

Manual Calculations for two iterations with first two samples (Momentum optimizer)

Sample	x	y
1	0.2	3.4
2	0.4	3.8

$$V_t = \gamma V_{t-1} - \eta \frac{\partial F(x)}{\partial \theta}$$

$$\theta = \theta + V_t$$

$$\gamma \rightarrow 0.5 - 0.9$$

Step-1: $\eta = 0.1$, $m = 1$, $c = -1$, epochs = 2, $\gamma = 0.9$, $V_m = 0$, $V_c = 0$

Step-2: $it = 1$

Step-3: sample = 1

Step-4: $\frac{\partial E}{\partial m} = -(3.4 - (1)(0.2) + 1)0.2 = -0.84$

$$\frac{\partial E}{\partial c} = -(3.4 - (1)(0.2) + 1) = -4.2$$

Step-5: $V_m = \gamma V_m - \eta \frac{\partial E}{\partial m} = 0.9 \times 0 - (0.1)(-0.84)$

$$V_m = 0.084$$

$$V_c = \gamma V_c - \eta \frac{\partial E}{\partial c} = 0.9 \times 0 - (0.1)(-4.2)$$

$$V_c = 0.42$$

Step-6: $m = m + V_m = 1 + 0.084 = 1.084$

$$c = c + V_c = -1 + 0.42 = -0.58$$

Step-7: sample = 2

Step-8: if (sample ^{2 > 2})

Step 9

else

Step-4

$$\text{Step-4: } \frac{\partial E}{\partial m} = -0.4(3.8 - (1.084)(0.4) + 0.58) = -1.578$$

$$\frac{\partial E}{\partial c} = -(3.8 - (1.084)(0.4) + 0.58) = -3.94$$

$$\text{Step-5: } v_m = \delta v_m - \eta \frac{\partial E}{\partial m}$$

$$v_m = 0.9 \times 0.084 - (0.1)(-1.578) = 0.233$$

$$v_c = \delta v_c - \eta \frac{\partial E}{\partial c} = 0.9 \times 0.42 - (0.1)(-3.94)$$

$$v_c = 0.772$$

$$\text{Step-6: } m = m + v_m = 1.084 + 0.233 = 1.317$$

$$c = c + v_c = -0.53 + 0.772 = 0.192$$

Step-7: Sample = 3

Step-8: if (3 > 2)

Step 9

Step-9: ito = 2

Step-10: if (ito ^{2 > 2} epochs) (x)

go to step-3

Step-3: Sample = 1

$$\text{Step-4: } \frac{\partial E}{\partial m} = -(3.4 - 1.317 \times 0.2 - 0.192)0.2 = -0.588$$

$$\frac{\partial E}{\partial c} = -(3.4 - 1.317 \times 0.2 - 0.192) = -2.944$$

$$\text{Step-5: } V_m = \lambda V_m - \eta \frac{\partial E}{\partial m}$$

$$V_m = 0.9 \times 0.233 + (0.1)(0.588) = 0.2685$$

$$V_c = \lambda V_c - \eta \frac{\partial E}{\partial c}$$

$$= 0.9 \times 0.772 + (0.1)(2.944) = 0.9892$$

$$\text{Step-6: } m = m + V_m = 1.317 + 0.268 = 1.58$$

$$C = C + V_c = 0.192 + 0.989 = 1.18$$

$$\text{Step-7: Sample} = 2$$

$$\text{Step-8: if } (2 > 2)$$

step 9

else

step-4

$$\text{Step-4: } \frac{\partial E}{\partial m} = -(3.8 - 1.58 \times 0.4 - 1.18) \times 0.4 = -0.79$$

$$\frac{\partial E}{\partial c} = -(3.8 - 1.58 \times 0.4 - 1.18) = -1.98$$

$$\text{Step-5: } V_m = \lambda V_m - \eta \frac{\partial E}{\partial m}$$

$$= 0.9 \times 0.26 + (0.1)(0.79) = 0.313$$

$$V_c = \lambda V_c - \eta \frac{\partial E}{\partial c} = 0.9 \times 0.98 + 0.1 \times 1.98 = 1.08$$

$$\text{Step-6: } m = m + V_m = 1.58 + 0.313 = 1.89$$

$$C = C + V_c = 1.58 + 1.08 = 2.26$$

$$\text{Step-7: Sample} = 3$$

$$\text{Step-8: if } (3 > 2) \text{ step 9}$$

$$\text{Step-9: } i = 3$$

$$\text{Step-10: if } (3 > 2)$$

step 11

$$\text{Step-11: } m = 1.89, C = 2.26$$