

Time: 03:00 Hr

Maximum Marks: 60

Note: Attempt all Questions. If any data is missing, assume as per requirement and mention the same.

1(a). Determine the transfer function  $\frac{C_1}{R_1}$ ,  $\frac{C_2}{R_2}$ ,  $\frac{C_1}{R_2}$  and  $\frac{C_2}{R_1}$  from the block diagram as shown in figure 1.

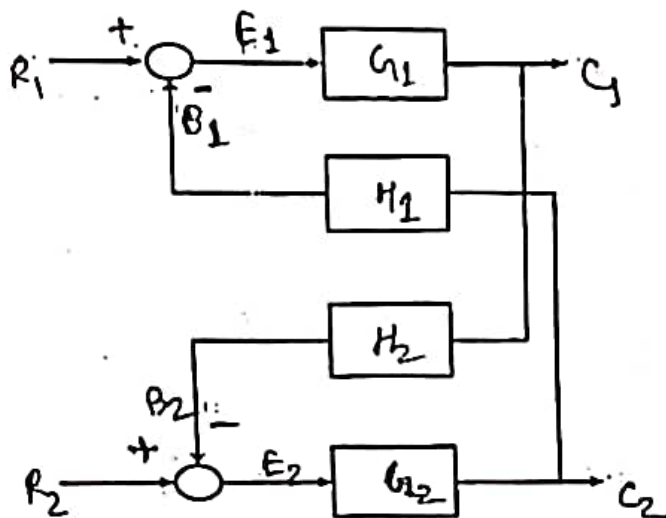


Figure 1

(5)

(b). A system is represented by following equations as below

$$x_2 = a_{12}x_1 + a_{22}x_2 + a_{42}x_4 + a_{32}x_5$$

$$x_3 = a_{23}x_2$$

$$x_4 = a_{34}x_3 + a_{44}x_4$$

$$x_5 = a_{35}x_3 + a_{45}x_4$$

Find the transfer function  $\frac{x_5}{x_1}$  with the help of signal flow graph technique.

(5)

2 (a). The open loop transfer function of unity feedback system is given by  $G(s) = \frac{K}{s(1+sT)}$ . Where K and T are

forward path gain and time constant. By what factor should the gain K be reduced such that

(i) The peak overshoot of the system to unit step input is reduced to from 75% to 25% and

(ii) The damping ratio increases from 0.1 to 0.6.

(6)

(b). Determine the range of values of K of  $G(s) = \frac{K}{s(1+s)}$  for unity feedback system so that steady state error

$$e_{ss} < 0.004 \text{ when } r(t) = 0.2t$$

(4)

3(a). The characteristic equation of feedback control system is  $s^4 + 20s^3 + 15s^2 + 2s + K = 0$

- Determine the range of  $K$  for the system to be stable.
- Can the system marginally stable? If so, find the required value of  $K$  and frequency of sustain oscillation.
- Also determine the range of  $K$  for the system has roots more negative than  $s = -1$  to be stable. (5)

(b). Plot the root locus for  $G(s)H(s) = \frac{K}{s(s^2 + 6s + 8)}$  then find the value of  $K$

- For marginal Stability
- At the breakaway point
- For the damping ratio  $\xi = 0.5$  (5)

4. Draw the bode plot on semi-log paper for unity feedback system whose open loop transfer function is given by

$$G(s) = \frac{500}{s(s+1)(s+50)}$$

$$= \frac{500}{j\omega (j\omega + 1)(j\omega + 50)}$$

$$= \frac{10}{s(s+1)(s+50)}$$

From the bode plot, determine the following

- Gain crossover frequency and phase crossover frequency
- Gain margin and phase margin
- Comment on stability

$$= \frac{10}{j\omega (j\omega + 1)(j\omega + 50)}$$

5. A unity feedback system has open loop transfer function  $G(s) = \frac{1}{s(s+1)(2s+1)}$  sketch the Nyquist plot for the

system and also calculate the Gain Margin and Phase Margin. (10)

6. Design a lag compensator for a system whose open loop transfer function  $G(s) = \frac{K}{s(s+4)(s+5)}$  to meet the following specifications

(i)  $\xi = 0.707$

(ii)  $K_v \geq 5$

(iii)  $\omega_n = 2 \text{ rad/sec}$

$$r_n = \omega_n \sqrt{1 - \xi^2}$$

$$\frac{dK}{ds} =$$

$$\begin{aligned} \beta &= \frac{K}{s(s+4)(s+5)} \\ \frac{d\beta}{ds} &= \frac{K}{s^2(s+4)(s+5)} \\ &= \frac{K}{s^2(s^2+9s+20)} \\ &= \frac{K}{s^2(s^2+9s+20)} \end{aligned}$$