## Zero Knowledge Proofs

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What is it?

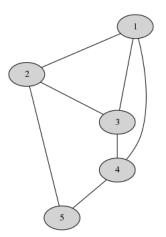
A zero-knowledge proof is an algorithm allowing a party to prove to another party that they have a solution to a given problem, without divulging any details about the solution. It requires no trust between the two parties.

### Example scenario

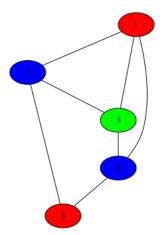
- ► Alice has a hard problem she wishes to solve, say, a graph 3-coloring or a sudoku problem
- ▶ Bob has a solution. He wishes to prove to Alice that he has this solution.
- ► However, he does not want Alice to know the solution immediately
- ► He can use a zero-knowledge proof!

Three-coloring a graph (so that no two adjacent nodes have the same color) is a hard problem.

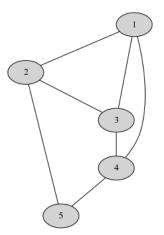
Alice has such a graph



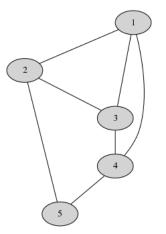
Bob has a solution.



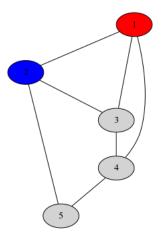
Alice draws the graph on a piece of paper and gives it to Bob, who goes into another room.



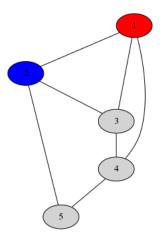
He colors it in, and then covers each node. He comes out of the room.



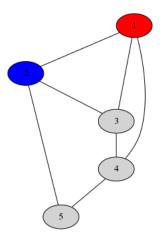
Alice now requests two adjacent nodes be uncovered.



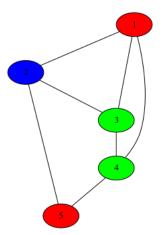
This is done in sight of Alice, so there can be no tampering of the colors.



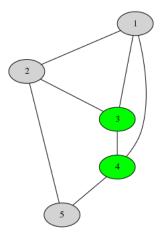
Alice can easily verify that the two adjacent nodes have a different color.



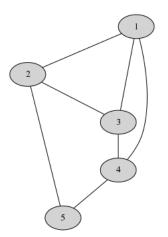
There's still a chance Bob's solution is wrong, from Alice's point of view



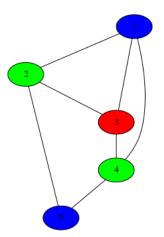
For the given wrong solution, Alice would have to choose the following nodes to detect the deception



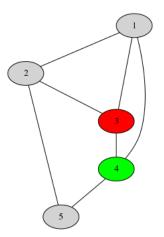
So, we try again



Bob first permutes his coloring,



Bob first permutes his coloring, and Alice requests two adjacent nodes to be uncovered



Each round, Alice has a chance of revealing a deception.

As the number of rounds increases, Alice can become sure that there isn't any and that Bob has a correct solution

At the same time, each round, Alice only sees the information "these two nodes have different colors, as they should". No additional information about the coloring is leaked.

#### Issues

- ► This requires physical presence
- ► This requires physical trust (i.e. that Alice will not simply snatch the covered graph and uncover it herself)
- ► This is not scalable

### Doing this the cryptographic way

We use hashes and nonces to make *commitments*. For each node, Bob chooses a random *nonce*, and hashes the concatenation of the nonce with the color. He shares these hashes with Alice. When he has to reveal the colors for two nodes, he simply reveals the nonces and colors for those nodes. Alice can verify that they match the hash. It is hard for Bob to fake values that produce a hash, so this has the same effect as covering the colors on a piece of paper – it can't be tampered with.

The algorithm is similar. Bob permutes the solution, and makes commitments to each individual cell. Alice asks him to reveal a single row, column, or 3x3 sub-square. If the row/column/subsquare contains pre-set values (from the problem statement), Bob must additionally reveal all other spots on the grid where these values are pre-set.

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							4	
					2	1	8	
7				5				
3	2							
			1		4			9
					8			
	4	1		6				
				3				5

Alice then verifies if the row/column/subsquare has all 9 numbers in it, and if the pre-set values match up.

### Demo

http://manishearth.github.io/netsec-assignments/zkp.html

There is a general algorithm that lets one do a zero-knowledge proof for almost any problem. We've analysed this in depth in http://manishearth.github.io/blog/2016/03/05/exploring-zero-knowledge-proofs/

Using this algorithm, one can actually use zero knowledge proofs with bitcoin for securely swapping information for money. Bob can sell his solution to Alice without any trust required – Alice will not lose money if the solution is wrong, and Alice cannot see the solution unless Bob gets the money.

To do this, Bob first hashes his solution S to get hash H and shares this hash. A program is written which can verify the following *compound* statement:

- ► *S* is a solution to Alice's problem
- ▶ *H* is the hash of *S*

Using the general zero-knowledge proof algorithm, a zero-knowledge proof is executed with this program, and Alice is convinced that Bob has such a solution.

Now, Bob simply needs to securely swap the pre-image of H (that is, S) with Alice. The Bitcoin protocol can do this for us.

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Instead, we make the script two-fold, as "whoever can sign this transaction with the private key corresponding to the receiver's address, \*and\* has the pre-image of H".

The moment Bob attempts to take the money by providing the pre-image of H, this pre-image will be visible to the Bitcoin network and thus Alice. Since hashes are hard to fake, this will be the solution.

### Further reading

- http://manishearth.github.io/blog/2016/03/05/exploring-zero-knowledge-proofs/
- https://bitcoincore.org/en/2016/02/26/zero-knowledgecontingent-payments-announcement/
- https://people.xiph.org/~greg/simple\_verifyable\_execution.txt
- ► https://github.com/scipr-lab/libsnark

# Thank you!