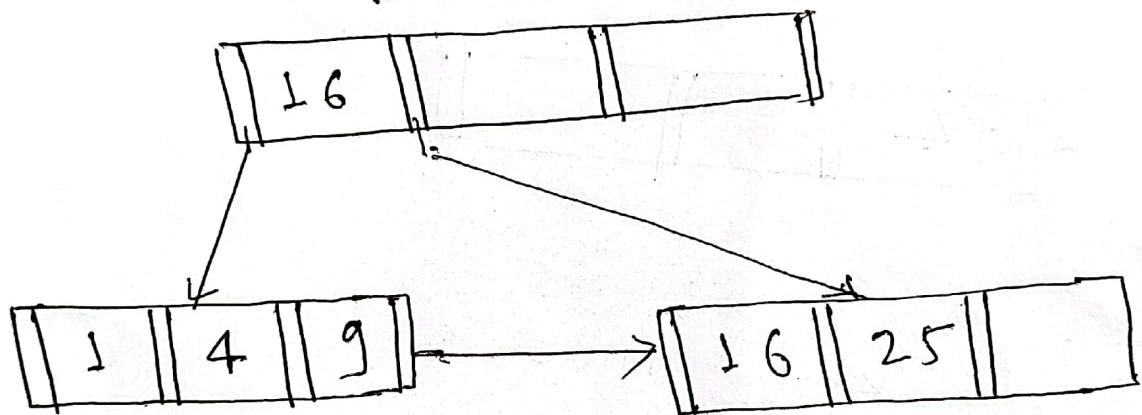
Insert key value 25

Now, Node becomes full, so splitting the nodes we get



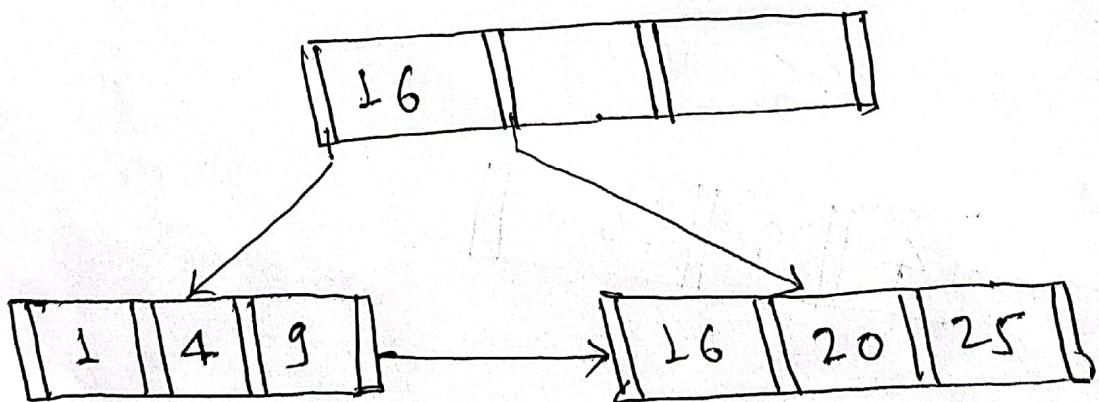
Step - 5

Insert key value 1



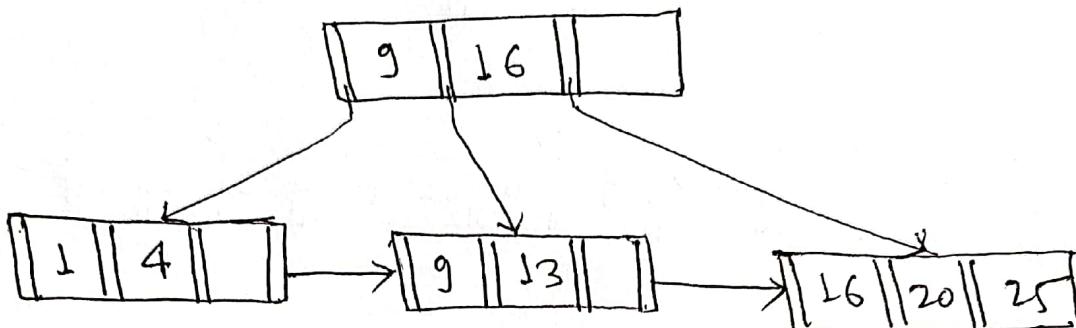
Step - 6

Insert key value 20



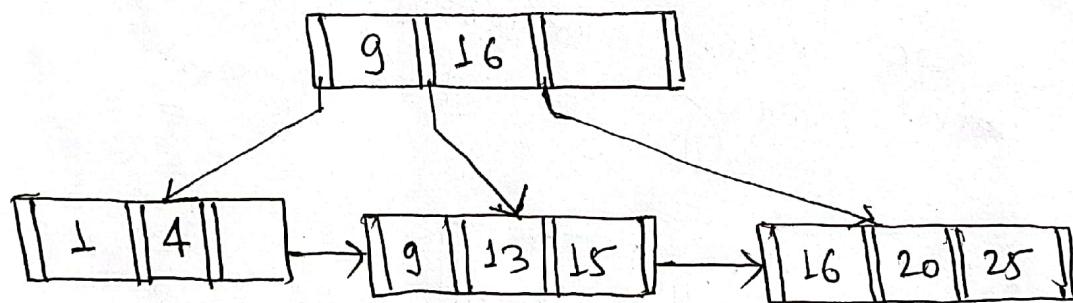
Step - 7

Insert key value 13,
Now, first leaf node is full, now splitting nodes



Step - 8

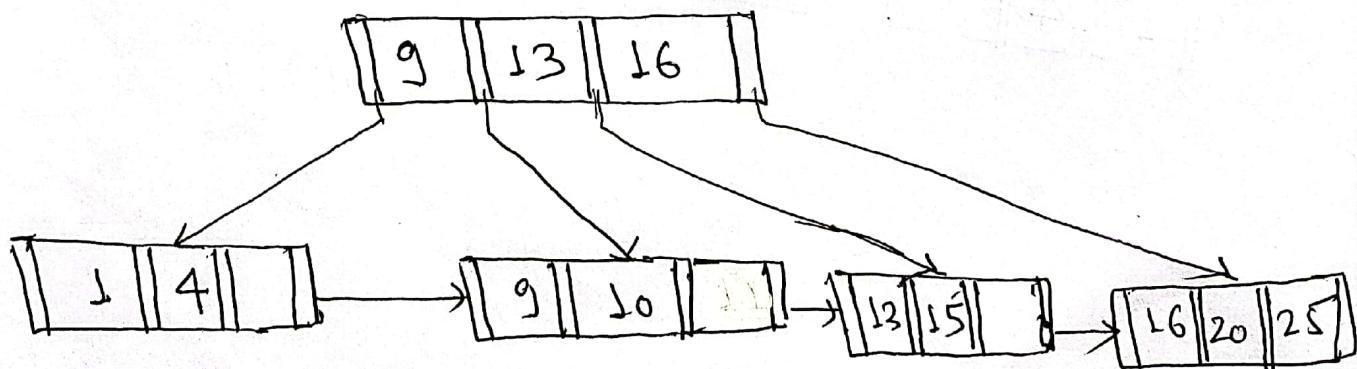
Insert key value 15



Step - 9

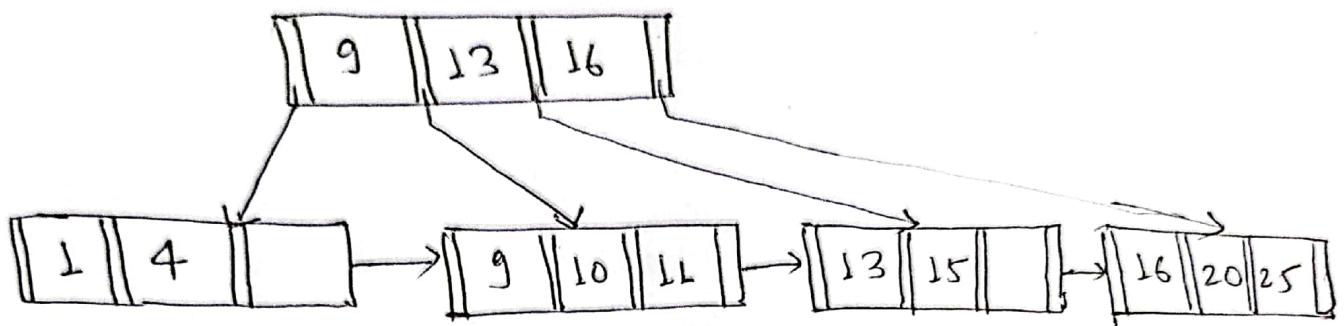
Insert key value 10

Now, Second leaf node is full, now splitting nodes.



Step - 10

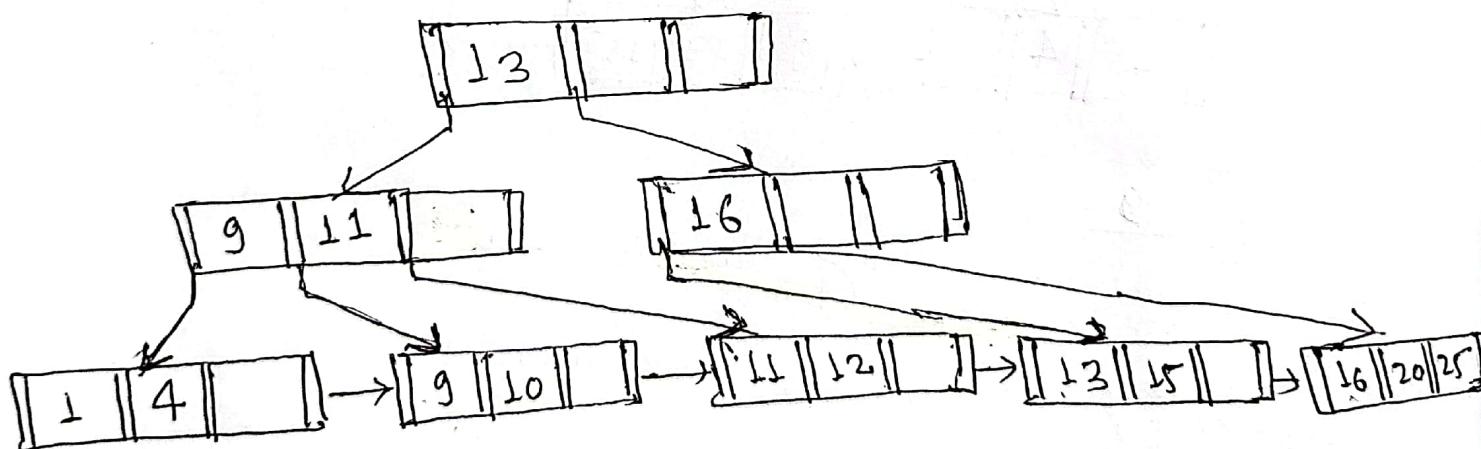
Insert key value 11



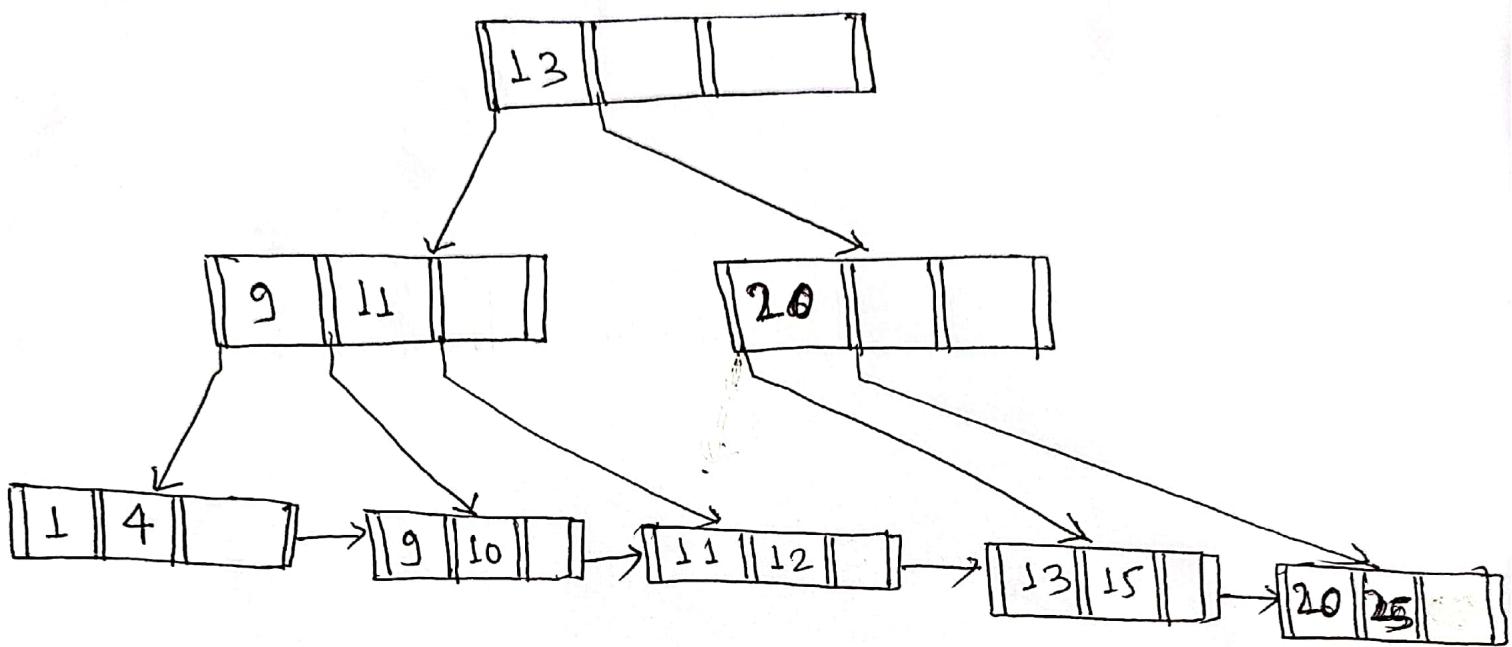
Step - 11

Insert key value 12

This causes overflow in 2nd leaf node. splitting
the leaf node causes overflow in its parent node
as well. finally B+ tree becomes.



After deletion of 16



Construct a B+ tree for the following set of key values. (1, 3, 6, 7, 11, 17, 19, 23, 30, 32). Assume that the tree is initially empty and values are added in ascending order. Construct B+ tree for the case where the numbers of pointers that will fit in one node is four. Also show the form of the tree after insertion of 9. [PU: 2018 fall]

Soln:

Construction of B+ tree for order $n=4$.

As we know,

- Internal nodes (non-leaf nodes) must hold at least $\lceil n/2 \rceil$ and at most n children. (Pointers to children)

So, for order $n=4$

$$\text{Minimum pointers in internal nodes} = \lceil 4/2 \rceil = 2$$

$$\text{Maximum pointers in internal nodes} = 4$$

Similarly,

- Each leaf node must hold between $\lceil (n-1)/2 \rceil$ and $(n-1)$ value.

NOW,

Minimum number of search key values

$$= \frac{(4-1)}{2} = 3/2$$

$$= \text{ceiling}(1.5) \\ = 2$$

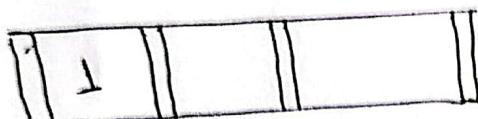
Node gets merged if count goes below in particular node

∴ maximum number of search key values = 3

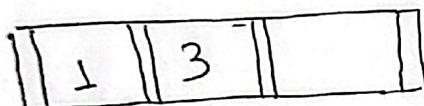
Here, Node gets split when number of search key values reaches 4 in particular node.

⇒ If the root node is not a leaf, it has at least 2 children

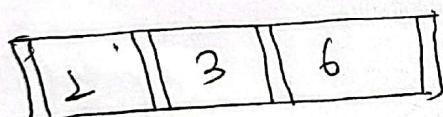
Step 1 Insert key value 1



Step 2 Insert key value 3

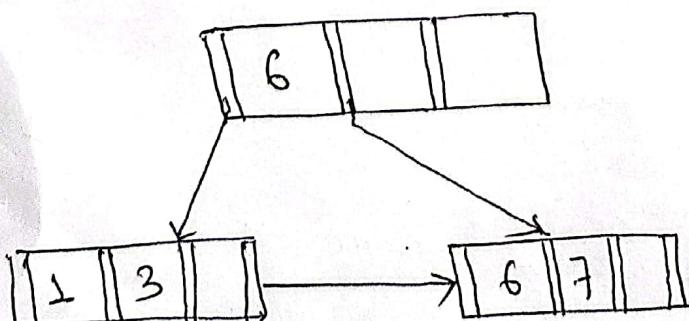


Step 3 Insert key value 6

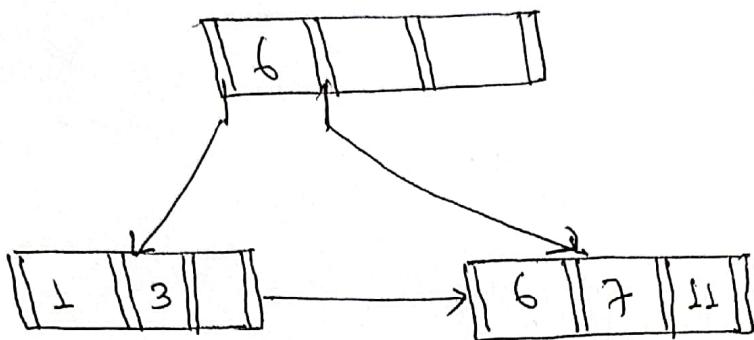


Step 4 Insert key value 7

Now, Node becomes full. Splitting the nodes

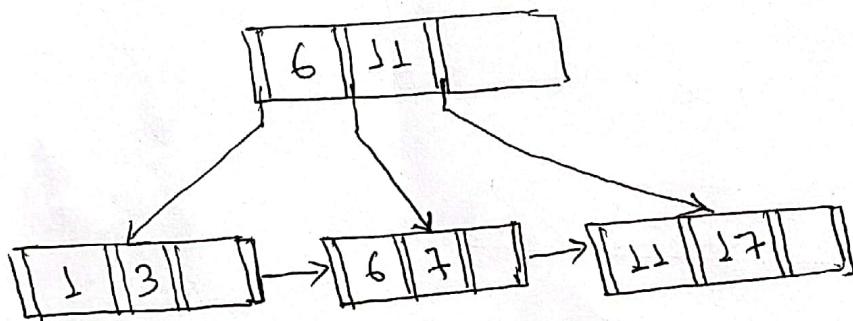


Step-5 Insert key value 11



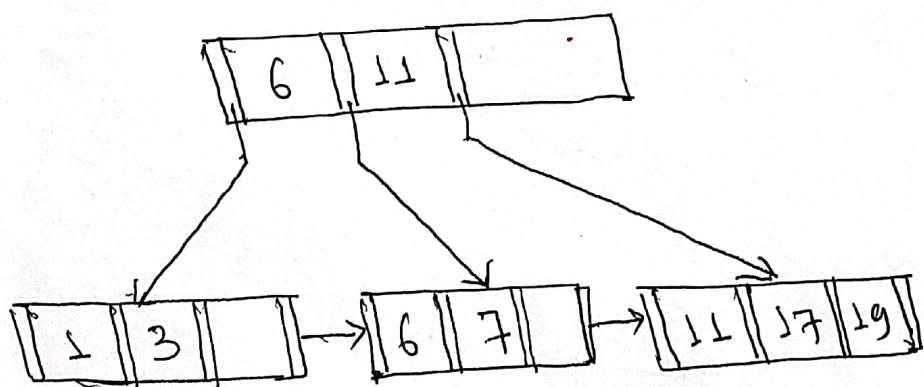
Step-6

Insert key value 17, here, second leaf node becomes full, now splitting leaf node.



Step-7

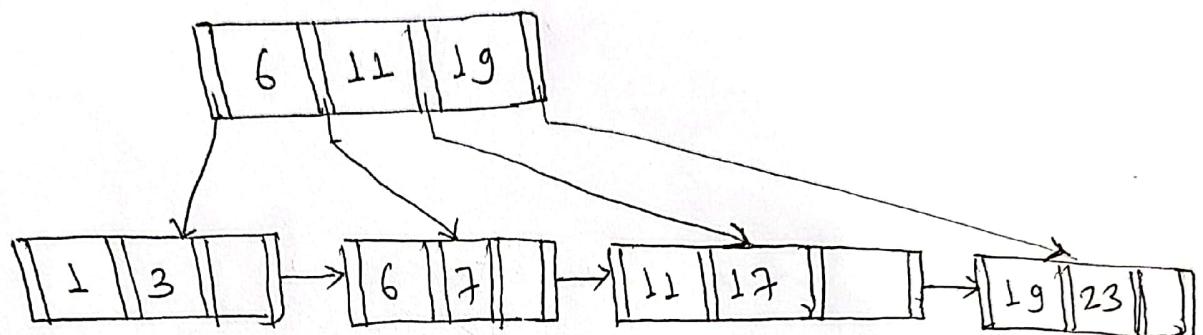
Insert key value 19



Step - 8

Insert key value 23

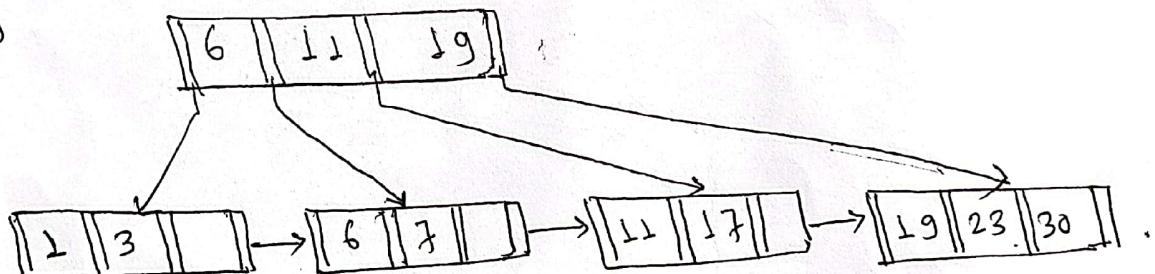
Here Third leaf node becomes full. Now splitting the nodes we get.



Step - 9

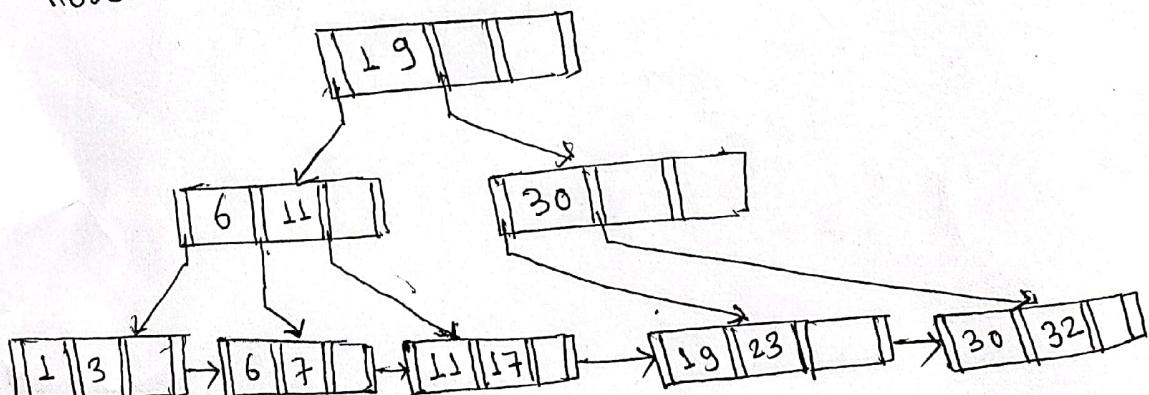
Insert key value 30

~~here~~



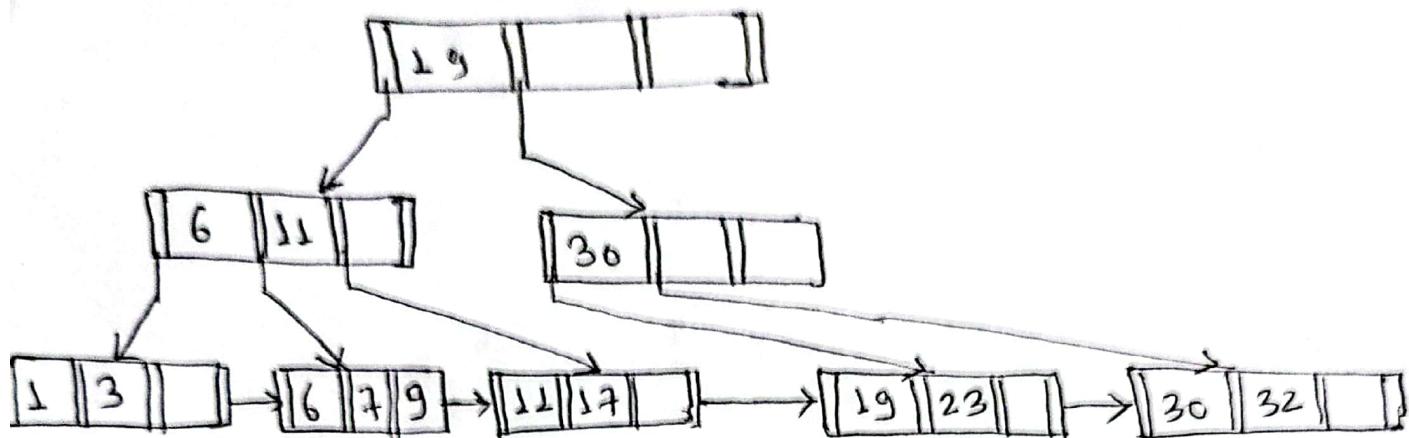
Step - 10

Insert key value 32, This causes rightmost leaf node full and splitting the nodes causes its parent node also full, finally B+ becomes



After inserting 9

B+ tree becomes



Construct a B+ tree for the following set of key values ~~(1, 4, 7, 10, 17, 21, 31, 25, 19, 20, 28)~~
Assume that tree is initially empty and value are added in ascending order. Construct B+ tree for the case where the number of pointers that will be fit in one node is Four.

Soln:

Construction of B+ tree for order $n=4$,

As we know,
→ Internal nodes (non-leaf nodes) must hold at least $\lceil n/2 \rceil$ and at most n children.
(pointers to children)

Here, for order $n=4$

Minimum pointers in internal nodes $= (4/2) = 2$

Maximum pointers in internal nodes $= 4$

Similarly,

→ Each leaf node must hold between $\lceil (n-1)/2 \rceil$ and $(n-1)$ value.

Now,
Minimum number of search key values
 $= \left(\frac{4-1}{2} \right) = 3/2$

$$= \text{ceiling}(1.5)$$

$$= 2$$

∴ Maximum number of search key values $= 3$

→ If the root is not a leaf, it has at least 2 children.

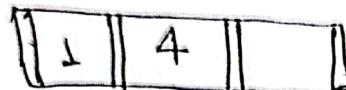
Step 1

Insert key value 1



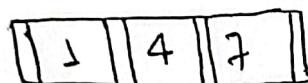
Step 2

Insert key value 4



Step 3

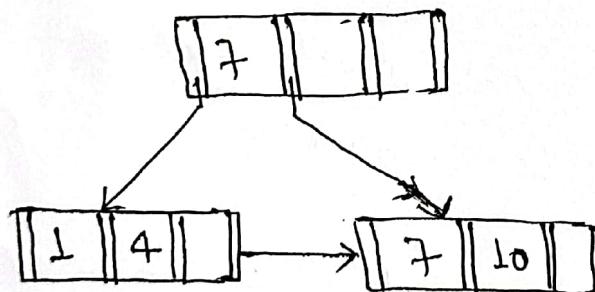
Insert key value 7



Step 4

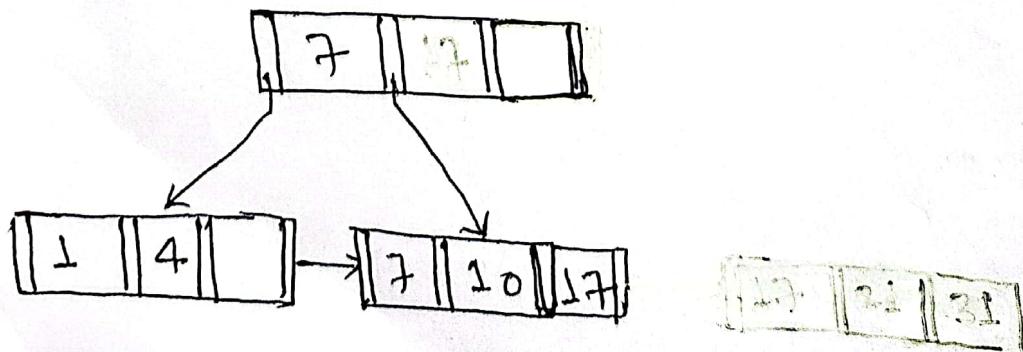
Insert key value 10

Now, node becomes full, splitting the nodes



Step 5

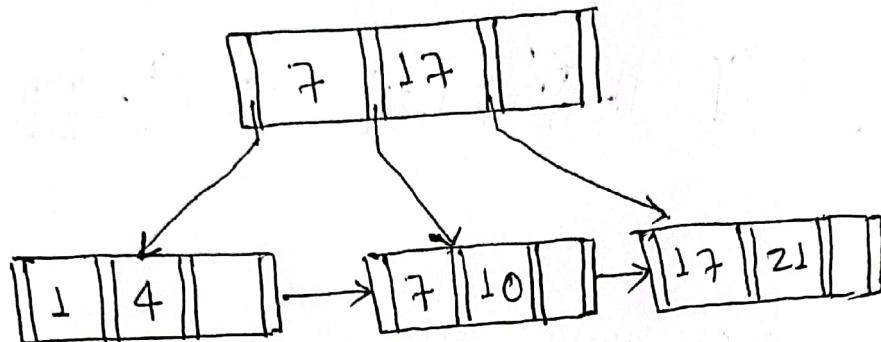
Insert key value 17



Step - 6

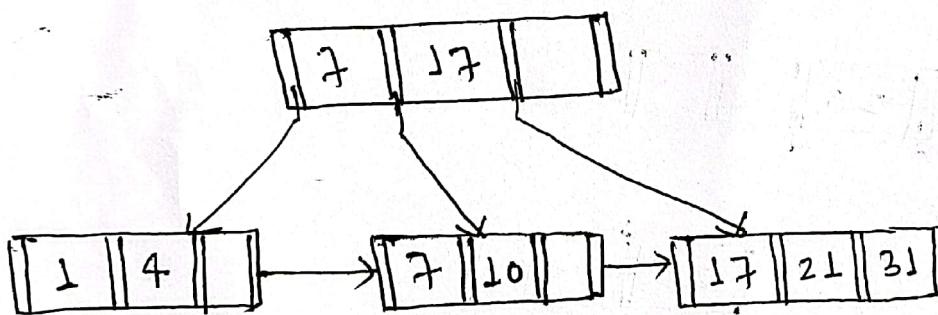
Insert key value 21

Now, second leaf node becomes full. Splitting the nodes we get.



Step 7

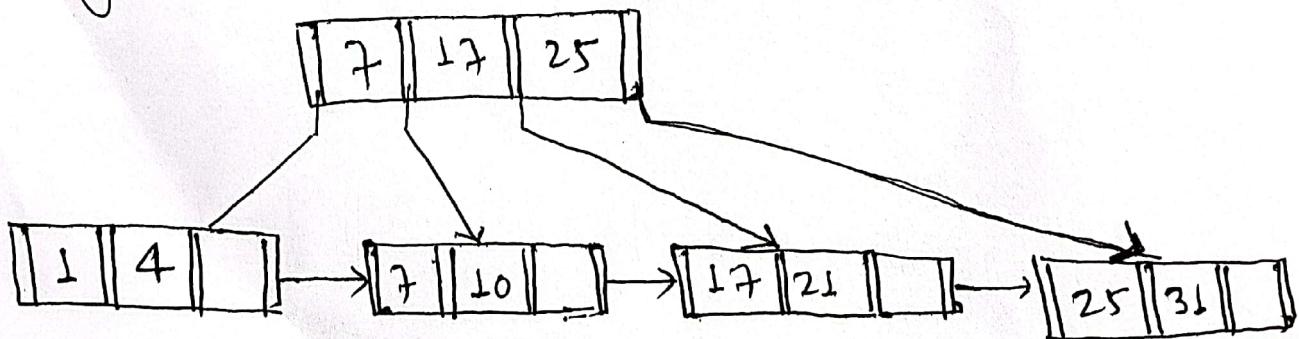
Insert key value 31



Step 8

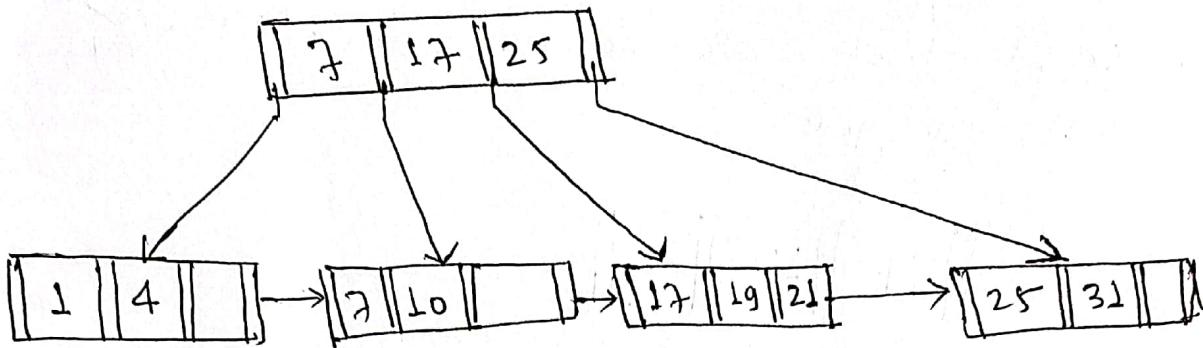
Insert key value 25

Now, rightmost leaf node becomes full. Now splitting the nodes we get



Step -9

Insert key value 19

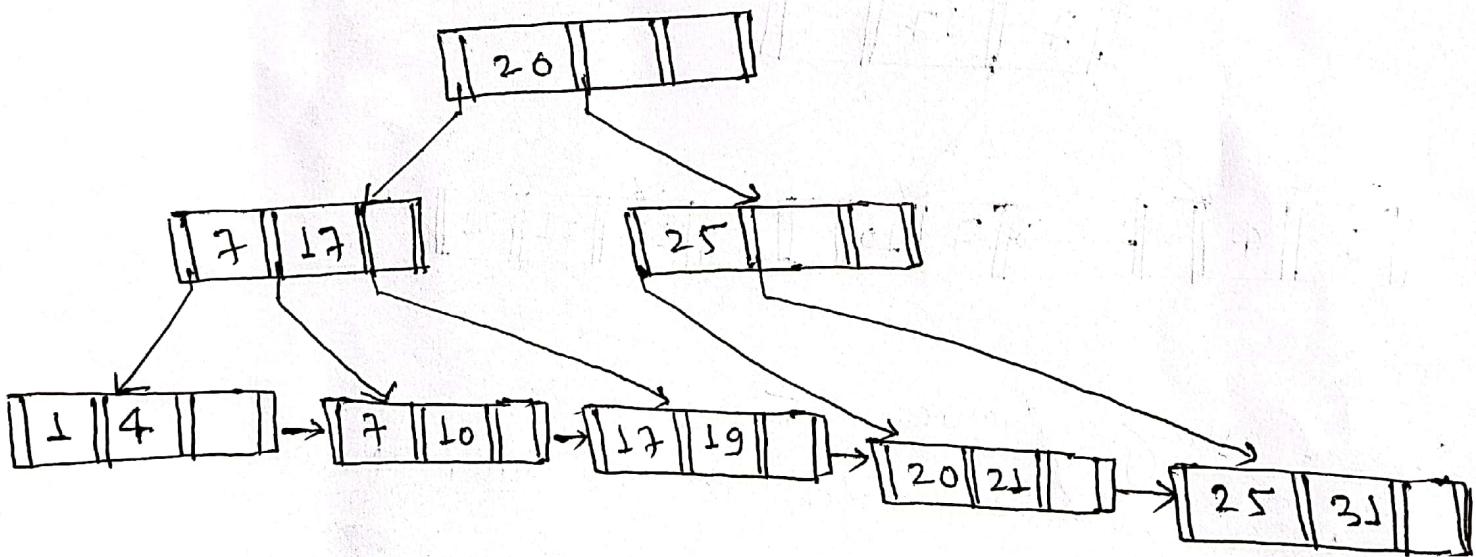


Step -10

Insert key value 20

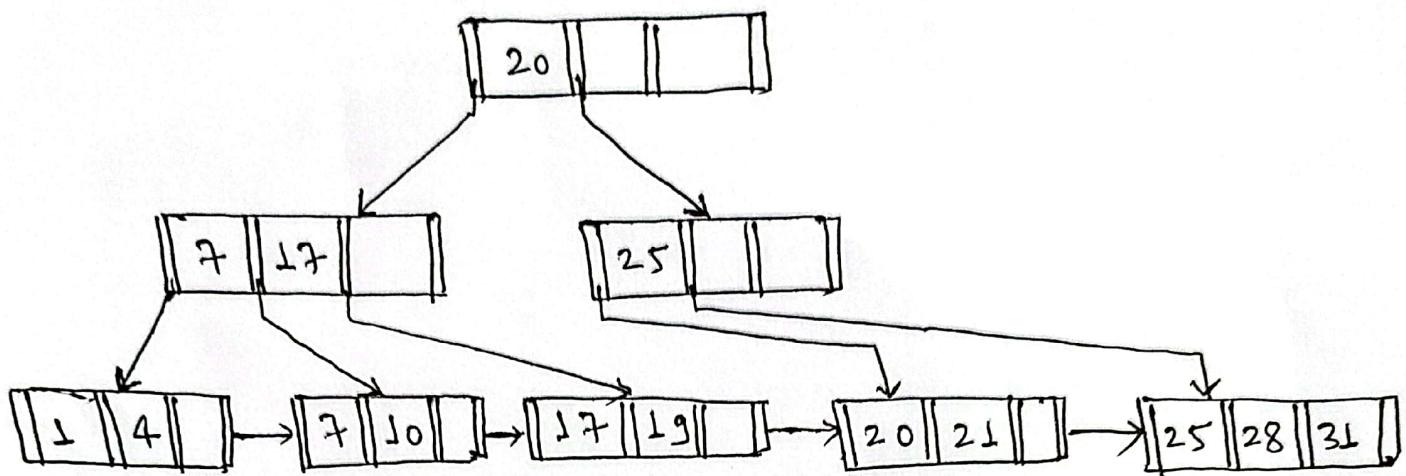
Here, leaf node becomes full, splitting causes its parent node full, Now again parents node, B+ tree becomes.

The ~~leaf~~ leaf nodes splitting



Step - 11

Insert key value 28



Construct a B+ tree for the following set of key values (5, 15, 25, 30, 45, 60, 18, 28).

Assume root tree is initially empty and

values are added in ascending order.

Construct B+ tree for the case where the number of pointers that will fit in one node is three.

Soln:

Construction of B+ tree for order $n=3$.

As we know,

→ Internal nodes (non-leaf nodes) must hold at least $\lceil n/2 \rceil$ and at most n children.
(Pointers to children).

for order $n=3$

Minimum number of pointers in

$$\text{internal nodes} = \lceil 3/2 \rceil = 1.5 \\ = \text{ceiling}(1.5) \\ = 2$$

Maximum number of pointers in internal nodes = 3

Similarly,

→ Each leaf node must hold between $\lceil (n-1)/2 \rceil$ and $(n-1)$ value

Now, minimum number of search key values = $\frac{(3-1)}{2}$
 $= 1$

Maximum number of search key values = 2

→ If the root node is not a leaf it has at least 2 children.

Step 1

Insert key value 5



Step 2

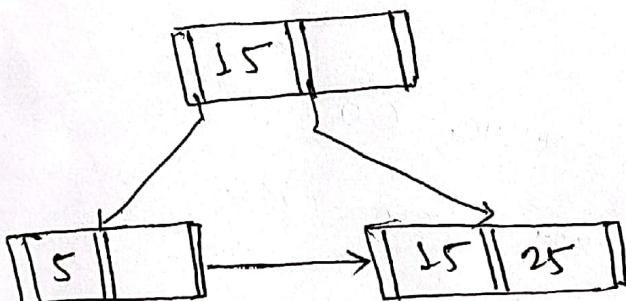
Insert key value 15



Step 3

Insert key value 25

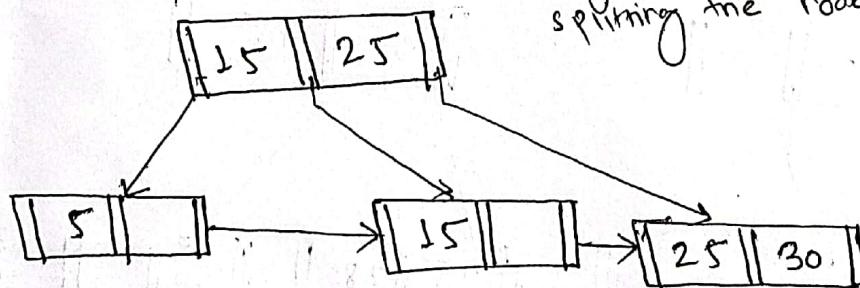
Now, node becomes full, splitting the nodes we get,



Step 4

Insert key value 30

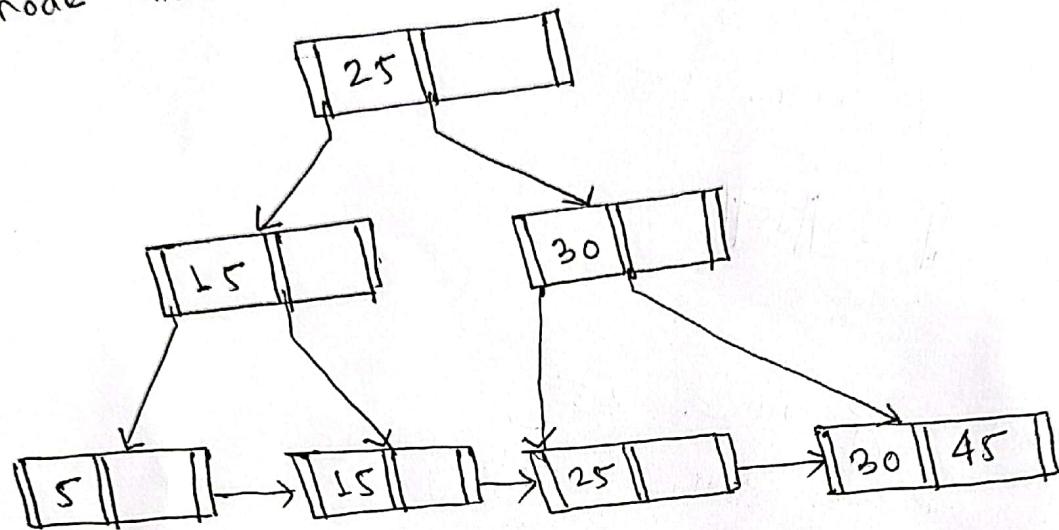
Now, rightmost node becomes full, splitting the nodes we get



Step-5

Insert key value 45

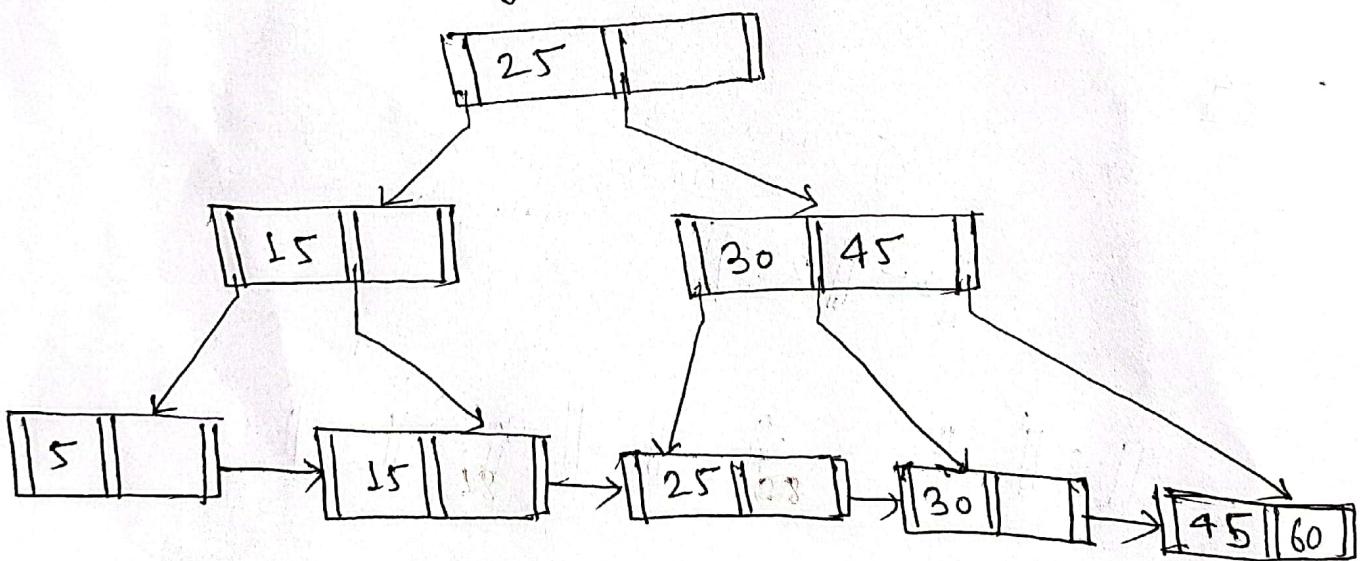
This causes rightmost leaf node full.
Splitting the leaf node causes its parent
node full.



Step-6

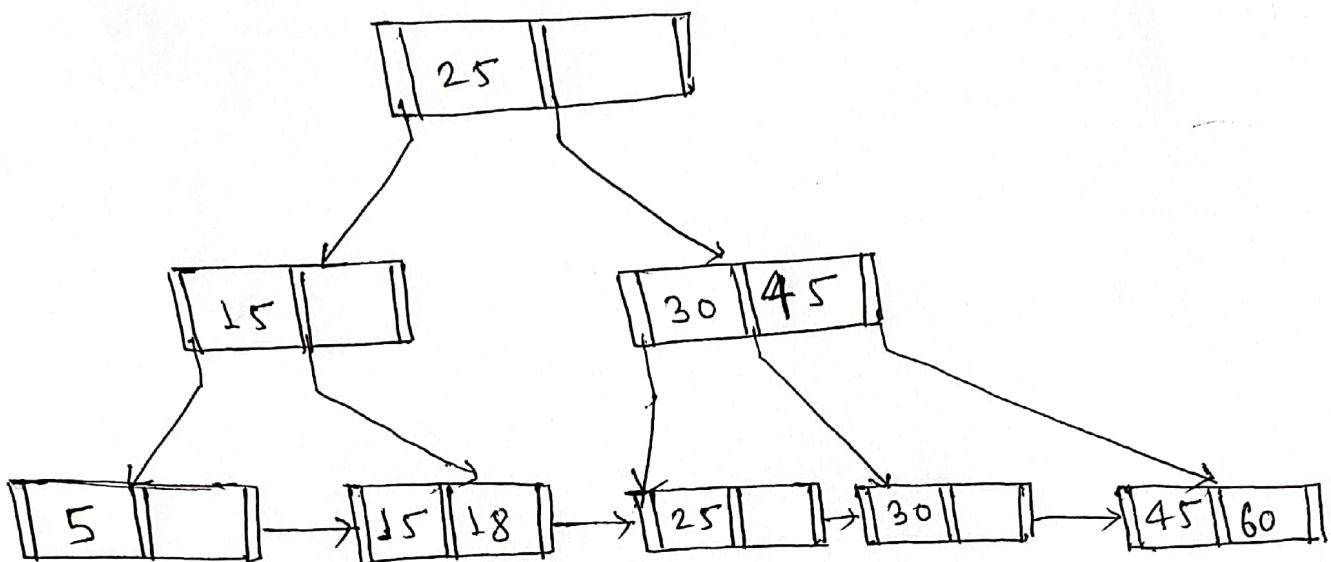
Insert key value 60

This causes rightmost leaf node full, splitting
the nodes we get



Step - 7

Insert key value 18



Step - 8

Insert key value 28

