

# 3.1 SYMBOL TABLES

- **API**
- elementary implementations
- ordered operations

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▶ API

elementary implementations

ordered operations

Algorithms

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http://algs4.cs.princeton.edu

## Symbol tables

#### Key-value pair abstraction.

- Insert a value with specified key.
- Given a key, search for the corresponding value.

#### Ex. DNS lookup.

· Insert domain name with specified IP address.

key

· Given domain name, find corresponding IP address.

domain name	IP address
www.cs.princeton.edu	128.112.136.11
www.princeton.edu	128.112.128.15
www.yale.edu	130.132.143.21
www.harvard.edu	128.103.060.55
www.simpsons.com	209.052.165.60
<b>↑</b>	<b>↑</b>



# Symbol table applications

application	purpose of search	key	value		
dictionary	find definition	word	definition		
book index	find relevant pages	term	list of page numbers		
file share	find song to download	name of song	computer ID		
financial account	process transactions	account number	transaction details		
web search	find relevant web pages	keyword	list of page names		
compiler	find properties of variables	variable name	type and value		
routing table	route Internet packets	destination	best route		
DNS	find IP address	domain name	IP address		
reverse DNS	find domain name	IP address	domain name		
genomics	find markers	DNA string	known positions		
file system	find file on disk	filename	location on disk		

### Symbol tables: context

Also known as: maps, dictionaries, associative arrays.

Generalizes arrays. Keys need not be between 0 and N-1.

#### Language support.

- External libraries: C, VisualBasic, Standard ML, bash, ...
- Built-in libraries: Java, C#, C++, Scala, ...
- Built-in to language: Awk, Perl, PHP, Tcl, JavaScript, Python, Ruby, Lua.

every array is an every object is an table is the only associative array associative array primitive data structure

hasNiceSyntaxForAssociativeArrays["Python"] = true
hasNiceSyntaxForAssociativeArrays["Java"] = false

legal Python code

# Basic symbol table API

Associative array abstraction. Associate one value with each key.

```
public class ST<Key, Value>
                 ST()
                                                  create an empty symbol table
          void put(Key key, Value val)
                                                 put key-value pair into the table ← a[key] = val;
         Value get(Key key)
                                                      value paired with key
                                                                                 __ a[key]
      boolean contains(Key key)
                                                 is there a value paired with key?
          void delete(Key key)
                                               remove key (and its value) from table
       boolean isEmpty()
                                                       is the table empty?
           int size()
                                               number of key-value pairs in the table
Iterable<Key> keys()
                                                     all the keys in the table
```

#### **Conventions**

- Values are not null. ← Java allows null value
- Method get() returns null if key not present.
- Method put() overwrites old value with new value.

#### Intended consequences.

• Easy to implement contains().

```
public boolean contains(Key key)
{ return get(key) != null; }
```

• Can implement lazy version of delete().

```
public void delete(Key key)
{  put(key, null); }
```

## Keys and values

Value type. Any generic type.

specify Comparable in API.

#### Key type: several natural assumptions.

- Assume keys are Comparable, use compareTo().
- Assume keys are any generic type, use equals() to test equality.
- Assume keys are any generic type, use equals() to test equality;
   use hashCode() to scramble key.

built-in to Java (stay tuned)

Best practices. Use immutable types for symbol table keys.

- Immutable in Java: Integer, Double, String, java.io.File, ...
- Mutable in Java: StringBuilder, java.net.URL, arrays, ...

## **Equality test**

All Java classes inherit a method equals().

Java requirements. For any references x, y and z:

- Reflexive: x.equals(x) is true.
- Symmetric: x.equals(y) iff y.equals(x).
- Transitive: if x.equals(y) and y.equals(z), then x.equals(z).
- Non-null: x.equals(null) is false.

```
do x and y refer to
the same object?
```

Default implementation. (x == y)

Customized implementations. Integer, Double, String, java.io.File, ...

User-defined implementations. Some care needed.

equivalence relation

## Implementing equals for user-defined types

#### Seems easy.

```
public
             class Date implements Comparable<Date>
   private final int month;
   private final int day;
   private final int year;
   public boolean equals(Date that)
                                                           check that all significant
      if (this.day != that.day ) return false;
                                                           fields are the same
      if (this.month != that.month) return false;
      if (this.year != that.year ) return false;
      return true;
```

## Implementing equals for user-defined types

typically unsafe to use equals() with inheritance Seems easy, but requires some care. (would violate symmetry) public final class Date implements Comparable<Date> private final int month; must be Object. private final int day; Why? Experts still debate. private final int year; public boolean equals(Object y) optimize for true object equality if (y == this) return true; check for null if (y == null) return false; objects must be in the same class if (y.getClass() != this.getClass()) (religion: getClass() vs. instanceof) return false; Date that = (Date) y; cast is guaranteed to succeed if (this.day != that.day ) return false; check that all significant if (this.month != that.month) return false; fields are the same if (this.year != that.year ) return false; return true;

## Equals design

#### "Standard" recipe for user-defined types.

- Optimization for reference equality.
- Check against null.
- Check that two objects are of the same type and cast.
- Compare each significant field:
  - if field is a primitive type, use ==
     but use Double.compare() with double (or otherwise deal with -0.0 and NaN)
     if field is an object, use equals()
  - if field is an array, apply to each entry \( \cdot \) can use Arrays.deepEquals(a, b) but not a.equals(b)

#### Best practices.

- e.g., cached Manhattan distance
- No need to use calculated fields that depend on other fields.
- Compare fields mostly likely to differ first.
- Make compareTo() consistent with equals().

```
x.equals(y) if and only if (x.compareTo(y) == 0)
```

#### ST test client for traces

Build ST by associating value i with  $i^{th}$  string from standard input.

```
public static void main(String[] args)
{
   ST<String, Integer> st = new ST<String, Integer>();
   for (int i = 0; !StdIn.isEmpty(); i++)
   {
      String key = StdIn.readString();
      st.put(key, i);
   }
   for (String s : st.keys())
      StdOut.println(s + " " + st.get(s));
}
```

```
keys S E A R C H E X A M P L E values 0 1 2 3 4 5 6 7 8 9 10 11 12
```

#### output

```
A 8
C 4
E 12
H 5
L 11
M 9
P 10
R 3
S 0
X 7
```

## ST test client for analysis

Frequency counter. Read a sequence of strings from standard input and print out one that occurs with highest frequency.

```
% more tinyTale.txt
it was the best of times
it was the worst of times
it was the age of wisdom
it was the age of foolishness
it was the epoch of belief
it was the epoch of incredulity
it was the season of light
it was the season of darkness
it was the spring of hope
it was the winter of despair
                                                        tiny example
% java FrequencyCounter 1 < tinyTale.txt</pre>
                                                        (60 words, 20 distinct)
it 10
                                                        real example
% java FrequencyCounter 8 < tale.txt</pre>
                                                        (135,635 words, 10,769 distinct)
business 122
                                                        real example
% java FrequencyCounter 10 < leipzig1M.txt ←
                                                        (21,191,455 words, 534,580 distinct)
government 24763
```

## Frequency counter implementation

```
public class FrequencyCounter
   public static void main(String[] args)
      int minlen = Integer.parseInt(args[0]);
                                                                               create ST
      ST<String, Integer> st = new ST<String, Integer>();
      while (!StdIn.isEmpty())
         String word = StdIn.readString();
                                                      ignore short strings
         if (word.length() < minlen) continue;</pre>
                                                                                read string and
         if (!st.contains(word)) st.put(word, 1);
                                                                                update frequency
                                   st.put(word, st.get(word) + 1);
         else
      String max = "";
      st.put(max, 0);
                                                                                print a string
      for (String word : st.keys())
                                                                               with max freq
         if (st.get(word) > st.get(max))
            max = word;
      StdOut.println(max + " " + st.get(max));
```

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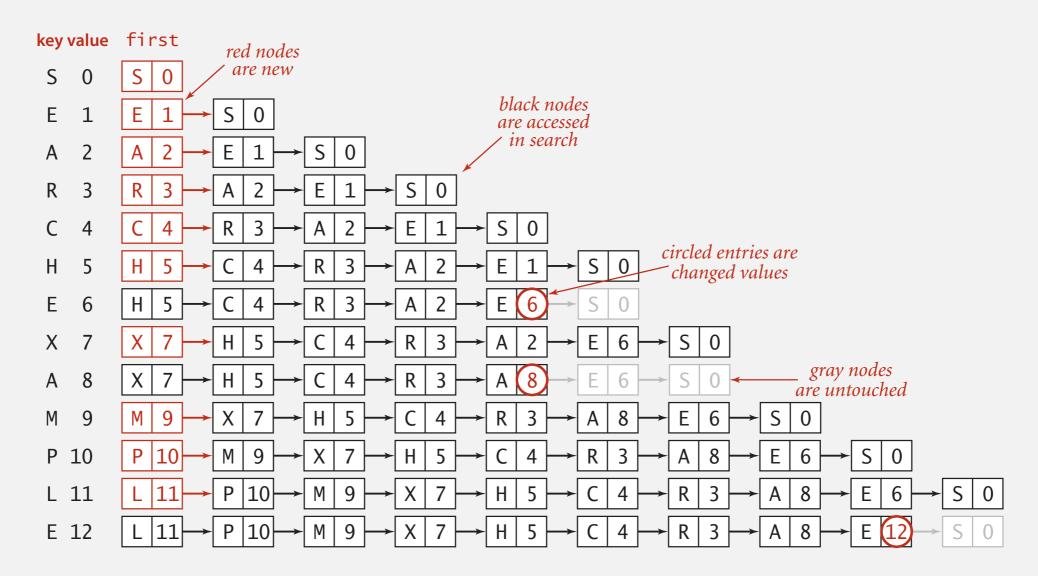
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## Sequential search in a linked list

Data structure. Maintain an (unordered) linked list of key-value pairs.

Search. Scan through all keys until find a match.

Insert. Scan through all keys until find a match; if no match add to front.



Trace of linked-list ST implementation for standard indexing client

# Elementary ST implementations: summary

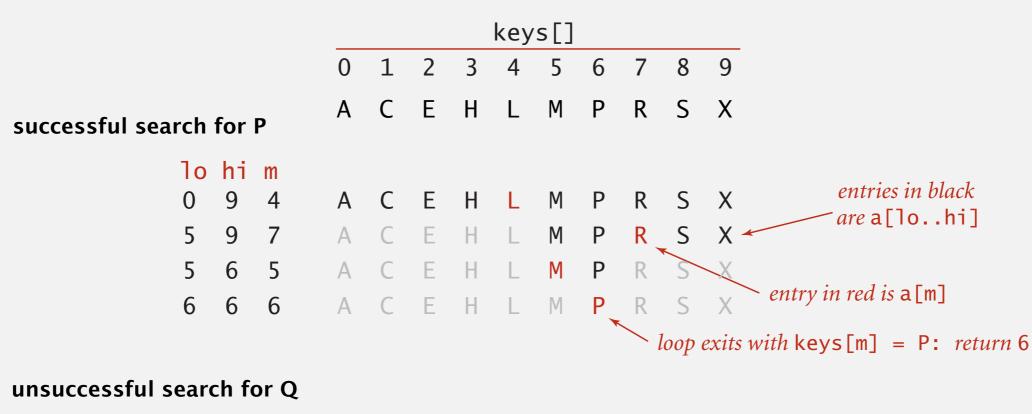
ST implementation	guara	ıntee	avera	key	
31 implementation	search	insert	search hit	insert	interface
sequential search (unordered list)	N	N	N / 2	N	equals()

Challenge. Efficient implementations of both search and insert.

## Binary search in an ordered array

Data structure. Maintain an ordered array of key-value pairs.

Rank helper function. How many keys < k?



```
10 hi m
0 9 4 A C E H L M P R S X
5 9 7 A C E H L M P R S X
5 6 5 A C E H L M P R S X
7 6 6 A C E H L M P R S X
loop exits with 10 > hi: return 7
```

## Binary search: Java implementation

```
public Value get(Key key)
   if (isEmpty()) return null;
   int i = rank(key);
   if (i < N && keys[i].compareTo(key) == 0) return vals[i];
   else return null;
private int rank(Key key)
                                           number of keys < key
   int lo = 0, hi = N-1;
   while (lo <= hi)
   {
       int mid = 10 + (hi - 10) / 2;
       int cmp = key.compareTo(keys[mid]);
       if (cmp < 0) hi = mid - 1;
       else if (cmp > 0) lo = mid + 1;
       else if (cmp == 0) return mid;
  return lo;
```

# Binary search: trace of standard indexing client

Problem. To insert, need to shift all greater keys over.

						key	's []										va	ls[]				
key	value	0	1	2	3	4	5	6	7	8	9	N	0	1	2	3	4	5	6	7	8	9
S	0	S										1	0									
Ε	1	Ε	S			0	ntrie	c in 1	red			2	1	0					itries ved to			L
Α	2	Α	Ε	S			vere i					3	2	1	0			7 1110	veu ii	) iiie	rigni	•
R	3	A	Е	R	S							4	2	1	3	0						
C	4	Α	C	Ε	R	S			en	tries	in gra	<sub>1y</sub> 5	2	4	1	3	0					
Н	5	Α	C	Е	Н	R	S				ot moi		2	4	1	5	3	0		iled e lange		s are
Ε	6	Α	C	Е	Н	R	S					6	2	4	(6)	5	3	0	CII	unge	or von	wes
X	7	Α	C	Е	Н	R	S	X				7	2	4	6	5	3	0	7			
Α	8	Α	C	Е	Н	R	S	X				7	(8)	4	6	5	3	0	7			
M	9	Α	C	Е	Н	M	R	S	X			8	8	4	6	5	9	3	0	7		
Р	10	Α	C	Е	Н	M	P	R	S	X		9	8	4	6	5	9	10	3	0	7	
L	11	Α	C	Е	Н	L	M	P	R	S	Χ	10	8	4	6	5	11	9	10	3	0	7
Ε	12	Α	C	Е	Н	L	$\mathbb{M}$	Р	R	S	X	10	8	4 (	12)	5	11	9	10	3	0	7
		Α	C	Ε	Н	L	M	Р	R	S	Χ		8	4	12	5	11	9	10	3	0	7

# Elementary ST implementations: summary

ST implementation	guara	ıntee	avera	key	
31 implementation	search	insert	search hit	insert	interface
sequential search (unordered list)	N	N	N/2	N	equals()
binary search (ordered array)	log N	N	log N	(N/2)	compareTo()

Challenge. Efficient implementations of both search and insert.

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## Examples of ordered symbol table API

```
values
                                 keys
                    min() \longrightarrow 09:00:00 Chicago
                              09:00:03 Phoenix
                              09:00:13 Houston
            get(09:00:13) 09:00:59 Chicago
                              09:01:10
                                         Houston
          floor(09:05:00) \longrightarrow 09:03:13
                                          Chicago
                                          Seattle
                              09:10:11
                select(7) \longrightarrow 09:10:25
                                         Seattle
                              09:14:25 Phoenix
                             09:19:32
                                          Chicago
                             09:19:46
                                          Chicago
keys(09:15:00, 09:25:00) \longrightarrow 09:21:05
                                         Chicago
                             09:22:43
                                         Seattle
                              09:22:54 Seattle
                              09:25:52
                                         Chicago
        ceiling(09:30:00) \rightarrow 09:35:21
                                          Chicago
                                         Seattle
                              09:36:14
                    max() \longrightarrow 09:37:44 Phoenix
size(09:15:00, 09:25:00) is 5
     rank(09:10:25) is 7
```

# Ordered symbol table API

public class	public class ST <key comparable<key="" extends="">, Value&gt;</key>						
Key	min()	smallest key					
Key	max()	largest key					
Key	floor(Key key)	largest key less than or equal to key					
Key	<pre>ceiling(Key key)</pre>	smallest key greater than or equal to key					
int	rank(Key key)	number of keys less than key					
Key	<pre>select(int k)</pre>	key of rank k					
void	<pre>deleteMin()</pre>	delete smallest key					
void	deleteMax()	delete largest key					
int	size(Key lo, Key hi)	number of keys between lo and hi					
Iterable <key></key>	keys()	all keys, in sorted order					
Iterable <key></key>	keys(Key lo, Key hi)	keys between lo and hi, in sorted order					

# Binary search: ordered symbol table operations summary

	sequential search	binary search
search	N	$\log N$
insert / delete	N	N
min / max	N	1
floor / ceiling	N	$\log N$
rank	N	$\log N$
select	N	1
ordered iteration	$N \log N$	N

order of growth of the running time for ordered symbol table operations