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## NCERT Discrete

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#### **Question 11.9.3.18:**

Find the sum to n terms of the sequence 8, 88, 888, 8888...

#### **Solution:**

Parameter	Value	description
x(0)	8	First term
x(1)	88	Second term
x(n)	$(\sum_{k=0}^{n} 8(10)^k)u(n)$	General term
S(n)	$S(n) = \sum_{k=0}^{n-1} x(k)$	Sum of n terms

INPUT PARAMETERS

### From (I)

$$s(n) = x(n) * u(n) \tag{1}$$

### Z transform of general term

$$X(z) = \sum_{n=-\infty}^{\infty} \left(\sum_{k=0}^{n} 8(10)^{k}\right) u(n) z^{-n}$$
 (2)

$$X(z) = \sum_{n=0}^{\infty} \left(\sum_{k=0}^{n} 8(10)^{k}\right) z^{-n}$$
 (3)

$$\implies X(z) = \left(\frac{8z^2}{(z-10)(z-1)}\right) \quad |z| > 10 \quad (4)$$

#### From (1), we get

$$\implies S(z) = \left(\frac{8z^2}{(z-10)(z-1)}\right) \left(\frac{1}{z-1}\right) \quad (5)$$

$$S(z) = \left(\frac{8z^2}{(z-10)(z-1)^2}\right) \tag{6}$$

$$s(n) = \frac{1}{2\pi j} \oint_{c} \frac{8z^{2}}{(z-10)(z-1)^{2}} (z^{n-1}) dz$$
(7)

$$s(n) = \frac{1}{2\pi j} \oint_c \left( \frac{800z^{n-1}}{81(z-10)} - \frac{8z^{n-1}}{9(x-1)^2} - \frac{152z^{n-1}}{8(z-1)} \right)$$
(8)

$$\implies s(n) = \lim_{z \to 10} \frac{1}{0!} \left( \frac{800z^{n-1}}{81} \right) - \lim_{z \to 1} \frac{1}{1!} \frac{d}{dz} \left( \frac{8z^{n-1}}{9} \right) - \lim_{z \to 1} \frac{1}{0!} \left( \frac{152z^{n-1}}{8} \right)$$
(9)

$$s(n) = \left(\frac{8}{81}\right) \left(10^{n+1} - 9n - 10\right) \tag{10}$$