

Bernoulli Distribution:-

→ what is the difference between Defective & Defects?

Defective means either a product to purchase it or not  
↳ classification

Defects means no. of defects present in the given product  
↳ countable

Ex:- Throwing a die we have a chance saying

$$P(X=2) = 1/6 \longrightarrow p \longrightarrow \text{Success}$$

$$P(\bar{X}=2) = 5/6 \longrightarrow 1-p \longrightarrow \text{Failure}$$

( $\bar{X}$  is called Complement)

So, here ' $X$ ' is Bernoulli Random Variable then our values of  $X$  is 1, 0

	$X$	$P(X)$
Success	1	$p$
Failure	0	$q = 1-p$

So, whenever any variables contains of data YES/NO Considered as Bernoulli variable Ex:- pass/fail in exam

We derived probability mass function [ $X \in \{0,1\}$ ]

$$f(X=x) = p^x (1-p)^{1-x}$$

Substitute the above success, failures values i.e., 0, 1

$$f(X=1) = p^1 (1-p)^{1-1} = p$$

$$f(X=0) = p^0 (1-p)^{1-0} = 1-p$$

Let us find out  $E(X)$ ,  $V(X)$

$$E(X) = \sum_{i=0}^1 x \cdot p(x)$$

put our possible values of ' $x$ '  
i.e., 0, 1

$$= 1 \cdot p + 0(1-p)$$

$$= p + 0 = p \Rightarrow E(X) = p$$

$$\hookrightarrow V(X) = E(X^2) - [E(X)]^2$$

we already known  $E(x) = p$ , let us find out  $E(x^2)$

$$\text{i.e., } E(x^2) = \sum_{i=0}^1 x^2 \cdot p(x)$$

$$= 1^2 \cdot p + 0(p) = p$$

$$\therefore V(x) = p - (p)^2 = p - p^2 = p(1-p) = pq$$

$$\Rightarrow \boxed{E(x) = p, V(x) = p(1-p)}$$

i.e.,  $X \sim \text{Ber}(p)$ , where 'p' stands for parameter