

## **Introduction**

Histogram Equalization is an image processing method which primarily uses the histogram of an image. It is used in order to increase the contrast of the image. In certain grayscale images, all the features are not clearly visible due to the excess of certain grayscale pixels. Therefore, in order to make the image have a better contrast, the pixels between 0 to 255 are distributed in a better manner. A cumulative sum function is useful in order to perform this operation.

## **Algorithm for Histogram Equalization**

**function img\_out = HistoEqualization(img\_in);**

**img\_in is the input image**

**img\_out is the output image**

1. Create a Histogram for the Grayscale Input Image, by which, we have a table which holds values from 0 – 255 (Grayscale Levels), along with the no of pixels for each grayscale value. For ex. If an input image has 20 pixels of grayscale 0, 10 pixels of grayscale 1 and so on.
2. Next, we calculate a table which has the Probability Density (PDF) values. This table stores the information about each grayscale value and its relative no of pixels. For ex. If there are 4000 pixels, and there are 200 pixels of grayscale 0, then its relative value is  $200/4000$  which is 0.05. This is done for each grayscale value from 0-255.
3. After this, we calculate the Cumulative Density (CDF) values. This table stores the cumulative values of the previous table. For ex, in an input image, the Cumulative density table for grayscale 0 has just the probability density value for grayscale 0, but for grayscale 1, has both the values of 0 and 1. And this continues till grayscale value 255
4. Then, in another table, we multiply this cumulative density values with (256-1), as there are 255 values which are not zero.
5. After this, the values are rounded off to perform Quantization
6. This gives us the new histogram after equalization
7. After this, we iterate over the input image and check for the old Intensity levels and then replace it with the new intensity values by looping over two arrays
8. And then, the output image is created

## Result Analysis

The results can be seen in the following images

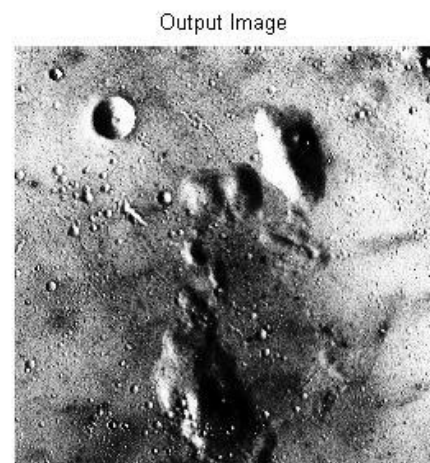
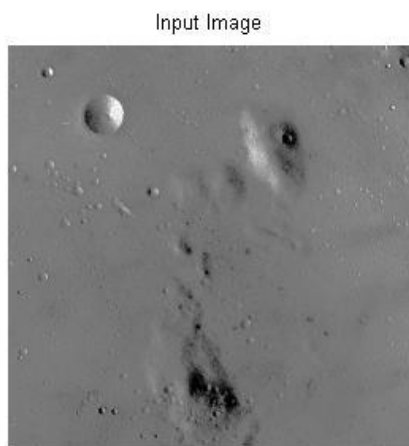


Fig 1. The Input Image

Fig 2. Image after Histogram Equalization

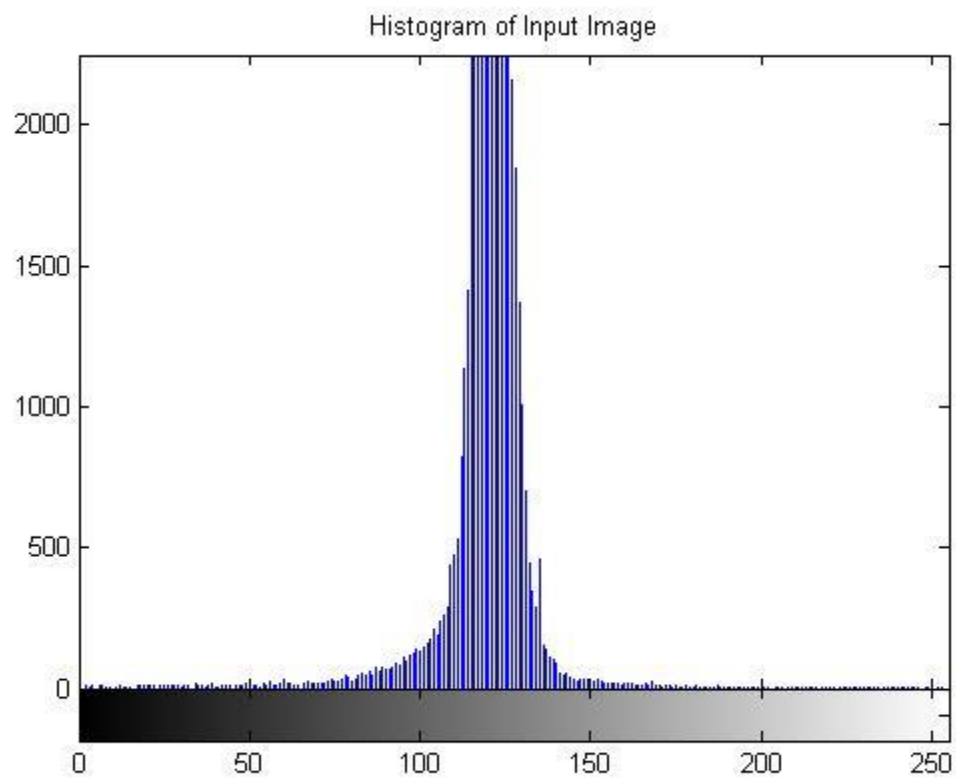


Fig 3. Histogram of Input Image

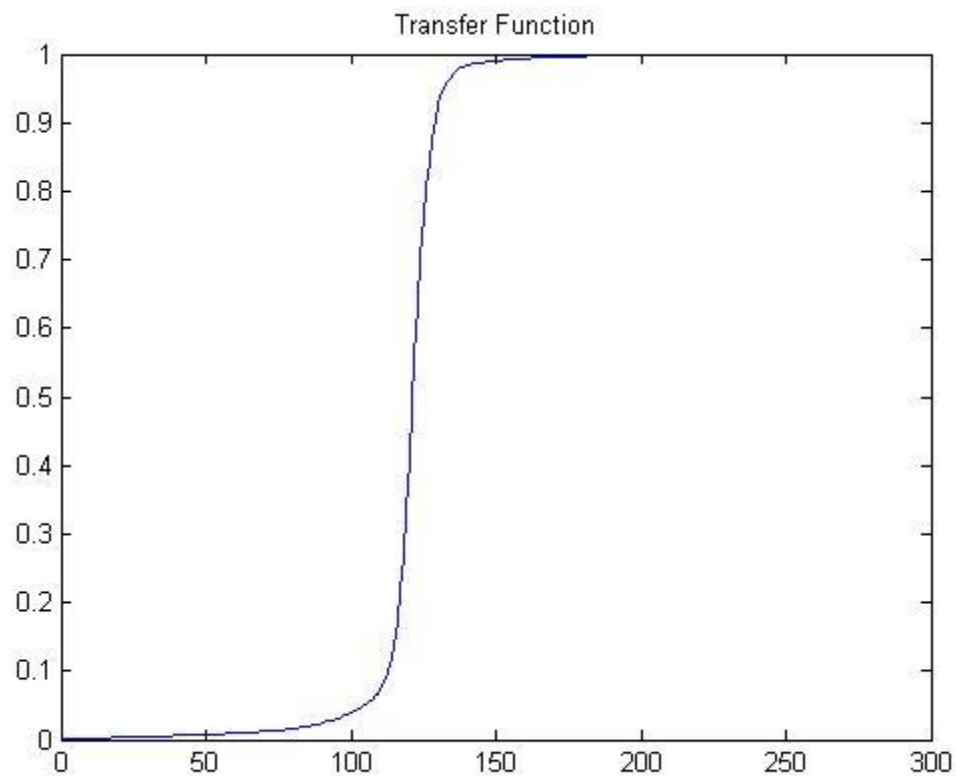


Fig 4. Transfer Function used

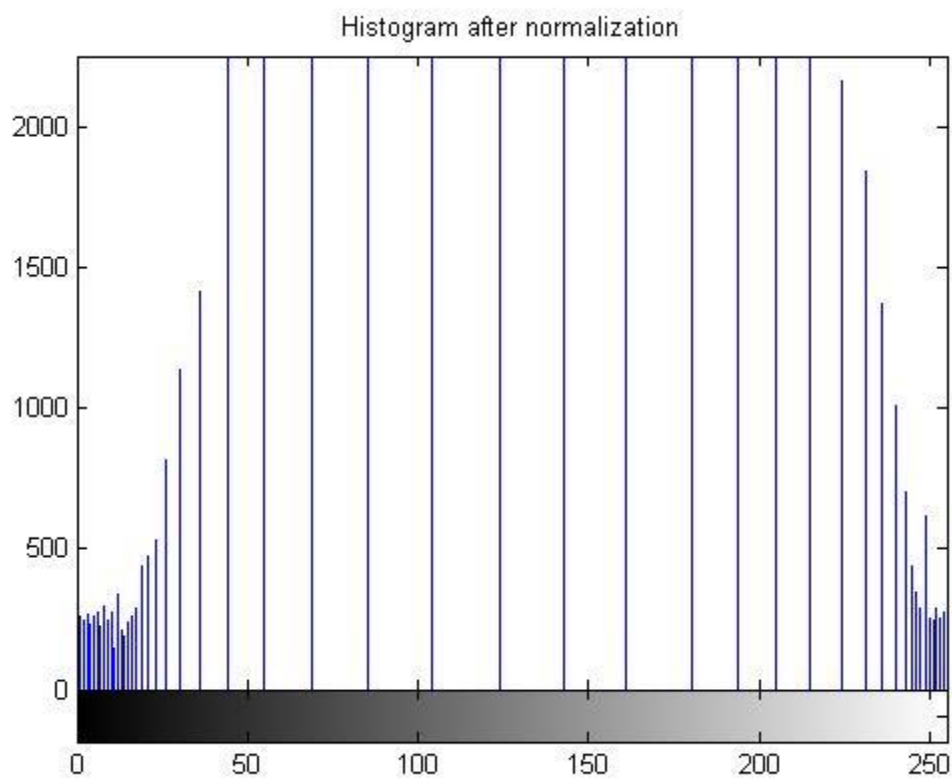


Fig 5. Histogram after the equalization process

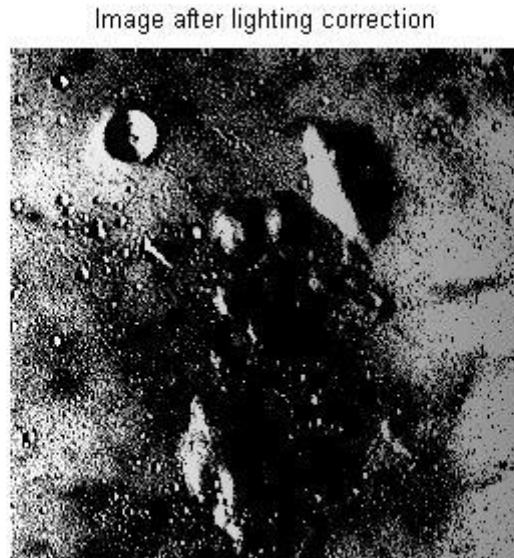


Fig 6. Image after Lighting Correction

The results can be analyzed as follows:

- Fig 1. Shows the Input Image, which is not very clear and not distinct
- But Fig 2. Which shows the Output Image (After Histogram Equalization) is much more distinct
- Fig 3 shows the Histogram of the Input Image
- Fig 4 shows the Transfer Function
- Fig 5 shows the Histogram after Histogram Equalization
- Fig 6 shows the Image after Lighting Correction

As you can see in Fig 1, the input image isn't very clear. But the output image in Fig 2 is very much clear and distinct. As you can see from the Histogram of the Input image in Fig 3, most of the pixels had an intensity between 100 and 150. Therefore, the image did not have a sharp contrast and all the pixels looked the same. However, in the histogram after equalization, you can see that the pixels are more evenly spread out from 25 to 225, therefore there is a much sharper image than the input image.

## Bonus: Lighting Correction

### Algorithm for Lighting Correction:

1. Primarily, Lighting correction works on least square regression
2. The main concept behind this is that, for a group of data points, we try to represent in the form of a straight line in such a way that the least square distance from each of the data points to the line would be a minimum
3. Therefore, the data set can be represented in the form of an equation  $a \cdot X + b \cdot Y + c = Z$
4. Therefore, for the given input image, we need to calculate these co-efficients (a, b, c) to fit the line and data points
5. So, we take the x-axis co-ordinates of all values in the input image into the X vector
6. All the y-axis co-ordinates of the input image in the Y vector
7. And the pixel intensities in the vector of Z

8. But, in order to find the inverse, we need to treat the  $(ax+by+c = z)$  as a system, so we club the x and y co-ordinates into the same matrix (X)
9. So, in order to solve for the vector which has the co-efficients of (a, b, c) we can employ the formula  $\text{inv}(X'X) * X'Y$
10. Where X is a matrix which is of the form  $[1 \times (1) \ y \ (1); 1 \times (2) \ y \ (2); \dots\dots]$  and Y is a matrix with the pixel intensities of the entire input image
11. Solving this set of equations using the Matrix method, we obtain a vector with the values of (a, b, c)
12. Once we have these values, we take each pixel of the input image and then subtract  $(ax+by+c)$  from each pixel
13. Thus, we obtain the new image which has been corrected for lighting

Fig 6 shows the Output Image after Lighting Correction. This is done using the Linear Method. A quadratic method of correction would have been a better solution.