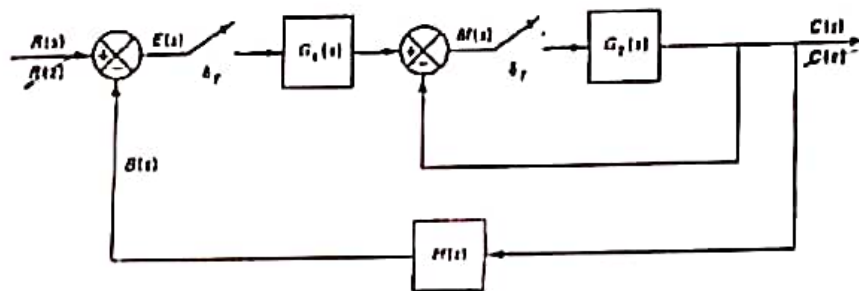


1. Using inversion integral method, obtain the inverse z transform of

$$G(z) = \frac{1 + 6z^{-1} + z^{-2}}{(1 - z^{-1})(1 - 0.2z^{-1})}$$

2. Obtain the discrete time output $C(z)$ and continuous time output $C(s)$ in terms of input and transfer function of the blocks for following discrete time control system



3. Consider the following filter defined by

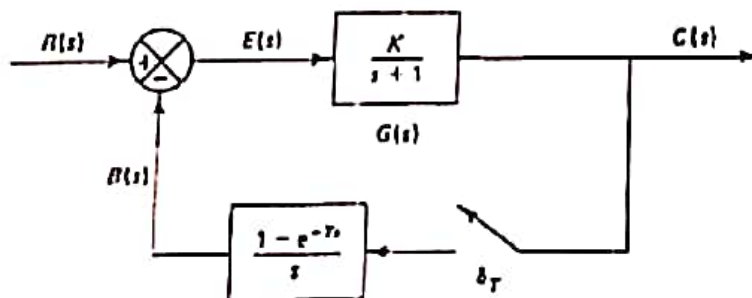
$$G(z) = \frac{2 + 2.2z^{-1} + 0.2z^{-2}}{1 + 0.4z^{-1} - 0.12z^{-2}}$$

Realize this filter in (a) series, (b) parallel and (c) ladder schemes.

4. Discuss / Derive

- a) Constant damping, Constant frequency and Constant damping ratio Loci for discrete time systems.
b) Ackerman's formula for pole placement design

5. Consider the following system with sampling period T as 0.2 sec and gain constant K as unity



Determine response $c(kT)$ for $k = 0, 1, 2, 3$ and 4 when the input $r(t)$ is unit step function and final value $c(\infty)$.

6. ✓ Consider the system defined by

ch. 6

5

$$\begin{bmatrix} x_1(k+1) \\ x_2(k+1) \\ x_3(k+1) \end{bmatrix} = \begin{bmatrix} 0 & 1 & 0 \\ 0 & 0 & 1 \\ -0.16 & 0.84 & 0 \end{bmatrix} \begin{bmatrix} x_1(k) \\ x_2(k) \\ x_3(k) \end{bmatrix} + \begin{bmatrix} 1 \\ 1 \\ 1 \end{bmatrix} u(k)$$

§13

-0.5

Determine the state feedback gain matrix K such that when the control signal is given by $u(k) = -Kx(k)$, the closed loop system will exhibit the deadbeat response to any initial state $x(0)$.

7. ✓ Consider the system defined by

$$x(k+1) = Gx(k) + C^* u(k)$$

$$y(k) = Cx(k)$$

ch(6)

§11

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and

$$G = \begin{bmatrix} 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \\ 1 & 0 & 0 & 0 \end{bmatrix}, C = [1 \ 0 \ 0 \ 0]$$

Show system is completely state controllable and observable. Show also that given any initial state $x(0)$, every state vector can be brought to the origin in at most four sampling periods if and only if the control signal is given by $u(k) = -Cx(k)$.

8. ✓

Consider the pulse transfer function system defined by $G(z) = \frac{b_0 + b_1 z^{-1} + \dots + b_n z^{-n}}{1 + a_1 z^{-1} + \dots + a_n z^{-n}}$. Using nested programming method, derive the state space representation of this system.

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