

## Problem Statement

### (30 points) Harris Corner Detection.

*Input image: 2/data/boat.mat.*

Assume the pixel dimensions to be equal along both axes, i.e., assume an aspect ratio of 1:1 for the axes. Shift and rescale the intensities in the image to lie within the range  $[0, 1]$ . Implement the Harris corner detector algorithm. The parameters underlying this algorithm are: two Gaussian smoothing levels involved in computing the structure tensor, the constant  $k$  in the corner-ness measure. Tune these three parameters to get the best results.

1. Write a function `myHarrisCornerDetector.m` to implement this.
2. Display the derivative images, corresponding to the derivatives along the X and Y axes.
3. Display the images (along with a colormap) of the two eigenvalues of the structure tensor, evaluated at each pixel.
4. Display the image (along with a colormap) of the Harris corner ness measure. Positive values in this image must correspond to a corner structure in the image.
5. Report all three parameter values used.

## Code

### Harris Corner Detection Code

```
1 function [outputImage, H, Ix, Iy, A,B,C] =  
    myHarrisCornerDetection(inputImage, sigma1, sigma2, k)  
2  
3     W = 5;  
4  
5     h = fspecial('gaussian', [2, 2], sigma1);  
6     inputImage = imfilter(inputImage, h);  
7     FilterX = [-1 0 1;-2 0 2;-1 0 1];  
8     FilterY = FilterX';  
9     Ix = imfilter(inputImage, FilterX);  
10    Iy = imfilter(inputImage, FilterY);  
11  
12  
13  
14    Ix2 = Ix.^ 2;  
15    Ixy = Ix.* Iy;  
16    Iy2 = Iy.^ 2;
```

```

17
18     h = fspecial('gaussian', [W, W], sigma2);
19
20     A = imfilter(Ix2, h);
21     B = imfilter(Ixy, h);
22     C = imfilter(Iy2, h);
23
24     M1 = (A .* C) - B .^ 2;
25     M2 = (A + C) .^ 2;
26     H = M1 - (k * M2);
27
28     % imregional max used for non-maximal supression and the
        product for the cornerness measure
29     corners = imregionalmax(H) .* (H > 0.1);
30     outputImage = corners;
31 end

```

### Main Script

```

1 %% MyMainScript
2
3 tic;
4 %% Your code here
5 boat_struct = load(' ../data/boat ');
6 boat = myLinearContrastStretching(boat_struct.imageOrig);
7 [corners, h, Ix, Iy, A, B, C] = myHarrisCornerDetector(boat,
    0.66, 1, 0.01);
8 imshow(boat, []);
9 hold on;
10 [row, col] = find(corners);
11 plot(row, col, 'r*');
12 figure(2)
13 subplot(121)
14 imshow(Ix)
15 title('I_x: X Derivative of Image');
16
17 subplot(122)
18 imshow(Iy)
19 title('I_y: Y Derivative of Image');
20
21 [eig1, eig2] = myFindEigenValue(A,B,C);
22 figure(3)
23 subplot(121)
24 imshow(eig1)
25 title('EigenValue Images(I)');
26 subplot(122)
27 imshow(eig2)
28 title('EigenValue Images (II)');
29

```

## Implementation Details

Firstly the image was smoothed with a Gaussian filter of size  $[W, W]$  and variance  $\sigma_{smooth}$ . Then the X and Y Derivatives of the image ( $I_x$  and  $I_y$ ) were calculated by filtering the image with the Sobel operators for X and Y axis respectively.

**For boundary conditions** i.e. the points where mask lied outside the image, the rest of the image pixels were considered zero (Dirichlet boundary conditions). Then  $I_x^2$ ,  $I_y^2$ ,  $I_{xy}$  images were calculated using the derivatives and another Gaussian window of size  $[W1, W1]$  and variance  $\sigma_{autocorrelation}$  was applied to these images. Dirichlet boundary conditions as explained above were used. Next for each pixel, cornerness was measured:

$$\text{Cornerness} = \lambda_1 \lambda_2 - k(\lambda_1 + \lambda_2)^2$$

$$\text{Cornerness} = \text{Det}(A) - k(\text{Trace})^2$$

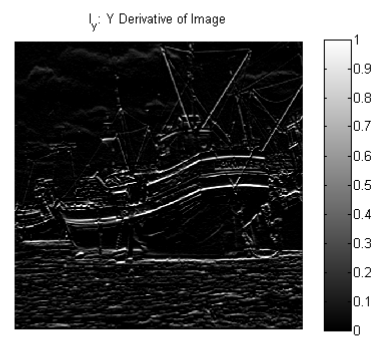
$$\text{Cornerness} = (I_x^2 I_y^2 - I_{xy}^2) - k(I_x^2 + I_y^2)^2$$

After thresholding the cornerness image with parameter  $\epsilon$ , and non maximum suppression, we get the resulting corners as shown in the next section.

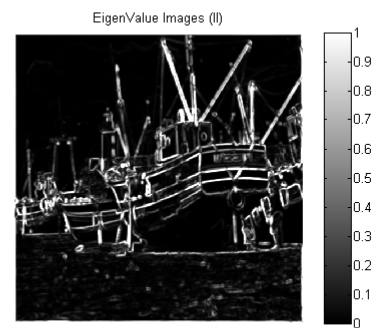
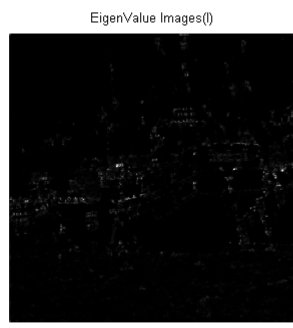
## Result Images



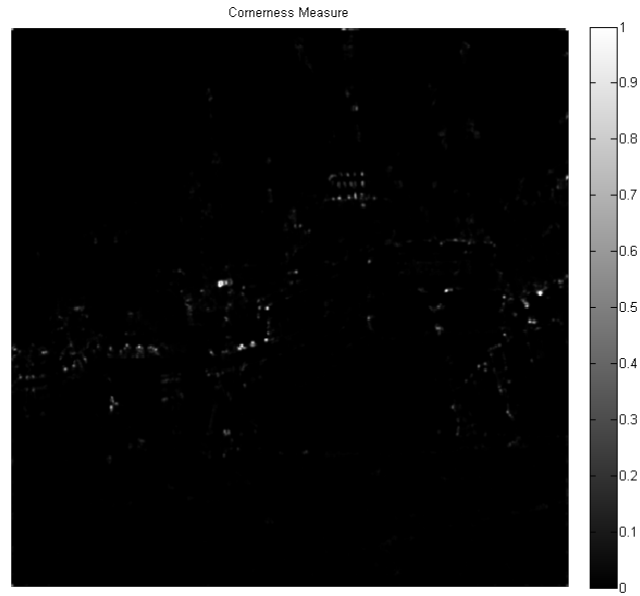
**Final Corners in the image**



Derivative of Image along X and Y Axis respectively



Eigenvalues of structure tensor



**Corners Measure**

## Optimum Parameters

**Gaussian Mask for Smoothing the image:** Window Size: [5 5], Variance = 0.66

**Gaussian Mask for Calculating  $I_x^2, I_{xy}, I_y^2$ :** Window Size: [5 5], Variance = 1

**k used for Cornerness Measure:** 0.01

**i.e. Theshold Parameter:** 0.1