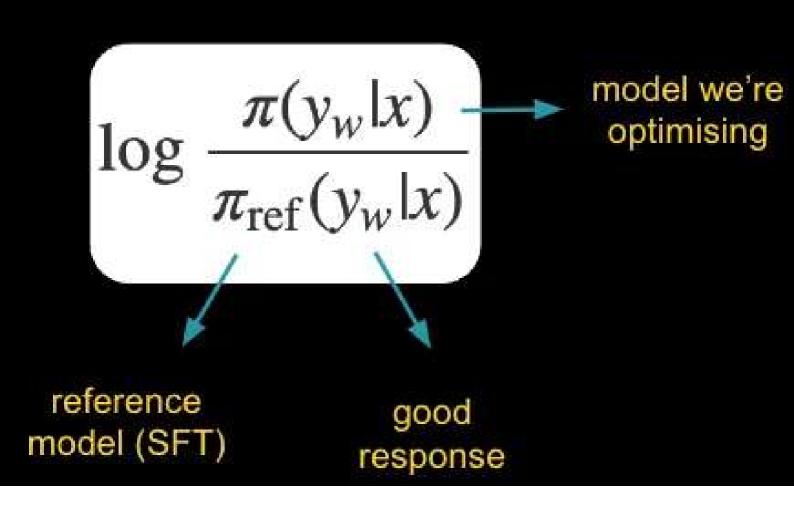
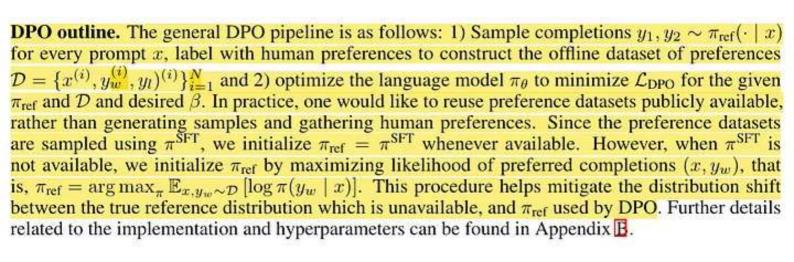
| Intuitively DPO uses preference data (given a context/prompt, there is a preferred/good response over a dis-preferred/bad response). |
|--------------------------------------------------------------------------------------------------------------------------------------|
| preferred/good response over a dis-preferred/bad response). |
| At the heart of DPO is formulation of loss function that considers the |
| likelihood of preferred response over dis-preffered response and optimizes the LLM model towards that objective: |
| |
| Dataset of preferences {(x,yw,yl)}, where x is a prompt and yw, yl are the preferred and dis-preferred responses. |
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$$\max_{\pi} \underset{(x, y_w, y_l) \sim \mathcal{D}}{\mathbb{E}} \log \sigma \left(\beta \log \frac{\pi(y_w | x)}{\pi_{\text{ref}}(y_w | x)} - \beta \log \frac{\pi(y_l | x)}{\pi_{\text{ref}}(y_l | x)} \right)$$





What does the DPO update do? For a mechanistic understanding of DPO, it is useful to analyze the gradient of the loss function \mathcal{L}_{DPO} . The gradient with respect to the parameters θ can be written as:

$$\nabla_{\theta} \mathcal{L}_{\mathrm{DPO}}(\pi_{\theta}; \pi_{\mathrm{ref}}) = \\ -\beta \mathbb{E}_{(x, y_w, y_l) \sim \mathcal{D}} \left[\underbrace{\sigma(\hat{r}_{\theta}(x, y_l) - \hat{r}_{\theta}(x, y_w))}_{\text{higher weight when reward estimate is wrong}} \left[\underbrace{\nabla_{\theta} \log \pi(y_w \mid x)}_{\text{increase likelihood of } y_w} - \underbrace{\nabla_{\theta} \log \pi(y_l \mid x)}_{\text{decrease likelihood of } y_l} \right] \right],$$

where $\hat{r}_{\theta}(x,y) = \beta \log \frac{\pi_{\theta}(y|x)}{\pi_{\text{ref}}(y|x)}$ is the reward implicitly defined by the language model π_{θ} and reference model π_{ref} (more in Section 3). Intuitively, the gradient of the loss function \mathcal{L}_{DPO} increases the likelihood of the preferred completions y_w and decreases the likelihood of dispreferred completions y_l . Importantly, the examples are weighed by how much higher the implicit reward model \hat{r}_{θ} rates the dispreferred completions, scaled by β , i.e, how incorrectly the implicit reward model orders the completions, accounting for the strength of the KL constraint. Our experiments suggest the importance of this weighting, as a naïve version of this method without the weighting coefficient can cause the language model to degenerate (Appendix Table 3).