Artificial & Computational Intelligence

AIML CLZG557

M1 : Introduction

&

M2 : Problem Solving Agent using Search

Indumathi V

Guest Faculty,

BITS - WILP

BITS Pilani

Pilani Campus

Course Plan

M1	Introduction to AI
M2	Problem Solving Agent using Search
M3	Game Playing
M4	Knowledge Representation using Logics
M5	Probabilistic Representation and Reasoning
M6	Reasoning over time
M7	Ethics in AI

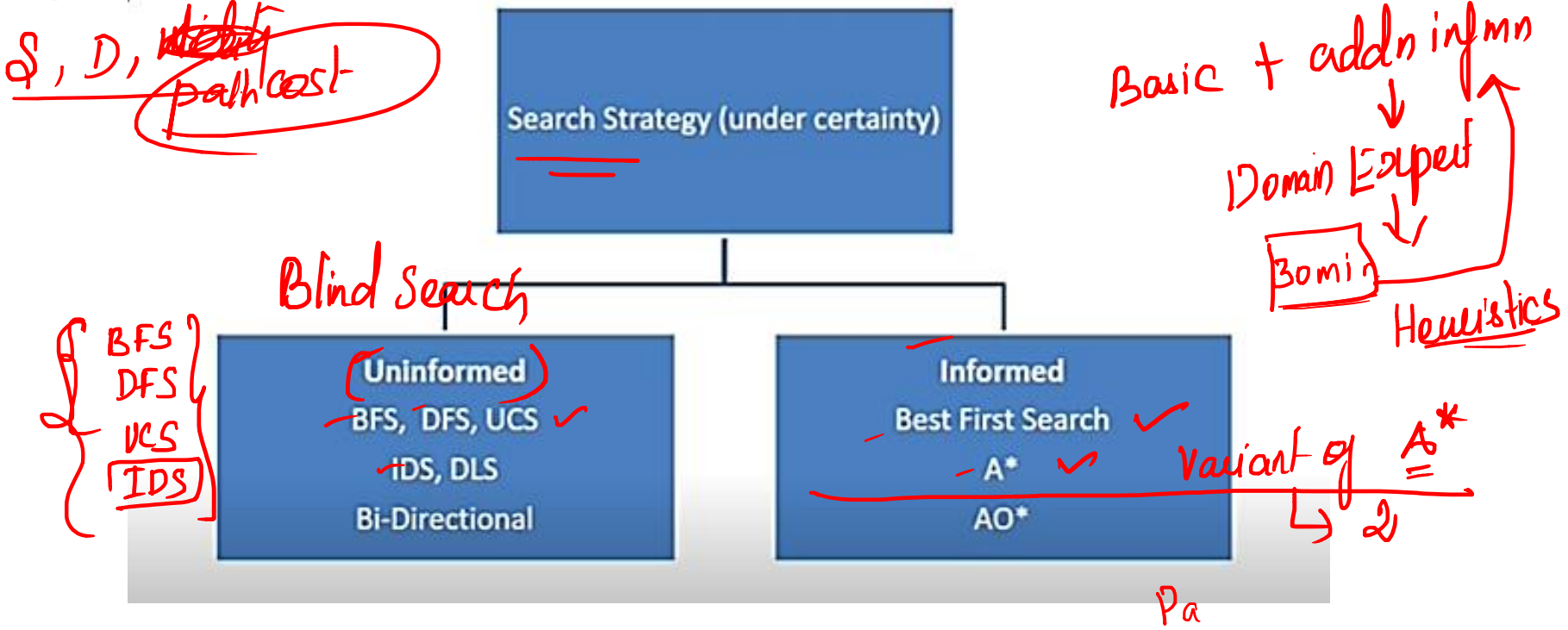
Learning Objective

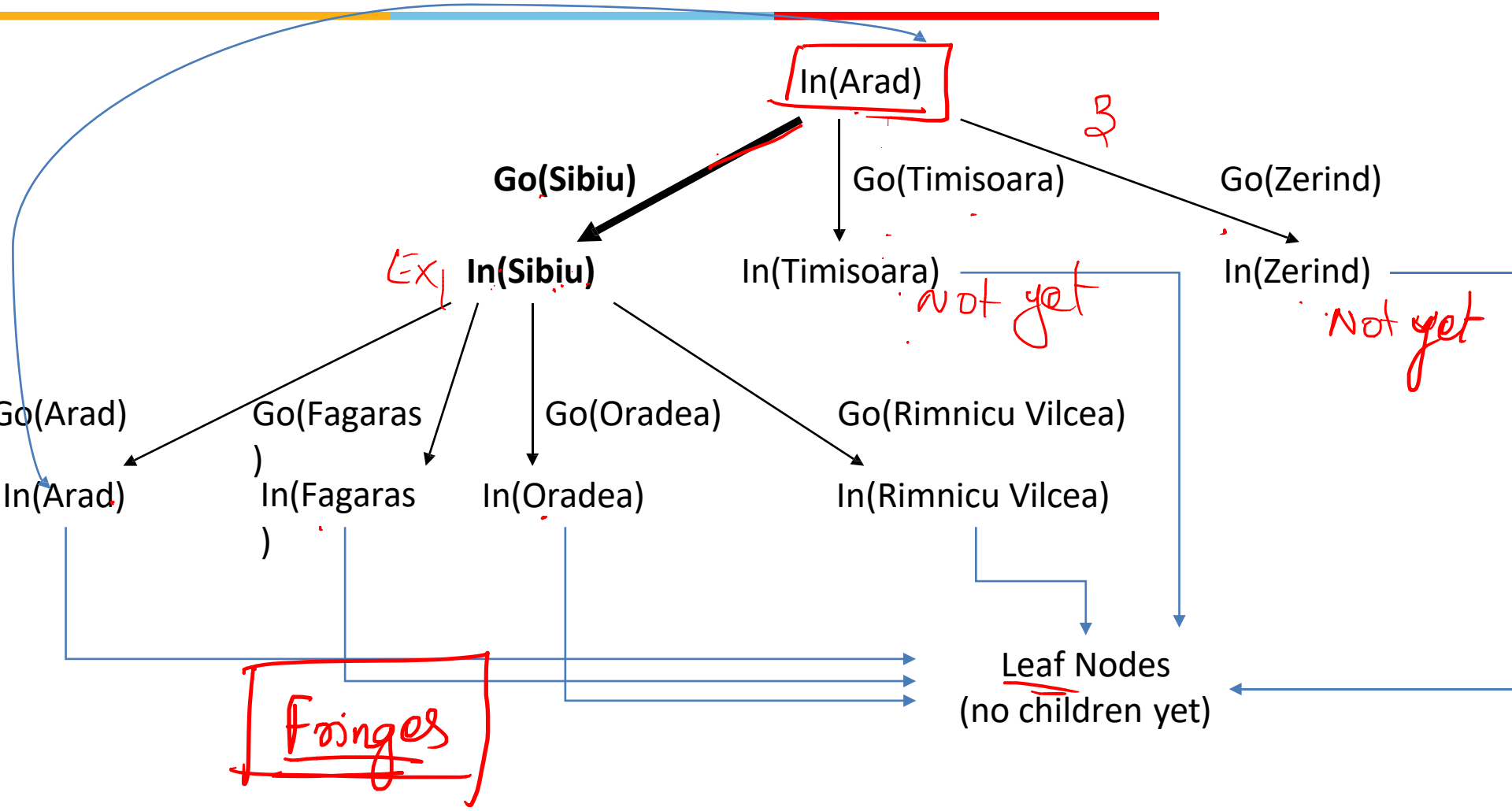
At the end of this class , students Should be able to:

1. Design problem solving agents
2. Create search tree for given problem
3. Apply uninformed search algorithms to the given problem
4. Compare performance of given algorithms in terms of completeness, optimality, time and space complexity
5. Differentiate for which scenario appropriate uninformed search technique is suitable and justify

Searching for Solutions

Choosing the current state, testing possible successor function, expanding current state to generate new state is called Traversal. Choice of which state to expand – Search Strategy




In(Arad)
Go(Sibiu)
Go(Timisoara)
Go(Zerind)
In(Sibiu)
In(Timisoara)
In(Zerind)
not yet
Not yet
Go(Arad)
Go(Fagaras)
Go(Oradea)
Go(Rimnicu Vilcea)
In(Arad)
In(Fagaras)
In(Oradea)
In(Rimnicu Vilcea)
Leaf Nodes
(no children yet)
Fringes

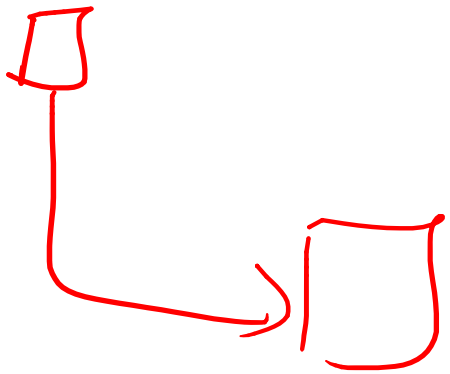
Application

Breadth First Search

- Finding path in a graph (many solutions)
- Finding the Bipartitions in a graph

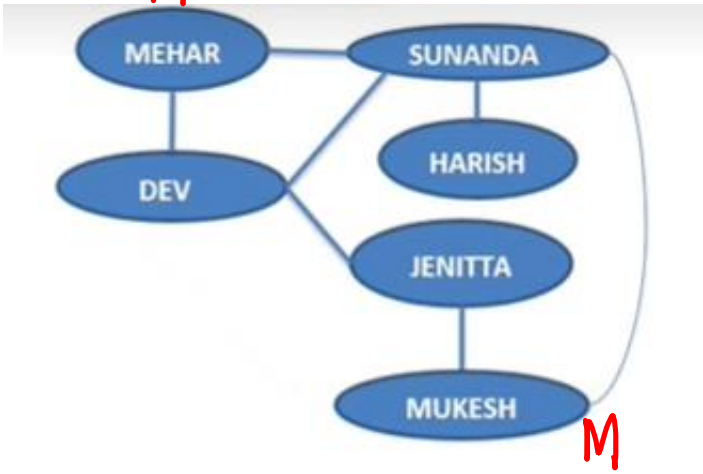
Depth First Search

- Find the Connectedness in a graph
- Topological Sorting



Application

Breadth First Search



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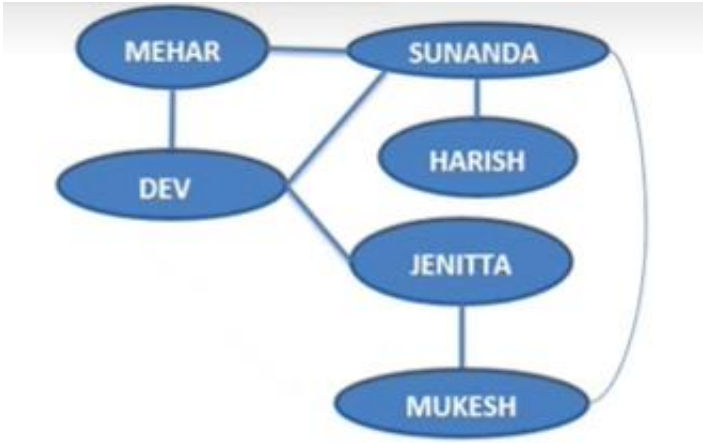
Application

Breadth First Search



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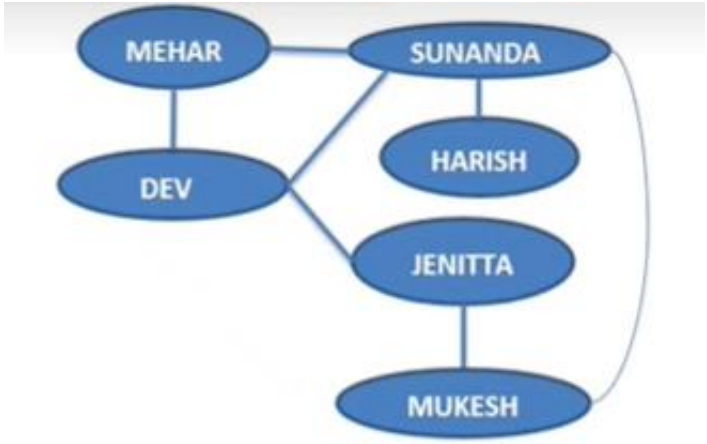
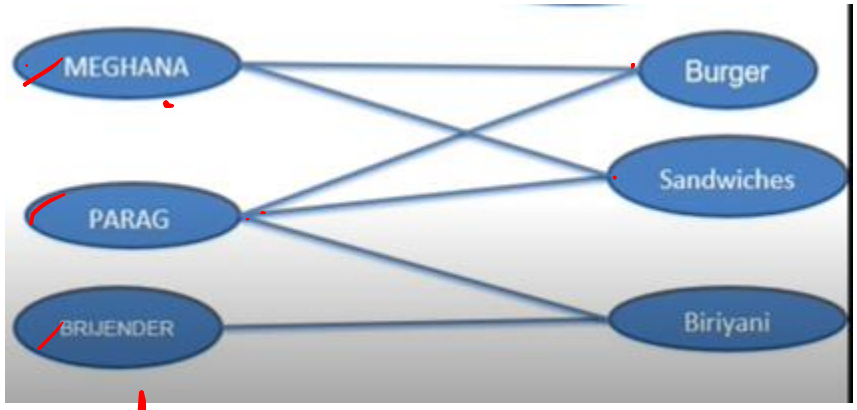


Application

Breadth First Search

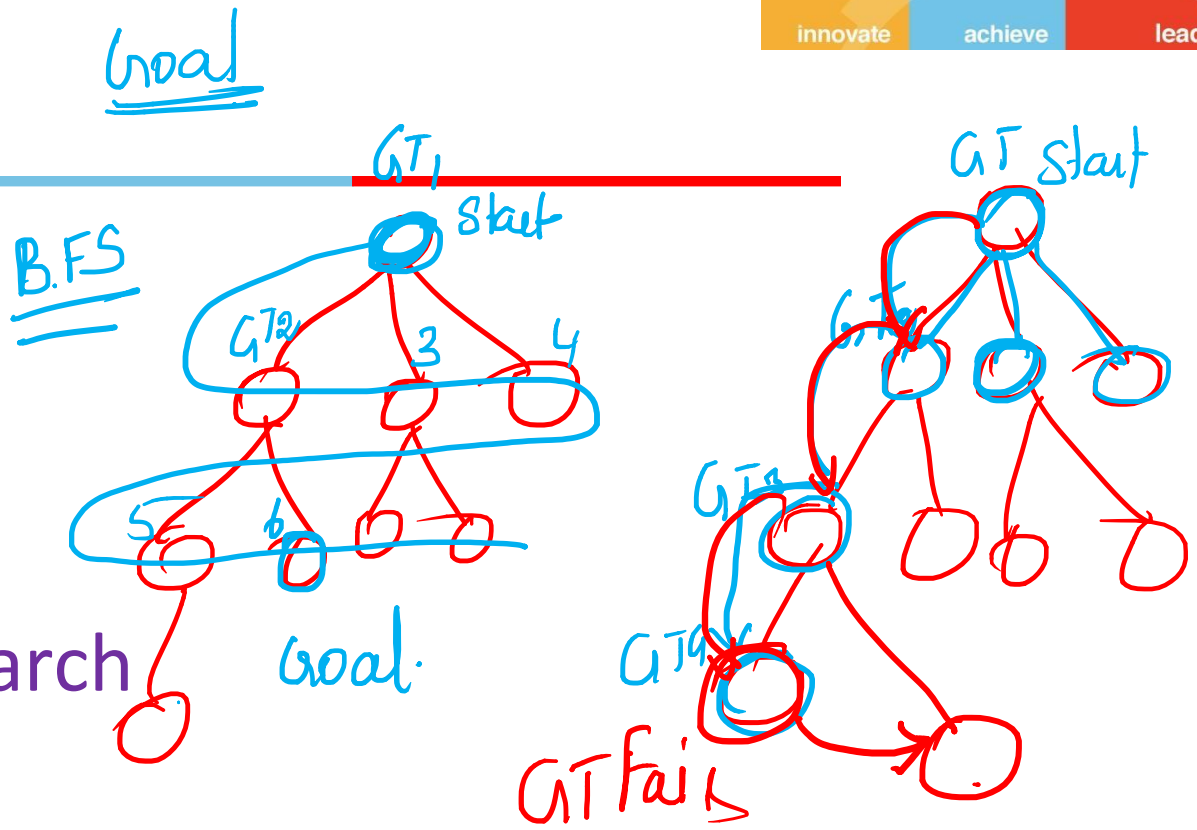


- Finding path in a graph (many solutions)
- Finding the Bipartitions in a graph

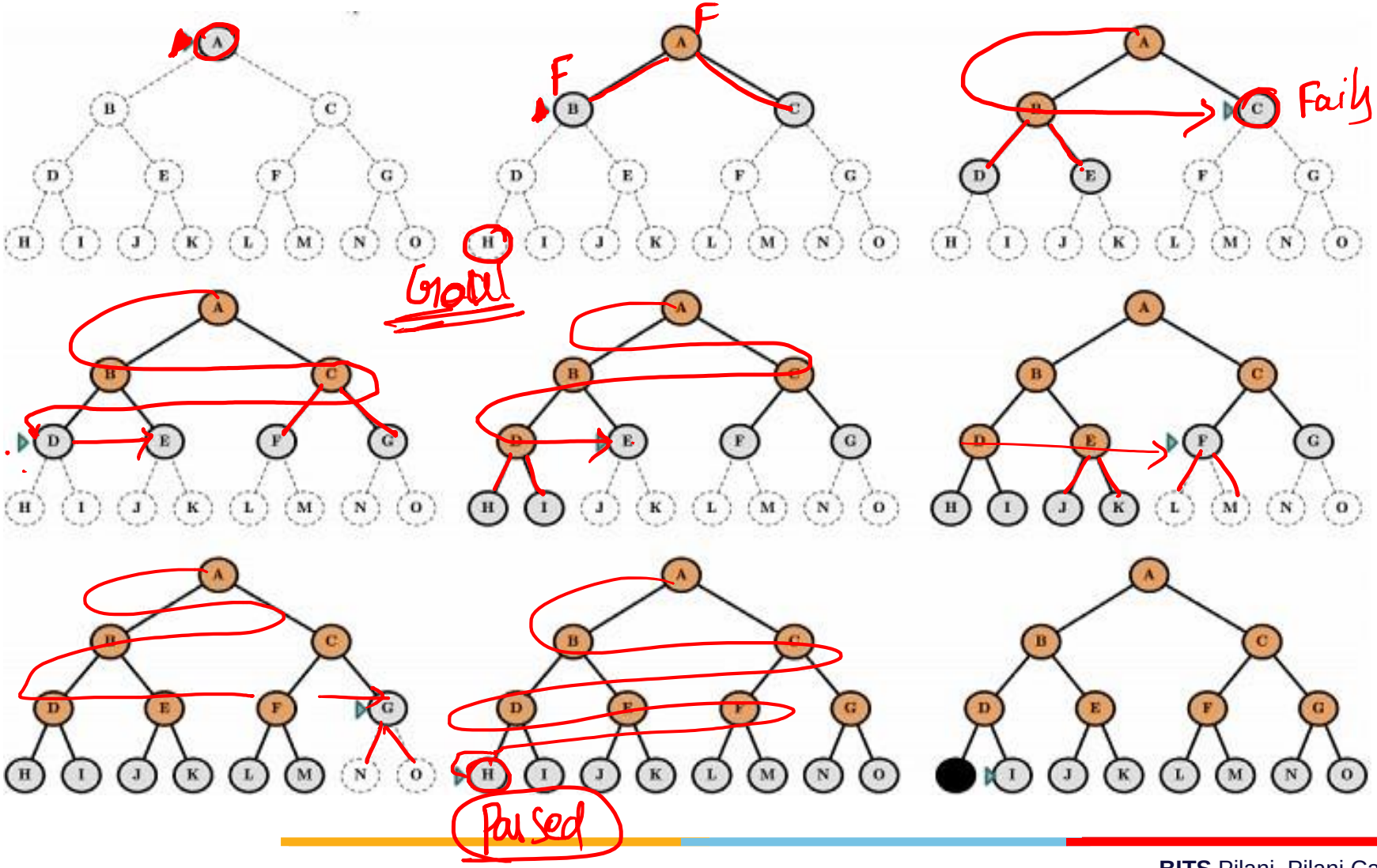
Depth First Search

- Find the Connectedness in a graph
- Topological Sorting

Uninformed Search Overview



Breadth First Search (BFS)



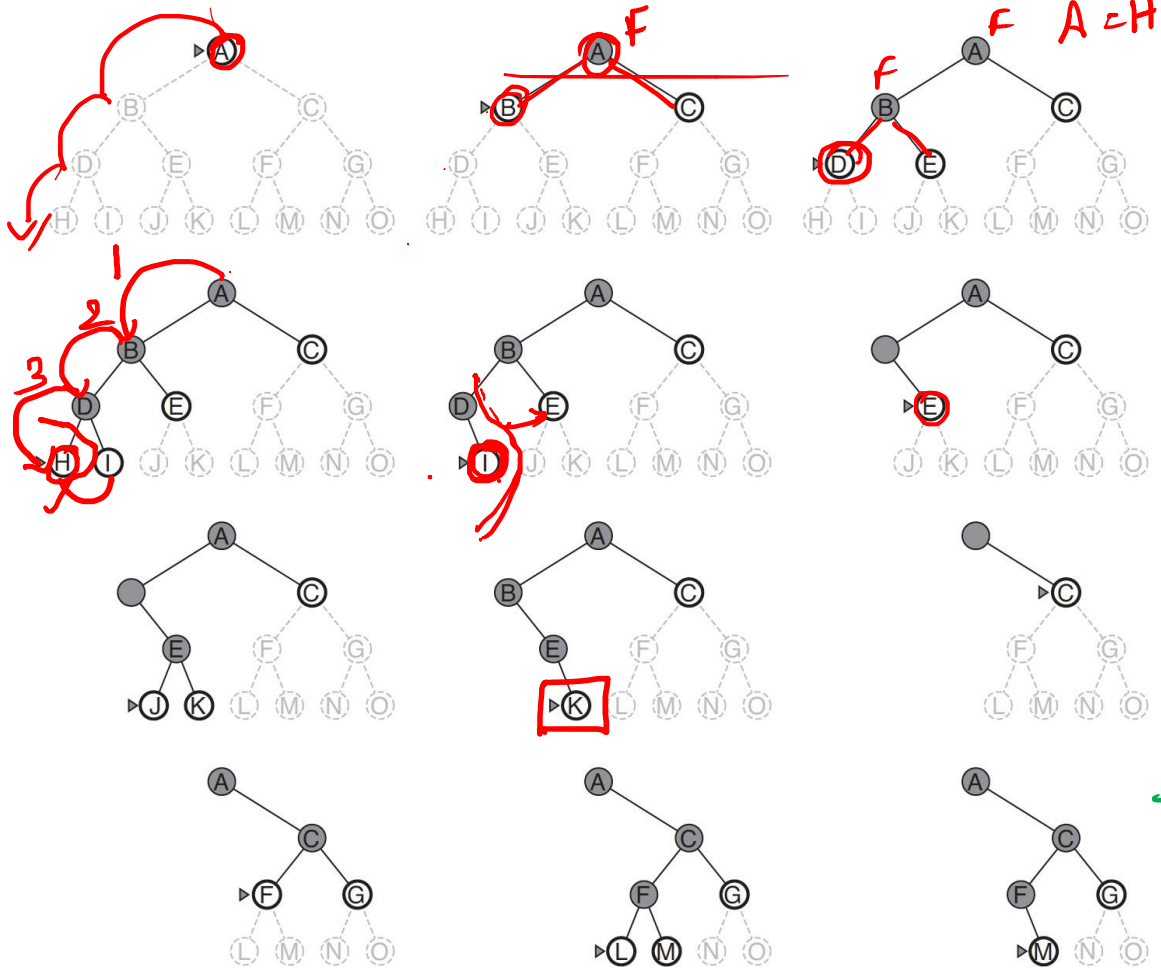
Depth First Search (DFS)

Start state : A

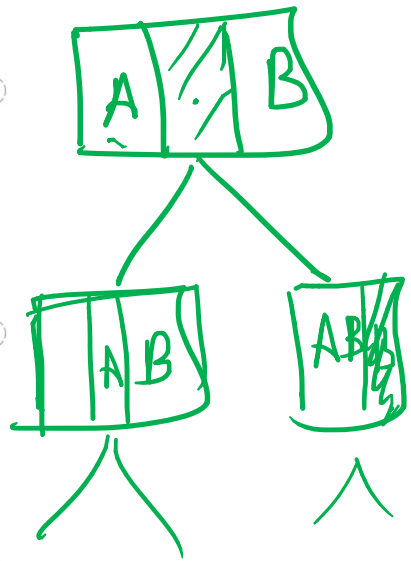
Goal : H

DFS

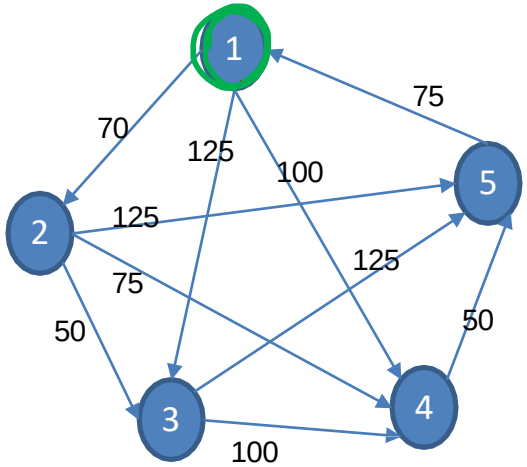
Memory efficient

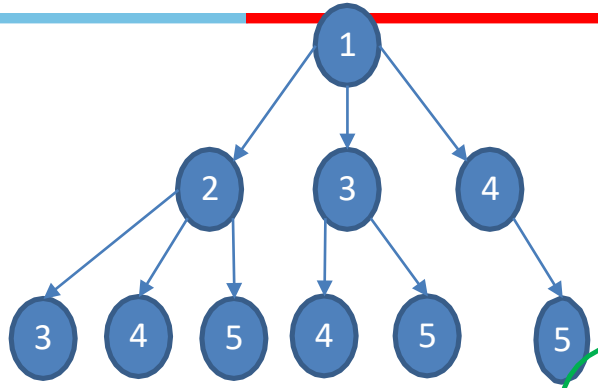


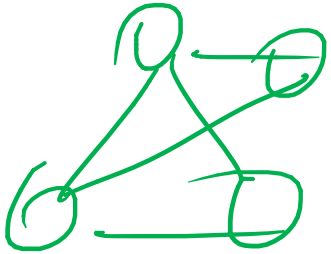
So

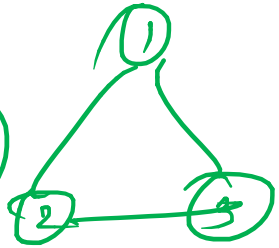


Search Tree – Sample Generation



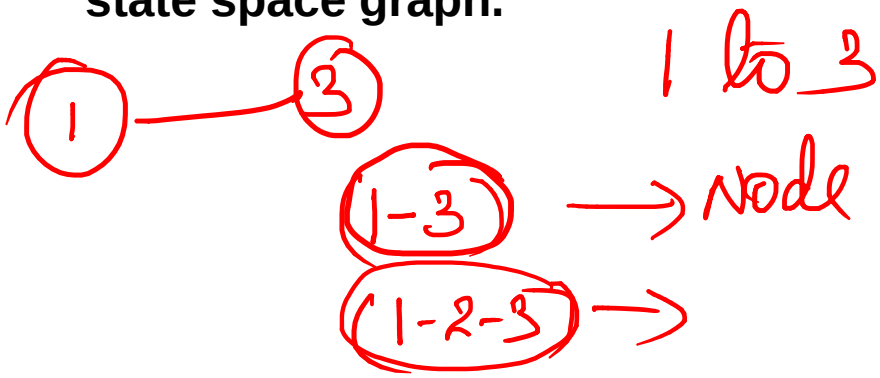






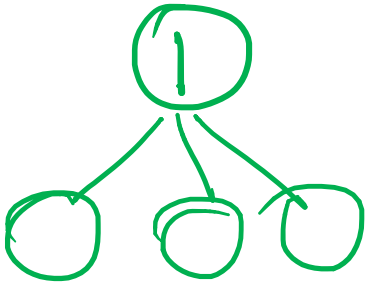
Path

Each NODE in in the search tree denotes an entire PATH through the state space graph.



1 to 3

node

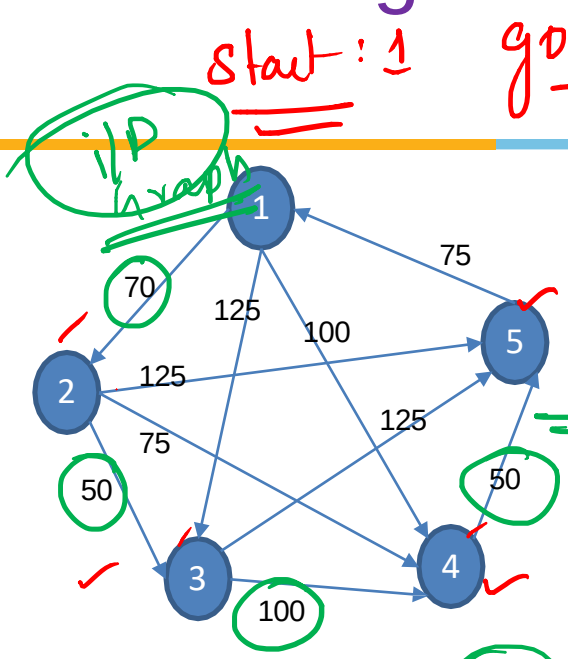


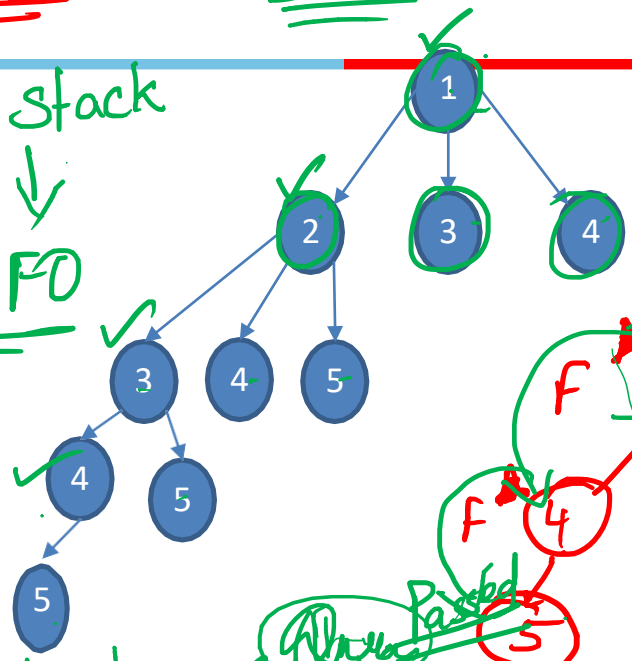
1 — 2, 3

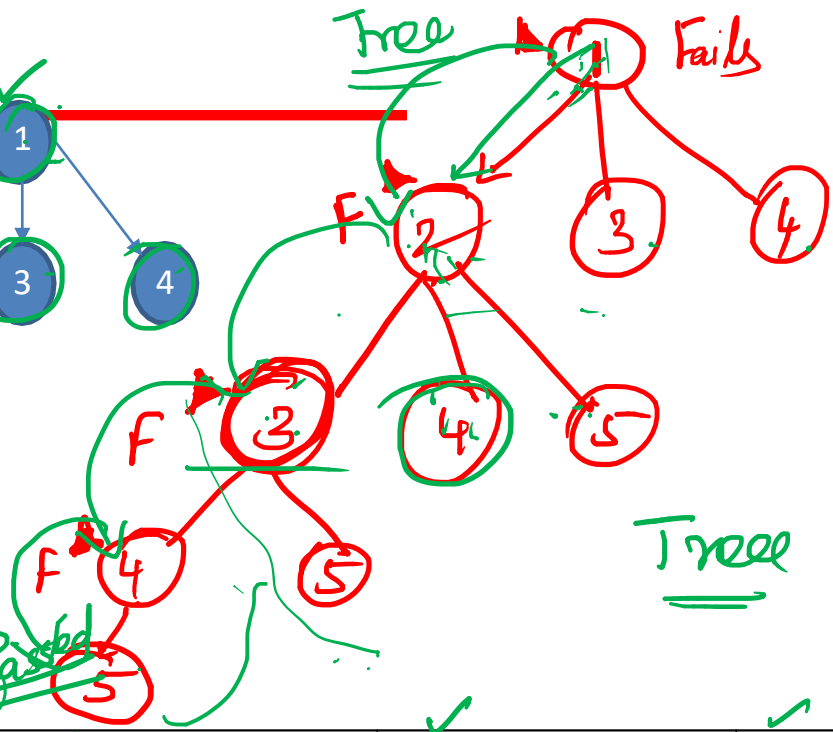
2 → 1, 3

3 — 1, 2

Search Algorithm – Uninformed Example - 1





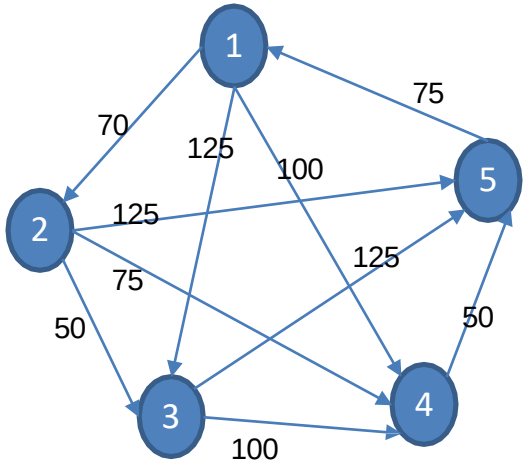


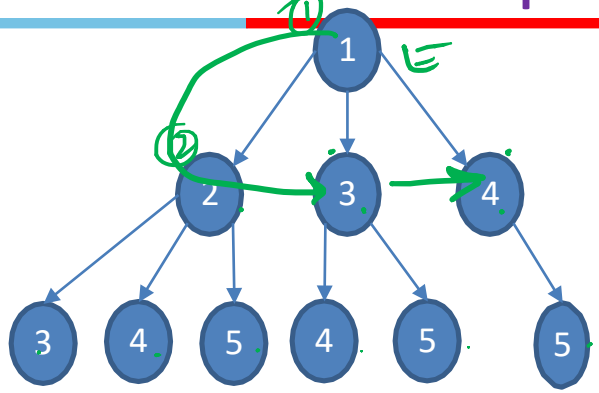
(1)
(1 2) (1 3) (1 4)
(1 2 3) (1 2 4) (1 2 5) (1 3) (1 4)
(1 2 3 4) (1 2 3 5) (1 2 4) (1 2 5) (1 3) (1 4)
(1 2 3 4 5) (1 2 3 5) (1 2 4) (1 2 5) (1 3) (1 4)

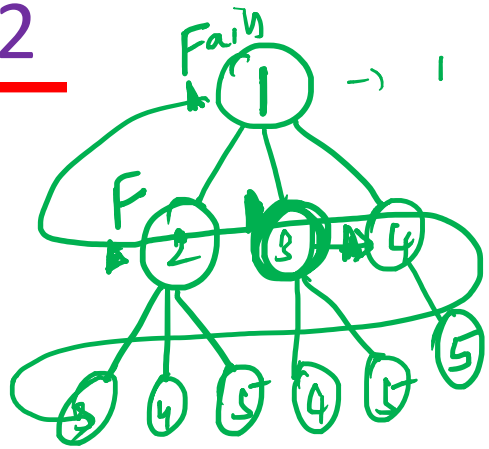
C(1-2-3-4-5) = 70 + 50 + 100 + 50 = 270
Expanded : 4
Generated : 10
Max Queue Length : 6

Iter	Open List / Frontiers / Fringes	Closed List	Goal Tes
1.	(1)		Fail on (1)
2.	(12) (13) (14)	(1)	Fail(12)
	(123) (124) (125) (13) (14)	(1) (12)	F
	(1234) (1235)	(1) (12) (123)	F
	(12345)	(1234)	P

Search Algorithm – Uninformed Example - 2







(1)
(1 2) (1 3) (1 4)
TEST FAILED

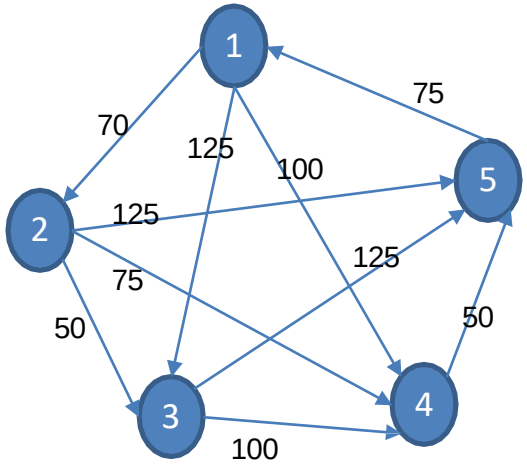
(1 3) (1 4) (1 2 3) (1 2 4) (1 2 5)
(1 2 3) (1 2 4) (1 2 5) (1 3 4) (1 3 5) (1 4 5)

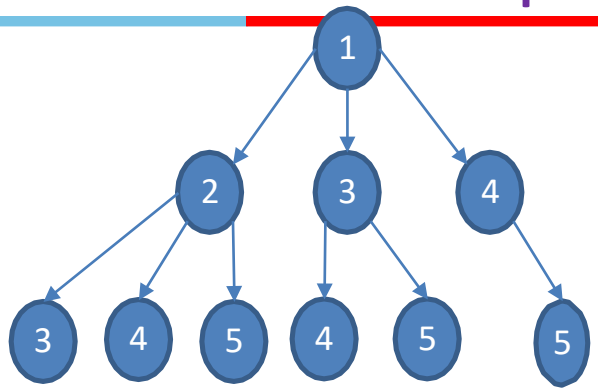
C(1-2-5) = 70 + 125 =195
Expanded : 4
Generated : 10
Max Queue Length : 6

open	closed	Goal
(1)		
(12)(13)(14)		
(13)(14)	(12)	

BFS

Search Algorithm – Uninformed Example - 2





Iter	Open List / Frontiers / Fringes	Closed List	Goal Test
1.	(1)		Fail on (1)
2.			
3.			

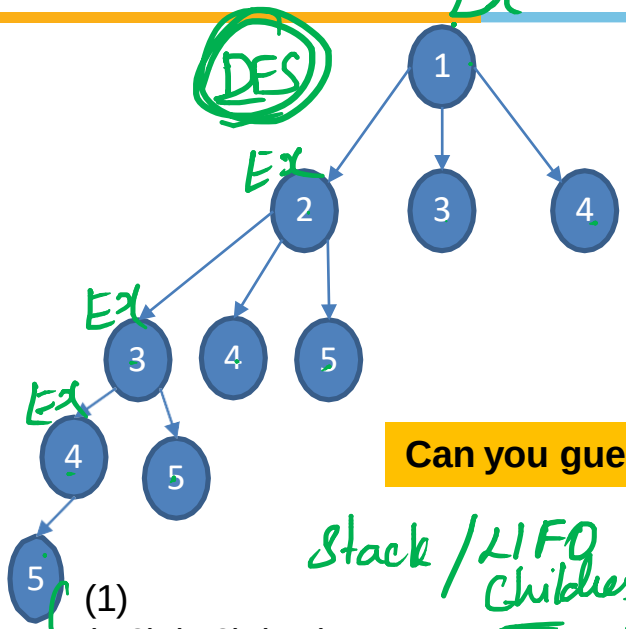
(1)
(1 2) (1 3) (1 4)
TEST FAILED

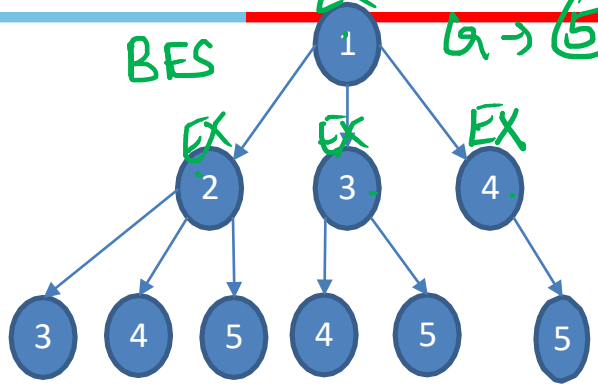
(1 3) (1 4) (1 2 3) (1 2 4) (1 2 5)
(1 2 3) (1 2 4) (1 2 5) (1 3 4) (1 3 5) (1 4 5)

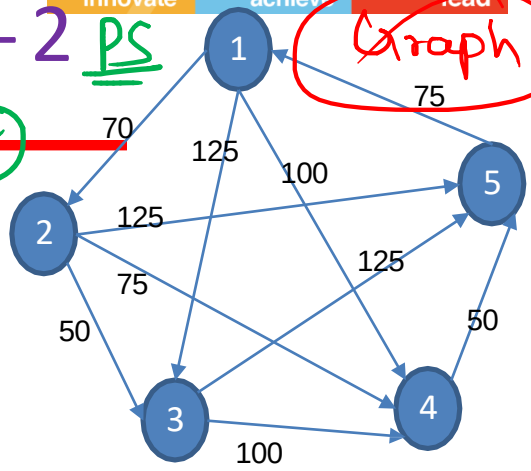
C(1-2-5) = 70 + 125 =195
Expanded : 4
Generated : 10
Max Queue Length : 6

125

Search Algorithm – Uninformed Example - 2







Can you guess which algorithm are these ?

(1)
(1 2) (1 3) (1 4)
(1 2 3) (1 2 4) (1 2 5) (1 3) (1 4)
(1 2 3 4) (1 2 3 5) (1 2 4) (1 2 5) (1 3) (1 4)
(1 2 3 4 5) (1 2 3 5) (1 2 4) (1 2 5) (1 3) (1 4)

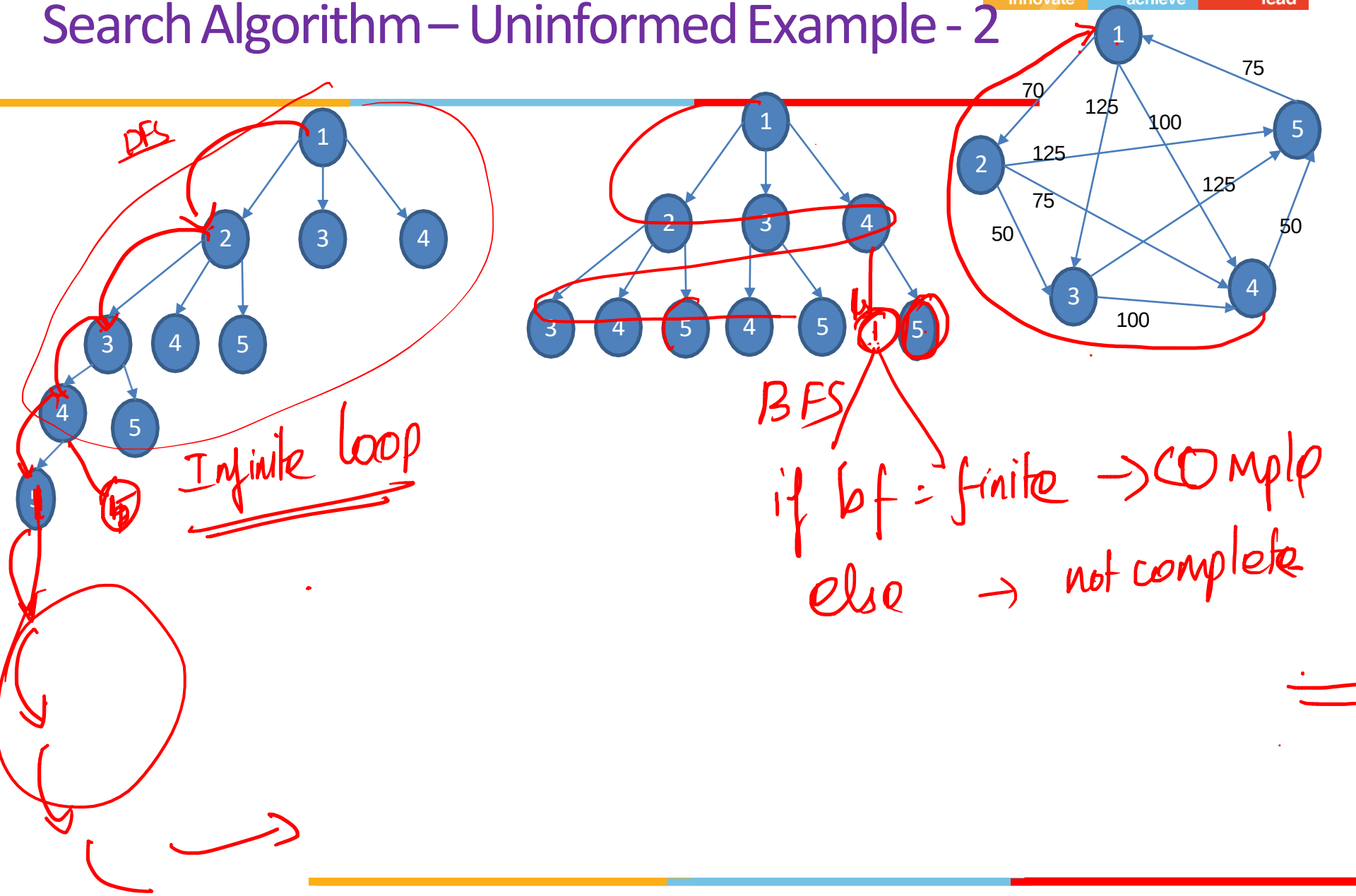
C(1-2-3-4-5) = 70 + 50 + 100 + 50 = 270
Expanded : 4
Generated : 10
Max Queue Length : 6

(1)
(1 2) (1 3) (1 4)
TEST FAILED

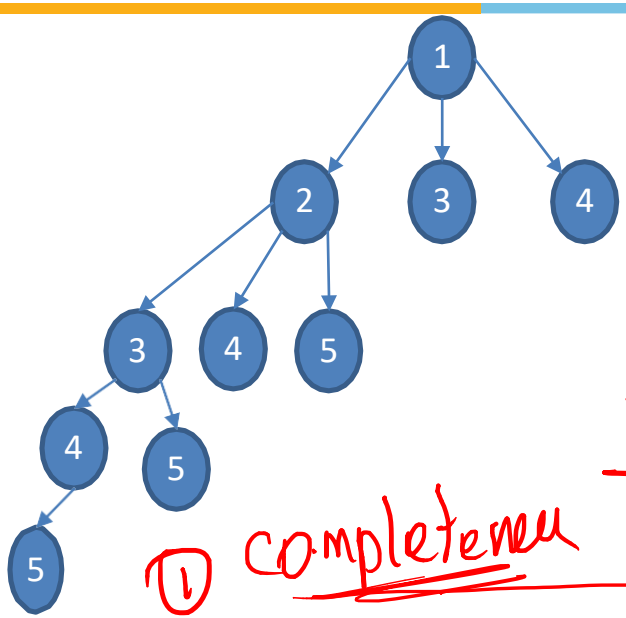
(1 3) (1 4) (1 2 3) (1 2 4) (1 2 5)
(1 2 3) (1 2 4) (1 2 5) (1 3 4) (1 3 5) (1 4 5)
TEST PASSED

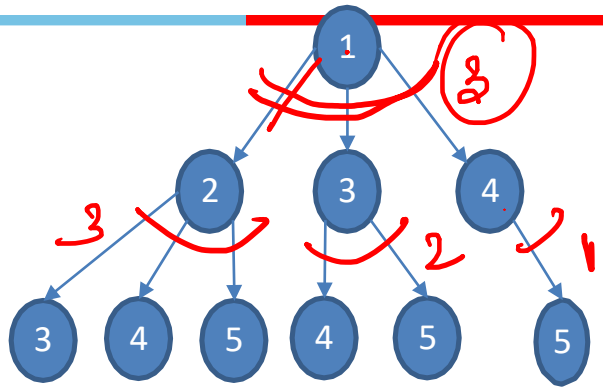
C(1-2-5) = 70 + 125 = 195
Expanded : 4
Generated : 10
Max Queue Length : 6

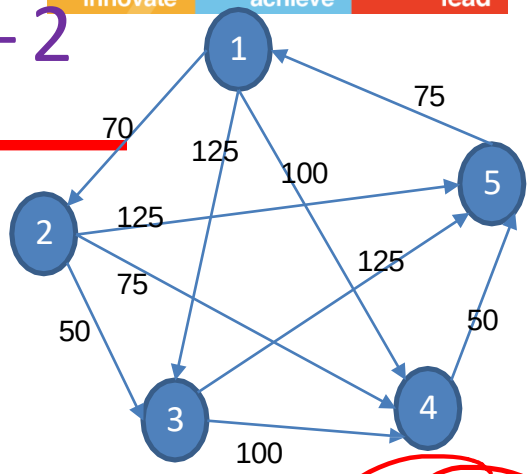
Search Algorithm – Uninformed Example - 2



Search Algorithm – Uninformed Example - 2

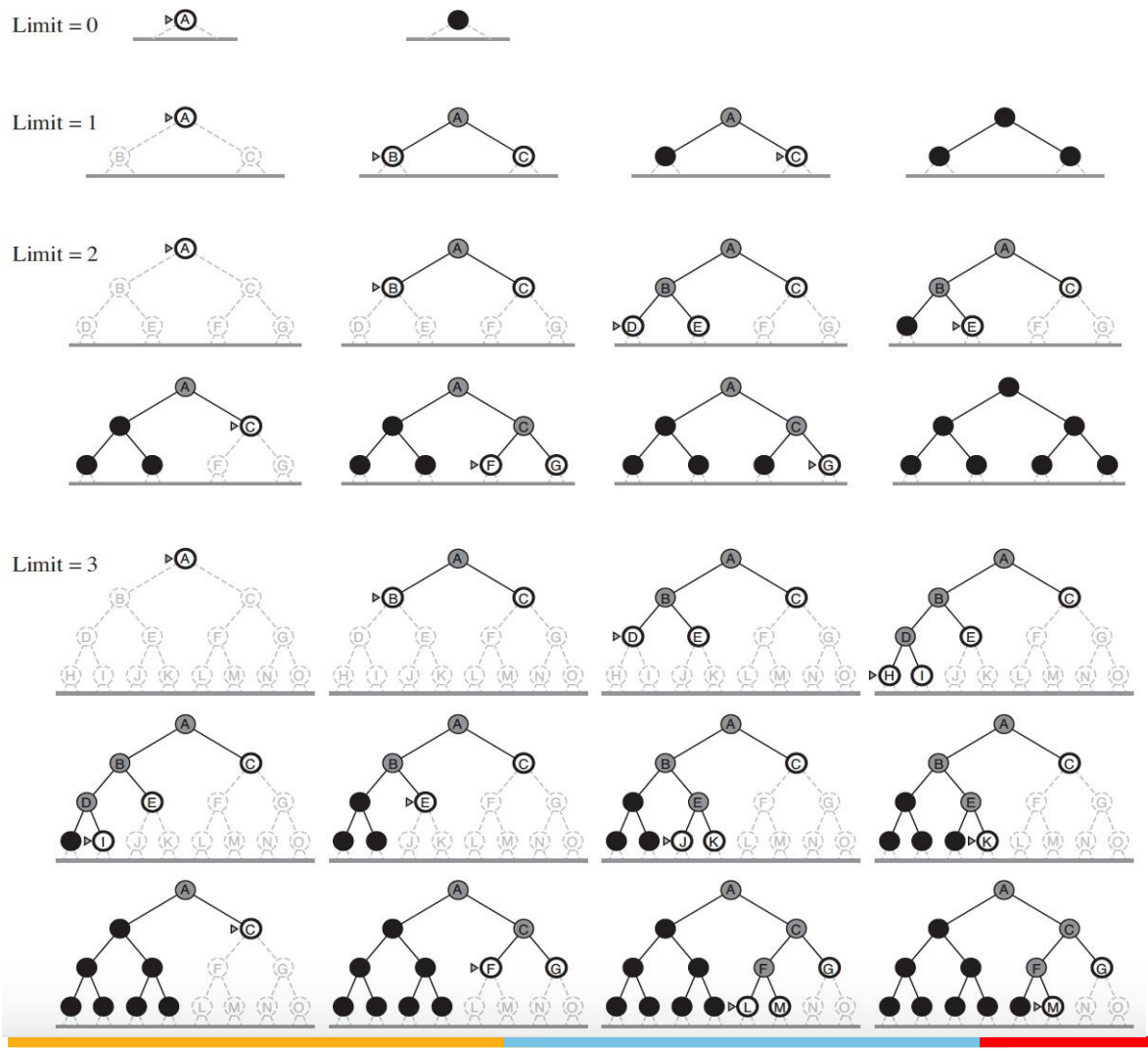






	DFS	BFS
1. Completeness	Not comp	if branching factor finite → optimal else "" "not" → No optimal
2. Optimality	Not opt	Can be optimal
3. Time Complexity		
4. Space Complexity		

Iterative Deepening Depth First Search (IDS)



Algorithm Tracing

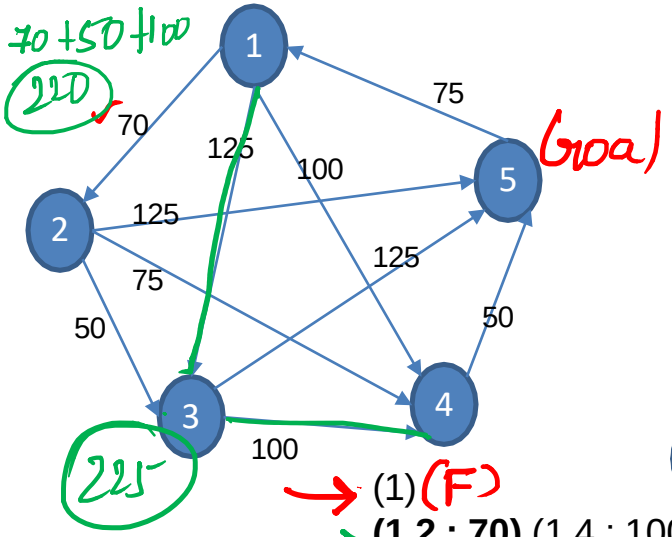
Students must follow this in the exams for all the search algorithms in addition to the search tree constructions. The ordering of the Open Lists must be in consistent with the algorithm with a note on the justification of the order expected!

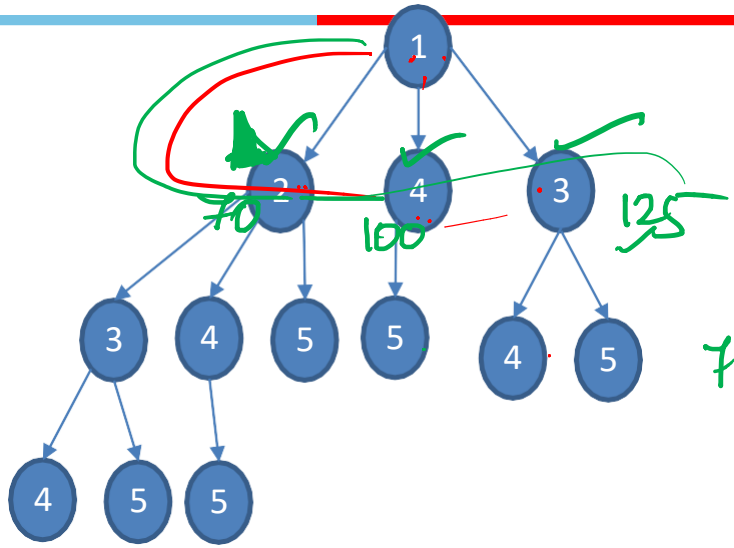
Iter	Open List / Frontiers / Fringes	Closed List	Goal Test
1.	(1)		Fail on (1)
2.			

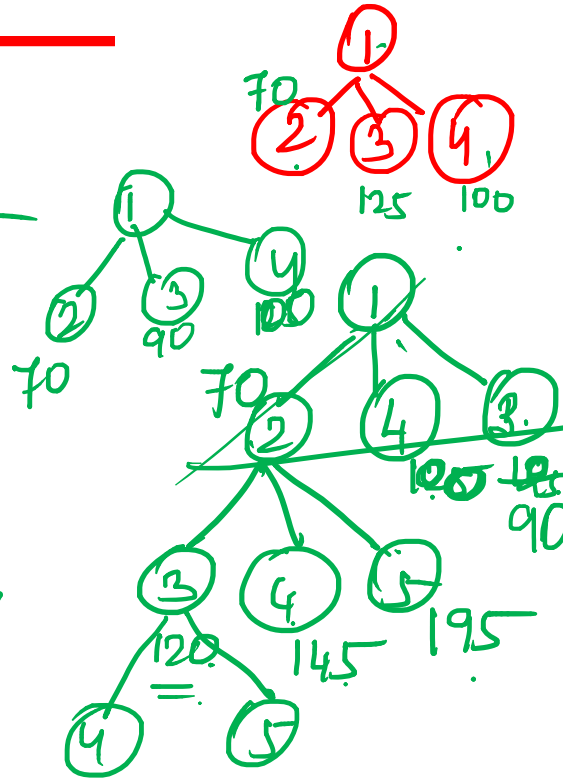
Variant BFS

UCS → Uniform Cost search

Priority Queue







(1) (F)

(1 2 : 70) (1 4 : 100) (1 3 : 125)

TEST-F

(1 4 : 100) (1 2 3 :120)(1 3 : 125) (1 2 4 : 145) (1 2 5 : 195)

TEST-F

(1 2 3 :120)(1 3 : 125) (1 2 4 : 145) (1 4 5: 150)(1 2 5 : 195)

TEST-F

(1 3 : 125) (1 2 4 : 145) (1 4 5: 150) (1 2 3 4:170) (1 2 5 : 195) (1 2 3 5 : 245)

TEST-F

(1 2 4 : 145) (1 4 5: 150) (1 2 3 4:170) (1 2 5 : 195) (1 3 4 : 225) (1 2 3 5 : 245) (1 3 5 : 250)

TEST-F

(1 4 5: 150) (1 2 3 4:170) (1 2 4 5 : 195) (1 2 5 : 195) (1 3 4 : 225) (1 2 3 5 : 245) (1 3 5 : 250)

TEST - P

FIFO

Passed

Uniform Cost Search

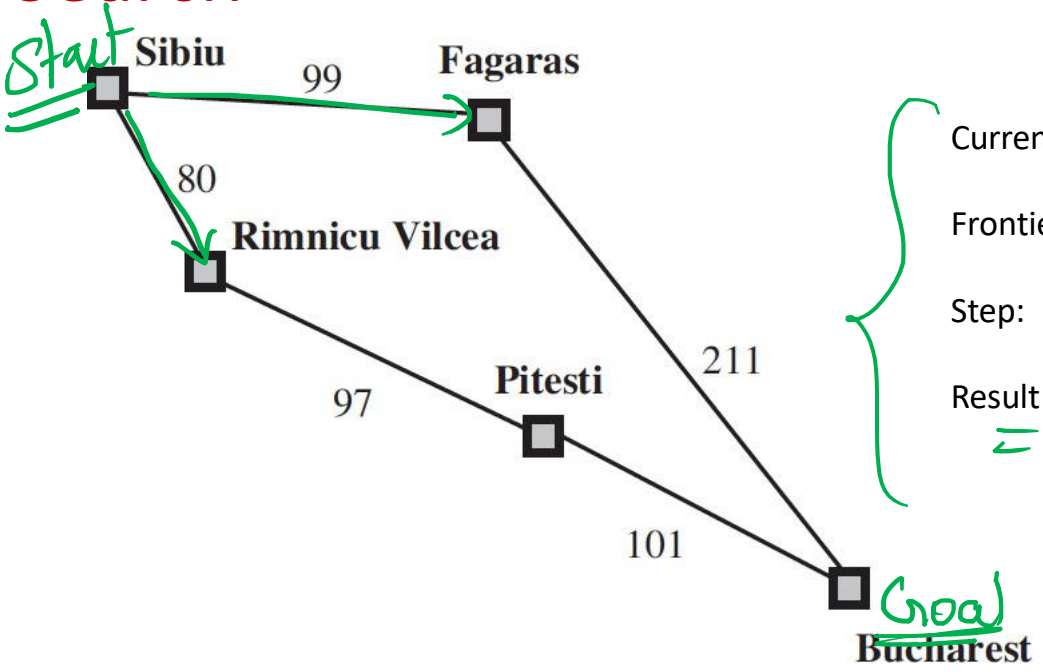
Instead of expanding the shallowest node, Uniform-Cost search expands the node n with the lowest path cost g(n)

Sorting the Frontier as a priority queue ordered by g(n)

Goal test is applied during expansion

- The goal node if generated may not be on the optimal path
- Find a better path to a node on the Frontier

Uniform Cost Search



Current State: Sibiu

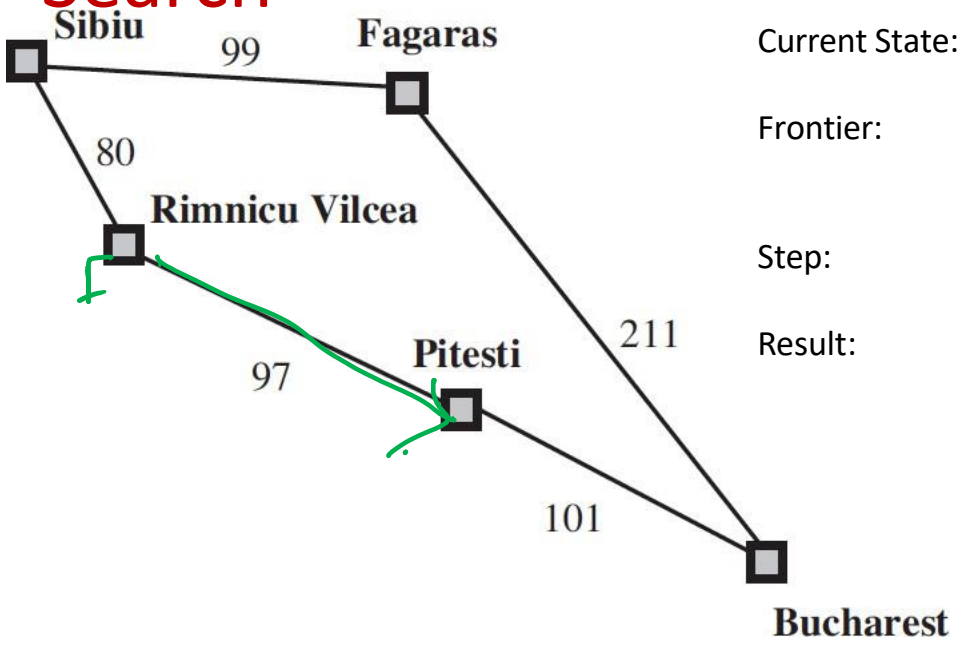
Frontier: []

Step: Expand Sibiu

Result: Generates ("Rimnicu Vilcea" 80)
("Fagaras", 99)
Add to Frontier

Initial State: Sibiu
Goal State: Bucharest

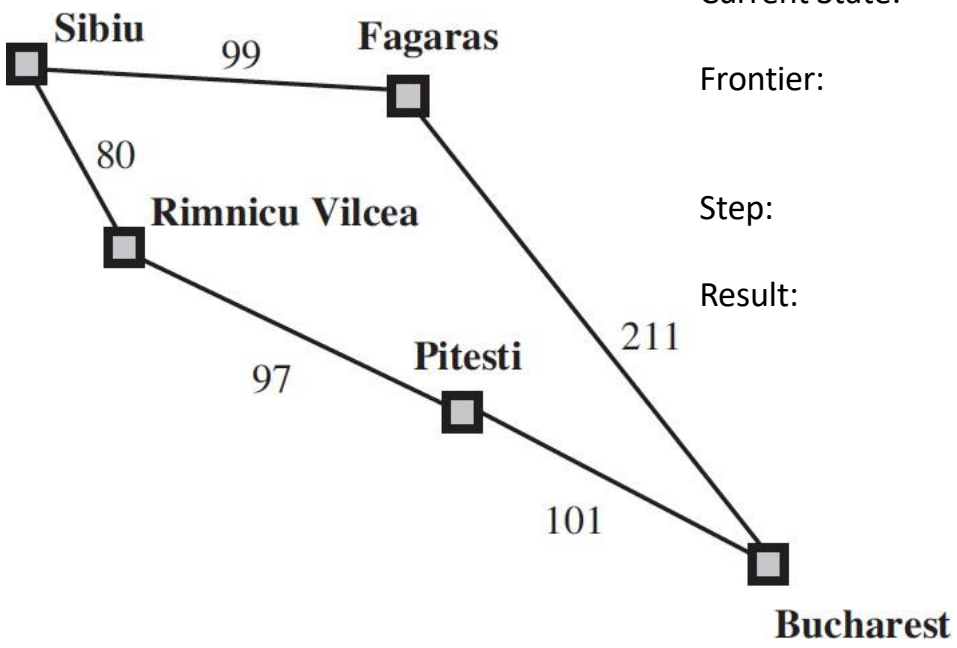
Uniform Cost Search



Current State:	Sibiu
Frontier:	[(“Rimnicu Vilcea” 80) (“Fagaras”, 99)]
Step:	Expand “Rimnicu Vilcea” (least cost)
Result:	Generates (“Pitesti”, 177) Add to Frontier

Initial State:	Sibiu
Goal State:	Bucharest

Uniform Cost Search



Current State: Rimnicu Vilcea (not a Goal state)

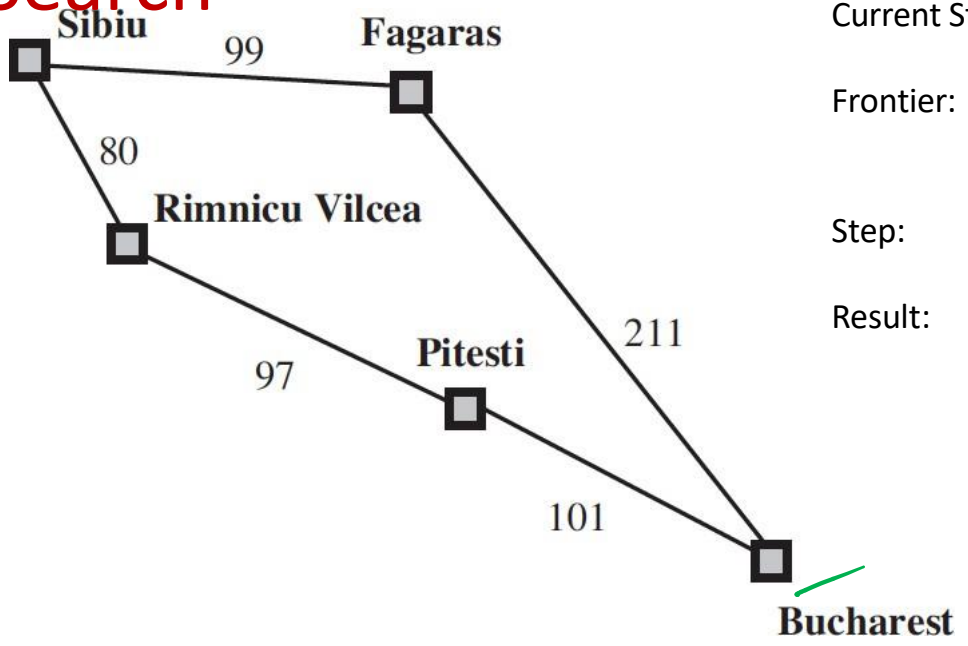
Frontier: [(“Fagaras”, 99)
(“Pitesti”, 177)]

Step: Expand “Fagaras” (least cost)

Result: Generates (“Bucharest”, 310)
Add to Frontier
(It’s a Goal State but we won’t test during generation)

Initial State: Sibiu
Goal State: Bucharest

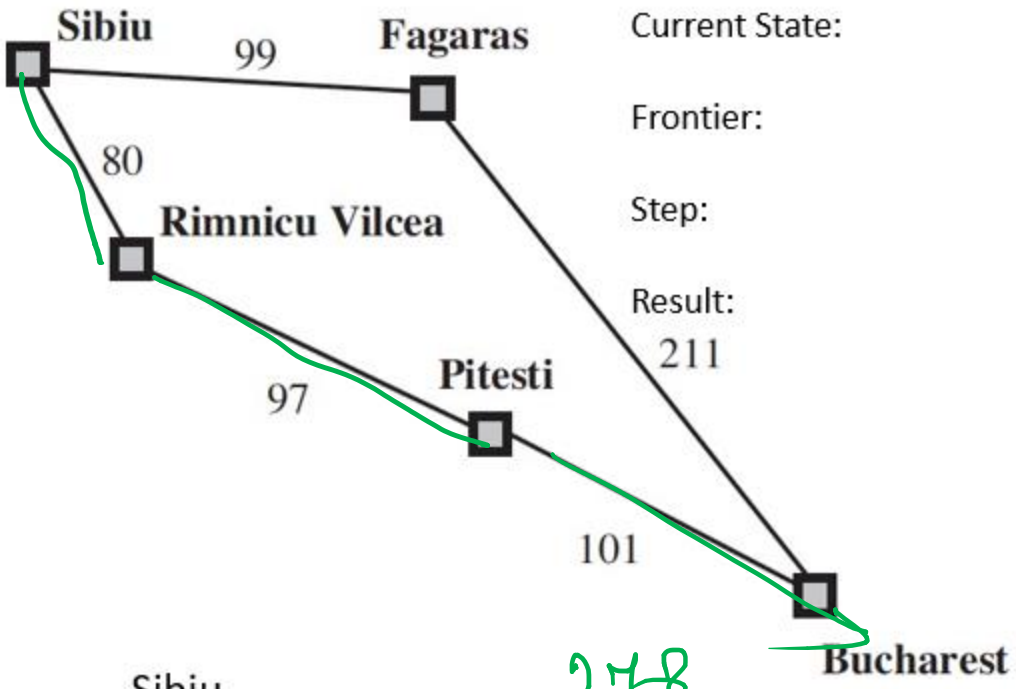
Uniform Cost Search



Current State:	Fagaras (not a goal state)
Frontier:	[(“Pitesti”, 177) (“Bucharest”, 310)]
Step:	Expand “Pitesti” (least cost)
Result:	Generates (“Bucharest” 278) Replace in Frontier (It’s a Goal State but we won’t test during generation)

Initial State:	Sibiu
Goal State:	Bucharest

Uniform Cost Search



Initial State: Sibiu
Goal State: Bucharest

Current State: Pitesti (not a goal state)

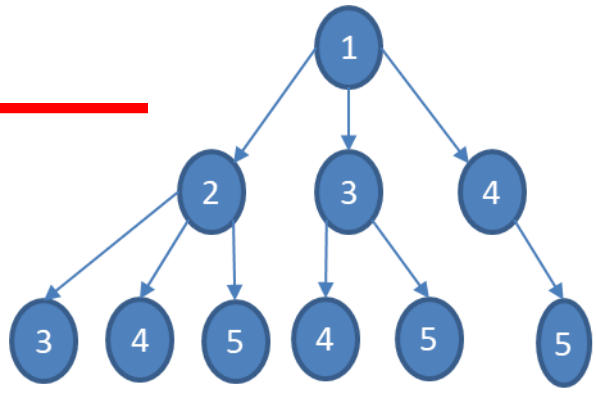
Frontier: [("Bucharest", 278)]

Step: Expand "Bucharest"

Result: No further generation as Goal Test satisfied Return Solution

278

Sample Evaluation of the Algorithm



Complete – If the shallowest goal node is at a depth d, BFS will eventually find it by generating all shallower nodes

Optimal – Not necessarily. Optimal if path cost is non-decreasing function of depth of node.
E.g., all actions have same cost

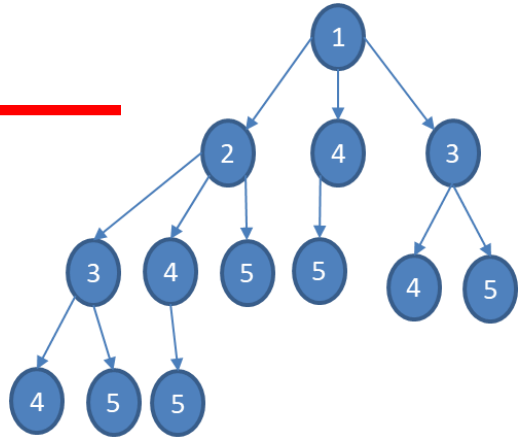
Time Complexity – $G(b^d)$ b - branching factor, d – depth

- Nodes expanded at depth 1 = b
- Nodes expanded at depth 2 = b^2
- Nodes expanded at depth d = b^d
- Goal test is applied during generation, time complexity would be $G(b^{d+1})$

Space Complexity – $G(b^d)$

- $G(b^{d-1})$ in explored set
- $G(b^d)$ in frontier set

Uniform Cost Search – Evaluation



Completeness – It is complete if the cost of every step > small +ve constant ∈

- It will stuck in infinite loop if there is a path with infinite sequence of zero cost actions

Optimal – It is Optimal. Whenever it selects a node, it is an optimal path to that node.

Time and Space complexity – Uniform cost search is guided by path costs not depth or branching factor.

- If C* is the cost of optimal solution and ∈ is the min. action cost
- Worst case complexity = $G(b^{1+\frac{C^*}{\epsilon}})$,
- When all action costs are equal ⇨ $G(b^{d+1})$, the BFS would perform better
  - As Goal test is applied during expansion, Uniform Cost search would do extra work

Terminologies – Learnt Today

- Nodes
- States
- Frontier | Fringes
- Search Strategy : LIFO | FIFO | Priority Queue
- Performance Metrics
  - Completeness
  - Optimality
  - Time Complexity
  - Space Complexity
- Algorithm Terminology

- d Depth of a node	- m – maximum
- b Branching factor	- C* - Optimal Cost
- n – nodes	- E – least Cost
- l – level of a node	- N –total node generated

Module 2 : Problem Solving Agent using Search

A. Uninformed Search

B. Informed Search

C. Heuristic Functions

D. Local Search Algorithms & Optimization Problems

Learning Objective

At the end of this class , students Should be able to:

1. Differentiate between uninformed and informed search requirements
2. Apply UCS, GBFS & A* algorithms to the given problem
3. Prove if the given heuristics are admissible and consistent
4. Design and compare heuristics apt for given problem
5. Apply A* variations algorithms to the given problem

Informed Search

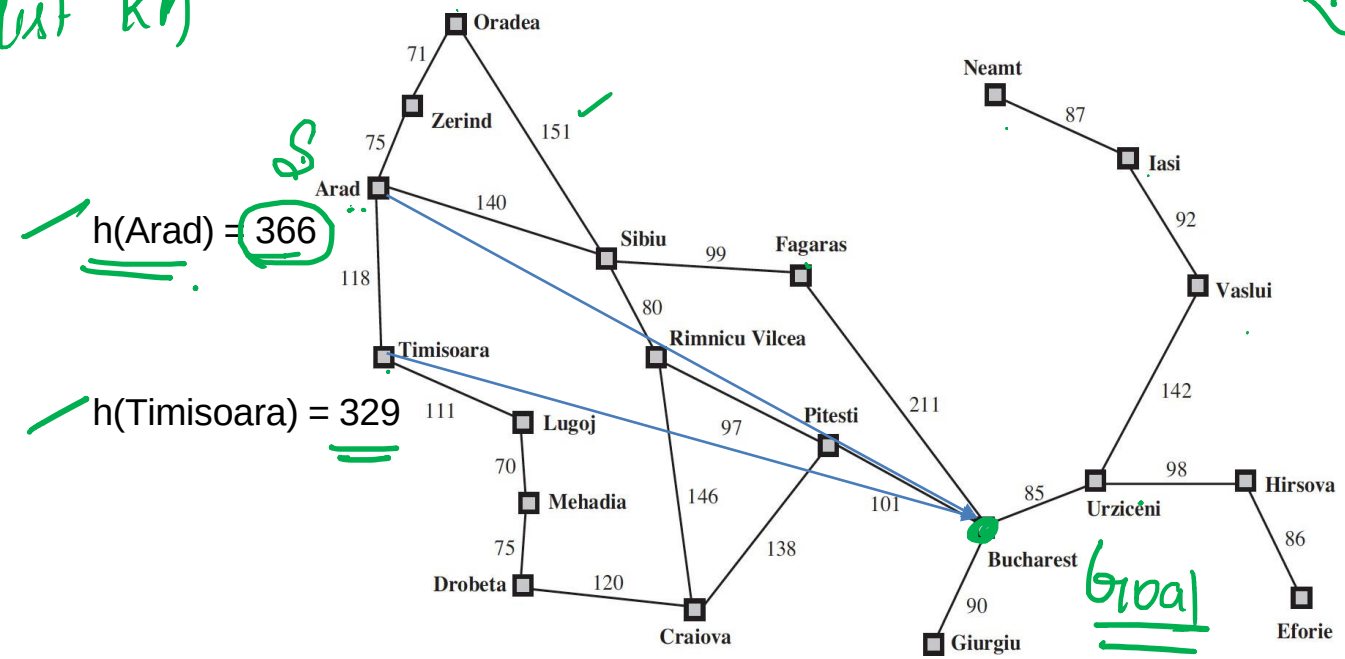
1. Greedy Best First
2. A*

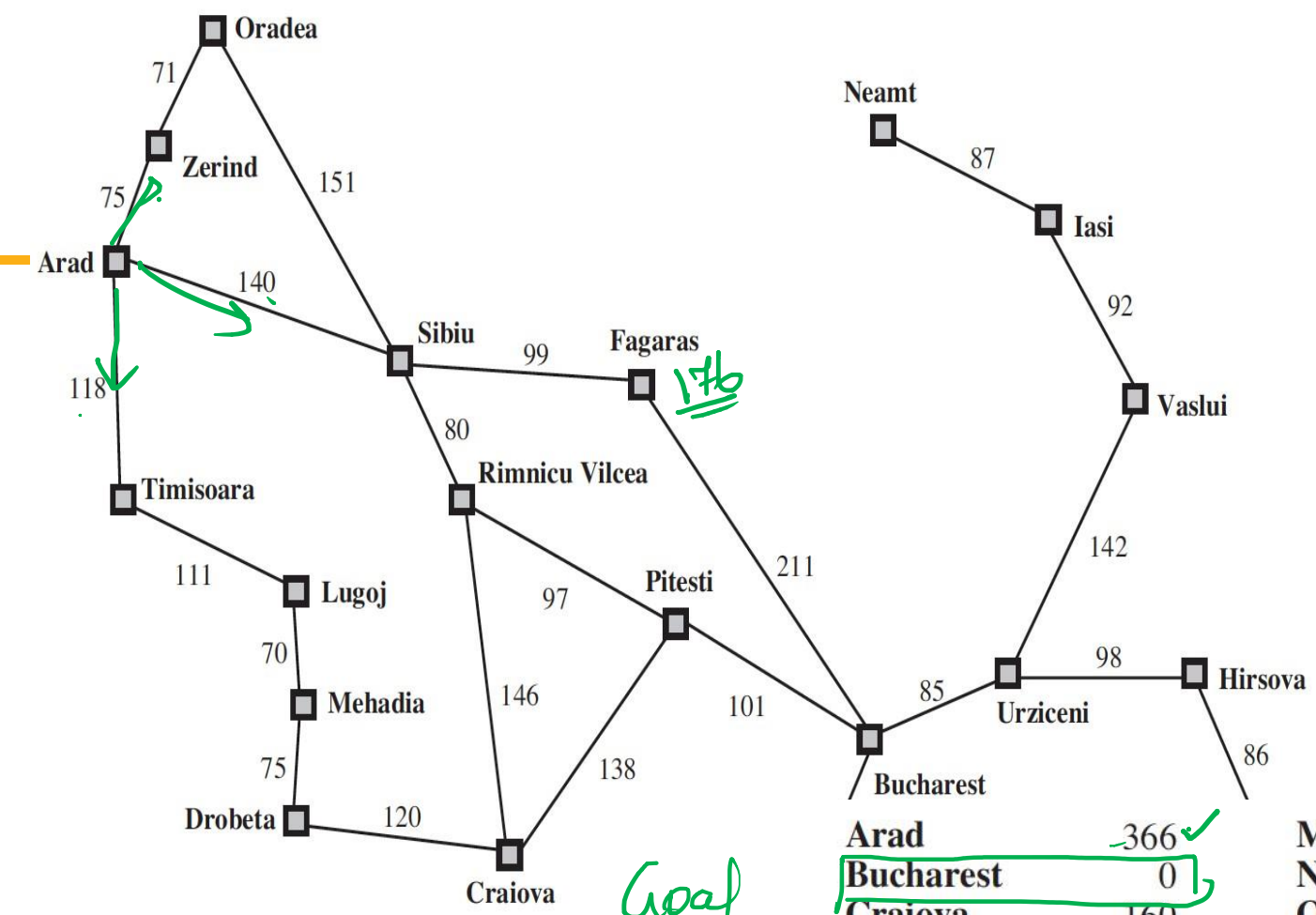
Informed /Heuristic Search

Strategies that know if one non-goal state is more promising than another non-goal state

h(Arad) = 366

h(Timisoara) = 329





Goal

Goal

Arad	366
Bucharest	0
Craiova	160
Drobeta	242
Eforie	161
Fagaras	176
Giurgiu	77
Hirsova	151
Iasi	226
Lugoj	244

Mehadia	241
Neamt	234
Oradea	380
Pitesti	100
Rimnicu Vilcea	193
Sibiu	253
Timisoara	329
Urziceni	80
Vaslui	199
Zerind	374

Domain expert

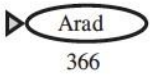
Greedy Best First Search

Expands the node that is closest to the goal

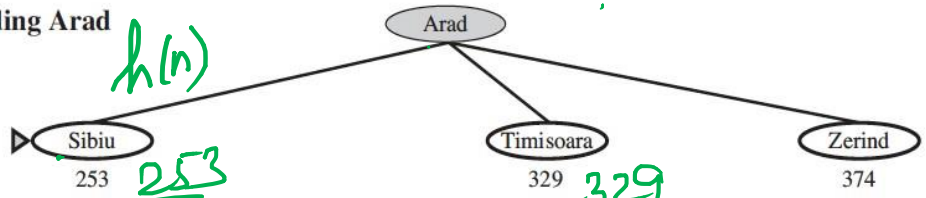
Thus, **f(n) = h(n)**

Arad	366	**Mehadia**	241
Bucharest	0	**Neamt**	234
Craiova	160	**Oradea**	380
Drobeta	242	**Pitesti**	100
Eforie	161	**Rimnicu Vilcea**	193
Fagaras	176	**Sibiu**	253
Giurgiu	77	**Timisoara**	329
Hirsova	151	**Urziceni**	80
Iasi	226	**Vaslui**	199
Lugoj	244	**Zerind**	374

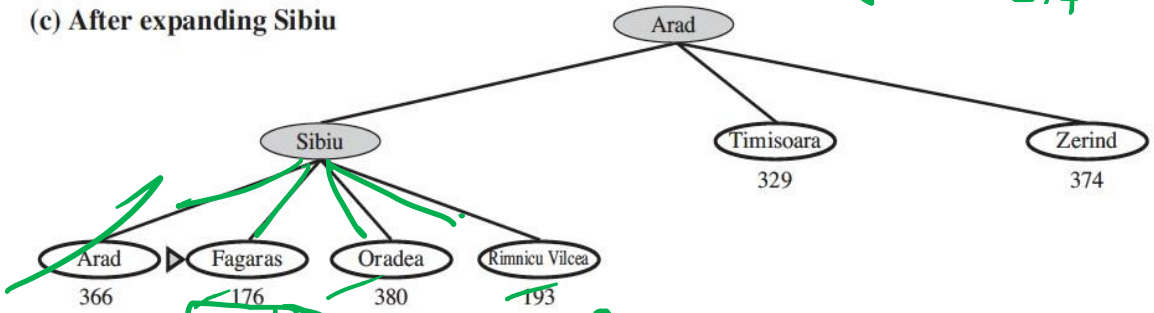
(a) The initial state



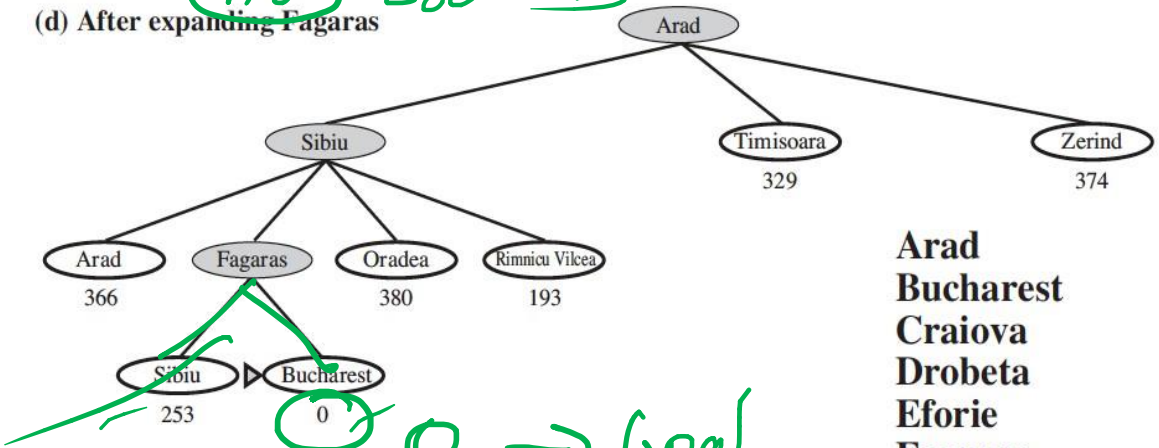
(b) After expanding Arad



(c) After expanding Sibiu

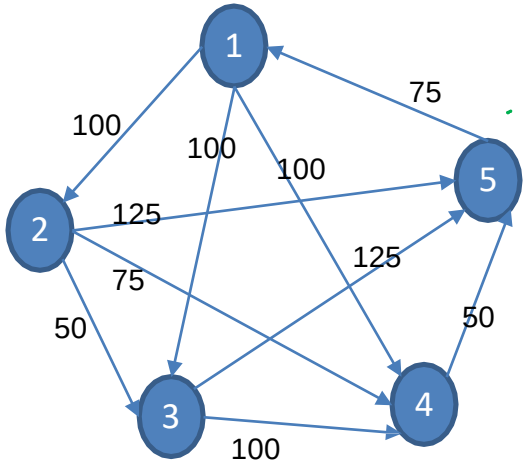


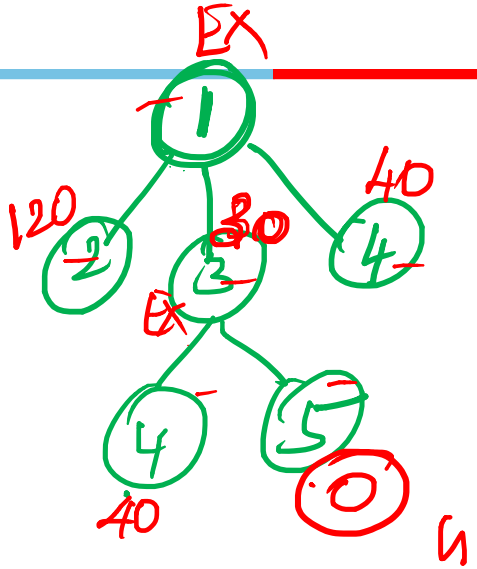
(d) After expanding Fagaras

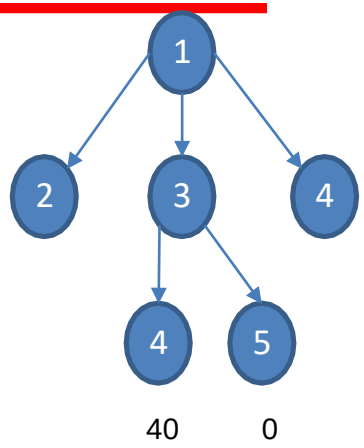


Arad	366	Mehadia	241
Bucharest	0	Neamt	234
Craiova	160	Oradea	380
Drobeta	242	Pitesti	100
Eforie	161	Rimnicu Vilcea	193
Fagaras	176	Sibiu	253
Giurgiu	77	Timisoara	329
Hirsova	151	Urziceni	80
Iasi	226	Vaslui	199
Lugoj	244	Zerind	374

Greedy Best First Search







Given

n	h(n)
1	60
2	120
3	30
4	40
5	0

(1)
(1 3) (1 4) (1 2)
(1 3 5) (1 3 4)

C(1-3-5) = 100 + 125 =225
Expanded : 2
Generated : 6
Max Queue Length : 3

A* Search

Expands the node which lies in the closest path (estimated cheapest path) to the goal

Evaluation function **f(n) = g(n) + h(n)**

g(n) – the cost to reach the node

h(n) – the expected cost to go from node to goal

f(n) – estimated cost of cheapest path through node n

Arad	366	**Mehadia**	241
Bucharest	0	**Neamt**	234
Craiova	160	**Oradea**	380
Drobeta	242	**Pitesti**	100
Eforie	161	**Rimnicu Vilcea**	193
Fagaras	176	**Sibiu**	253
Giurgiu	77	**Timisoara**	329
Hirsova	151	**Urziceni**	80
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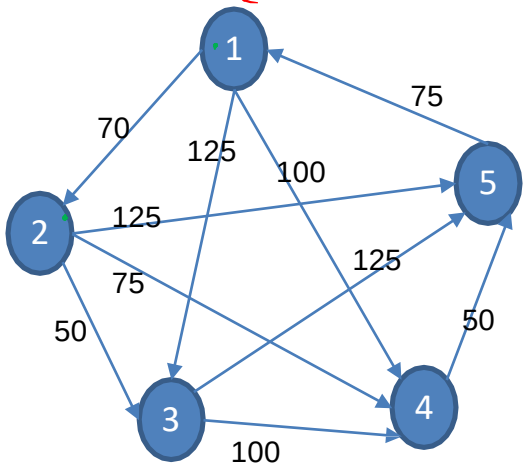
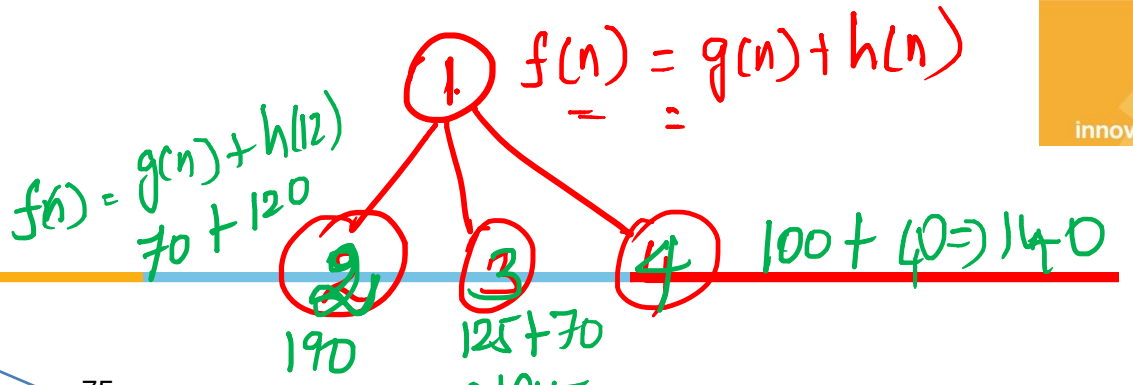
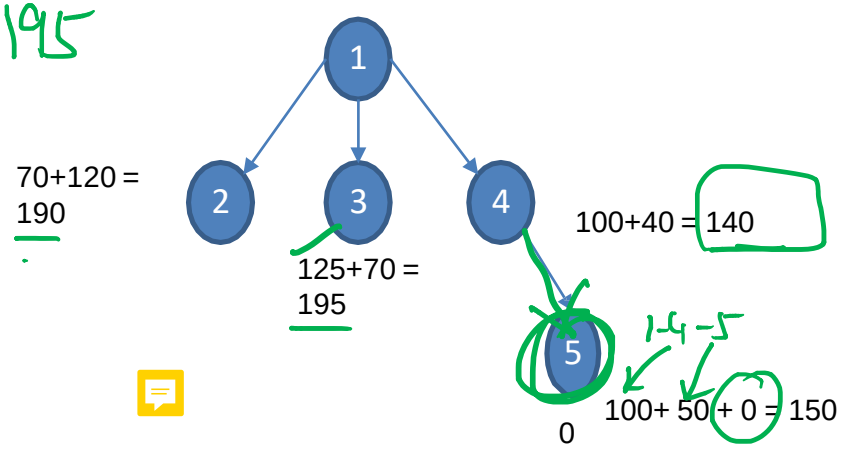
A* Search







n	h(n)
1	60
2	120
3	70
4	40
5	0

(1)
(1 4) (1 2) (1 3)
(1 4 5) (1 2) (1 3)

C(1-4-5) = 100 + 150 =150
Expanded : 2
Generated : 5
Max Queue Length : 3

1-4-5

Required Reading: AIMA - Chapter #1, 2, 3.1, 3.2, 3.3

Thank You for all your Attention

Note : Some of the slides are adopted from AIMA TB materials