Project: CNN

Team members:

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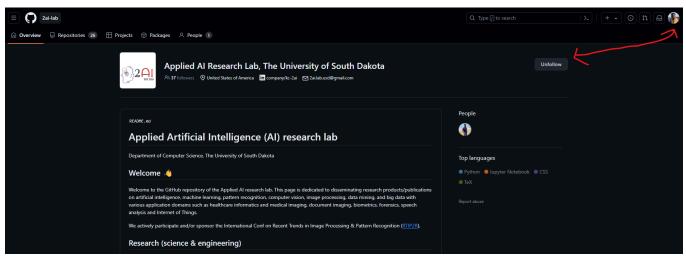
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Followed Applied AI Research Lab, The University of South Dakota-- Proof:



Overview

The goal of this project is to build and evaluate a Convolutional Neural Network (CNN) for recognizing handwritten digits from the MNIST Dataset.

Data Exploration and Preparation

This version of MNIST dataset titled 'Optical Recognition of Handwritten Digits' is hosted in UC Irvine Machine Learning Repository.

Datasets can be directly fetched by using their python library called ucimlrepo.

Installing the ucimlrepo python library.

```
!pip install ucimlrepo

Collecting ucimlrepo
    Downloading ucimlrepo-0.0.6-py3-none-any.whl (8.0 kB)
Installing collected packages: ucimlrepo
Successfully installed ucimlrepo-0.0.6
```

Fetching the dataset from the UCI Machine Learning Repository

```
from ucimlrepo import fetch_ucirepo
# fetch dataset
optical_recognition_of_handwritten_digits = fetch_ucirepo(id=80)
# data (as nandas datafnames)
```

```
π uaca (as panuas uacan ames)
X = optical_recognition_of_handwritten_digits.data.features
y = optical_recognition_of_handwritten_digits.data.targets
print(optical_recognition_of_handwritten_digits.metadata)
# variable information
print(optical_recognition_of_handwritten_digits.variables)
     {'uci_id': 80, 'name': 'Optical Recognition of Handwritten Digits', 'repository_url': 'https://archive.ics.uci.edu/dataset/80/optical+re
                        role
                                      type demographic description units \
                name
     0
          Attribute1 Feature
                                   Integer
                                                  None
                                                              None
                                                                    None
     1
          Attribute2 Feature
                                   Integer
                                                  None
                                                              None
                                                                    None
     2
          Attribute3 Feature
                                   Integer
                                                  None
                                                              None
                                                                    None
     3
          Attribute4 Feature
                                   Integer
                                                  None
                                                              None
                                                                    None
                                  Integer
     4
          Attribute5 Feature
                                                  None
                                                              None
                                                                    None
       Attribute61 Feature
                                   Integer
                                                  None
                                                              None
                                                                    None
     61 Attribute62 Feature
                                   Integer
                                                  None
                                                                    None
                                                              None
     62 Attribute63 Feature
                                   Integer
                                                  None
                                                              None
                                                                    None
     63 Attribute64 Feature
                                   Integer
                                                  None
                                                              None
                                                                    None
     64
              class Target Categorical
                                                  None
                                                              None None
        missing_values
     0
     1
                    no
     2
                    no
     3
                    no
     4
                    no
                   . . .
     60
                    no
     61
                    no
     62
                    no
     63
                    nο
     64
     [65 rows x 7 columns]
```

Important necessary libraries for data manipulation

```
import numpy as np
import matplotlib.pyplot as plt
```

Grouping the dataset by class so that a random data can be picked from each class.

```
gk = y.groupby('class')
```

Storing class names as it comes in the dataset

```
class_labels = y['class'].unique()
```

This version of MNIST dataset has already been normalized and dimensionality reduced.

The images are in the form of matrix of size 8*8 where each element is an integer in the range 0...16.

However, the image is flatten into an array of length 64.

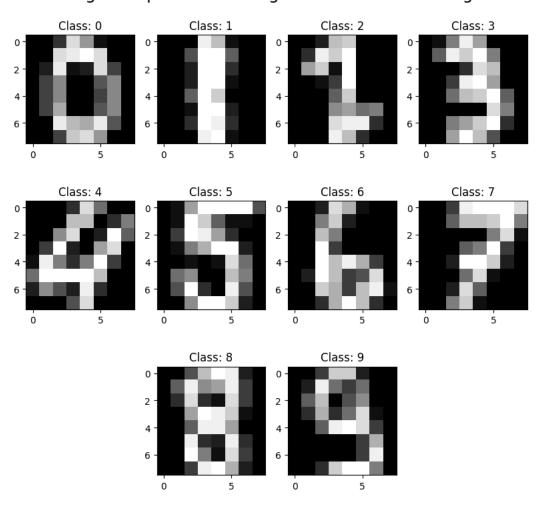
The feature set is reshaped from 1D to 2D (8*8 pixels), aligning with the CNN's input requirements.

```
X_images = X.to_numpy().reshape(-1, 8, 8)
```

Method to get a random index for sample images of each class so that a sample image for each digit class can be visualized.

```
def get_index_sample_each_class():
  sample_indices = []
  for i in range(10):
    sample_indices.append(gk.get_group(i).sample().index[0])
  return sample_indices
Visualizing a sample image from each digit class
sample_idxs = get_index_sample_each_class()
plt.figure(figsize=(8, 8))
for i in range(10):
  plt.subplot(3, 4, i + 1 if i < 8 else i + 2)
  plt.imshow(X_images[sample_idxs[i]], cmap='gray', interpolation='none')
  plt.title(f'Class: {i}')
plt.suptitle('Random image samples of each digit class from MNIST Digits dataset',
             fontsize=18)
plt.tight_layout()
plt.show()
```

Random image samples of each digit class from MNIST Digits dataset



The dataset is divided into training and testing sets with an 80-20 split to ensure a fair evaluation of the model. The training set helps in fitting the model, while the testing set is used to evaluate its generalization capability.

from sklearn.model_selection import train_test_split

The labels are converted from a class vector (integers) to binary class matrix for use with categorical crossentropy during the training of the model.

```
from keras.utils import to_categorical

y_train_labels = y_train
y_test_labels = y_test

y_train = to_categorical(y_train, num_classes=10)
y_test = to_categorical(y_test, num_classes=10)
```

Convolutional Neural Network Architecture

Importing necessary modules from keras

```
from keras.models import Sequential, load_model
from keras.layers import Dense, Dropout, Flatten
from keras.layers import Conv2D, MaxPooling2D, BatchNormalization
from keras.optimizers import Adam
from keras.models import Model
```

Method to build CNN architecture

```
def create_cnn_model():
 model = Sequential()
 model.add(Conv2D(filters=16,
                  kernel_size=(3, 3),
                  activation='relu',
                  strides=1,
                  padding='same',
                  data_format='channels_last',
                  input_shape=(8, 8, 1)))
 model.add(MaxPooling2D(pool_size=(2, 2),
                        strides=2,
                        padding='valid'))
 model.add(Dropout(0.25))
 model.add(Conv2D(filters=32,
                  kernel_size=(3, 3),
                  activation='relu',
                  strides=1,
                  padding='same',
                  data_format='channels_last'))
 model.add(MaxPooling2D(pool_size=(2, 2),
                        strides=2,
                        padding='valid'))
 model.add(Dropout(0.25))
 model.add(Conv2D(filters=64,
                  kernel_size=(3, 3),
                  activation='relu',
                  strides=1,
                  padding='same',
                  data_format='channels_last'))
 model.add(MaxPooling2D(pool_size=(2, 2),
                        strides=2,
                        padding='valid'))
 model.add(Dropout(0.25))
 model.add(Flatten())
 model.add(Dense(128, activation='sigmoid'))
 model.add(Dropout(0.25))
 model.add(Dense(512, activation='sigmoid'))
 model.add(Dropout(0.25))
 model.add(Dense(10, activation='softmax'))
 return model
model = create_cnn_model()
Visualizing the CNN architecture
```

model.summary()

Model: "sequential"

Layer (type)	Output Shape	Param #
conv2d (Conv2D)	(None, 8, 8, 16)	160
<pre>max_pooling2d (MaxPooling2 D)</pre>	(None, 4, 4, 16)	0
dropout (Dropout)	(None, 4, 4, 16)	0
conv2d_1 (Conv2D)	(None, 4, 4, 32)	4640

<pre>max_pooling2d_1 (MaxPoolin g2D)</pre>	(None, 2, 2, 32)	0	
dropout_1 (Dropout)	(None, 2, 2, 32)	0	
conv2d_2 (Conv2D)	(None, 2, 2, 64)	18496	
<pre>max_pooling2d_2 (MaxPoolin g2D)</pre>	(None, 1, 1, 64)	0	
dropout_2 (Dropout)	(None, 1, 1, 64)	0	
flatten (Flatten)	(None, 64)	0	
dense (Dense)	(None, 128)	8320	
dropout_3 (Dropout)	(None, 128)	0	
dense_1 (Dense)	(None, 512)	66048	
dropout_4 (Dropout)	(None, 512)	0	
dense_2 (Dense)	(None, 10)	5130	
Total params: 102794 (401.54 KB) Trainable params: 102794 (401.54 KB) Non-trainable params: 0 (0.00 Byte)			

The CNN architecture designed for recognizing 8x8 pixel images of handwritten digits comprises several layers, each with specific functions aimed at processing and transforming the input images into a form where digit classifications can be made effectively.

1. First Convolutional Layer

- o Parameters: Consists of 16 filters, each of size 3x3.
- · Activation: Utilizes the ReLU activation function.
- o Dimensions: Maintains the same spatial dimensions (8x8) due to the 'same' padding strategy.
- Effect: This layer is responsible for capturing basic visual features such as edges and gradients within the image. Each filter
 produces a separate feature map, resulting in 16 different representations of the input image, each highlighting different aspects of
 the image.

2. First Pooling Layer

- o Pooling Size: Uses a 2x2 window for pooling.
- o Strides: With a stride of 2 and 'valid' padding, it reduces the spatial dimensions of each feature map from 8x8 to 4x4.
- Effect: Pooling layers serve to reduce the spatial dimensions of the feature maps, which decreases the number of parameters and computation in the network. This operation helps in extracting the dominant features while reducing the sensitivity to the exact locations of features.

3. First Dropout Layer

- o Dropout Rate: Set at 25%.
- Effect: Dropout layers randomly set a fraction of the input units to zero during training, which helps in preventing overfitting by
 ensuring that no single set of neurons within the layer overly specializes to the training data.

4. Second Convolutional Layer

- o Parameters: Increases to 32 filters, maintaining the 3x3 size.
- o Activation: Continues with ReLU activation.
- o Dimensions: The feature maps remain at 4x4 due to 'same' padding.
- Effect: This layer extracts more complex features from the simplified outputs provided by the first pooling layer. By increasing the number of filters, it allows the network to develop a richer understanding of the input data.

5. Second Pooling Layer

- Pooling Size and Strides: Same as the first pooling layer, reducing each feature map size further from 4x4 to 2x2.
- Effect: Further reduces the spatial dimensions, focusing on the most salient features, and helps in further reducing the computational complexity.

6. Second Dropout Layer

- o Dropout Rate: Maintains at 25%.
- o Effect: Adds another layer of regularization to enhance the model's generalization capabilities.

7. Third Convolutional Layer

- o Parameters: Further increases the filter count to 64.
- · Activation: Uses ReLU activation.
- o Dimensions: Maintains the 2x2 dimensions with 'same' padding.
- Effect: This layer captures even higher-level features from the input data. With more filters, the network can capture a more diverse set of features, crucial for accurate classification tasks.

8. Third Pooling Layer

· Effect: Reduces each 2x2 feature map to 1x1, effectively distilling the feature maps to their most essential elements.

9. Third Dropout Layer

Effect: Further ensures that the model avoids overfitting, especially important as the complexity of the model increases.

10. Flatten Layer

Effect: Transforms the 3D output of the previous convolutional layers to a 1D array without affecting the batch size. This layer
prepares the data for the final classification steps in the dense layers.

11. Dense and Dropout Layers

- Configuration: Includes dense layers with 128 and 512 neurons, each followed by a dropout layer, with sigmoid activation for the dense layers and softmax for the final output.
- Effect: These layers integrate the features learned by the convolutions into predictions for the 10 classes of digits. The dropout layers interspersed between them prevent overfitting by randomly dropping a portion of the neurons, ensuring that different neurons can learn to identify various features independently.

12. Output Layer

- · Activation: Uses softmax activation.
- Effect: Outputs the probability distribution across the 10 digit classes, allowing for the classification of the input digit image into one
 of these classes based on the highest probability.

Model Compilation

Optimizer:

The model uses the Adam optimizer, which is an extension to stochastic gradient descent. This optimizer is particularly effective for problems involving a lot of data or parameters. Adam combines the best properties of the AdaGrad and RMSProp algorithms to provide an optimization algorithm that can handle sparse gradients on noisy problems.

Loss Function: categorical_crossentropy loss function is used when there are two or more label classes. The labels are expected to be provided in a one-hot representation. This is appropriate since the network's output uses a softmax activation function, which outputs a probability distribution over the classes. Categorical crossentropy will compare the distribution produced by the output layer with the true distribution, where the true probability is 100% for the actual class.

```
optimizer = Adam(learning_rate=0.001, beta_1=0.9, beta_2=0.999)
model.compile(optimizer=optimizer, loss="categorical_crossentropy", metrics=["accuracy"])
```

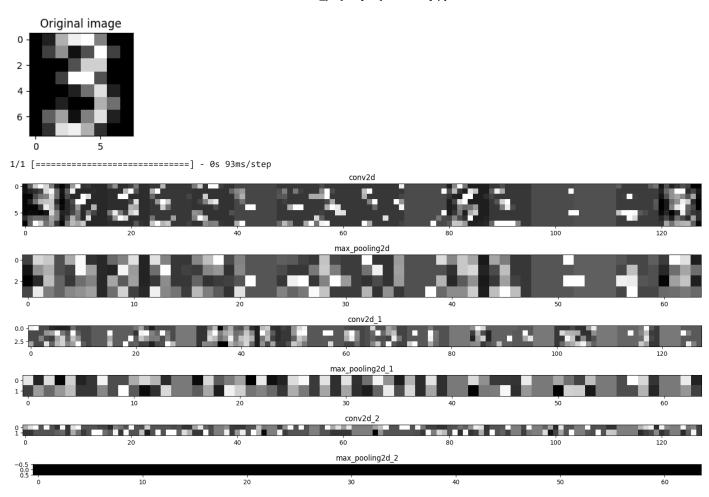
Visualizing CNN feature maps

Visualizing the feature maps of the CNN architecture after it processes the input image.

activation_model is a new model derived from the original model but designed to output the activations from each convolutional and max pooling layer instead of just the final output.

For each layer, a grid of all filter outputs (feature maps) is displayed. The grid is scaled based on the number of filters, providing a clear view of each filter's pattern recognition.

```
from keras.models import Model
import matplotlib.pyplot as plt
import numpy as np
activation_model = Model(inputs=model.input,
                         outputs=[layer.output for layer in model.layers if isinstance(layer, (Conv2D, MaxPooling2D))])
def display_feature_maps(image_index, X_images):
    input_tensor = np.expand_dims(X_images[image_index], axis=0)
    plt.figure(figsize=(2, 2))
    plt.title('Original image')
    plt.imshow(X_images[image_index], aspect='auto', cmap='gray')
    plt.show()
    activations = activation_model.predict(input_tensor)
    for layer, layer_activation in zip([layer for layer in model.layers if isinstance(layer, (Conv2D, MaxPooling2D))], activations):
        num_filters = layer_activation.shape[-1]
        size = layer_activation.shape[1]
        display_grid = np.zeros((size, size * num_filters))
        for i in range(num_filters):
           x = layer_activation[0, :, :, i]
            x -= x.mean()
           if x.std() > 0:
               x /= x.std()
            x *= 64
           x += 128
           x = np.clip(x, 0, 255).astype('uint8')
           display_grid[:, i * size : (i + 1) * size] = x
        scale = 20. / num_filters
        plt.figure(figsize=(scale * num_filters, scale))
        plt.title(layer.name)
        plt.grid(False)
        plt.imshow(display_grid, aspect='auto', cmap='gray')
        plt.show()
display_feature_maps(59, X_images)
```



This demonstrates the CNN's ability to hierarchically extract and abstract features from raw pixel values.

As the image moves through the layers of the network, we can observe the transition from simple, low-level features to complex, high-level features that contribute to the network's understanding and classification of the image.

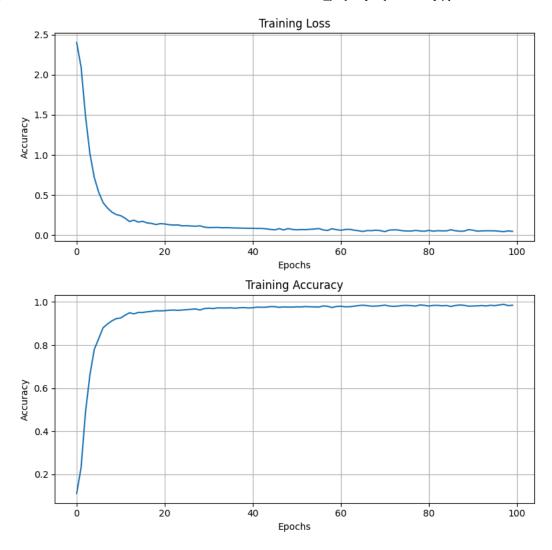
Model Training

The CNN model is trained on the training data for 100 epochs with a batch size of 128.

```
36/36 [=============== ] - 1s 26ms/step - loss: 1.4897 - accuracy: 0.4867
Epoch 4/100
Epoch 5/100
Epoch 6/100
Epoch 7/100
Epoch 8/100
Epoch 9/100
Epoch 10/100
Epoch 11/100
Epoch 12/100
Epoch 13/100
Epoch 14/100
Epoch 15/100
Epoch 16/100
Epoch 17/100
Epoch 18/100
Epoch 19/100
Epoch 20/100
Epoch 21/100
Epoch 22/100
Epoch 23/100
Epoch 24/100
Fnoch 25/100
Epoch 26/100
Epoch 27/100
Epoch 28/100
Epoch 29/100
```

Visualizing loss and accuracy while training

```
train_loss = history.history['loss']
train_acc = history.history['accuracy']
plt.figure(figsize=(8, 8))
plt.subplot(2, 1, 1)
plt.plot(train_loss, label='Training Loss')
plt.title('Training Loss')
plt.xlabel('Epochs')
plt.ylabel('Accuracy')
plt.grid()
plt.subplot(2, 1, 2)
plt.plot(train_acc, label='Training Accuracy')
plt.title('Training Accuracy')
plt.xlabel('Epochs')
plt.ylabel('Accuracy')
plt.grid()
plt.tight_layout()
plt.show()
```



Model Evaluation

Evaluating the CNN model on the test data.

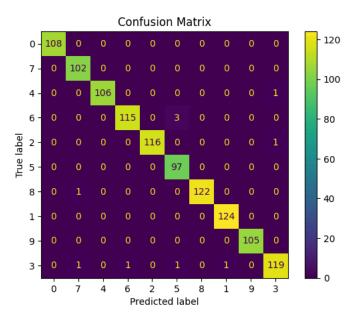
The loss and accuracy metrics indicates good model performance with high accuracy and low loss on the test set.

Other metrics are also calculated and visualized

The metrics show near perfect scores.

```
from sklearn.metrics import accuracy_score, precision_score, recall_score
from sklearn.metrics import f1_score, confusion_matrix, ConfusionMatrixDisplay
from sklearn.metrics import roc_curve, RocCurveDisplay, roc_auc_score
y_test_labels = np.argmax(y_test, axis=1)
y_pred_labels = np.argmax(y_pred, axis=1)
print(f"Accuracy: {accuracy_score(y_test_labels, y_pred_labels)*100:.2f}")
print(f"Precision: {precision_score(y_test_labels, y_pred_labels, average='macro')*100:.2f}")
print(f"Recall: {recall_score(y_test_labels, y_pred_labels, average='macro')*100:.2f}")
print(f"F1 \ Score: \ \{f1\_score(y\_test\_labels, \ y\_pred\_labels, \ average='macro')*100:.2f\} \setminus n")
cm = confusion_matrix(y_test_labels, y_pred_labels)
disp = ConfusionMatrixDisplay(cm, display_labels=class_labels)
disp.plot()
disp.ax_.set_title('Confusion Matrix')
plt.show()
     Accuracy: 99.11
     Precision: 99.08
     Recall: 99.16
```

F1 Score: 99.11



K-Fold Cross-Validation

Since the model shows near perfect metrics in all categories, validating these results with a proper cross-validation approach.

from sklearn.model_selection import KFold

K-Fold cross-validation for the CNN model from scratch.

- Folds: 5
- Initializes empty lists to store the loss and accuracy for each fold.
- · Iterates over each fold, training a new model on the training set and evaluating it on the validation set.
- · For each fold, it compiles a new instance of the CNN model with the Adam optimizer.
- Trains the model quietly (verbose=0 so it doesn't print out logs) for 100 epochs with a batch size of 128.
- Evaluates the model on the validation set and prints the fold number along with the validation results.

```
n folds = 5
epochs = 100
batch_size = 128
kfold = KFold(n_splits=n_folds, shuffle=True)
kfold_hist_loss, kfold_hist_acc = [], []
fold_count = 1
print(f'K-Fold\ Cross-Validation\ on\ the\ CNN\ model\ [\{n\_folds\}\ Folds]')
for train_index, val_index in kfold.split(X_images, y):
  t x, val x = X images[train index], X images[val index]
  t_y, val_y = y.iloc[train_index], y.iloc[val_index]
  t_y = to_categorical(t_y, num_classes=10)
  val_y = to_categorical(val_y, num_classes=10)
  model_tmp = create_cnn_model()
  optimizer_tmp = Adam(learning_rate=0.001, beta_1=0.9, beta_2=0.999)
  model_tmp.compile(optimizer=optimizer_tmp, loss="categorical_crossentropy", metrics=["accuracy"])
  print(f"\nFold {fold_count} - Training")
  model_tmp.fit(t_x, t_y, epochs=epochs, batch_size=batch_size, verbose=0)
  val_loss, val_acc = model_tmp.evaluate(val_x, val_y, verbose=0)
  print(f'Fold {fold_count} - Validation')
  kfold_hist_loss.append(val_loss)
  kfold_hist_acc.append(val_acc)
  fold count += 1
     K-Fold Cross-Validation on the CNN model [5 Folds]
     Fold 1 - Training
     Fold 1 - Validation
     Fold 2 - Training
     Fold 2 - Validation
     Fold 3 - Training
     Fold 3 - Validation
     Fold 4 - Training
     Fold 4 - Validation
     Fold 5 - Training
     Fold 5 - Validation
Results of the K-fold cross-validation
print(f'Validation Loss and Accuracy across {n_folds} Folds.')
for i in range(n_folds):
  print(f'Fold {i+1}\tLoss: {kfold_hist_loss[i]}\tAccuracy: {kfold_hist_acc[i]}')
print(f'\nMean loss across {n_folds} folds: {np.mean(kfold_hist_loss)}')
print(f'\nMean cross-validation score: {np.mean(kfold_hist_acc)}')
print(f"Standard deviation of cross-validation scores: {np.std(kfold_hist_acc)}")
     Validation Loss and Accuracy across 5 Folds.
                                             Accuracy: 0.9875444769859314
     Fold 1 Loss: 0.04249735549092293
     Fold 2 Loss: 0.049108102917671204
                                             Accuracy: 0.9884341359138489
     Fold 3 Loss: 0.03023604303598404
                                             Accuracy: 0.9928825497627258
                                             Accuracy: 0.9902135133743286
     Fold 4 Loss: 0.04305674880743027
     Fold 5 Loss: 0.01646474562585354
                                             Accuracy: 0.9937722682952881
     Mean loss across 5 folds: 0.03627259917557239
     Mean cross-validation score: 0.9905693888664245
     Standard deviation of cross-validation scores: 0.0024267342001183744
```

Plotting the loss and accuracy of the CNN model across folds

```
train_loss = history.history['loss']
train_acc = history.history['accuracy']

plt.figure(figsize=(8, 8))

plt.subplot(2, 1, 1)
plt.plot(kfold_hist_loss, label='Validation loss', marker='o')
plt.axhline(y=np.mean(kfold_hist_loss), color='r', linestyle='--', label='Mean loss')
plt.xlabel('Fold')
plt.ylabel('Loss')
plt.title('Cross-Validation Loss Across Folds')
plt.legend()
```