

Problem Statement

(30 points) Harris Corner Detection.

Input image: 2/data/boat.mat.

Assume the pixel dimensions to be equal along both axes, i.e., assume an aspect ratio of 1:1 for the axes. Shift and rescale the intensities in the image to lie within the range $[0, 1]$. Implement the Harris corner detector algorithm. The parameters underlying this algorithm are: two Gaussian smoothing levels involved in computing the structure tensor, the constant k in the corner-ness measure. Tune these three parameters to get the best results.

1. Write a function `myHarrisCornerDetector.m` to implement this.
2. Display the derivative images, corresponding to the derivatives along the X and Y axes.
3. Display the images (along with a colormap) of the two eigenvalues of the structure tensor, evaluated at each pixel.
4. Display the image (along with a colormap) of the Harris corner ness measure. Positive values in this image must correspond to a corner structure in the image.
5. Report all three parameter values used.

Code

Harris Corner Detection Code

```
1 function [outputImage, H, Ix, Iy, A,B,C] =  
    myHarrisCornerDetection(inputImage, sigma1, sigma2, k)  
2  
3     W = 5;  
4  
5     h = fspecial('gaussian', [2, 2], sigma1);  
6     inputImage = imfilter(inputImage, h);  
7     FilterX = [-1 0 1;-2 0 2;-1 0 1];  
8     FilterY = FilterX';  
9     Ix = imfilter(inputImage, FilterX);  
10    Iy = imfilter(inputImage, FilterY);  
11  
12  
13  
14    Ix2 = Ix.^ 2;  
15    Ixy = Ix.* Iy;  
16    Iy2 = Iy.^ 2;
```

```

17
18     h = fspecial('gaussian', [W, W], sigma2);
19
20     A = imfilter(Ix2, h);
21     B = imfilter(Ixy, h);
22     C = imfilter(Iy2, h);
23
24     M1 = (A .* C) - B .^ 2;
25     M2 = (A + C) .^ 2;
26     H = M1 - (k * M2);
27
28     % imregional max used for non-maximal supression and the
        product for the cornerness measure
29     corners = imregionalmax(H) .* (H > 0.1);
30     outputImage = corners;
31 end

```

Main Script

```

1 %% MyMainScript
2
3 tic;
4 %% Your code here
5 boat_struct = load(' ../data/boat ');
6 boat = myLinearContrastStretching(boat_struct.imageOrig);
7 [corners, h, Ix, Iy, A, B, C] = myHarrisCornerDetector(boat,
    0.7, 2, 0.03);
8 figure(1);
9 imshow(boat, []);
10 colorbar;
11 hold on;
12 [row, col] = find(corners);
13 plot(col, row, 'r*');
14
15 figure(2)
16 subplot(121)
17 imshow(Ix)
18 title('I_x: X Derivative of Image');
19 colorbar;
20
21 subplot(122)
22 imshow(Iy)
23 title('I_y: Y Derivative of Image');
24 colorbar;
25
26 [eig1, eig2] = myFindEigenValue(A,B,C);
27 figure(3)
28 subplot(121)
29 imshow(eig1)

```

```

30 colorbar;
31 title('EigenValue Images(I)');
32
33 subplot(122)
34 imshow(eig2)
35 title('EigenValue Images (II)');
36 colorbar;
37
38 figure(4)
39 imshow(h)
40 title('Corners Measure');
41 colorbar;
42 toc;

```

Implementation Details

Firstly the image was smoothed with a Gaussian filter of size $[W, W]$ and variance σ_{smooth} . Then the X and Y Derivatives of the image (I_x and I_y) were calculated by filtering the image with the Sobel operators for X and Y axis respectively.

For boundary conditions i.e. the points where mask lied outside the image, the rest of the image pixels were considered zero (Dirichlet boundary conditions). Then I_x^2 , I_y^2 , I_{xy} images were calculated using the derivatives and another Gaussian window of size $[W1, W1]$ and variance $\sigma_{autocorrelation}$ was applied to these images. Dirichlet boundary conditions as explained above were used. Next for each pixel, cornerness was measured:

$$\text{Cornersness} = \lambda_1 \lambda_2 - k(\lambda_1 + \lambda_2)^2$$

$$\text{Cornersness} = \text{Det}(A) - k(\text{Trace})^2$$

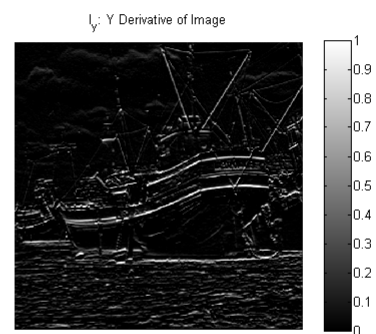
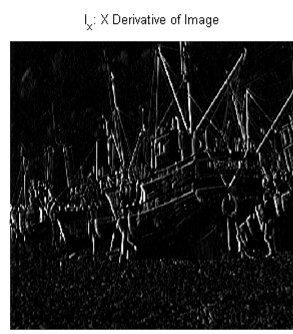
$$\text{Cornersness} = (I_x^2 I_y^2 - I_{xy}^2) - k(I_x^2 + I_y^2)^2$$

After thresholding the cornerness image with parameter ϵ , and non maximum suppression, we get the resulting corners as shown in the next section.

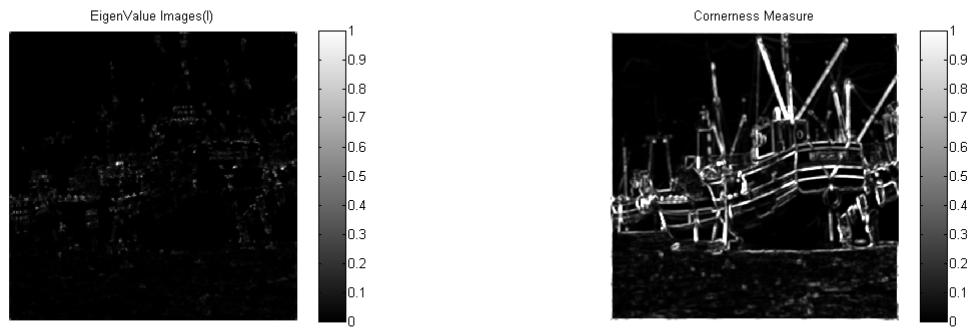
Result Images



Final Corners in the image



Derivative of Image along X and Y Axis respectively



Eigenvalues of structure tensor



Cornerness Measure

Optimum Parameters

Gaussian Mask for Smoothing the image: Window Size: [5 5], Variance = 0.7

Gaussian Mask for Calculating I_x^2, I_{xy}, I_y^2 : Window Size: [5 5], Variance = 2

k used for Cornerness Measure: 0.03

ϵ i.e. Theshold Parameter: 0.1

