Grid Unique Paths II - Maze Obstacles



Problem Statement

We are given an MxN Maze. The maze contains some obstacles. A cell is 'blockage' in the maze if its value is -1. 0 represents non-blockage. There is no path possible through a blocked cell.

We need to count the total number of unique paths from the top-left corner of the maze to the bottom-right corner. At every cell, we can move either down or towards the right.

Editorial

Recursion

Approach

Understand the Movement and Base Rules: A cell maze[i][j] == -1 is blocked: cannot step into it.

Define the Subproblem: Let **f(i, j)** represent the **number of unique paths to reach cell (i, j)** from the top-left, considering blockages.

Note: If (i,j) is **blocked**, there is **no path** that can ever end at this cell.

That is, we can return 0 if the element is -1.

```
if (maze[i][j] == -1) return 0;
```

We will be doing a top-down recursion, i.e we will move from the <code>cell[M-1][N-1]</code> and try to find our way to the <code>cell[0][0]</code>. Therefore at every index, we will try to move up and towards the left.

Code

```
int f(int i, int j, vector<vector<int>>& maze){
    if(i == 0 && j == 0) return 1;
    if(i < 0 || j < 0) return 0;

if(maze[i][j] == -1) return 0;

return f(i - 1, j, maze) + f(i, j - 1, maze);
}</pre>
```

Complexity Analysis

Time Complexity: O(2^(m+n)) - because each cell may branch into two recursive calls (up and left), leading to exponential growth.

Space Complexity: O(m+n) - due to the maximum depth of the recursion stack from top-left to bottom-right.

Memoization

Approach

General steps:

- Store the result.
- · Return value if already calculated.

Code

```
int f(int i, int j, vector<vector<int>>& maze, vector<vector<int>>& dp) {
   if (i < 0 || j < 0) return 0;
   if (maze[i][j] == -1) return 0;
   if (i == 0 && j == 0) return 1;
   if (dp[i][j] != -1) return dp[i][j];
   return dp[i][j] = f(i - 1, j, maze, dp) + f(i, j - 1, maze, dp);
}</pre>
```

Complexity Analysis

Time Complexity: O(m*n) - each subproblem (i, j) is solved only once and stored in the dp table.

Space Complexity: O(m*n) - for the dp table used in memoization and recursion stack depth.

Tabulation

Approach

For each cell (i, j), skip it if it's blocked; otherwise:

- If it's the start cell (0, 0), set dp[0][0] = 1
- Otherwise, set dp[i][j] = dp[i-1][j] + dp[i][j-1] (handling bounds).

Corner cases: If the starting cell (0,0) is blocked (-1), return 0 immediately.

Code

```
int f(vector<vector<int>>& maze) {
  int m = maze.size(), n = maze[0].size();
  if (maze[0][0] == -1 || maze[m - 1][n - 1] == -1) return 0;

vector<vector<int>> dp(m, vector<int>(n, 0));

for (int i = 0; i < m; i++) {
  for (int j = 0; j < n; j++) {
    if (maze[i][j] == -1) {
      dp[i][j] = 0;
      continue;
    }
  if (i == 0 && j == 0) {
      dp[i][j] = 1;
    } else {
    int up = (i > 0) ? dp[i - 1][j] : 0;
}
```

```
int left = (j > 0) ? dp[i][j - 1] : 0;
    dp[i][j] = up + left;
    }
}

return dp[m - 1][n - 1];
}
```

Complexity Analysis

Time Complexity: O(m*n) - each cell in the grid is visited once.

Space Complexity: O(m * n) - for storing the DP table.

Space optimization

Approach

prev question code:

```
int f(int m, int n) {
  vector<int> prev(n, 0);
  for (int i = 0; i < m; i++) {
     vector<int> curr(n, 0);
     for (int j = 0; j < n; j++) {
        if (i == 0 \&\& j == 0) {
           curr[j] = 1;
        } else {
           int up = (i > 0) ? prev[j] : 0;
           int left = (j > 0) ? curr[j - 1] : 0;
           curr[j] = up + left;
        }
     }
     prev = curr;
  }
  return prev[n - 1];
}
```

For each cell (i, j):

• If the cell is blocked (1), set curr[j] = 0

Code

```
int uniquePathsWithObstacles(vector<vector<int>>& maze) {
   int m = maze.size(), n = maze[0].size();
   if (maze[0][0] == -1 || maze[m - 1][n - 1] == -1) return 0;
   vector<int> prev(n, 0);
   for (int i = 0; i < m; i++) {
      vector<int> curr(n, 0);
      for (int j = 0; j < n; j++) {
        if (maze[i][j] == -1) {</pre>
```

```
curr[j] = 0;
} else if (i == 0 && j == 0) {
    curr[j] = 1;
} else {
    int up = (i > 0) ? prev[j] : 0;
    int left = (j > 0) ? curr[j - 1] : 0;
    curr[j] = up + left;
}

prev = curr;
}
return prev[n - 1];
}
```

Complexity Analysis

Time Complexity: O(m*n) - every cell is processed once

Space Complexity: O(n) - only two 1D arrays of size n are used to store state

THE END