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NCERT Discrete

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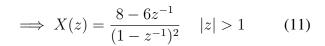
Question 10.5.2.8:

An AP consists of 50 terms of which 3^{rd} term is 12 and the last term is 106. Find the 29^{th} term.

Solution:

Parameter	Value	description
x(2)	12	Third term
x(49)	106	Last term
x(0)		First term
d		Common difference
x(n)	(x(0) + nd)u(n)	general term

TABLE I
INPUT PARAMETERS



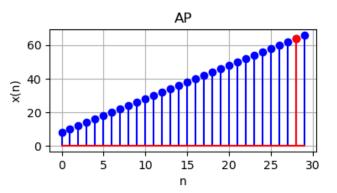


Fig. 1. graph of the given AP

$$\begin{pmatrix} x(2) \\ x(49) \end{pmatrix} = \begin{pmatrix} 1 & 2 \\ 1 & 49 \end{pmatrix} \begin{pmatrix} x(0) \\ d \end{pmatrix} \tag{1}$$

$$\begin{pmatrix} 12\\106 \end{pmatrix} = \begin{pmatrix} x(0) & 2d\\x(0) & 49d \end{pmatrix} \tag{2}$$

$$R_2 \to R_2 - R_1 \tag{3}$$

$$\begin{pmatrix} 12\\94 \end{pmatrix} = \begin{pmatrix} x(0) & 2d\\0 & 47d \end{pmatrix} \tag{4}$$

1) From column 2 we get

$$\implies d = 2$$
 (5)

2) Substituting (5) in column 1, we get

$$\implies x(0) = 8$$
 (6)

3) From the Table I:

$$x(n) = (x(0) + nd)u(n) \tag{7}$$

$$\implies x(n) = (8+2n)u(n) \tag{8}$$

4) Finding x(28):

$$x(28) = x(0) + 28(2) \tag{9}$$

$$\implies x(28) = 64 \tag{10}$$

5) Z-transform: