# SPECIAL TOPICS IN TRANSPORTATION ENGINEERING: TRANSPORTATION NETWORK OPTIMIZATION

#### Spring 2024

Course number	CVL851	No. of credits	3 credits (3-0-0)
Meeting time:	Slot A (M, Th at 8-9:30A.M.)	Instructor's name:	Pramesh Kumar
Email:	pkk@iitd.ac.in	Instructor's office:	322, Block-IV
Location:	LH620	Office Hours:	M 2:30-3:30 P.M.
Teaching assistant:	-		322, Block-IV

Course website: Access the course material from https://prameshk.github.io/CVL851.html. Submit homework assignments and project deliverable through Moodle.

Course prerequisites: Student should have good knowledge of calculus and linear algebra. Computer programming is required to do homeworks.

Course description: This course is designed to introduce optimization techniques for solving transportation network optimization problems. Topics include introduction to network flow problems, linear programming, simplex method, duality theory, dynamic programming, integer programming and convex programming.

### Student learning aims/outcomes:

- Modeling transportation network flow problems.
- Solving standard network flow problems
- Formulating and solving linear programs and applying duality theory.
- Formulating integer programming problems
- Formulating nonlinear programming problems
- Using computer programming packages available for optimization

#### Reference Books:

- 1. Vanderbei, Robert J., *Linear Pogramming: Foundations and Extensions*, Springer Fifth Edition, 2020. [Link]
- 2. Ahuja, R., Magnanti, T., and Orlin, J., Network Flows: Theory, Algorithms, and Applications, Pearson, 2014. [Free PDF copy].
- 3. Boyd, Stephen P., and Lieven Vandenberghe. *Convex optimization*, Cambridge university press, 2004. [Free PDF copy]
- 4. Cormen, Thomas H., Charles E. Leiserson, Ronald L. Rivest, and Clifford Stein, *Introduction to algorithms*, MIT press, 2022. [Link]

# Tentative topics to be covered (may not cover all the topics)

#### 1. Introduction

- Introduction to the course
- Graphs and Network Flow Problems
- Data structures
- Computational complexity

# 2. Introduction to Linear Programming

- Modeling linear programming problems
- Simplex method
- Farkas Lemma and LP Duality theory

#### 3. Introduction to Dynamic Programming

# 4. Network flow problems

- Graph search algorithms
- Minimum spanning tree
- Shortest path
- Max-flow and min-cut
- Min-cost algorithms
- Matching
- Network simplex algorithm

#### 5. Introduction to Integer Programming

- Modeling IP problems
- Branch-and-bound method
- Vehicle routing problem and heuristics

# 6. Introduction to Convex Programming

- Convex sets, convex functions
- First order optimality conditions
- KKT conditions
- Gradient method

Homework assignments: You are encouraged (but not required) to use LATEX to typeset your assignments. Please refer to this website to learn LATEX. Late submission of assignment will be allowed up to two days after the deadline. For each day, there will be a penalty of 25% deduction in points.

Grading and other class policy: The following is the breakdown for grading:

In-class exercises (10%)Homework assignments (20%)Minor exam (15%)Major exam (25%)Project (30%)

The major (final) exam will be cumulative, i.e., it will cover all the material taught during the semester. Participation in all components of this course is required to pass the course. Other policies are as follows:

- Letter grades: For the description of the letter grades and their cut offs, please refer to this link.
- Attendance: If a student's attendance is less than 75%, institute rules will apply. Please refer to Courses of Study.
- Auditing the course: If a student is auditing the course, then she has to get at least 30% of the total marks (aggregated) and more than or equal to 75% attendance for obtaining audit pass **NP** grade. Otherwise, the student will be awarded **NF** grade.
- Re-grade requests: Requests for re-grading questions on an assignment/exam will be considered if submitted in writing within one week from the time the work is returned in class. Note that the score may change in either direction as a result of a re-grade. The instructor reserves the right to limit the number and scope of re-grades requested by a student.
- Make-up exams: Make-up exams can be arranged as per the institute rules.
- Academic integrity: All activities in this course must be done independently unless taken permission from the instructor. While solving the problems, you may discuss it your peers but the final answer must be your own. Copying from another student or plagiarizing from other sources will be considered cheating. You may be awarded a Fail F grade for academic dishonesty. The case will also be forwarded to student advisor and Dean, Academics. For more information about the honor code, refer to Courses of study.
- Resources for differently-abled students: If you require assistance in this regard, please refer and contact Office of accessible education.

# Tentative Schedule

Monday	Thursday	
Jan 1: Intro to the course and graph theory	Jan 4: Intro to graph theory and networkx	
Jan 8: Modeling optimization problems	Jan 11: Modeling optimization problems	
Jan 15: Simplex method	Jan 18: Simplex method	
Jan 22: LP Duality	Jan 25: LP Duality	
Jan 29: Dynamic Programming	Feb 1: Data structures	
Feb 5: Computational complexity	Feb 8: Computational complexity	
Feb 12: Graph search	Feb 15: Make-up or revision	
Feb 19*: No class: Minor exam	Feb 22: Shortest path	
Feb 26: Shortest path	Feb 29: Max flow min cut	
Mar 4*: No class: Friday Timetable	Mar 7: Max flow min cut	
Mar 11: Min cost flow	Mar 14: Min cost flow	
Mar 18: Minimum spanning tree	Mar 21: Bipartite matching	
Mar 25*: No class: Holi	Mar 28: Network simplex	
Apr 1: Branch-and-bound	Apr 4: Vehicle Routing	
Apr 8: Vehicle routing	Apr 11*: Idu'l Fitr	
Apr 15: Convex analysis	Apr 18: Optimality conditions	
Apr 22: Gradient method	Apr 25: Project presentations	

<sup>\*</sup>This is the end of the text\*