#### 1

## NCERT Discrete

# Pragnidhved Reddy EE23BTECH11050

### **Question 11.9.3.18:**

Find the sum to n terms of the sequence 8, 88, 888, 8888...

#### **Solution:**

	(8)
$\implies s(n) = \left(\frac{8}{81}\right) (10^{n+1} - 9n - 10)$	(9)

 $\implies s(n) = \lim_{z \to 10} \frac{1}{1!} \left( \frac{8z^{n+1}}{(z-1)^2} \right) + \lim_{z \to 1} \frac{1}{0!} \frac{d}{dz} \left( \frac{8z^{n+1}}{(z-10)} \right)$ 

Value	description
8	First term
88	Second term
$(\sum_{k=0}^{n} 8(10)^k)u(n)$	General term
$S(n) = \sum_{k=0}^{n-1} x(k)$	Sum of n terms
	$ \begin{array}{c} 8 \\ 88 \\ (\sum_{k=0}^{n} 8(10)^{k}) u(n) \end{array} $

INPUT PARAMETERS

#### From (I)

$$s(n) = x(n) \star u(n) \tag{1}$$

#### Z transform of general term

$$X(z) = \sum_{l=-\infty}^{\infty} \left(\sum_{k=0}^{l} 8(10)^{k}\right) u(n) z^{-l}$$
 (2)

$$X(z) = \sum_{l=0}^{\infty} \left(\sum_{k=0}^{l} 8(10)^{k}\right) z^{-l}$$
 (3)

$$\implies X(z) = \left(\frac{8z^2}{(z-10)(z-1)}\right) \quad |z| > 10 \quad (4)$$

#### From (1), we get

$$\implies S(z) = \left(\frac{8z^2}{(z-10)(z-1)}\right) \left(\frac{1}{z-1}\right) \quad (5)$$

$$S(z) = \left(\frac{8z^2}{(z-10)(z-1)^2}\right) \tag{6}$$

$$s(n) = \frac{1}{2\pi j} \oint_{c} \frac{8z^{2}}{(z-10)(z-1)^{2}} (z^{n-1}) dz$$
(7)