

Introduction to Machine Learning

CSE474/574: Lecture 3

Varun Chandola <chandola@buffalo.edu>

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Outline

- 1 Learning Conjunctive Concepts
 - Find-S Algorithm
 - Version Spaces
 - LIST-THEN-ELIMINATE Algorithm
 - Compressing Version Space

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A Simple Algorithm (Find-S [1, Ch. 2])

- 1 Start with $h = \emptyset$
- 2 Use next input $\{x, c(x)\}$
- 3 If $c(x) = 0$, goto step 2
- 4 $h \leftarrow h \wedge x$ (*pairwise-and*)
- 5 If more examples: Goto step 2
- 6 Stop

Pairwise-and rules:

$$a_h \wedge a_x = \begin{cases} a_x & : \text{ if } a_h = \emptyset \\ a_x & : \text{ if } a_h = a_x \\ ? & : \text{ if } a_h \neq a_x \\ ? & : \text{ if } a_h = ? \end{cases}$$

Simple Example

Target concept

`{?,large,?,?,thick}`

- How many positive examples can there be?
- What is the minimum number of examples need to be seen to learn the concept?
 - 1 {circular,large,light,smooth,thick}, malignant
 - 2 {oval,large,dark,irregular,thick}, malignant
- Maximum?

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Partial Training Data

- ① {circular, large, light, smooth, thick}, malignant
 - ② {circular, large, light, irregular, thick}, malignant
 - ③ {oval, large, dark, smooth, thin}, benign
 - ④ {oval, large, light, irregular, thick}, malignant
 - ⑤ {circular, small, light, smooth, thick}, benign
- Concept learnt:
 - {?, large, light, ?, thick}
 - What mistake can this “concept” make?

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Recap of Find-S

- Objective: Find *maximally specific* hypothesis
- Admit all positive examples and nothing more
- Hypothesis never becomes any more specific

Questions

- Does it converge to the target concept?
- Is the most specific hypothesis the best?
- Robustness to errors
- **Choosing best among potentially many maximally specific hypotheses**

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- Hypothesis chosen by **Find-S**:
 - {?, large, light, ?, thick}
- Other possibilities that are **consistent** with the training data?
- What is **consistency**?
- **Version space**: Set of *all* consistent hypotheses.

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List Then Eliminate

- 1 $VS \leftarrow \mathcal{H}$
 - 2 *For Each* $\langle x, c(x) \rangle \in D$:
 Remove every hypothesis h from VS such that $h(x) \neq c(x)$
 - 3 *Return* VS
- Issues?
 - How many hypotheses are removed at every instance?

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Compressing Version Space

More_General_Than Relationship

$$h_j \geq_g h_k \quad \text{if} \quad h_k(x) = 1 \Rightarrow h_j(x) = 1$$

$$h_j >_g h_k \quad \text{if} \quad (h_j \geq_g h_k) \wedge (h_k \not\geq_g h_j)$$

- In a version space, there are:
 - ① Maximally general hypotheses
 - ② Maximally specific hypotheses
- Boundaries of the version space

References



T. M. Mitchell.

Machine Learning.

McGraw-Hill, Inc., New York, NY, USA, 1 edition, 1997.