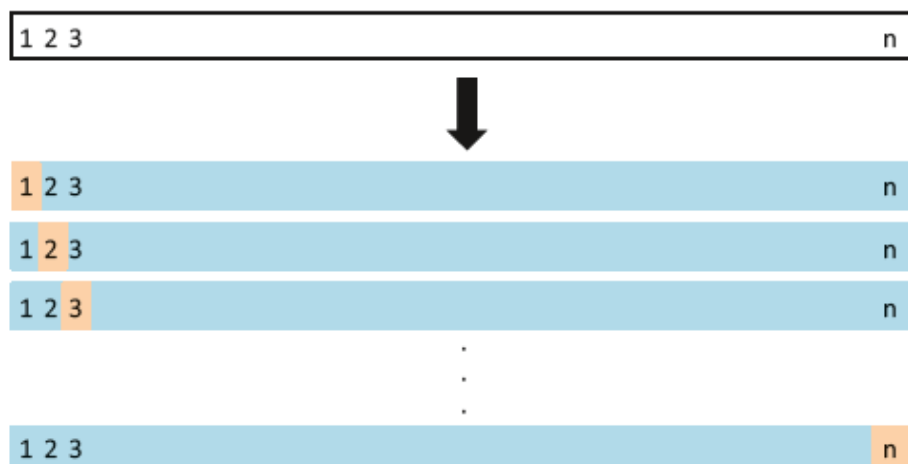


## Leave-One-Out Cross-Validation

LOOCV involves splitting the set of observations into two parts.

1. Create two subsets of comparable size, a single observation  $(x_1, y_1)$  is used for the validation set, and the remaining observations  $\{(x_2, y_2), \dots, (x_n, y_n)\}$  are used for the training set.
2. The statistical learning method is fit on the  $n - 1$  training observations, and a prediction  $\hat{y}_1$  is made for the excluded observation, using its value  $x_1$ .
3. Calculate  $MSE_1 = (y_1 - \hat{y}_1)^2$  provides an approximately unbiased estimate for the test error.
4. We can repeat the procedure by selecting  $(x_2, y_2)$  for the validation data, training the statistical learning procedure on the  $n - 1$  observations  $\{(x_1, y_1), (x_3, y_3), \dots, (x_n, y_n)\}$ , and computing  $MSE_2 = (y_2 - \hat{y}_2)^2$ .
5. Repeating this approach  $n$  times produces  $n$  squared errors,  $MSE_1, \dots, MSE_n$ .
6. The LOOCV estimate for the test MSE is the average of these  $n$  test error estimates:

$$CV_{(n)} = \frac{1}{n} \sum_{i=1}^n MSE_i.$$



Draw backs:

- If the data set is very huge we cannot remove each observation and do the process.
- Time consuming.

Advantages:

- It is less bias and high variance.
- Building the model using  $(n-1)$  observations.
- When compare with validation set approach, LOOCV give same kind of models since every time removing only 1 observation from data set.
- LOOCV is a general method can be used for any model/classifier.