

Manual Calculations for two iterations of RMS optimizer

Sample	$x$	$y$
1	0.2	3.4
2	0.4	3.8
3	0.6	4.2
4	0.8	4.6

Step-1:  $\eta = 0.1$ , epochs = 2,  $m = 1$ ,  $c = -1$ ,  $\beta = 0.9$ ,  $E_m, E_c = 0$ ,  
 $\varepsilon = 10^{-8}$

Step-2:  $itr = 1$

Step-3: Sample = 1

Step-4:  $g_m = -(3.4 - (1)(0.2) + 1)0.2 = -0.84$

$$g_c = -(3.4 - (1)(0.2) + 1) = -4.2$$

Step-5:  $E_m = (0.9)(0) + (1-0.9)(-0.84)^2 = 0.07$

$$E_c = (0.9)(0) + (1-0.9)(-4.2)^2 = 1.764$$

Step-6:  $\Delta m = \frac{-0.1}{\sqrt{0.07 + 10^{-8}}} \quad x - 0.84 = 0.31$

$$\Delta c = \frac{-0.1}{\sqrt{1.764 + 10^{-8}}} \quad x - 4.2 = 0.31$$

Step-7:  $m = m + \Delta m = 1 + 0.31 = 1.31$

$$c = c + \Delta c = -1 + 0.31 = -0.69$$

Step-8: Sample = Sample + 1 = 1 + 1 = 2

Step-9: if (sample > n<sub>s</sub>)  
 go to next step  
 else  
 go to step-4

Step-4:  $g_m = -(3.8 - (1.31)(0.4) + 0.64)0.4 = -1.3$   
 $g_c = -(3.8 - (1.31)(0.4) + 0.64) = -3.9$

Step-5:  $E_m = (0.4)(0.07) + (0.1)(-1.3)^2 = 0.28$   
 $E_c = (0.4)(0.74) + (0.1)(-3.9)^2 = 3.1$

Step-6:  $\Delta m = \frac{-0.1}{\sqrt{0.28 + 10^{-8}}} \times -1.3 = 0.28$

$\Delta c = \frac{-0.1}{\sqrt{0.28 + 10^{-8}}} \times -3.9 = 0.22$

Step-7:  $m = m + \Delta m = 1.31 + 0.28 = 1.34$   
 $c = c + \Delta c = -0.69 + 0.22 = -0.47$

Step-8: sample = sample + 1 = 2 + 1 = 3

Step-9: if (sample > n<sub>s</sub>)  
 step 10

Step-10: itr = itr + 1 = 1 + 1 = 2

Step-11: if (itr > epochs)  
 go to step-12  
 else  
 go to step-3

Step-3: Sample = 1

$$\text{Step-4: } g_m = -(3.4 - (1.50)(0.2) + 0.47)(0.2) = -0.7$$

$$g_c = -(3.4 - (1.50)(0.1) + 0.47) = -7.8$$

$$\text{Step-5: } E_m = (0.9)(0.28) + (0.1)(-0.7)^2 = 0.3$$

$$E_c = (0.9)(3.1) + (0.1)(-3.5)^2 = 4.0$$

$$\text{Step-6: } \Delta m = \frac{-0.1}{\sqrt{0.3 + 10^8}} \times -0.7 = 0.12$$

$$\Delta c = \frac{-0.1}{\sqrt{4.0 + 10^8}} \times -3.3 = 0.17$$

$$\text{Step-7: } m = m + \Delta m = 1.50 + 0.12 = 1.71$$

$$c = c + \Delta c = -0.47 + 0.17 = -0.3$$

$$\text{Step-8: } \text{Sample} = \text{Sample} + 1 = 1 + 1 = 2$$

$$\text{Step-9: } \text{if}(\text{Sample} > n_s)$$

go to step 10

else

go to step 4

$$\text{Step-4: } g_m = -(3.8 - (1.71)(0.4) + 0.3) \times 0.4 = -1.4$$

$$g_c = -(3.8 - (1.71)(0.4) + 0.3) = -3.6$$

$$\text{Step-5: } E_m = (0.9)(0.3) + (0.1)(1.4)^2 = 0.46$$

$$E_c = (0.9)(4.0) + (0.1)(-3.6)^2 = 4.89$$

$$\text{Step-6: } \Delta m = \frac{-0.1}{\sqrt{0.46 + 10^8}} \times -1.4 = 0.2$$

$$\Delta c = \frac{-0.1}{\sqrt{4.89 + 10^8}} \times -3.6 = 0.16$$

Step-7:  $m = m + \Delta m = 1.71 + 0.2 = 1.91$   
 $C = C + \Delta m = -0.3 + 0.16 = -0.14$

Step-8:  $\text{sample} = \text{sample} + 1 = 2 + 1 = 3$

Step-9: if ( $\text{sample} > n_s$ )  
    go to next step  
    else  
        go to step-4

Step-10:  $\text{itr} = \text{itr} + 1 = 2 + 1 = 3$

Step-11: if ( $\text{itr} > \text{epochs}$ )  
    go to next step

Step-12:  $m = 1.91, C = -0.14$