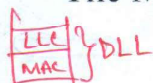


Chapter 4

The Medium Access Control Sublayer



MAC → Sublayer of DLL

The Channel Allocation Problem

- Dedicated resource (channel for FDM, time for TDM) for a user
- Static Channel Allocation in LANs and MANs
- Dynamic Channel Allocation in LANs and MANs
- No dedicated resource. Here, all frames can be assumed to be somehow magically arranged orderly in a big central queue. Let, mean time delay → T , channel capacity C bps, arrival rate λ frames/s, frame length follows an exponential probability density function with mean $1/\mu$ frames/bits/frame. Now, from queuing theory, it can be shown for Poisson arrival and service time, $T = \frac{1}{\mu(C - \lambda)}$

→ FDM

Let, N independent channels; So, capacity = C/N , mean input rate = λ/N

$$\text{So, } T_{\text{static}} = \frac{1}{\mu(C/N) - (\lambda/N)} = \frac{N}{\mu C - \lambda} = N T_{\text{dynamic}}$$

So, delay using FDM is N times worse than static dynamic case [similar logic holds for TDM]

Dynamic Channel Allocation in LANs and MANs

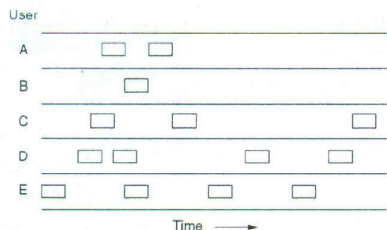
1. Station Model. → N independent stations/terminals
2. Single Channel Assumption. → A single channel is available
3. Collision Assumption. → Simultaneous tx of two frames makes a collision
4. (a) Continuous Time. → Frame tx can begin at any time
(b) Slotted Time. → Time is divided into discrete intervals (slots). Frame tx begins always at the start of a slot.
5. (a) Carrier Sense. → Station senses the channel for being idle before using it
(b) No Carrier Sense. → No sensing

Multiple Access Protocols

- ALOHA ← Pure Slotted
- Carrier Sense Multiple Access Protocols ← Persistent, Non-persistent, CSMA with collision detect
- Collision-Free Protocols ← Bitmap, Binary countdown
- Limited-Contention Protocols ← Adaptive tree walk
- Wavelength Division Multiple Access Protocols
- Wireless LAN Protocols ← MACA, MATAW

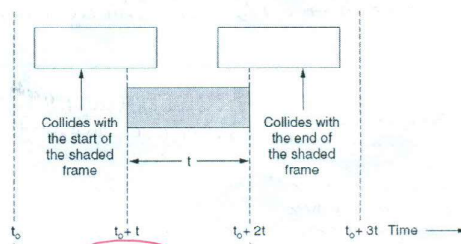
→ Norman Abramson (1970) = University of Hawaii

Pure ALOHA → let users transmit whenever they have data to be sent



In pure ALOHA, frames are transmitted at completely arbitrary times.

Pure ALOHA (2)



→ If any frame gets generated within this time (2 frame time) then there will be a collision

G → mean # of attempts per frame time [$G \geq N$]
 N → mean # of generation

$N > 1$: Almost always collision; Low load: $N \approx 0$; So, $G \approx N$
 $0 < N < 1$: Reasonable throughput; High load: $G > N$

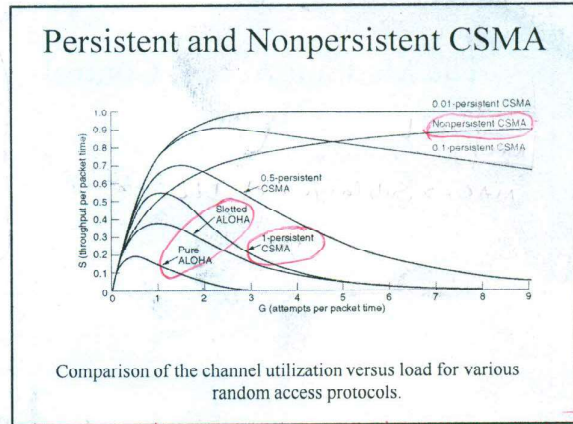
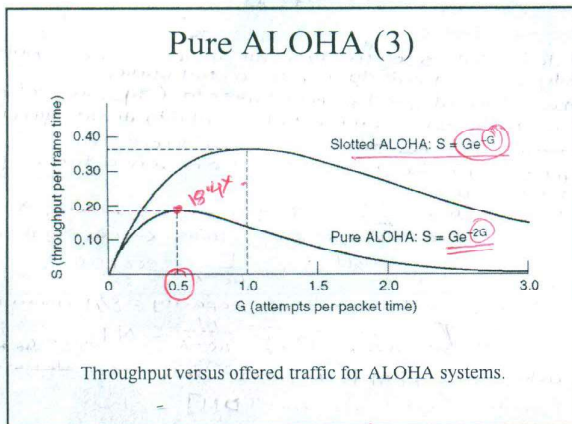
- * Throughput = offered load * prob of a tx succeeding = $G * P_0$
- * Prob that k frames are generated during a given frame time is given by the Poisson distribution: $Pr[k] = \frac{G^k e^{-G}}{k!}$
- So, prob of 0 frame = $P_0 [0] = e^{-G}$
- Now, vulnerable time period is two frame long; So, here mean # of frames generated is $2G$.
- * So, prob of no frame during the vulnerable period is $P_0 = e^{-2G}$

So, throughput, $S = G * P_0 = G * e^{-2G}$
for max S , $G = 0.5$; $S = 0.5 * e^{-1} = 0.184$

So, best channel utilization = 18.4%
for max S , $\frac{dS}{dG} = 0$; So, $e^{-2G} + G(-2)e^{-2G} = 0$
So, $1 - 2G = 0$; So, $G = 1/2 = 0.5$

Slotted ALOHA \Rightarrow Time is divided into discrete intervals. A station is not permitted to send whenever a frame is generated, rather it is required to wait for the beginning of the next slot. So, now the vulnerable period becomes one frame slot.
 $S_0, P(0) = G \cdot e^{-G} = e^{-G}$; $S_0, S = G \cdot e^{-G}$; $P_0 = G \cdot e^{-G}$
 For max $S, \frac{dS}{dG} = 0$; $S_0, e^{-G} + (-1)G \cdot e^{-G} = 0$; $S_0, 1 - G = 0$; $S_0, G = 1$
 $S_0, S_{max} = 1 \cdot e^{-1} = 0.368$; \Rightarrow So, for slotted ALOHA, the best we can hope for is 37% slots empty, 37% success, and 26% collision.
 $P_0 = e^{-G}$
 $S = G \cdot e^{-G}$
 $100 - 37 - 37 = 26$

Now, prob of avoiding collision = e^{-G} ; So, prob. of collision = $1 - e^{-G}$.
 Therefore, prob of a tx requires exactly k attempts = $e^{-G} (1 - e^{-G})^{k-1}$
 So, expected # of tx $\Rightarrow E = \sum_{k=1}^{\infty} k \cdot P_k = \sum_{k=1}^{\infty} k \cdot e^{-G} (1 - e^{-G})^{k-1} = e^{-G}$
 The exponential dependence indicates that small increase in channel load (G) drastically reduces its performance.



Carrier sense protocols: Stations listen for a carrier and act accordingly.

1-persistent: Senses carrier to be found it to be idle. If it is found to be idle, then a sta. transmits its frame (prob of tx sensing is 1). If a second sta. senses a channel to be idle where the first station's tx is yet to be received, then there is a collision.
 In case a channel is found busy, a sta. waits for a while it gets idle and then it tx.
 Problem: Sure tx after finishing the ongoing sensed tx. It can result in collision in case of multiple sensing sta's.

CSMA with Collision Detection
 CSMA/CD can be in one of three states: contention, transmission, or idle.
 Collision detect \Rightarrow Analog process
 Half-duplex system, as the receiving line is busy for idle listening to detect collision.
 Bad performance for large $2T$; This can happen for long cable, small frame.
 Problem of CSMA/CD \rightarrow collision can still occur in contention period.

can be a chance of experiencing collision (if the second one transmits).
 If a sta. experiences a collision after sending its packet, then it waits for a random amount of time, and then starts all over again.
 If the propagation delay is larger, then the chance of collision is higher.
 Even if the prop. delay is zero, collision may happen in case of attempt at the beginning of a slot.
 Non-persistent \Rightarrow in case of sensing a busy channel, waits for a random time. If the channel is idle, then starts transmitting.

Collision-Free Protocols
 p-persistent \Rightarrow Uses slotted channels. If a sta. becomes ready to send, it senses the channel. If the channel is found to be idle, then the sta. txs with prob p or defers until beginning of the next slot by prob $q = 1 - p$. If next slot is idle, then it either txs or defers by prob p or q . If the channel is found busy, it waits until the next slot and applies the above algo.
 Reservation protocol: Broadcasts desire to tx before actual tx. Each contention period consists of exactly N slots, 1 for each sta. A sta. inserts a 1 to its allocated slot, if it has a frame to tx. After the contention slots get over, each sta. has a complete knowledge of which sta's wish to tx. They begin tx in numeric order.
 The basic bit-map protocol.
 Low load: high # of sta's need to wait for $0.5N$ slots on an avg.
 So, sta's need to wait for N slots on avg. \leftarrow Overhead period.
 High load: All sta's must have something to send all the time. So, the overhead is only 1 bit per frame.
 Efficiency: $\frac{1}{d+N}$ for low load; $\frac{1}{d+1}$ for high load [d = # of data bits]

Collision-Free Protocols (2)
 High priority for higher # of sta.
 Broadcasts address as a binary string, with higher # of bit first.
 Equal length for all addresses.
 A sta. gives up broadcasting its intent through broadcasting its binary bit string address, once it sees a higher-order bit posn set by someone else.
 If the first field of a frame could be made address, then efficiency will be 100%.
 Parallel interface: Successful sta's get circularly permuted in order to give higher priorities to sta's that have been silent unusually long.
 The binary countdown protocol. A dash indicates silence.

Limited-Contention Protocols
 Probability of success \Rightarrow Pr [success with optimal prob of access to channel] = $\frac{(K-1)^{K-1}}{K^K}$
 for small K , the Pr val is good. As K increases, the Pr significantly decreases towards an asymptotic value of $\frac{1}{e}$.
 Acquisition probability for a symmetric contention channel.
 Performance measure \Rightarrow 1) delay for low-load, 2) Efficiency for high load.
 Low-load: Pure / Slotted ALOHA.
 High-load: Collision-free protocol (as efficiency higher).
 P: Prob of channel acquire/access; K : # of sta's contending for channel.
 Pr [some sta. successfully acquire the channel] = $K \cdot P(1-P)^{K-1}$
 For best performance \Rightarrow optimal $P, \frac{dP}{dK} = 0$; $S_0, K(1-P)^{K-1} - K(K-1)P(1-P)^{K-2} = 0$
 $S_0, K(1-P) - K(K-1)P = 0$; $S_0, K - KP - K^2P + KP = 0$; $S_0, P = \frac{1}{K}$
 So, Pr [success with optimal P] = $K \cdot \frac{1}{K} (1 - \frac{1}{K})^{K-1} = \frac{(K-1)^{K-1}}{K^K}$

Extreme cases
 1) sta. per group: Binary countdown/bit-map
 2) 1 gr with all sta's: Slotted ALOHA

Slotted ALOHA among sta's
 Group 1, Group 2, ...
 Bitmap or Binary countdown
 contention-free protocol