

Aim: Knapsack problem by using Genetic Algorithm

Item	Weight(kg)	Value
A	5	12
B	3	5
C	7	10
D	2	7

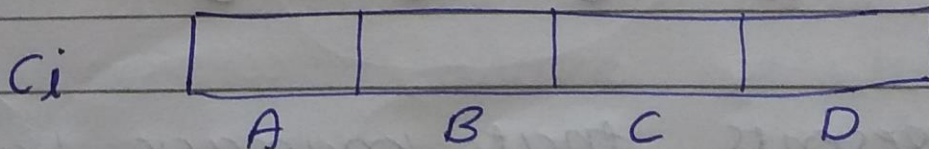
- There are four items. Each item is associated with some weight(w) and value at item(v).
- There is a knapsack K with limited capacity that can hold almost 12 kg

Problem

The problem is that which item should be kept in the knapsack so as it will maximizes knapsack value without breaking knapsack.

Step 1 Chromosomes Encoding

Consider an array C_i represents all items together



Gene 0 - represents absence of item in the knapsack

1 - represents presence of item in the knapsack

4-bits are requested to represent chromosomes Encoding

$$\text{set space} = 2^4$$

Initial population is created and chromosomes randomly created.

generation 1

C_1	0	1	1	0
C_2	0	1	0	1
C_3	1	1	0	1
C_4	1	1	1	1

Step 2 fitness function

- Next step is to determine fitness function which is used to evaluate how good particular solution is

Lets take C_1

0	1	1	0
A	B	C	D

represents that knapsack has presence of item B & C and absence of item A & D

value of knapsack = value of B + value of C

$$= 5 + 10$$

$$= 15$$

weight of knapsack = weight of B + weight of item C

$$= 3 + 7$$

$$= 10 \text{ kg}$$

knapsack capacity = 12 kg

as $12 \text{ kg} > 10 \text{ kg}$

so, C_1 is accepted

→ similar check for C_2, C_3, C_4

<u>Generation 1</u>					W	fitness V
C_1	0	1	1	0	10	15
C_2	0	1	0	1	5	12
C_3	1	1	0	1	10	24
C_4	1	1	1	1	17	34

step 3: selection

→ Next step is to collect the fittest individual and wake up the next generation chromosome

By using Roulette wheel selection

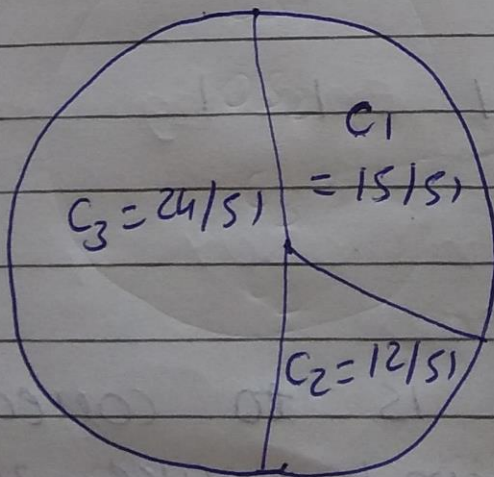
- spin the Roulette wheel and whenever the wheel stops, the individual gets selected at that point.
- The individual that has the highest fitness value gets larger share of the wheel

e.g. Total fitness value = $15 + 12 + 24 + 0$
= 51

fitness value of $c_3 = 24$; largest fitness

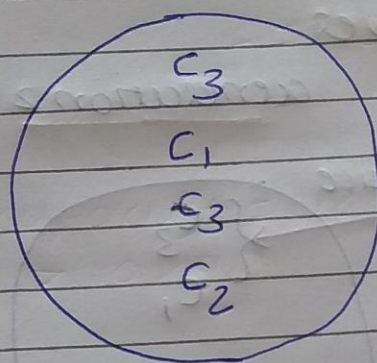
so, c_3 occupies half of the wheel as $24/51$

c_4 has zero chance of winning, c_3 has the highest probability of getting selected in the next generation



→ After spinning Roulette wheel, in the first spin c_3 will be selected and then c_1 after that c_3 and c_2

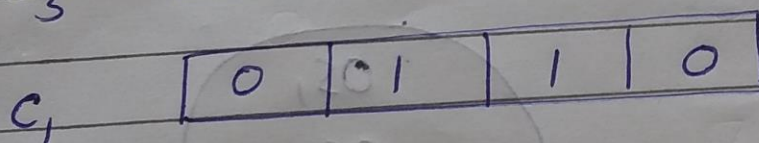
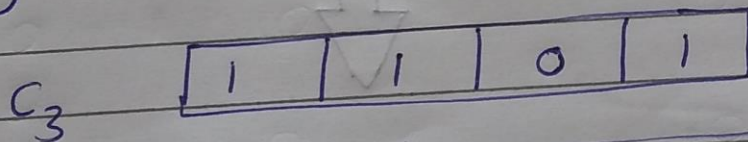
→ Individuals of next generation are selected as follows:



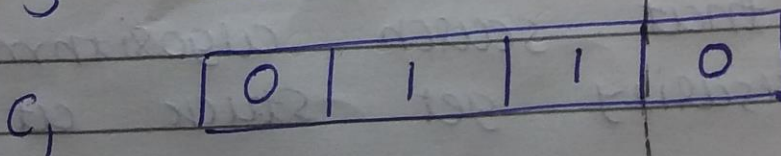
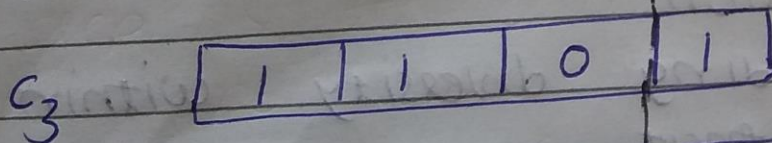
Generation 2

Step 4 crossover

→ The crossover operation takes the selected chromosomes for mating and mixes the genetic material to produce offspring



one-point crossover: Randomly select the position on the chromosomes about which gene would be exchange



← crossover point

Result of one point crossover
i.e. Produced offspring

OS₁

1	1	0	0
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OS₂

0	1	1	1
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- After crossover

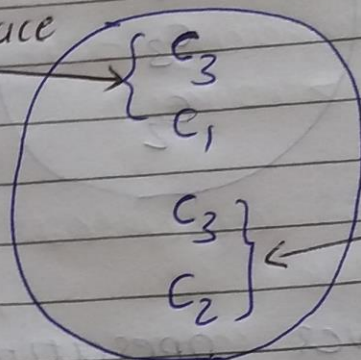
Generation 2

OS₁ will replace

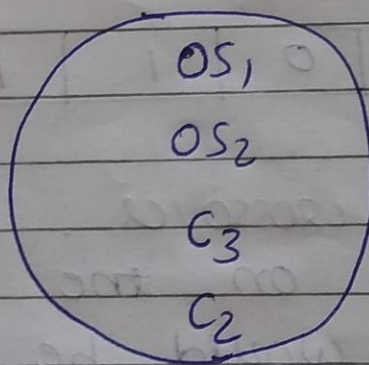
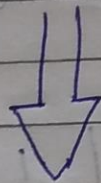
C₃ and OS₂

will replace

C₁



C₃ and C₂ do not go for the crossover so will remain in the next generation



~~Generation 3~~

Step 5: Mutation

- Providing diversity within population so that search algorithm does not necessarily get stuck at local maxima

Before applying mutation

OS_1 1 1 0 0

OS_2 0 1 1 1

C_3 1 1 0 1

C_2 0 1 0 1

After applying mutation

fitness

					w	v
OS_1	0	1	0	0	3	5
OS_2	0	0	1	1	9	17
C_3	1	1	0	1	10	24
C_2	0	1	0	1	5	12

$$\therefore \text{Total fitness value} = 5 + 17 + 24 + 12 \\ = 58$$