

## Find the kinematics of vertical piston

The figure shows a 2D mid-section of ship model which is pivoted at point  $O$  and needs to undergo simple harmonic roll motion about  $O$ ,  $\phi = \phi_a \sin(\omega t)$ . The beam of the ship model is  $b$ . The top corner of the deck at a distance  $r_1$  from the pivot  $O$  is connected to the vertical piston rod  $BC$  with the link  $AB$  of length  $r_2$  with hinges at  $A$  and  $B$ . The vertical piston is at a distance  $l$  from the pivot  $O$ . Friction in hinge joints  $A$  and  $B$  and the vertical rod  $BC$  are negligible.

- Determine the equation for stroke,  $s$ , of the vertical piston rod  $BC$  in order to achieve such prescribed roll motion  $\phi$ ?
- Can the same motion be imposed on the ship if the point  $A$  and  $B$  are identical (i.e without link  $AB$ )?

