







### New York Times Puzzle

https://www.nytimes.com/interactive/2015/07/03/upshot/a-quick-puzzle-to-test-your-problem-solving.html



# Hypothesis Testing



"I've narrowed it down to two hypothesis: it grew, or we shrunk."

# Test your hypothesis?





$$P("""] = \left(\frac{3}{4}\right)^{12} \approx 0.032 = 3.2\%$$







You go to a petrol bunk to fill 5 liters of Petrol/Gasoline

How are you sure that fuel quantity is correct?

How can a inspector validate this assumption?



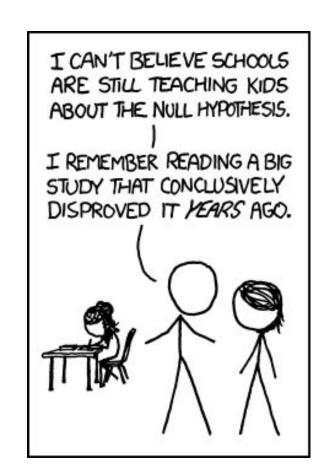
Is sex ratio in India 1:1?

How can you validate this hypothesis



## Hypothesis

- Statistical hypothesis is an assumption about a population parameter. This assumption may or may not be true
- Hypothesis testing refers to the formal procedures used by statisticians to accept or reject statistical hypotheses





# Types of Statistical Hypothesis

- **Null Hypothesis.** The null hypothesis, denoted by  $H_0$ , is usually the hypothesis that sample observations result purely from chance
- Alternative hypothesis. The alternative hypothesis, denoted by H1 or Ha, is the hypothesis that sample observations are influenced by some non-random cause.

# Is average Experience between DSS & BD different



#### **Current Batch**



dss\_exp = np.array([12, 15, 13, 20, 19, 20, 11, 19, 11, 12, 19, 13, 12, 10, 6, 19, 3, 1, 1, 0, 4, 4, 6, 5, 3, 7, 12, 7, 9, 8, 12, 11, 11, 18, 19, 18, 19, 3, 6, 5, 6, 9, 11, 10, 14, 14, 16, 17, 17, 19, 0, 2, 0, 3, 1, 4, 6, 6, 8, 7, 7, 6, 7, 11, 11, 10, 11, 10, 13, 13, 15, 18, 20, 19, 1, 10, 8, 16, 19, 19, 17, 16, 11, 1, 10, 13, 15, 3, 8, 6, 9, 10, 15, 19, 2, 4, 5, 6, 9, 11, 10, 9, 10, 9, 15, 16, 18, 13,])

$$n = 108$$
  
 $\mu = 10.43$ 

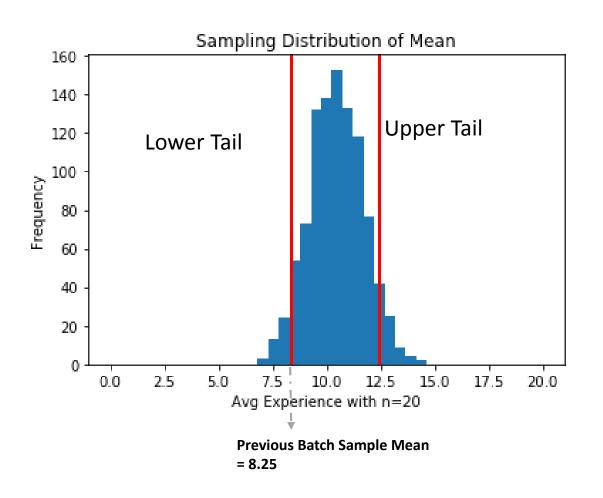
#### **Previous Batch**



$$n = 97$$
  
 $\mu = 8.04$ 

# Hypothesis Testing : n = 20, 90% Confidence Interval





### Reject Null Hypothesis !!!

N = 20 Confidence = 90% Significance = 0.1 T-Statistic = -1.725 P-Value = 0.10



### P-value

- **P-value**. The strength of evidence in support of a null hypothesis is measured by the **P-value**.
- Suppose the test statistic is equal to *S*. The P-value is the probability of observing a test statistic as extreme as *S*, assuming the null hypothesis is true.
- If p-value is less than the level of significance we reject the null hypothesis

# Calculating P-Value



Variable	Obs	Mean	Std. Dev.	Min	Max
У	90	-5.032836	3.566609	-13.51062	4.489684

The p value of a test is the probability of seeing a result at least as extreme as the one that you actually saw, assuming the null hypothesis is true.

In your example the null hypothesis is that  $\mu = -4$ . The standard test here is a two-sided t test, where we first compute the t-statistic:

$$t = \frac{\bar{x} - \mu}{s/\sqrt{n}}$$

where  $\bar{x}$  is the sample mean, s is the sample standard deviation and n is the number of observations in your sample. In your data  $\bar{x} = -5.033$ , s = 3.567 and n = 90, so

$$t = \frac{-5.033 + 4}{3.567/\sqrt{90}} = -2.747$$

This is then compared to a t distribution with n-1 degrees of freedom to calculate a p value. We want the probability that the result is at least as extreme as the one we saw, so we use a two-sided t test, since t<-2.747 and t>2.747 are both considered equally extreme.

Let  $T_{89}$  be a t-distributed random variable with 89 degrees of freedom. We have

$$P(T_{89} \le -2.747) = 0.00364$$

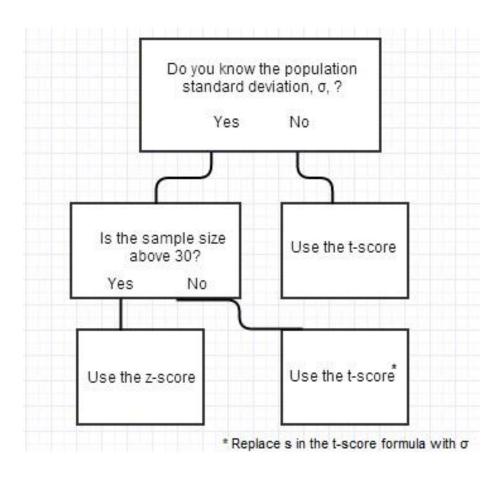
and  $P(T_{89} \geq 2.747)$  will be the same since the t distribution is symmetric, which means that your p -value is

$$p = 2 \times 0.00364 = 0.00727$$

so your null hypothesis is rejected at the 1% significance level.



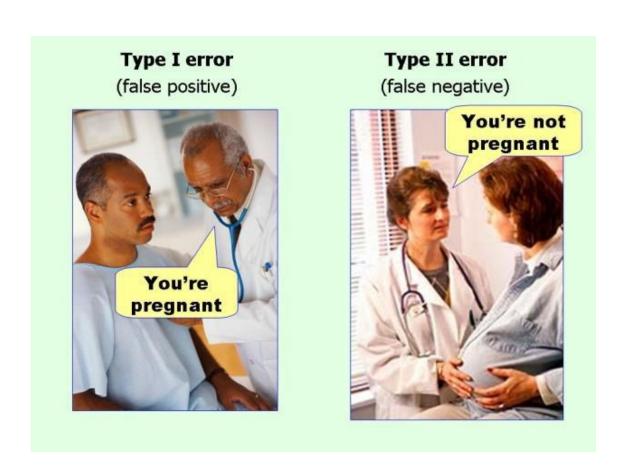






### **Decision Errors**

- **Type I error**: Rejecting a null hypothesis when it is true.
- Type II error: "accept" or fails to reject the null hypothesis when it is false.





# Putting it all in perspective

	H <sub>o</sub> True	H <sub>o</sub> False	
Reject H₀	Type I Error	Correct Rejection	
Fail to Reject H₀	Correct Decision	Type II Error	



# Python Basics



```
Variables and Data Types
   Variable Assignment
  >>> x=5
   >>> x
   Calculations With Variables
                               Sum of two variables
  >>> x+2
   >>> x-2
                               Subtraction of two variables
   >>> x*2
                               Multiplication of two variables
   >>> x**2
                               Exponentiation of a variable
                               Remainder of a variable
   >>> x%2
   >>> x/float(2)
                               Division of a variable
  Types and Type Conversion
                '5', '3.45', 'True'
                                       Variables to strings
               5, 3, 1
   int()
                                        Variables to integers
   float()
               5.0, 1.0
                                        Variables to floats
   bool()
               True, True, True
                                       Variables to booleans
```

#### 

#### Selecting List Elements Index starts at o Subset >>> my list[1] Select item at index 1 Select 3rd last item >>> my list[-3] Slice Select items at index 1 and 2 >>> my list[1:3] Select items after index o >>> my list[1:] Select items before index 3 >>> my list[:3] Copy my list >>> my list[:]

#### **List Operations**

```
>>> my_list + my_list
['my', 'list', 'is', 'nice', 'my', 'list', 'is', 'nice']
>>> my_list * 2
['my', 'list', 'is', 'nice', 'my', 'list', 'is', 'nice']
>>> my_list2 > 4
True
```

#### List Methods

```
Get the index of an item
>>> my list.index(a)
>>> my list.count(a)
                                Count an item
                                Append an item at a time
>>> my list.append('!')
                                Remove an item
>>> my list.remove('!')
>>> del(my list[0:1])
                                Remove an item
>>> my list.reverse()
                                Reverse the list
>>> my list.extend('!')
                                Append an item
>>> my list.pop(-1)
                                Remove an item
>>> my list.insert(0,'!')
                                Insert an item
>>> my list.sort()
                                Sort the list
```

## NumPy

#### NumPy

The NumPy library is the core library for scientific computing in Python. It provides a high-performance multidimensional array object, and tools for working with these arrays.

Use the following import convention:

>>> import numpy as np

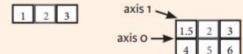


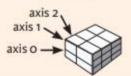
#### NumPy Arrays

1D array

#### 2D array

3D array





#### **Creating Arrays**

```
>>> a = np.array([1,2,3])
>>> b = np.array([(1.5,2,3), (4,5,6)], dtype = float)
>>> c = np.array([[(1.5,2,3), (4,5,6)], [(3,2,1), (4,5,6)]],
dtype = float)
```

#### Initial Placeholders

```
>>> np.zeros((3,4))
>>> np.ones((2,3,4),dtype=np.int16)
>>> d = np.arange(10,25,5)

>>> np.linspace(0,2,9)

>>> e = np.full((2,2),7)
>>> f = np.eye(2)
>>> np.random.random((2,2))
>>> np.empty((3,2))
```

Create an array of zeros
Create an array of ones
Create an array of evenly
spaced values (step value)
Create an array of evenly
spaced values (number of samples)
Create a constant array
Create a 2X2 identity matrix
Create an array with random values
Create an empty array



#### **Numpy Arrays**

```
>>> my_list = [1, 2, 3, 4]
>>> my_array = np.array(my_list)
>>> my_2darray = np.array([[1,2,3],[4,5,6]])
```

#### Selecting Numpy Array Elements

Index starts at o

#### 

#### Numpy Array Operations

```
>>> my_array > 3
    array([False, False, False, True], dtype=bool)
>>> my_array * 2
    array([2, 4, 6, 8])
>>> my_array + np.array([5, 6, 7, 8])
    array([6, 8, 10, 12])
```

#### Numpy Array Functions

```
Get the dimensions of the array
>>> my array.shape
>>> np.append(other array)
                                      Append items to an array
>>> np.insert(my array, 1, 5)
                                     Insert items in an array
>>> np.delete(my array,[1])
                                      Delete items in an array
>>> np.mean(my array)
                                      Mean of the array
>>> np.median(my array)
                                      Median of the array
>>> my array.corrcoef()
                                      Correlation coefficient
>>> np.std(my array)
                                      Standard deviation
```

# Acing the 'Axes'

Axis = 0 (Columns) Axis=1(Rows)

- Mean()
- Sum()
- Describe()
- Count()
- Sort\_index(by=)
- Fillna(method = ffill)



Axis = 0 (Rows) Axis=1(Columns)

- dropna()
- Apply()
- Cumsum()
- Drop()
- Concat()



### 1. Reading and Writing Data

a. Reading a CSV file

>>>df=pd.read\_csv('AnalyticsVidhya.csv')

b. Writing content of data frame to CSV file

>>>df.to\_csv('AV.csv')

c. Reading an Excel file

>>>df=pd.read\_excel('AV.xlsx','sheet1')

d. Writing content of data frame to Excel file

>>>df.to\_excel('AV2.xlsx',sheet\_name='sheet2')





### 2.Getting Preview of Dataframe

a. Looking at top n records

b. Looking at bottom n records

c. View columns name

>>>df.columns



#### 3. Rename Columns of Data Frame

a. Rename method helps to rename column of data frame.

>>>df2=df.rename(columns={'old\_columnname':'new\_columnname'})

This statement will create a new data frame with new column name.

b. To rename the column of existing data frame, set inplace=True.

>>>df.rename(columns={'old\_columnname':'new\_columnname'}, inplace=True)



#### 4. Selecting Columns or Rows

a. Accessing sub data frames

>>>df[['column1','column2']]

**b. Filtering Records** 

>>>df[ df['column1']><u>10]</u>

>>>df[ (df['column1']>10) & df['column2']==30]

>>>df[ (df['column1']>10) | df['column2']==30]





#### 5. Handling Missing Values

This is an inevitale part of dealing with data. To overcome this hurdle, use dropna or fillna function.

- a. dropna: It is used to drop rows or columns having missing data >>>df1.dropna()
- b. fillna: It is used to fill missing values
  - >>>df2.fillna(value=5) #It replaces all missing values with 5
  - >>>mean=df2['column1'].mean()
  - >>>df2['column1'].fillna(mean) #It replaces all missing values of column1 with mean of available values



### **6. Creating New Columns**

New column is a function of existing columns

>>>df['NewColumn1']=df['column2'] #Create a copy of existing column2

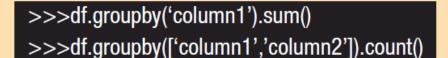
>>>df['NewColumn2']=df['column2']+10 #Add 10 to existing column2 then create a new one

>>>df['NewColumn3']= df['column1'] + df['column2'] #Add elements of column1 and column2 then create new column



#### 7. Aggregate

- a. Groupby: Groupby helps to perform three operations
  - i. Splitting the data into groups
  - ii. Applying a function to each group individually
  - iii. Combining the result into a data structure





b. Pivot Table: It helps to generate data structure. It has three components index, columns and values (similar to excel)

>>>pd.pivot\_table(df, values='column1', index=['column2','column3'], columns=['column4'])

By default, it shows the sum of values column but you can change it using argument aggfunc

>>>pd.pivot\_table(df, values='column1', index=['column2','column3'], columns=['column4'], aggfunc=len)

#it shows count



### 8. Merging/Concatenating DataFrames

It performs similar operation like we do in SQL.

- a. Concatenating: It concatenate two or more data frames based on their columns. >>>pd.concat([df1,df2])
- b. Merging: We can perform left, right and inner join also.

```
>>>pd.merge(df1, df2, on='column1', how='inner')
>>>pd.merge(df1, df2, on='column1', how='left')
>>>pd.merge(df1, df2, on='column1', how='right')
>>>pd.merge(df1, df2, on='column1', how='outer')
```



### 9. Applying function to element, column or dataframe

a. Map: It iterates over each element of a series.

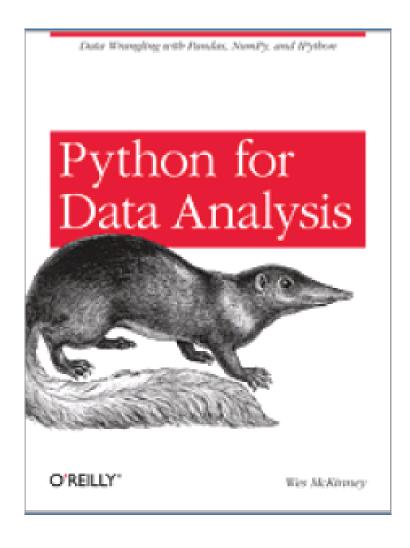
>>>df['column1'].map(lambda x: 10+x #this will add 10 to each element of column1

>>>df['column2'].map(lambda x: 'AV'+x) #this will concatenate "AV" at the beginning of each element of column2 (column format is string)

b. Apply: As the name suggests, applies a function along any axis of the DataFrame.

>>>df[['column1','column2']].apply(sum) #it will returns the sum of all the values of column1 and column2.





## Matplotlib vs Seaborn



- Matplotlib to be used for basic plotting bar charts, line graphs, scatter plots
- Matplotlib visualizations useful for quick prototyping
- Seaborn usually used for statistical visualizations heatmaps, pairplots, box plots
- Seaborn visualizations are aesthetically more appealing

### **Statistics**

### UDX Move up in life

#### **DEFINITIONS**

- ☐ STATISTICS A set of tools for collecting, organizing, presenting, and analyzing numerical facts or observations.
- 1. **Descriptive Statistics** procedures used to organize and present data in a convenient, useable, and communicable form.
- Inferential Statistics procedures employed to arrive at broader generalizations or inferences from sample data to populations.
- STATISTIC A number describing a sample characteristic. Results from the manipulation of sample data according to certain specified procedures.
- ☐ DATA Characteristics or numbers that are collected by observation.
- **POPULATION** A complete set of actual or potential observations.
- population characteristic; typically, inferred from sample statistic.
- □ **SAMPLE** A subset of the population selected according to some scheme.
- in such a way that each member of the population has an equal opportunity to be selected. Ex. lottery numbers in a fair lottery
- ☐ VARIABLE A phenomenon that may take on different values.

☐ **MEAN** - The point in a distribution of measurements about which the summed deviations are equal to zero. Average value of a sample or population.

#### POPULATION MEAN

#### SAMPLE MEAN

$$\mu = \frac{1}{N} \sum_{i=1}^{N} x_i$$

$$\bar{x} = \frac{1}{n} \sum_{i=1}^{n} x_i$$

**Note:** The mean is very sensitive to extreme measurements that are not balanced on both sides.

■ WEIGHTED MEAN - Sum of a set of observations multiplied by their respective weights, divided by the sum of the weights:

WEIGHTED MEAN  $\frac{\sum_{i=1}^{w_i} w_i}{\sum_{i=1}^{G} w_i}$ 

where  $w_i$  = weight;  $x_i$  = observation; G = number of observation groups. Calculated from a population, sample, or groupings in a frequency distribution.

Ex. In the Frequency Distribution below, the mean is 80.3; calculated by using frequencies for the  $w_i$ 's. When grouped, use class midpoints for  $x_i$ 's.

☐ MEDIAN - Observation or potential observation in a set that divides the set so that the same number of observations lie on each side of it. For an odd number of values, it is the middle value; for an even number it is the average of the middle two.

Ex. In the Frequency Distribution table below, the median is 79.5.

☐ MODE - Observation that occurs with the greatest frequency. Ex. In the Frequency Distribution table below, the mode is 88.

### MEASURES OF DISPERSION

SUM OF SQUARES (SS) - Deviations from the mean, squared and summed:  $(\nabla x)^2$ 

Population SS=
$$\sum (x_i - \mu_x)^2$$
 or  $\sum x_i^2 - \frac{(\sum x_i)^2}{N}$ 

Sample SS = 
$$\sum (x_i - \overline{x})^2$$
 or  $\sum x_i^2 - \frac{(\sum x_i)^2}{n}$ 

■ VARIANCE - The average of square differences between observations and their mean.

#### POPULATION VARIANCE SAMPLE VARIANCE

$$\sigma^2 = \frac{1}{N} \sum_{i=1}^{N} (x_i - \mu)^2 \qquad \qquad s^2 = \frac{1}{n-1} \sum_{i=1}^{n} (x_i - \overline{x})^2$$

#### VARIANCES FOR GROUPED DATA

#### **POPULATION**

#### SAMPLE

$$\sigma^2 = \frac{1}{N} \sum_{i=1}^{G} f_i (m_i - \mu)^2 s^2 = \frac{1}{n-1} \sum_{i=1}^{G} f_i (m_i - \bar{x})^2$$

STANDARD DEVIATION - Square root of the variance:

**Ex. Pop. S.D.** 
$$\sigma = \sqrt{\frac{1}{N} \sum_{i=1}^{N} (x_i - \mu)^2}$$

### **Statistics**



- Population and Sample
- Central Limit Theorem
- Z-scores
- Normal Distribution
- Hypothesis Testing



# Do you know what is so special about this guy?



**Invention** 

**Painting** 

**Sculpting** 

**Architecture** 

Science

Music

**Leonardo Da Vinci** 



**Specialty: Curiosity** 

**Mathematics** 

Literature

**Anatomy** 

Geology

**Astronomy** 

Cartography

## You too need to be curious......



**Programming** 

**Machine Learning** 

**Statistics** 

**Big Data** 

**Deep Learning** 

**Design Thinking** 

**Your Name** 



**Communication Skills** 

IoT

**Blockchain** 

**Augmented Reality** 

**Empirical Research** 

**Domain Expertise** 



# The Way Forward

- Master all the concepts we have covered in our 12 sessions
- Complete the project
- Explore the two books listed under 'Books to Refer' section in LMS
- Do not stop questioning 'Why' while learning anything new
- Most important of them all stay in touch with each other and always share your learnings!



Wish You All the Best For Your Future