Regression & Prediction

Theory and Practice with House Prices

Your Name

February 23, 2025

 $\times AI$

Our Housing Journey

- Starting Simple: Foundations
- Expanding the Scope: Complexity
- Refining Precision: Optimization

- Facing Challenges: Pitfalls
- Insights & Next Steps: Applications

Focus

Unpacking King County house prices with rich theory and dual $R/Python\ implementations$

Starting Simple

The Housing Puzzle

- Objective: Decode drivers of house prices in King County—size, location, features
- Regression: A statistical lens linking price (Y) to predictors like size (X)
- Purpose: Explain historical sales patterns and forecast future values for buyers and assessors

Simple Linear Regression: Theory & R

• Theory (p. 141): Models a straight-line relationship: $Y = b_0 + b_1 X + e$

 Assumes linearity and independence—foundation of regression

Random error

```
# R (p. 152 adapted)
simple_lm <- lm(AdjSalePrice ~ SqFtTotLiving, data
= house)
# Output: b_0 ~ base, b_1 ~ price/sq ft</pre>
```



Figure 1: Price vs. Size Fit

Simple Linear Regression: Python

- Practice: Fits price to living space, revealing size's impact
- Key Insight: Positive slope shows larger homes fetch higher prices

```
# Python (p. 152 adapted)
from sklearn.linear_model import LinearRegression
predictors = ['SqFtTotLiving']
outcome = 'AdjSalePrice'
simple_lm = LinearRegression()
simple_lm.fit(house[predictors], house[outcome])
# Example: Intercept ~ base, Coef ~ $ per sq ft
```

Size as a core driver

Finding the Best Fit: Least Squares

- How do we draw that line? We minimize the mess—sum of squared errors
- **Theory**: Finds the line minimizing residual sum of squares: $\sum_{i=1}^{n} (Y_i \hat{Y}_i)^2$
- **How**: Adjusts b_0 and b_1 to reduce prediction errors—optimal for linear fits
- History: Legendre (1805) and Gauss; computationally efficient but outlier-sensitive in small datasets

Expanding the Scope

More Clues: Multiple Linear Regression

Theory: Extends to multiple predictors:

$$Y = b_0 + b_1 X_1 + b_2 X_2 + \cdots + e$$

- Power: Captures combined effects—size, lot, bedrooms—assuming linearity
- Use: Explains complex housing dynamics

Size adds \$229/sq ft

Multiple Linear Regression: Python

- Practice: Models housing with multiple factors
- Key Insight: Negative bedroom coef suggests smaller rooms hurt value

 Bedrooms vs. size tension

Factor Variables: Theory & R

- Theory (p. 163): Encodes categorical variables (e.g., property type) as binary dummies
- Why: Allows non-numeric factors in regression; compares to a reference level
- Example: Single-family vs.

Townhouse effects

```
# R (p. 164)
prop_type_dummies <- model.matrix(~ PropertyType -</pre>
      1, data = house)
# Output: 1 for each type present
```

Type shifts price

Factor Variables: Python

- Practice: Integrates property type into price model
- Key Insight: Townhouses may differ from single-family homes

```
# Python (p. 166 adapted)
import pandas as pd
X = pd.get_dummies(house['PropertyType'], drop_
first=True)
# Drops first level (e.g., Multiplex) as reference
```

Baseline comparison

Nonlinear Fit: Theory & Splines in R

- Theory (p. 187): Nonlinear via polynomial segments joined at knots
- Why: Captures diminishing returns—e.g., small homes gain more per sq ft
- Advantage: Flexible fit without overfitting like high-order polynomials

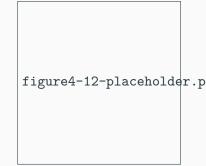


Figure 2: Spline Fit

Nonlinear Fit: Splines in Python

- Practice: Fits nonlinear price trends in zip 98105
- Key Insight: Better matches small vs. large home value shifts

Curves reflect reality

Refining Precision

Model Assessment: Theory

- Theory (p. 153): Measures prediction quality and fit
- RMSE: $\sqrt{\frac{\sum (y_i \hat{y}_i)^2}{n}}$ —average error magnitude
- R^2 : Proportion of variance explained (0-1); higher means better fit
- Use: Guides housing prediction accuracy

Cross-Validation: Theory

- **Theory (p. 155)**: Validates model on unseen data via *k*-fold splits
- **Process**: Divide data, train on k-1, test on 1, repeat, average RMSE
- Why: Ensures predictions generalize beyond training sales—crucial for real estate

Model Selection: Theory & R

- Theory (p. 156): Balances fit vs. complexity—Occam's razor
- AIC:
 2P + n log(RSS/n)—penalizes
 extra predictors
- Goal: Optimal housing model without overkill

Streamlined predictors

Model Selection: Python

- Practice: Automates predictor choice for housing
- Key Insight: Reduces noise, enhances prediction

Focused fit

Weighted Regression: Theory & R

- Theory (p. 159): Weights adjust influence by reliability
- Why: Older sales less relevant—recent data gets priority
- Impact: Refines coefficients for current market

Recent sales emphasized

Weighted Regression: Python

- Practice: Weights tune housing model
- Key Insight: Aligns predictions with market trends

Fresher focus

Facing Challenges

Prediction Limits: Theory

- Theory (p. 161): Extrapolation beyond data fails—e.g., empty lots
- Intervals: Confidence for b_i , wider prediction for \hat{Y}_i
- Why: Uncertainty spikes outside training range—limits housing forecasts

Interpreting Coefficients: Theory

- Theory (p. 171): Coefficients mislead if predictors correlate
- Multicollinearity: Size and bedrooms overlap—unstable fits
- Confounding: Missing location skews results
- Interactions: Size's effect varies by zip—needs modeling

Diagnostics: Theory & R

- Theory (p. 176): Residuals reveal model flaws
- Outliers: Extreme sales (e.g., \$119,748); Influence: Sway points
- Heteroskedasticity: Uneven errors signal gaps



Figure 3: Influence Plot

Diagnostics: Python

- Practice: Identifies \$119,748 as partial sale anomaly
- Key Insight: Diagnostics ensure robust housing predictions

Spots critical flaws

Insights & Next Steps

Housing Insights

- Findings: Linear ties price to size, splines capture nonlinear trends
- Diagnostics: Reveal quirks like partial sales—critical for accuracy
- Application: Real-world tool for buyers, sellers, and assessors

Key Takeaways

- Flexible: Evolves from simple lines to complex curves for housing
- Precise: RMSE and cross-validation ensure reliable price predictions
- Powerful: R and Python implementations unlock data-driven insights

Looking Ahead

- Resources: Statistical Learning (Hastie et al.), Time Series Forecasting (Shmueli)
- Next Steps: Dive into splines, time series for dynamic housing models
- Call: Blend theory and practice for smarter predictions