



FUNCTIONS AS OBJECTS



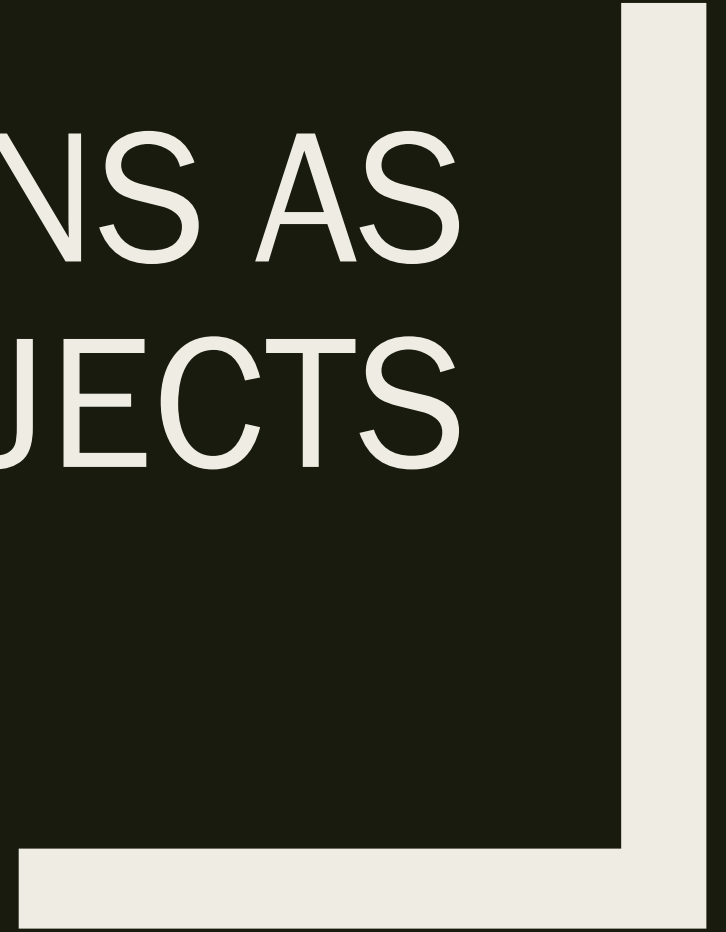
Brief Recap

- More on Classes
 - Class Variable
 - Private Variable
 - Functions: getattr, setattr
 - Destructors
- Python Iterables
 - Tuples
 - Dictionaries

Menu for Today!

- Functions as First Class Objects
- Functional Programming: map, filter and reduce
- List Comprehensions

FUNCTIONS AS OBJECTS



Are Functions Objects?

Python 3.6
[known limitations](#)

```
1 def add2(n):
2     return(n+2)
3 x = 40
4 y = add2(x)
→ 5 z = [x,y]
```

[Edit this code](#)

Frames

Global frame	
add2	•
x	40
y	42
z	•

Objects

function
add2(n)

list

0	1
40	42

So far, we have considered functions as code
The picture on the right seems to consider them as data

What Can We Do With Objects?

- Assign an object to a variable
- Return an object as the result from a function / method
- Pass an object as a parameter to a function / method
- Build complex structures (like lists) with the object as an element

Can we do all this with Functions?

Yes, we can!!!

Functions are “first class” objects

Assigning Functions to Variables

```
def add(n,m):  
    return (n + m)  
myFunc = add  
myFunc(2,3)
```

Anonymous Functions

- Python allows us to create objects without giving them names

```
myFunc(2, 3 + 5)
```

- How do we create functions without names: lambda

```
lambda n, m: n+m
```

```
myFunc1 = lambda n, m: n + m
```

```
def myAdd(n, m):  
    return(n + m)
```

```
add2 = lambda n : myAdd(n, 2)
```

```
add3 = lambda n : myAdd(n, 3)
```


Calling a Function assigned to a Variable

```
def myAdd(n,m):  
    return(n + m)
```

```
def mySub(n,m):  
    return(n-m)
```

```
myFunc = myAdd
```

```
add2 = lambda n : myFunc(n,2)
```

```
myFunc = mySub
```

```
x = add2(7)
```

At this point, myFunc points to myAdd

Now myFunc points to mySub

Which myFunc will be called?

Returning A Function

```
def addN (n):  
    def tempFn(m):  
        return(m+n)  
    return tempFn
```

```
def addN (N):  
    return (lambda m: add(m,n))
```

#alternate definition

```
add2 = addN(2)  
add3 = addN(3)
```

Passing Functions as Arguments

- Python allows us to pass functions as arguments to other functions

```
def doTwice(f,n):
```

```
    return(f(f(n)))
```

```
doTwice(add2, 5)
```

```
doTwice(add3, 5)
```

```
mult3 = lambda n : n * 3
```

```
doTwice(mult3,5)
```

What Functions Take Other Functions as Arguments?

- Remember map from the expression
`list(map(int,input().split()))`
 - `int` is a function that converts strings to integer
 - So map take a function as an argument
- Functions that take other functions as arguments or return functions as results are called **higher order functions**
- Commonly used higher order functions
 - `map`
 - `filter`
 - `reduce`

`map(fn, iterable1 [,iterable2, ...iterableN])`

- First argument is a function (often called an **transformation** function)
- The second argument is an iterable; could have more arguments
- The map function applies the function provided in the first argument to every element of the iterable provided in the second argument
- Returns a map object
 - *The map object is an iterator that yields items on demands*
 - *You can convert the map object to a list using `list()`*

```
square = lambda x: x * x
a = [1, 2, 3, 4, 5]
b = list(map(square, a))
prod = lambda x,y: x * y
c = list(map(prod, a, a))
```

What is Filtering

```
def isOdd(n):  
    return (n % 2 == 1)  
  
def extractOdd(myList):  
    oddNumber = []  
    for i in myList:  
        if (isOdd(i)):  
            oddNumber.append(i)  
    return(oddNumber)
```

`filter(fn, iterable)`

- First argument is a function that returns a `bool` value (often called a **predicate**)
- The second argument is an iterable
- The map function applies the function provided in the first argument to every element of the iterable provided in the second argument; if the result is `True` (or *truthy*) the element is added to resulting `filter` object
- Returns a `filter` object
 - *The `filter` object is an iterator that yields items on demands*
 - *You can convert the `filter` object to a list using `list()`*
- `filter` is an in-built function and often faster than the corresponding loop based implementation

```
def isOdd(n):  
    return (n % 2 == 1)  
  
extractOdd = lambda x: filter(isOdd,x)
```

Implementing Accumulator Pattern

- `map` and `filter` work on individual elements of an iterable (list)
- Often, we need to work with multiple elements of a list
 - *Examples include summing a list or find the max of a list*
- Broadly, we want to analyze a recursive structure and combine the results using a combining functions
- This pattern is also called fold, reduce or aggregate

```
def findMax(myList):  
    max = None  
    for i in myList:  
        if (i > max):  
            max = i  
    return(max)
```

```
def sum(myList):  
    sum = 0  
    for i in myList:  
        sum = sum + i  
    return(sum)
```


reduce(fn, iterable, initialiser)

- Defined in functools library

```
import functools
```

- Arguments:

- *First argument is a function of two variable*
- *The second argument is an iterable*
- *The third (optional) argument is an initializer*

- Semantics:

- *Apply a function to the first two items in an iterable and generate a partial result.*
- *Use that partial result, together with the third item in the iterable, to generate another partial result.*
- *Repeat the process until the iterable is exhausted and then return a single cumulative value.*
- *If you supply a value to `initializer`, then `reduce()` will feed it to the first call of function as its first argument.*

reduce(fn, iterable, initializer)

```
def reduce(function, iterable, initializer=None):  
    it = iter(iterable) #construct an iterator  
    if initializer is None:  
        value = next(it)  
    else:  
        value = initializer  
    for element in it:  
        value = function(value, element)  
    return value
```

Using reduce

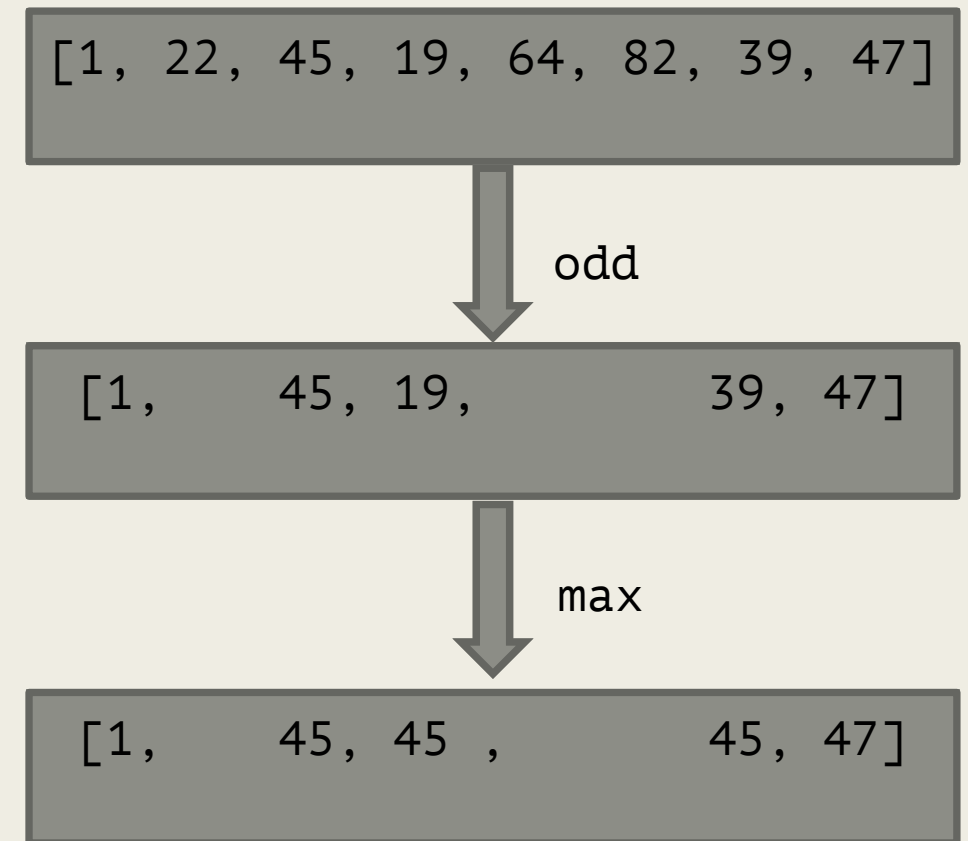
```
mySum = reduce((lambda x,y: x+y), myList)

def max(x,y):
    if x > y:
        return x
    else:
        return y

maxValue = reduce(max, myList)
```

Recall Iteration Patterns (Lecture 5)

- Find the max odd number is a list of positive integers
 - *Filter out odd numbers using enumerations*
 - *Keep track of the max number so far using an accumulator variable*
- We had implemented this using loops and if statements
- A cleaner method is using map-reduce



Some Basic Infrastructure

```
def isOdd(n):  
    return (n % 2 == 1)
```

```
def isEven(n):  
    return (n % 2 == 0)
```

```
def add(m,n):  
    return (m+n)
```

```
def max(m,n):  
    if n == None:  
        return m  
    elif m == None:  
        return n  
    elif m >= n:  
        return m  
    else:  
        return n
```

Putting It All Together

```
inputList = list(map(int, input().split()))  
oddMax = reduce(max, filter(isOdd, inputList), None)
```

- This seems like a lot of work for a simple task
- Why did we do all this work?
- We solved multiple problems at once

```
isEven = lambda n: n % 2 == 0  
sumEven = reduce(add, filter(isEven, inputList), 0)
```

- Bonus: this implementation is faster than using for loops!!

List Comprehension

- Coding using `map`, `reduce` and `filter` is typical of a style of programming called **functional programming**
- Python provides another (sometimes) faster form of iterating through lists called list comprehension
- We often encounter the expression `list(map(myFunc, myList))`
- Python has a recommended syntax for this: List comprehension
`[myFunc(x) for x in myList]`
- What about the expression `list(map(myFunc, filter(myFunc1, myList)))`
`[myFunc(x) for x in myList if myFunc1(x)]`

Some Examples

```
myMatrix = [[1,2,3],[4,5,6],[7,8,9]]
myRowSum = [sum(x) for x in myMatrix]
def transpose(matrix):
    return [[row[i] for row in matrix]
            for i in range(len(matrix[0]))]
myColSum = [sum(x) for x in transpose(myMatrix)]
```