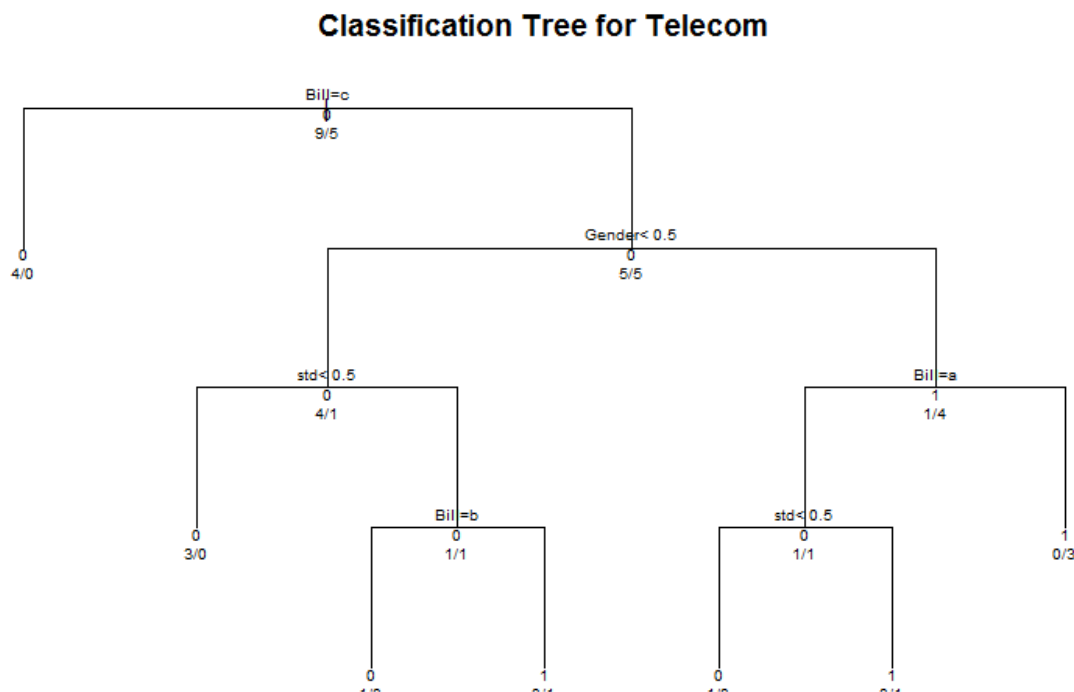


Decision Tree in R - A Telecom Case Study



So we have got the decision tree, now let's see how to interpret the same and also understand how R or any other software draw decision tree, using Entropy and Information gain base algorithm.

Our data looks like >>

There are four variables given in the data:

Monthly Billing : monthly bill of each individual

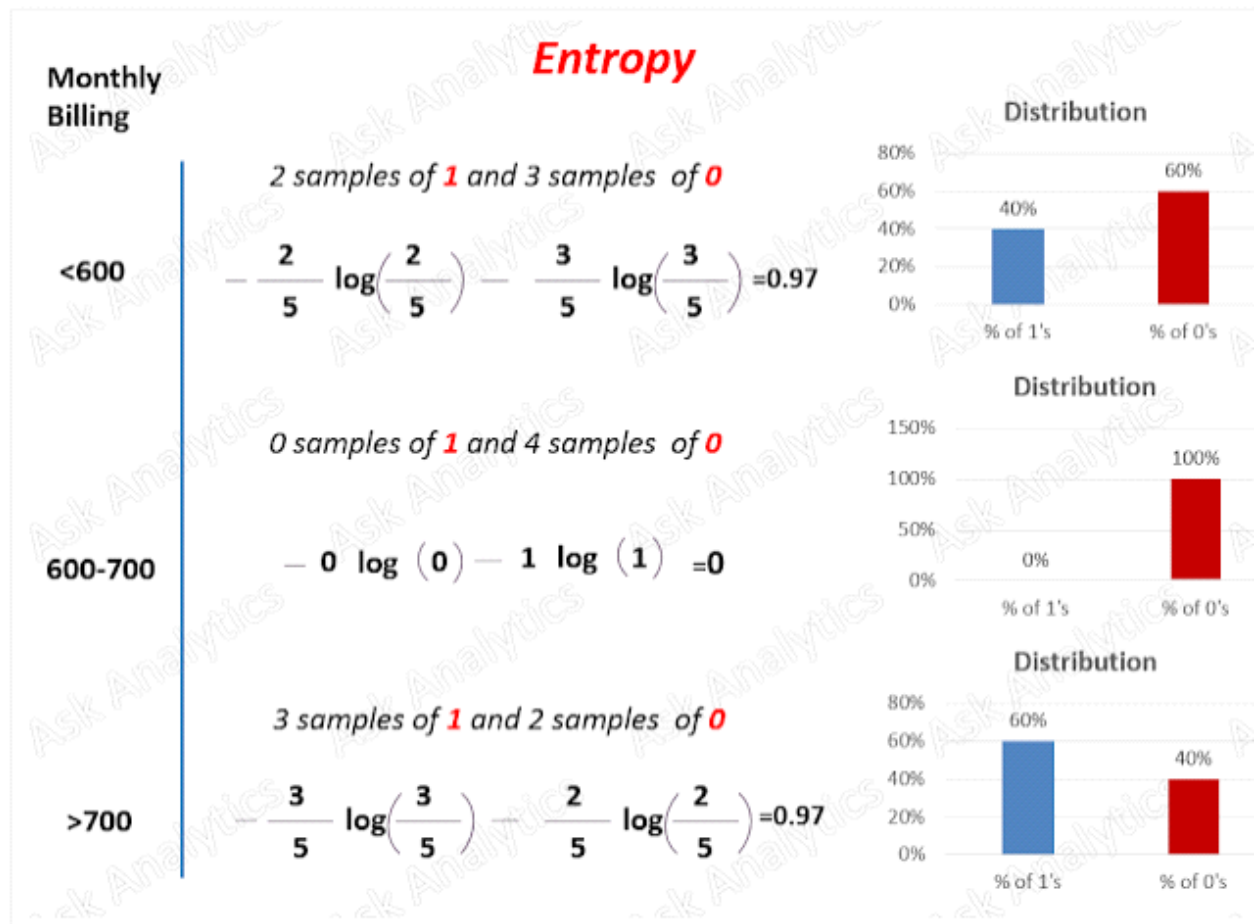
Gender : 1- Male , 0-female

Std : 1- taken std facility, 0 - has not taken std facility

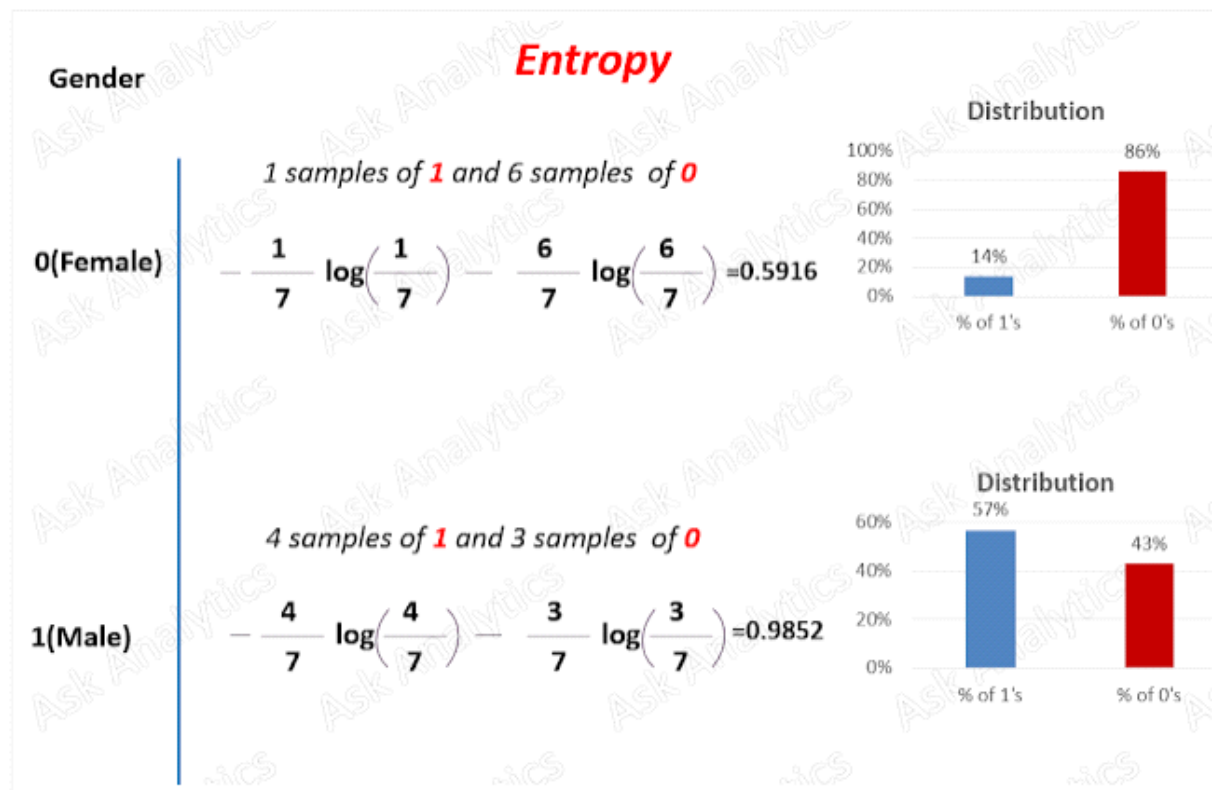
Leave service : 1 - Customer has moved to other telecom operator, 0- continuing services with same operator

It first calculates the entropy of each variable for every bucket :

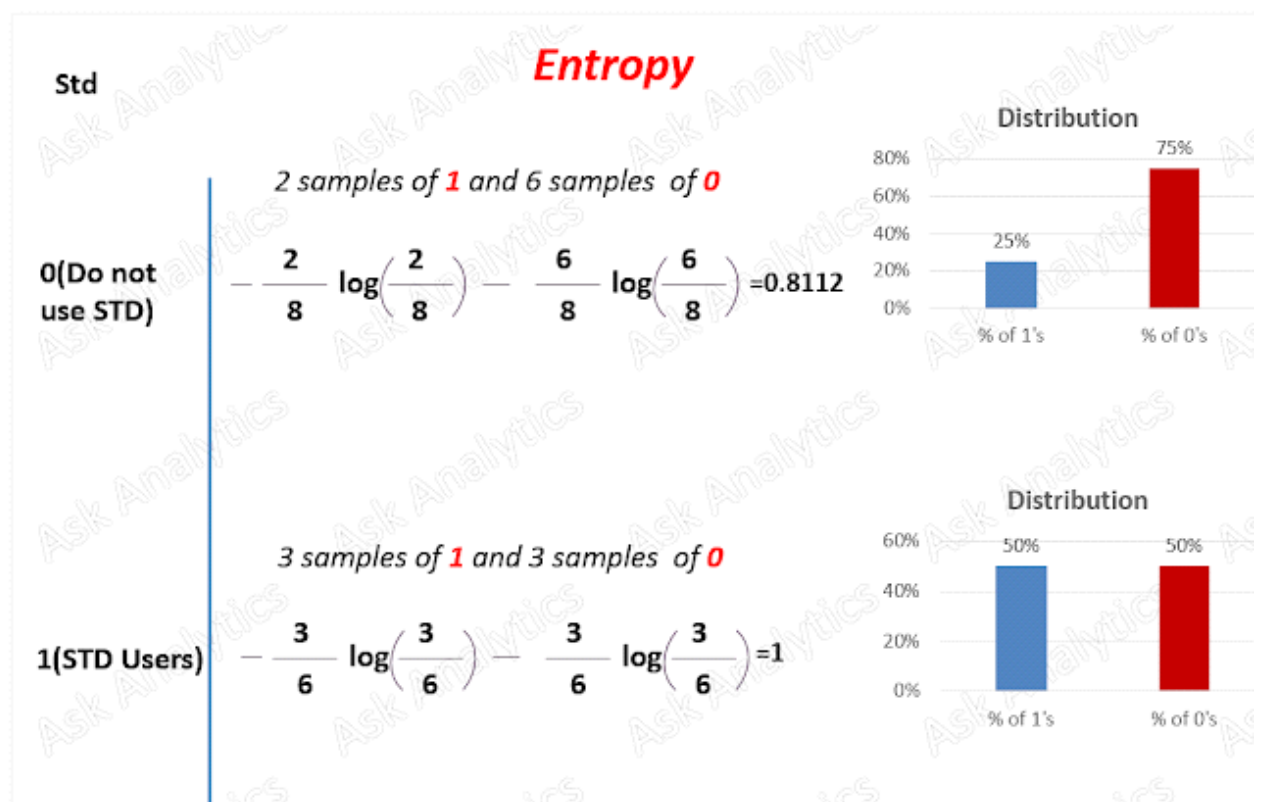
Entropy of Monthly Billing variable:



Entropy of Gender variable :



Entropy of Std variable:



Average Entropy

Variable(Monthly Billing) $:= .357 \cdot .97 + .285 \cdot 0 + .357 \cdot .97 = .6925$

Variable(Gender) $:= .50 \cdot .5916 + .50 \cdot .9852 = .7884$

Variable(Std) $:= .57 \cdot .8112 + .43 \cdot 1 = .892384$

Entropy(Sample) :

36% samples of 1 and 64% samples 0

$$E(S) = -(.36) \cdot \log(.36) - (.64) \cdot \log(.64) = .94268$$

Then it calculates the information gain:

Information Gain : Entropy(Sample) – Average Entropy(Variable)

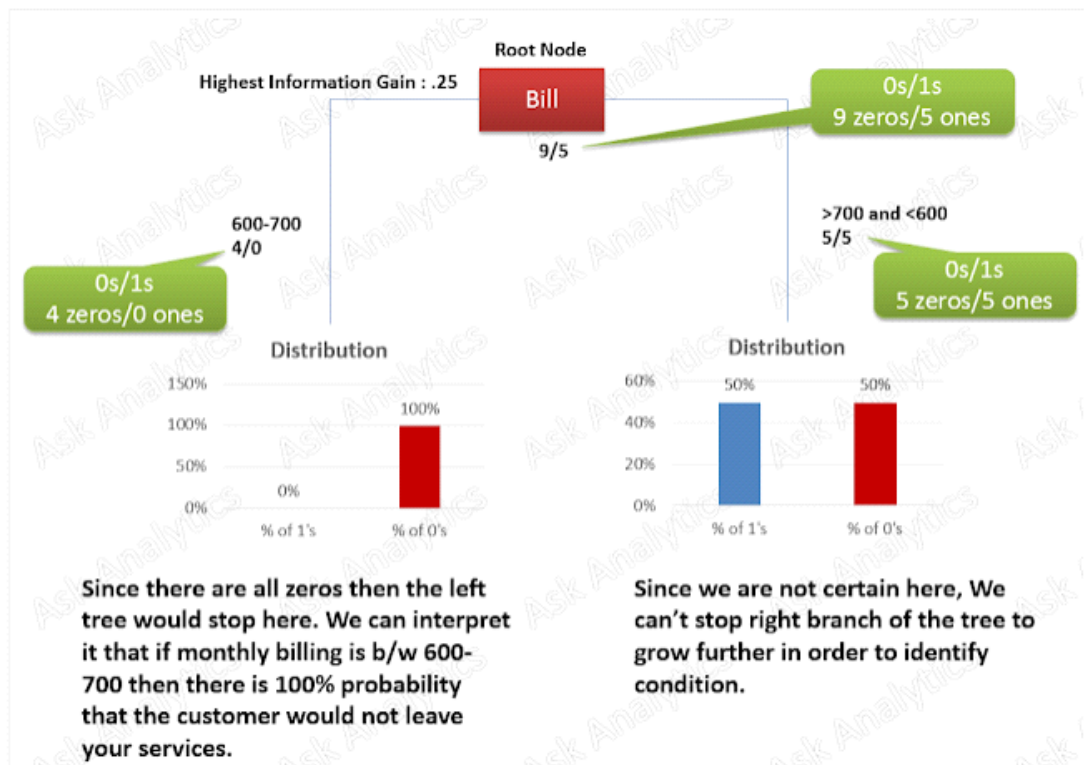
Information Gain(Monthly Billing) $= .94268 - .6925 = .2501$

Information Gain(Gender) $= .94268 - .7884 = .154283$

Information Gain(Std) $= .94268 - .892384 = .0502$

Since the monthly billing has maximum information gain value, it simply means that this variable has maximum ability to reduce the uncertainty and has best prediction ability.

So, monthly billing would be the root variable in decision tree.



Now we have to analyse only observations in which monthly billing is either >700 or <600.

We need to again calculate the information gain to further decide tree node.

Customer	Bill	Gender	Std Calls	Leave Service
1	>700	1	0	1
2	>700	1	1	1
4	<600	1	0	0
5	<600	0	0	0
6	<600	0	1	1
8	>700	1	0	1
9	>700	0	0	0
10	<600	0	0	0
11	>700	0	1	0
14	<600	1	1	1

Entropy

Monthly Billing

	0	1
<600	3	2
>700	2	3

$$=-(3/5)*\log(3/5)-(2/5)*\log(2/5)=.97$$

$$=-(3/5)*\log(3/5)-(2/5)*\log(2/5)=.97$$

Average Entropy

$$=.5*.97+.5*.97=.97$$

Gender

	0	1
0(Female)	4	1
1(Male)	1	4

$$=-(4/5)*\log(4/5)-(1/5)*\log(1/5)=.7219$$

$$=-(1/5)*\log(1/5)-(4/5)*\log(4/5)=.7219$$

Average Entropy

$$=.5*.7219+.5*.7219=.7219$$

Std

	0	1
0(Female)	4	2
1(Male)	1	3

$$=-(4/6)*\log(4/6)-(2/6)*\log(2/6)=.9182$$

$$=-(1/4)*\log(1/4)-(3/4)*\log(3/4)=.8112$$

Average Entropy

$$=.6*.9182+.4*.8112=.875$$

Entropy(Sample) :

50% samples of 1 and 50% samples 0

$$E(S)=-(.5)*\log(.5)-(.5)*\log(.5) = 1$$

Information Gain : Entropy(Sample) – Average Entropy(Variable)

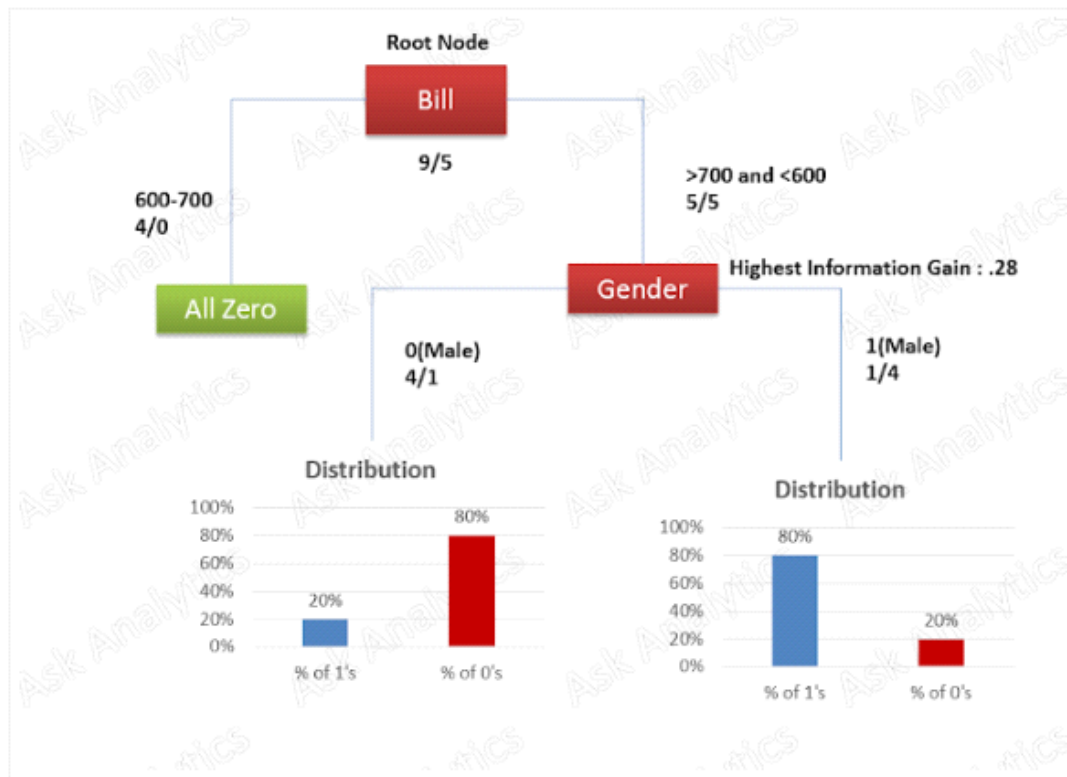
$$\text{Information Gain(Monthly Billing)}= 1 - .97 = .03$$

$$\text{Information Gain(Gender)}= 1 - .7219 = .28$$

$$\text{Information Gain(Std)}= 1 - .875 = .13$$

This time Gender variable has the maximum information gain therefore gender variable would better split the tree node. Hence the tree would be

This time Gender variable has the maximum information gain therefore gender variable would better split the tree node. Hence the tree would be



We will continue this process at each node to reach to the best separation of 1 and 0.

The final tree after this process would be

