

# Qualitative Analysis of Optical Flow for Motion Anomaly Detection

Pranav Megarajan

Supervised by:

Prof. Dr. Paul G. Plöger  
M. Sc. Santosh Thoduka

April 9, 2019



Hochschule  
Bonn-Rhein-Sieg  
University of Applied Sciences

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## Motion Anomaly Detection

- Anomaly is a context specific term.
- Motion Anomaly Detection: Learn the normal motion patterns and detect anomalies as non-conformities.
- This approach is efficient only when the context and state of the system remains constant over time.
- "How to detect motion anomalies as the system's context varies? How independent can the motion anomaly detector be from the context?"

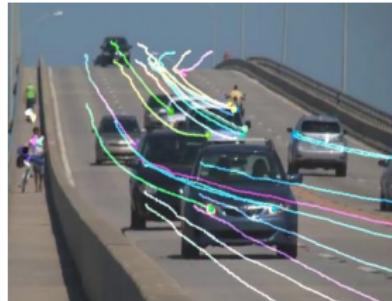
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# Applications



(a) Crowd Surveillance  
[1]



(b) Autonomous Cars [2]



(c) Traffic Signals [3]

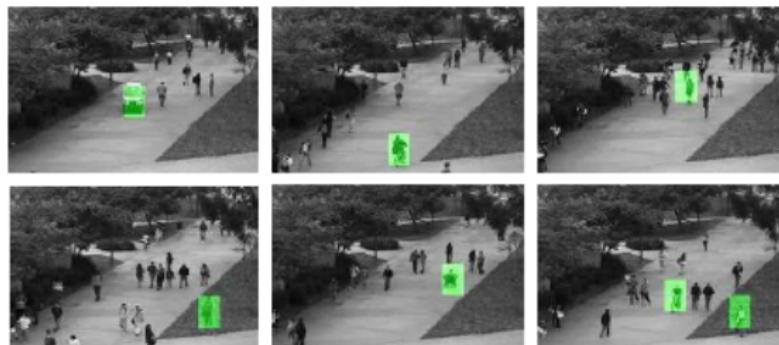
Figure 1: Application Scenarios

**Other Applications:** Robot Manipulation, Mobile Robots, Human-Robot Collaboration etc.

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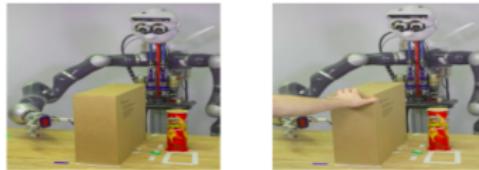
# Automated Crowd Surveillance



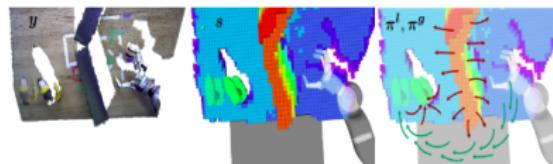
**Figure 2:** Automated Crowd Surveillance. The green part indicates the anomalies in the crowd. [4]

- Optical Flow is used to describe the movement within the frame.
- Several Learning methods are used to model the normal motion over the given dataset.

# Robot Manipulation



(a) Hand movement causes an anomaly.



(b) Optical Flow heat map.

Figure 3: Motion Anomalies in Manipulation Task [5]

- Optical Flow values are clustered to detect the outlier flow values.
- Works with a moving camera or frame.

- **Automated Crowd Surveillance:**

- ▶ Motion Anomalies are learnt from dataset, so as the context changes, we should relearn.
- ▶ Learning only done with data from Fixed Frame or Camera.

- **Robot Manipulation:**

- ▶ Does not work with change in context.

Can we utilize optical flow information to detect motion anomalies from a 'Moving Frame/ Camera' and can it be generalized in order to avoid 'learning' wherever possible ?

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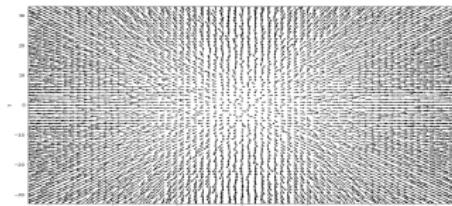
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# Optical Flow field as Vector field

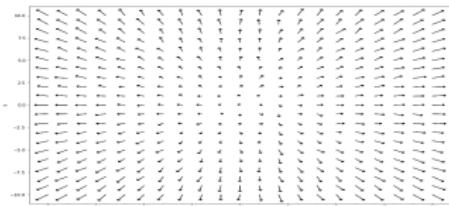
- Optical Flow fields are analysed using techniques used for **vector field** or **orientation field** classification.



Figure 4: Optical flow field superimposed on the image [6].



(a) Noisy flow field



(b) Smoothened flow field

Figure 5: Dominant orientations are obtained from (a) to form (b).

# Qualitative Analysis of Optical Flow

TYPE OF PHASE PORTRAIT	APPEARANCE OF PHASE PORTRAIT
NODE	
SADDLE	
STAR-NODE	
IMPROPER NODE	
CENTER	
SPIRAL	

Figure 6: Types of phase portraits [7]

- Classification of Optical Flow field into one of the phase portraits.
- Possible classifications are shown in Figure 6.
- The **Characteristic equation** of the flow fields is given by:

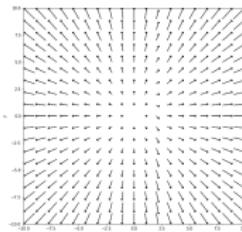
$$\dot{X} = A\bar{x} + B \quad (1)$$

$$\begin{bmatrix} \dot{x} \\ \dot{y} \end{bmatrix} = \begin{bmatrix} a & b \\ c & d \end{bmatrix} \begin{bmatrix} x \\ y \end{bmatrix} + \begin{bmatrix} e \\ f \end{bmatrix} \quad (2)$$

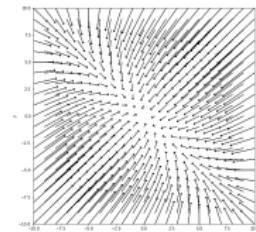
- Critical Point(c)**/ Fixed Point: Point of zero flow or origin.

$$X(c) = 0 \quad (3)$$

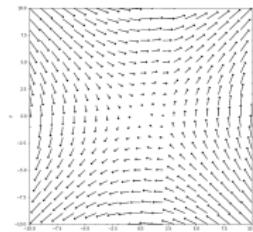
# Classifying Optical Flow



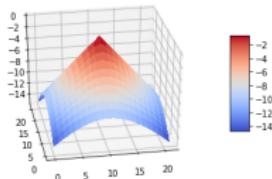
(a) Star Phase



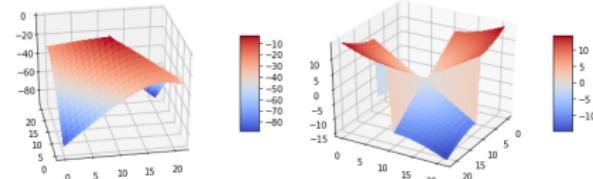
(b) Nodal Phase



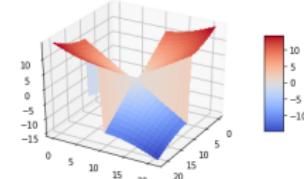
(c) Saddle Phase



(d) Equal/Same Signs



(e) Distinct/Same Signs



(f) Distinct/  
Different Signs

Figure 7: Classifications by **Eigen values**

# Classifying Optical Flow

CASE	JORDAN FORM	TYPE OF PHASE PORTRAIT	APPEARANCE OF PHASE PORTRAIT
1) Real distinct eigenvalues $\lambda_1, \lambda_2$ with $\lambda_1 > \lambda_2$	(a) $\begin{bmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{bmatrix}$ $\lambda_1$ and $\lambda_2$ have the same sign	NODE	
	(b) $\begin{bmatrix} \lambda_1 & 0 \\ 0 & \lambda_2 \end{bmatrix}$ $\lambda_1$ and $\lambda_2$ have opposite sign	SADDLE	
2) Equal eigenvalues $\lambda_1 = \lambda_2 = \lambda_0$	(a) $\begin{bmatrix} \lambda_0 & 0 \\ 0 & \lambda_0 \end{bmatrix}$	STAR-NODE	
	(b) $\begin{bmatrix} \lambda_0 & 1 \\ 0 & \lambda_0 \end{bmatrix}$	IMPROPER NODE	
3) Complex eigenvalues $\lambda_1 = \alpha + i\beta$ $\lambda_2 = \alpha - i\beta$ $\alpha = \frac{1}{2} \text{tr}(A)$ $\beta = \frac{1}{2} \sqrt{-\Delta}$	$\begin{bmatrix} \alpha & -\beta \\ \beta & \alpha \end{bmatrix}$	CENTER	
	(b) $\alpha \neq 0$	SPIRAL	

Figure 8: Overall classification of phase portraits based on eigenvalues and Jordan canonical forms. [7]

# Implementation

## Problems Faced:

- Non-Linear Optimization Problem
  - ▶ Levenberg-Marquardt - Non-Linear least Squares.
- Time taken - Approx. 5 min/frame.
  - ▶ Image Size = 1224x370, Window Size = 11x11.

## Solution:

- **CMA-ES**(Covariance Matrix Adaptation - Evolution Strategy.)
  - ▶ Reduced computation time to 1/4th(approx. 1.25 min/frame).
- Devised and implemented a **linear algorithm**.

# Linear Algorithm

- Non-linear optimization problem involved when approximating to the characteristic equation using a non-linear objective function.

- ▶ **Characteristic Equation:**

$$\dot{X} = A\bar{x} + B \quad (4)$$

- ▶ **Affine Transformation = Linear Transformation + Translation**

- Non-Linear optimization problem can be avoided when the above system is approximated to:

- ▶ **Linear Transformation:**

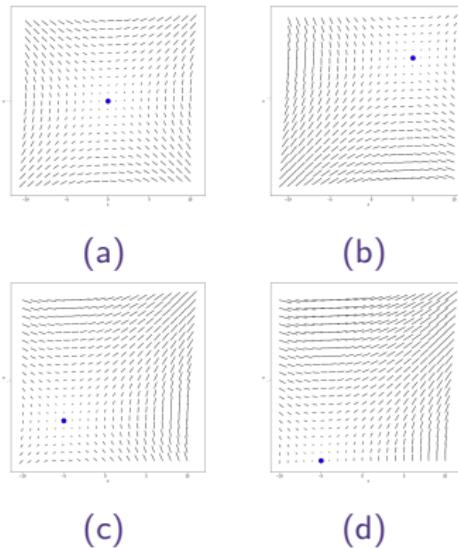
$$\dot{X} = A\bar{x} \quad (5)$$

- When can B be considered as a zero vector?

$$B = 0 \quad (6)$$

# Linear Algorithm

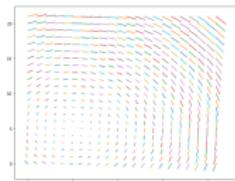
- $B = 0$  when critical point( $c$ ) and origin of co-ordinate system are same(i.e. no translation).



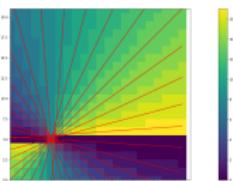
**Figure 9: Effect of Translation Matrix:** The flow fields above have been created with the same linear transformation part( $A$ ) but varying  $B$ , the translation part.

# Linear Algorithm

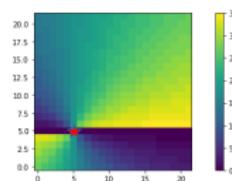
- Find the **critical point** and **shift co-ordinate system** to match with origin.
- **Critical Point Detection:** Cluster points with similar orientation and fit lines.



(a) Orientation Field



(b) Fitted Lines



(c) Critical point

Figure 10: Critical point estimation process can be seen above. Given the orientation field, the data is clustered, lines fitted and the critical point is estimated.

# Motion Anomaly Detection

Characteristics of the system equation:

- Type of **Phase portrait**
- **Critical Point** - Point of zero flow
- **Fit** - Closeness or similarity measure between two orientation fields.

Motion Anomalies can be detected by analysing all these characteristics !

# Detection by Type

- Example: Traffic Signals - Detecting Illegal Crossings and U-turns.

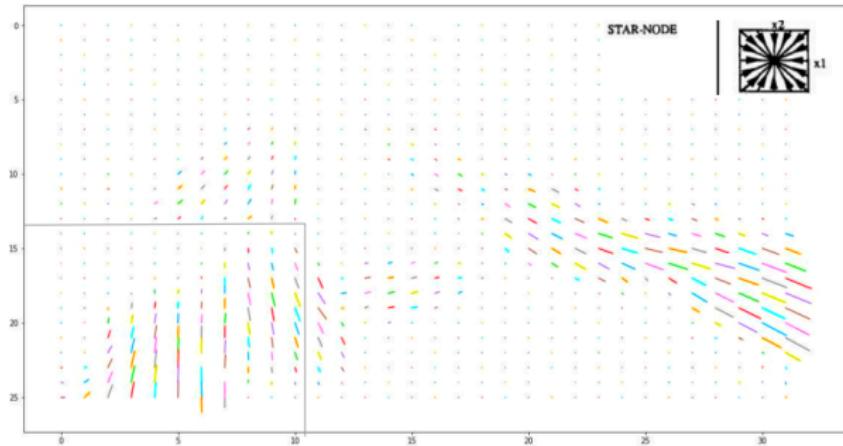


Figure 11: Orientation field obtained from the QMUL traffic signal dataset.

# Detection by Type

- Example: Traffic Signals - Detecting Illegal Crossings and U-turns.

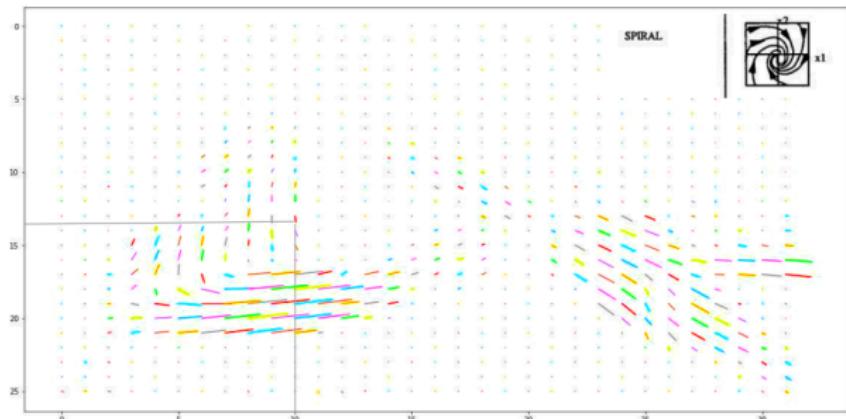


Figure 12: A spiral phase portrait is associated to illegal activities.

# Detection by Critical Point

- Example: Mobile robots/Autonomous cars - Detecting sudden turns.

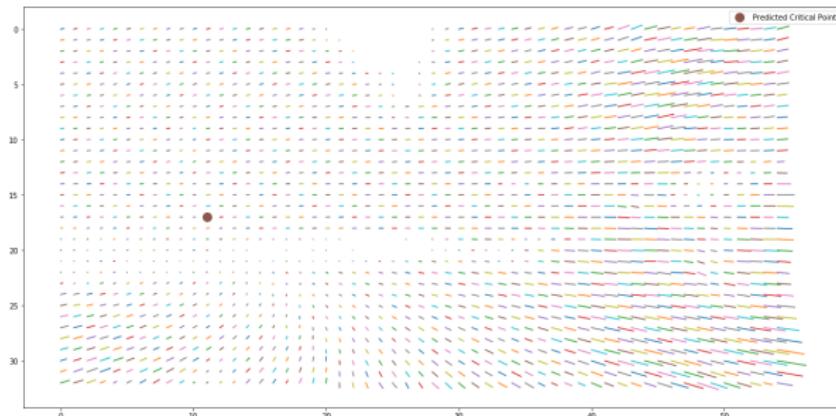


Figure 13: Critical point seen to the left extreme.

# Detection by Critical Point

- Example: Mobile robots/Autonomous cars - Detecting sudden turns.

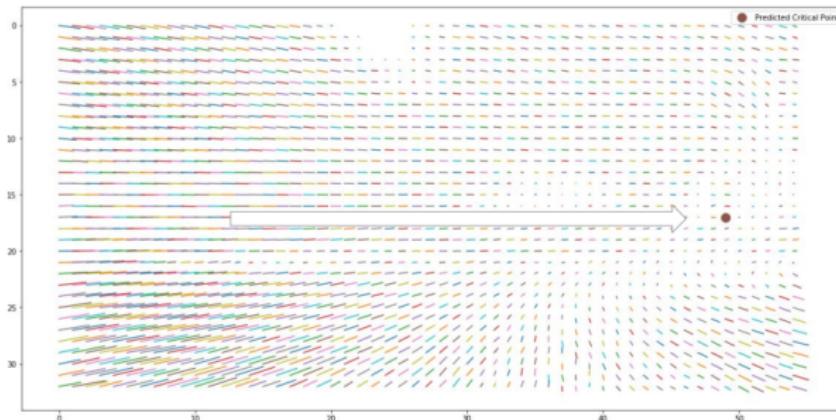
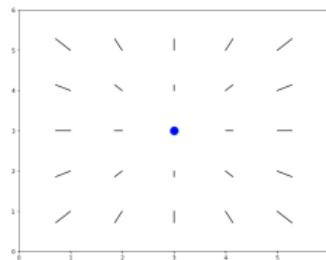
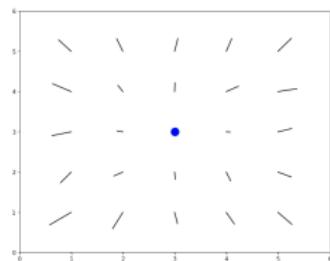


Figure 14: Drastic shift in critical point.

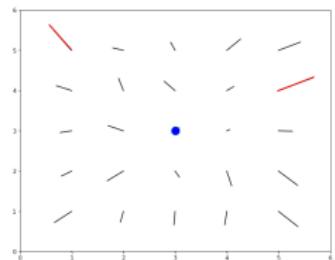
# Detection by Fit



(a) Mapped phase portrait



(b) Field (t-1)



(c) Field (t)

Figure 15: **Variance by Fit:** Two orientation fields share the same phase portrait and critical point but the fit varies. Fit is a measure of closeness or similarity.

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## Experiment - Dataset

- The dataset that was chosen for the experiment was the **UMN crowd activity**[1] dataset by the University of Minnesota.



(a) Gardens



(b) Halls



(c) Public pathways

Figure 16: **UMN-Crowd activity dataset**

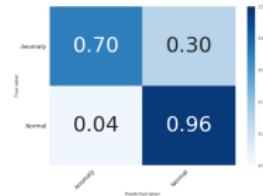
- UMN crowd activity dataset:
  - ▶ Total frames: 7719
  - ▶ Anomalous frames: 1136
- Demonstration datasets: KITTI and QMUL traffic junction dataset.

# Experiment

Parameter	Value
Actual Frame Size	320 x 240
Dominant Orientation Image Size	40 x 30
Frame Rate	30 fps
No. of Frames / Prediction	30,20,10
Anomaly Detector Window Size	10 x 10
Noise Threshold	0.05
Min. no. of Phase portrait changes	7

Table 1: Parameter Table

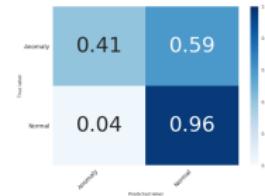
# Results



(a) Prediction per 30 frames



(b) Prediction per 20 frames



(c) Prediction per 10 frames

**Figure 17: Confusion Matrices:** The normalized confusion matrices for different prediction rates. Prediction per 30 frames works better than the other two.

- The false negative values are high because some anomalous frames in between become the new normal in the anomalous sequence.
- Performs significantly better with higher frames per prediction.
- Algorithm does not capture well the sudden change in magnitude of flow values.

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# Contributions and Future work

## Contributions:

- A context-independent motion anomaly detection algorithm.
- A faster non-linear phase portrait classification algorithm by using evolution strategies.
- A novel linear algorithm for phase portrait classification.
- Evaluation of the performance of the detection algorithm on a real-time static camera scenario.
- Demonstration of the generalizing capability with samples from dynamic camera scenarios.

## Future Work:

- Rigorous testing with dynamic camera scenarios.
- Testing with highly accurate optical flow estimators.
- Integration with other methods for motion anomaly detection.

# References

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Thank you!

Questions?