

Day - 3

i) Search in a 2D Matrix :- LC:- each row is sorted and the last ele. in cur. row is smaller than first ele. in next row
Gfth:- Each row is sorted, each col. is sorted.

① Brute force:- Do a linear traversal and search. [TC:- $O(n^2)$]

② Optimal:- On every row Do binary search. [TC:- $O(n \log(m))$]

③ Optimized:- target = 25

10	20	30	40
11	21	36	43
25	29	39	50
50	60	70	80

while
 $(j \geq 0 \text{ and } i < n)$

$\left\{ \begin{array}{l} \rightarrow \text{put pointer in top-right corner} \\ \text{ie. } i=0, j=m-1 \\ \rightarrow \text{if } (\text{target} < m[i][j]) \quad j-- ; \\ \rightarrow \text{else if } (\text{target} > m[i][j]) \quad i++ ; \\ \rightarrow \text{else} \quad \text{return true.} \end{array} \right.$

If not found then at last return false.

[TC:- $O(m+n)$]

ii) Pow (n, n) eg:- $n = 2.00000$, $n = 10$ O/P:- 1024.00000
 $n = 2.10000$, $n = 3$, O/P:- 9.26100

① Brute force:- multiply x , n times, If n is +ve return ans,
 If n is -ve, then there is an edge case, you need to store
 in long long, for -ve $\rightarrow \frac{1}{ans}$.

TC:- $O(n)$
 SC:- $O(1)$

Optimised:- x^n .

$$\text{eg:- } 2^{10} = (2 \times 2)^5 = (4)^5 = 1024$$

$$4^5 = 4 \times 4 \times 4 \times 4 \times 4$$

$$4^4 = (\cancel{4} \times \cancel{4})^2 = (4 \times 4)^2 = 16^2 = 256$$

$$16^2 = (16 \times 16)^1 = 256$$

$$256^1 = 256 \times (256)^0$$

} if (n is even) ~~$x = x \times x$~~
 $n = n/2$

else \rightarrow ~~$x = x \times x$~~
 $n = n-1$

TC:- $O(\log n)$
 SC:- $O(1)$

code

```
double pow(double x, int n) {
    double ans = 1.0;
    long long nn = n;
    if (nn < 0) nn = nn * (-1);
    while (nn) {
        if (nn % 2) {
            ans = ans * x;
            nn = nn - 1;
        }
        else {
            x = x * x;
            nn = nn / 2;
        }
    }
}
```

} if ($n < 0$) $ans = (\text{double})(1.0)/(\text{double})$
 ans ;
 return ans;

(iii) Majority element ($> n/2$ times), To find majority ele. in array, when if an ele. appears more than $\lfloor n/2 \rfloor$ times, then it is majority ele. eg:- [3, 2, 3] op:- 3

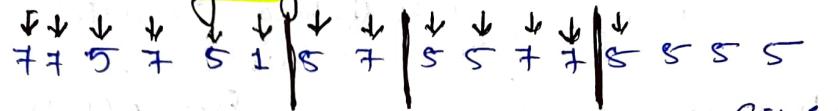
① Brute force:- for every ele. in array, check its occurrence in array and if (occurrence $> n/2$) then return that ele.

PC:- $O(n^2)$
SC:- $O(1)$

② Using Hashmap:- Store ele's in map and if for any key value $> n/2$, then that will be your answer.

PC:- $O(n)$ + $O(n \log n)$
SC:- $O(n)$

③ Moore Voting Algo:-



$$cnt = \emptyset * 2 * 2 * 1 * \emptyset$$

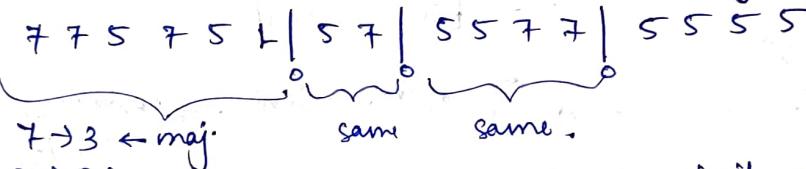
$\downarrow \emptyset$

$\downarrow 2 * 2 * 2 * 1 * 2 * 3 * 4$

$$ele = 8 * 7 * 5 * 5$$

$\left\{ \begin{array}{l} \text{if } (cnt == 0) \\ \quad ele = arr[0]; \\ \text{if } (ele == arr[i]) \\ \quad cnt++; \\ \text{else} \\ \quad cnt--; \end{array} \right.$

Intuition Behind Algo:- since majority ele. $> n/2$ times.



$7 \rightarrow 3 \leftarrow maj.$

same

same.

$5 \rightarrow 2 \leftarrow min.$

$1 \rightarrow 1 \leftarrow min.$

maj. = min., so
majority is cancelled
by minority ele.

Also, it is fixed
that there is
a majority ele.

\rightarrow So, if majority not found in left side, then last ele. will be majority

\rightarrow If majority appears on left prefix, then its count at max can be $\leq n/2$ (leftprefix/2). Since it has to appear more than $n/2$ times, therefore it is bound to appear as a majority in the last suffix.

code

```
{
    count = 0, candidate = 0;
    for (int num : nums) {
        if (count == 0)
            candidate = num;
        if (num == candidate)
            count++;
        else
            count--;
    }
    return candidate;
}
```

PC:- $O(n)$
SC:- $O(1)$

(iv) Majority element ($> \frac{n}{3}$ times), find all ele. that appears more than $\lfloor \frac{n}{3} \rfloor$ times. eg:- [3, 2, 3], O/P:- 3
 eg:- [1, 1, 1, 3, 3, 2, 2, 2] O/P:- [1, 2]

① Brute force:- for every ele. check its occurrence, if it is ($> \frac{n}{3}$) times then add it into your ans vector. TC:- $O(n^2)$
 SC:- $O(1)$

② using Hashmap:- Put ele's in map, and then iterate on map, and for every key check its value, if greater than $\frac{n}{3}$ times, then put in DS. TC:- $O(n)$ or $O(n \log n)$
 SC:- $O(n)$

③ Boyer Moore Voting Algo:- (At max you can have 2 majority ele, and at min 0)

num = [1 1 1 3 3 2 2 2]

$$\begin{aligned} \text{num1} &= 1 \\ \text{num2} &= 3 \\ c1 &= 0 \times 1 \times 1 \\ c2 &= 0 \times 2 \times 2 \end{aligned}$$

So,

$$[\text{num1} = 1], [\text{num2} = 2]$$

```
for (ele : nums) {
    if (ele == num1) c1++;
    else if (ele == num2) c2++;
    else if (c1 == 0) {
        num1 = ele;
        c1 = 1;
    } else if (c2 == 0) {
        num2 = ele;
        c2 = 1;
    } else {
        c1--;
        c2--;
    }
}
```

→ So, now for these two values check if their occurrence is any $> \frac{n}{3}$ times or not and accordingly add on ans DS.

Intuition Behind Algo:- This extension of previous question.



whenever $c_1 = 0 \rightarrow \text{num1} = \text{ele}$, when, $c_2 = 0 \rightarrow \text{num2} = \text{ele}$.

If ($\text{maj} = \text{min}$)

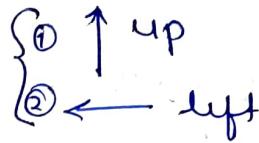
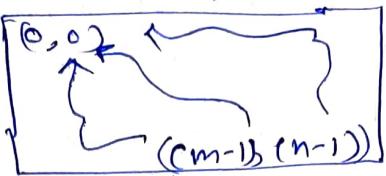
↓ ele's updated, it has to appear more than $\frac{n}{3}$ times.

#. code (on LC)

TC:- $O(n) + O(n) \cong O(n)$
SC:- $O(1)$

(Complexity - 29)
 Q) Grid unique paths [To go from $(0, 0) \rightarrow (m-1, n-1)$, find total unique paths. (we can only move right or down)]

① Brute force (ie Recursion), Instead of going $(0, 0) \rightarrow (m-1, n-1)$
 go opposite.
(Top-down)



Recursion:- Trying out all possible ways.

```
f(i, j) {
    if (i == 0 and j == 0)
        return 1;
    if (i < 0 or j < 0)
        return 0;
    up = f(i-1, j);
    left = f(i, j-1);
    return up + left;
}
```

exponential.

$T.C. := O(2^{m+n})$
 $S.C. := O(\text{path length}) + O(2^{m+n})$
 \downarrow
 $O((m-1) + (n-1))$.

↓ recursive stack space

② optimised (ie Memoisation) (overlapping subproblems),
 \downarrow $dp[i][j] \geq dp[i][j] \geq dp[i][j]$

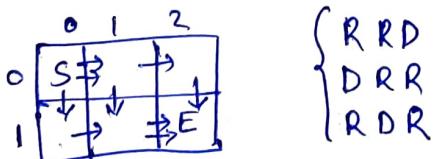
```
f(i, j) {
    if (i == 0 and j == 0) return 1;
    if (i < 0 or j < 0) return 0;
    if (dp[i][j] != -1) return dp[i][j];
    up = f(i-1, j);
    left = f(i, j-1);
    return dp[i][j] = up + left;
}
```

$T.C. := O(m \times n)$
 $S.C. := O(\text{path len}) + O(m \times n)$

↓ recursive stack space

These code can be further optimised by (Tabulation or space optimization)
 But all of these will have $T.C. := O(m \times n)$.

③ Most optimised solⁿ :- Using Combinations



Observation ① :- We always took 3 steps to reach S \rightarrow E, i.e., (in general) $((m-1) + (n-1)) = [m + n - 2]$ steps
obs. ② :- $(m-1)$ right step, $(n-1)$ down step

$$\rightarrow 2 + 3 - 2 = 3 \text{ steps.}$$

} to fill these 3 places,
 either we choose from 2 right steps, 3C_2 or 1 down step, 3C_1

$$3C_2 = 3$$

R R B
R B R
B R R

3 ways.

$$3C_1 = 3$$

B R L
R B R
R R B

3 ways.

→ for $(m+n-2)$ directions either place $m-1$ right paths
or
either place $n-1$ left paths.

$$m+n-2 \\ C_{m-1}$$

$$m+n-2 \\ C_{n-1}$$

any of above will give right answer.

and shortcut to find nCr , → eg:- $10C_3 = \frac{8 \times 9 \times 10}{3 \times 2 \times 1}$

TC:- $O(m-1)$; or $O(n-1)$
SC:- $O(1)$

for ans = $m+n-2 \\ C_{n-1}$

for ans = $m+n-2 \\ C_{m-1}$

code

```
uniquepaths(int m, int n){  
    int N = n+m-2;  
    int dr = m-1;  
    double res = 1;  
    for(int i=1; i<=dr; i++)  
        res = res * (N-dr+i)/i;  
    return (int)res;  
}
```

VI> Reverse Pairs :- $i < j$ and $\text{nums}[i] > 2 * \text{nums}[j]$

count all such pairs. e.g. - [1, 3, 2, 3, 1], op:- 2 ((3, 1), (3, 1))

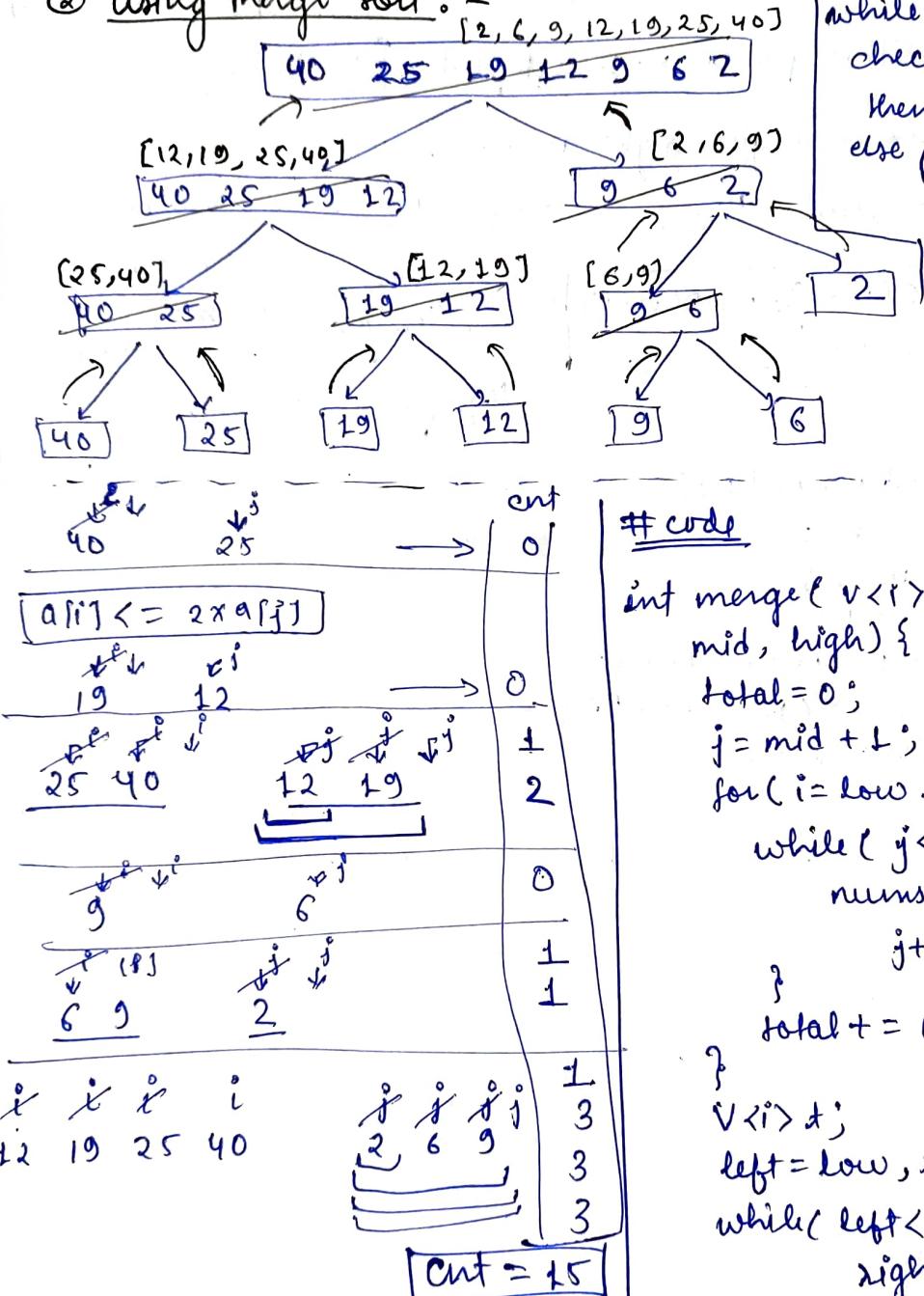
① Brute force :- for every i in nums, check of every j , such that $i < j$ and satisfied the condition $\text{nums}[i] > 2 * \text{nums}[j]$

$$\text{TC} := O(n^2)$$

$$\text{SC} := O(1)$$

(Here, we are considering all the pairs)

② using Merge Sort :-



$$\text{TC} := O(n \log n) + O(n) + O(n)$$

$$\text{SC} := O(n)$$

for merging for counting

while merging, we are checking if $a[i] \leq 2 * a[j]$

then $i++$ $a[i] = 0$

else $a[i] = j$ se petite

tk ka sb in 2nd part

and $j++$

while j moved, then

code

```
int merge(v<i>& nums, low, mid, high) {
    total = 0;
    j = mid + 1;
    for(i = low — i <= mid) {
        while(j <= high and
            nums[i] > 2 * nums[j]) {
            j++;
            total += (j - (mid + 1));
        }
        v<i>.push_back(nums[i]);
    }
    left = low, right = mid + 1;
    while(left <= mid and
        right <= high) {
        if(nums[left] <= nums[right])
            t.push_back(nums[left++]);
        else
            t.push_back(nums[right++]);
    }
}
```

```

        while (left <= mid) {
            t = p - b(nums[left++]);
        }
        while (right <= high) {
            t = p - b(nums[right++]);
        }
        for (i = low; i <= high; i++) {
            nums[i] = t + i - low;
        }
        return total;
    }

    int mergesort (vector<int> &nums, int low, int high) {
        if (low >= high) return 0;
        int mid = (low + high) / 2;
        int inv = mergesort (nums, low, mid);
        inv += mergesort (nums, mid + 1, high);
        inv += merge (nums, low, mid, high);
        return inv;
    }

    int reversepairs (vector<int> &arr) {
        return mergesort (arr, 0, arr.size() - 1);
    }
}

```