

Generative Modelling with GANs

<https://arxiv.org/pdf/1701.00160.pdf>

Real vs Fake



Two imaginary celebrities that were dreamed up by a random number generator

Image Source: [Nvidia Research](https://research.nvidia.com/publication/2018-04_progressive-growing-gans-improved-quality-stability-and-variation)

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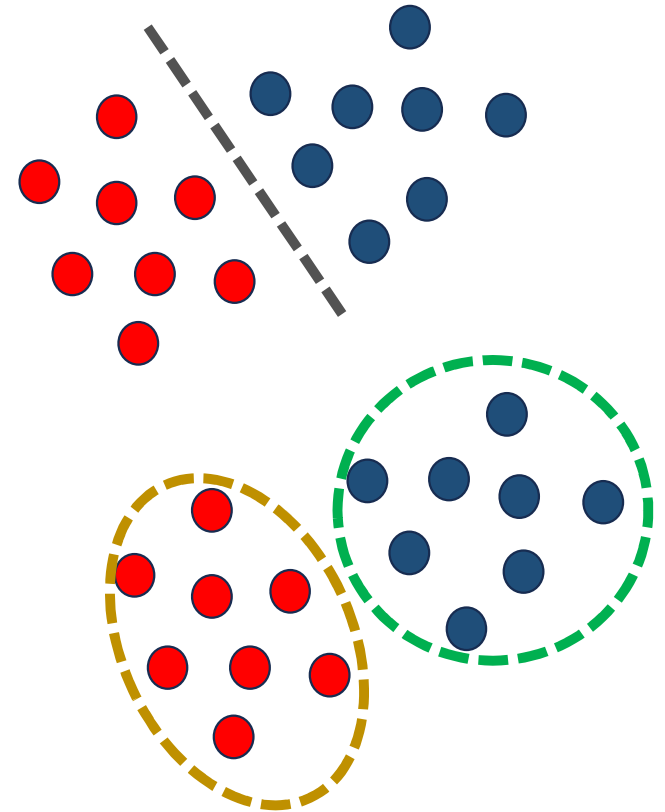
Generative vs. Discriminative Model

Discriminative Models:

- **Goal:** Learns to distinguish between different classes of data
- **Applications:** Models the decision boundary between the classes. Learns $P(Y|X)$

Generative Models:

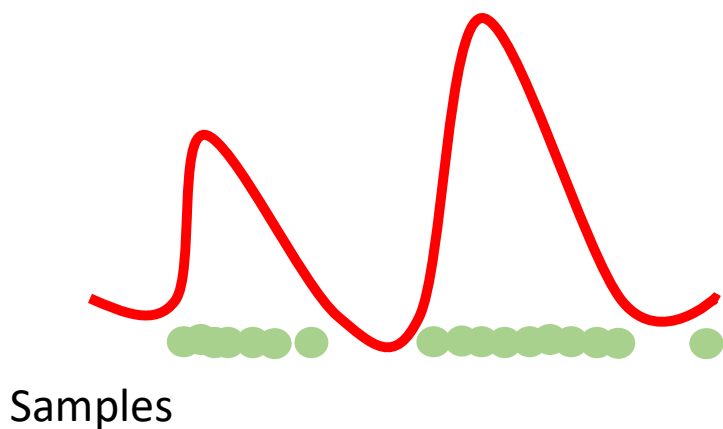
- **Goal:** Learns the distribution of data and generate new data from the distribution
- **Applications:** Models the actual distribution of each class. Learns $P(X,Y)$



Generative Modelling

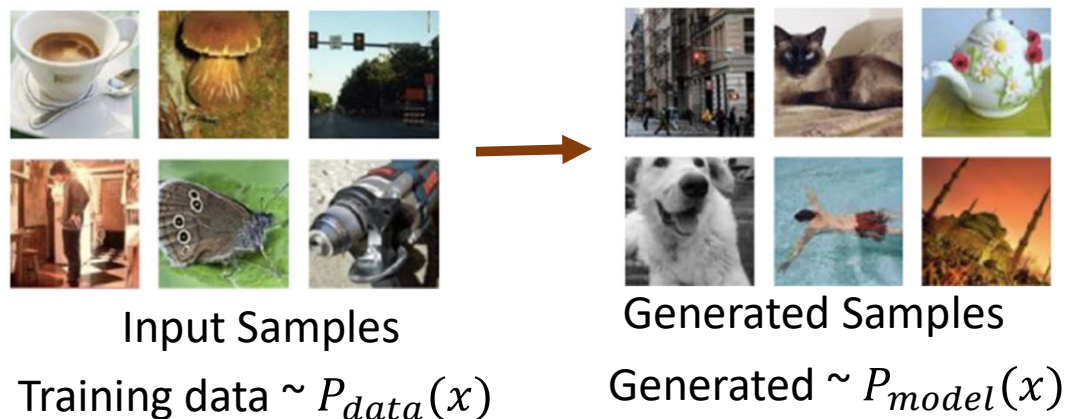
- Takes as input training samples from some distribution and learn a model that represents that distribution
- Output is some representation of probability distribution which defines the sample space

Density Estimation



How can we learn $P_{model}(x)$ similar to $P_{data}(x)$?

Sample Generation



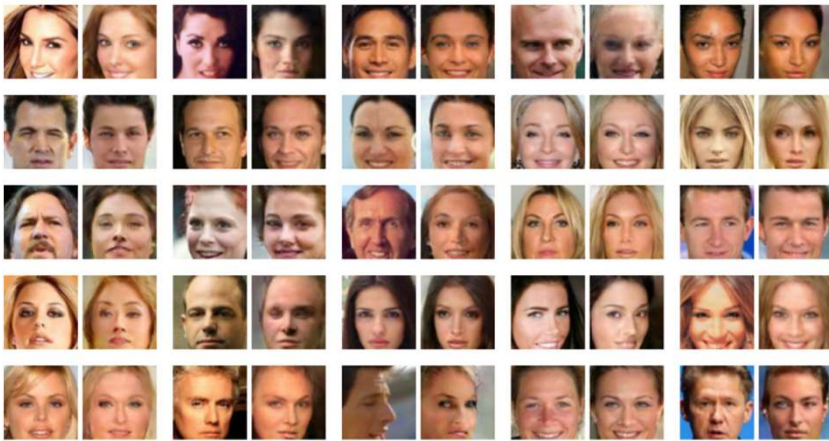
Why we care about Generative modelling?

- ❖ **Data Augmentation:** Capable of uncovering the **underlying features** in a dataset and generate synthetic data



Why we care about Generative modelling?

- ❖ **Debiasing:** Using the **underlying features** in a dataset, to build more fair and representative datasets



Homogenous skin colour, pose

vs.



Diverse skin colour, pose, illumination

Why we care about Generative modelling?

- ❖ **Outlier Detection:** Can detect outliers in the distribution. The outliers can be used during training to improve more.

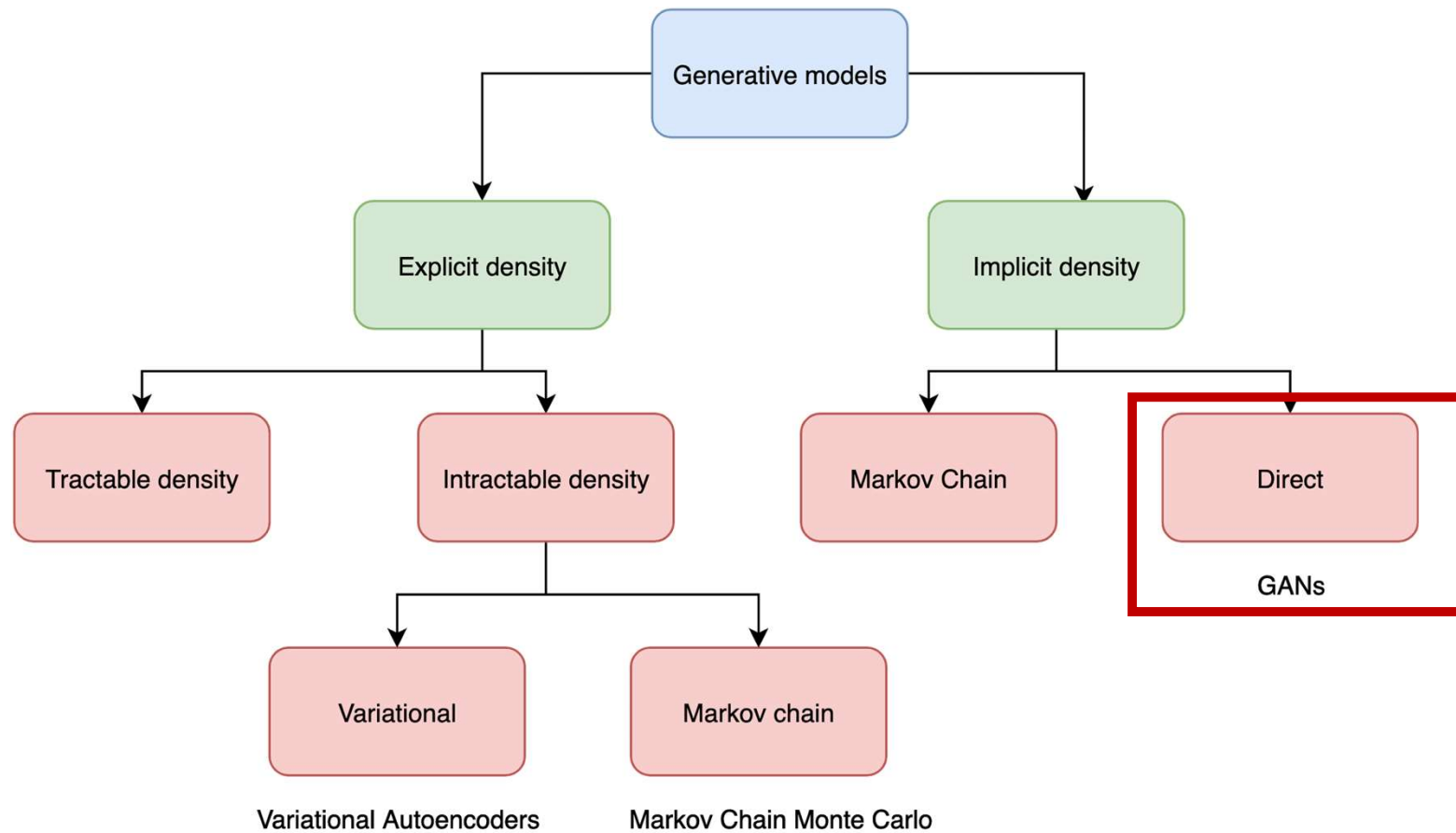
95% of Driving Data:
highway, straight road, fair weather



Detecting outliers to avoid unpredictable behaviour
when training



Generative Model - Prominent Types



Why GANs?

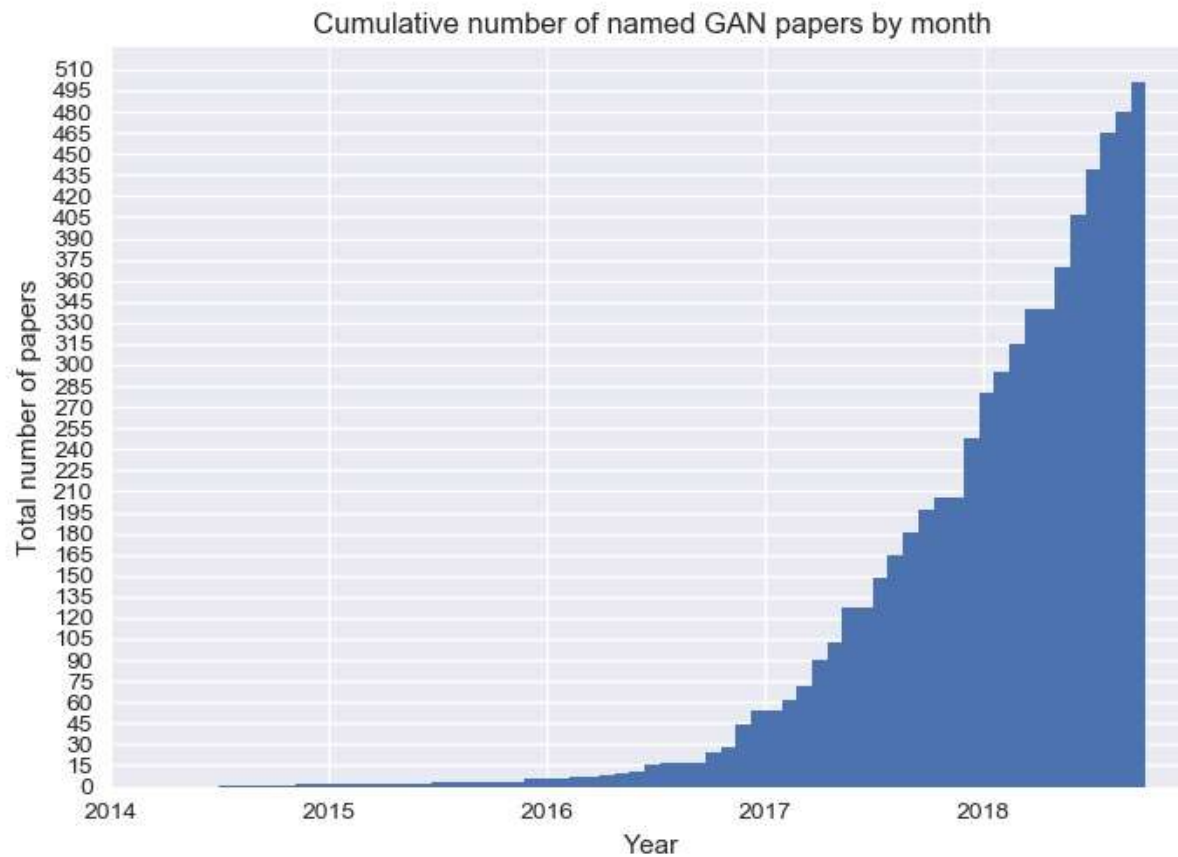


Image Source: <https://github.com/hindupuravinash/the-gan-zoo>

Generative Adversarial Networks (GANs)



- Generative Models: We try to learn the underlying distribution from which our dataset comes from.
- Adversarial Training: GANs are made up of two competing networks (adversaries) that are trying to beat each other
- Neural Networks
- Generative Adversarial Networks (GANs) are a way to make a generative model by having two neural networks compete with each other

GANs

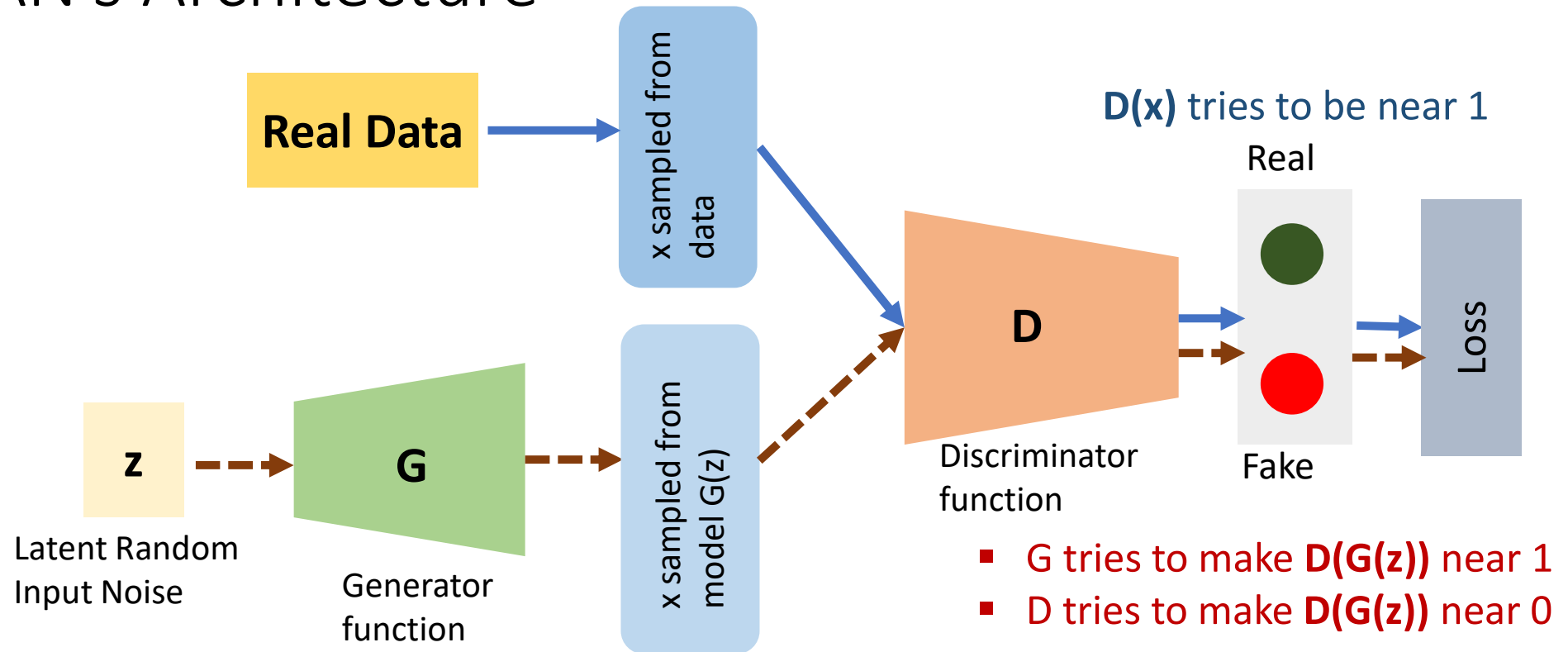
Quote from the original paper on GANs:

“The **generative model can be thought of as analogous to a team of counterfeiters, trying to produce fake currency and use it without detection, while the **discriminative model** is analogous to the police, trying to detect the counterfeit currency. Competition in this game drives both teams to improve their methods until the counterfeits are indistinguishable from the genuine articles.”**

- Goodfellow et. al., “Generative Adversarial Networks” (2014)



GAN's Architecture



Note: Backprop error to update discriminator and generator weights

What is a latent variable?

- It is a variable that is not directly observed or measured but is instead inferred from other observed variables.
- Latent variables are a transformation of the data points into a continuous lower-dimensional space

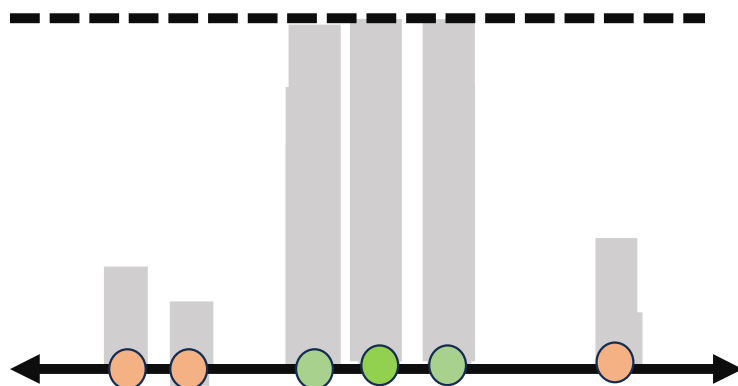
Person	Liked	Age	Movie	Genre
X	Y	16	Spiderman	Action
Y	N	9	Hangover	Comedy
Y	Y	9	Clueless	Comedy
X	Y	16	Black Panther	Action
Y	Y	9	Terminal	Comedy
Z	Y	27	Annabelle	Horror
X	Y	16	Star wars	Action
Z	N	27	The Nun	Horror
Z	Y	27	Conjuring	Horror
Y	Y	9	Ted	Comedy

Intuition behind GANs

- Generator starts from noise to try to create an imitation of the data
- Discriminator looks at both real data and fake data created by the generator
- Generator tries to improve its imitation of the data

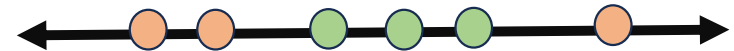
Discriminator

$P(\text{real}) = 1$



 Real Data

Generator



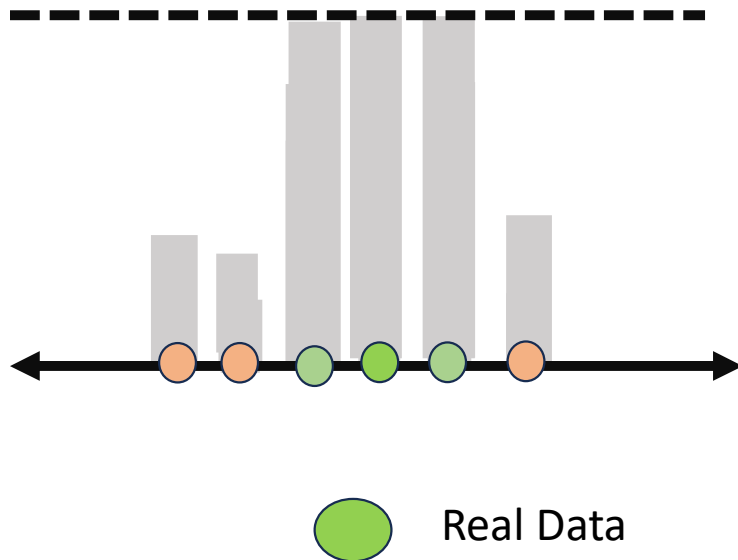
 Fake Data

Intuition behind GANs

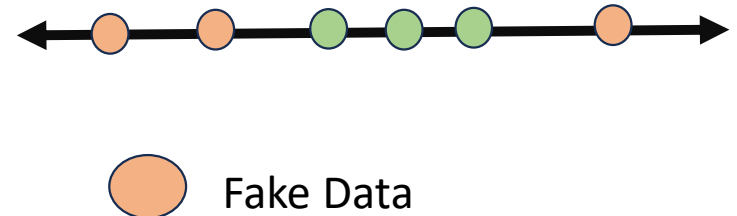
- Generator tries to improve its imitation of the data
- Discriminator tries to predict what's real and what's fake

Discriminator

$P(\text{real}) = 1$



Generator

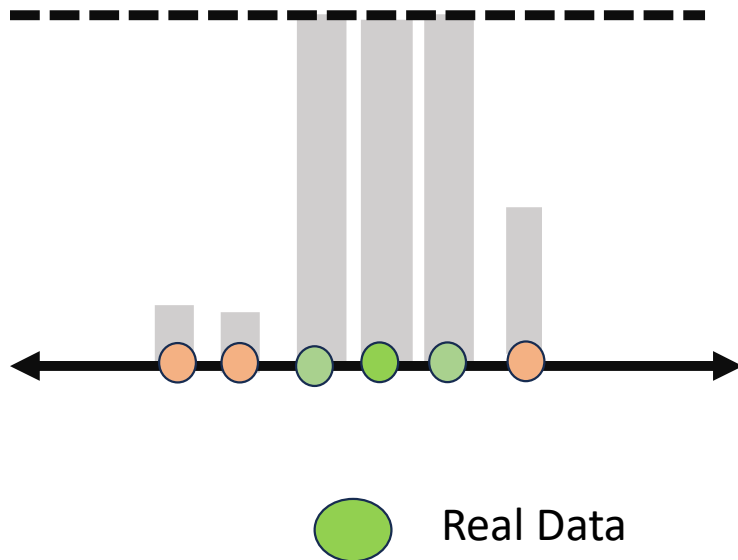


Intuition behind GANs

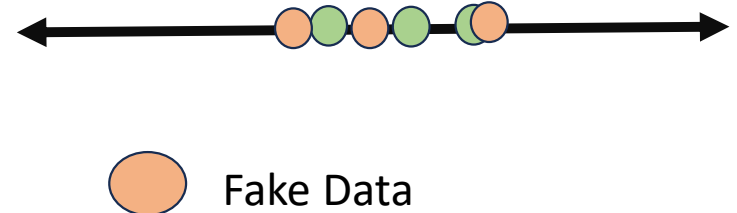
- Generator tries to create imitations of data to trick the discriminator
- Discriminator tries to identify real data from fakes created by the generator

Discriminator

$P(\text{real}) = 1$

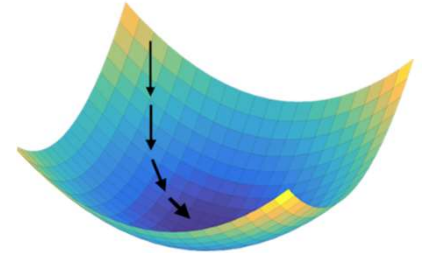


Generator



Training GAN's: Discriminator's cost (J^D)

$$\min_G \max_D V(D, G) = \max_G \min_D -J^D$$



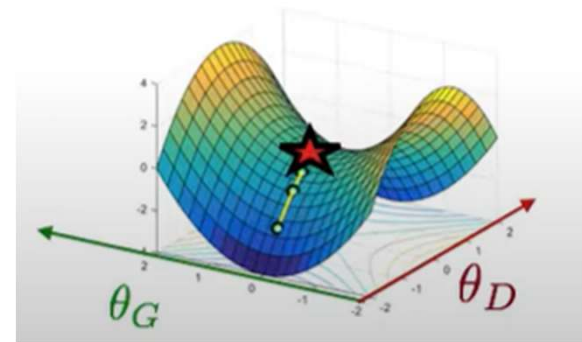
$$J^{(D)}(\theta^{(D)}, \theta^{(G)}) = -\frac{1}{2} \mathbb{E}_{x \sim p_{data}} [\log D(x)] - \frac{1}{2} \mathbb{E}_{z \sim q(z)} [\log(1 - D(G(z)))]$$

$$J^G(\theta^{(D)}, \theta^{(G)}) = -J^D$$

Discriminator output
for real data x

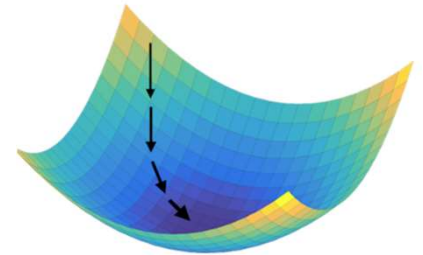
Discriminator output
for fake data $G(z)$

- Generator minimizes the probability of the discriminator being correct
- Saddle Point of discriminators loss



Training GAN's: Discriminator's cost (J^D)

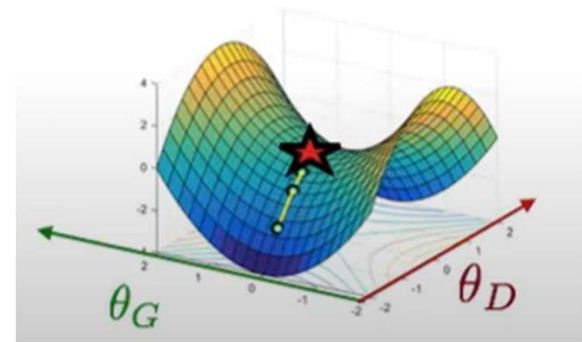
$$\min_G \max_D V(\mathbf{D}, \mathbf{G}) = \max_G \min_D -J^D$$



OPEN QUESTION:

- Is the equilibrium “locally (exponentially) stable”?
- When it is not, how do we make stable?

- Generator minimizes the probability of the discriminator being correct
- Saddle Point of discriminators loss



Min-max Game Approach

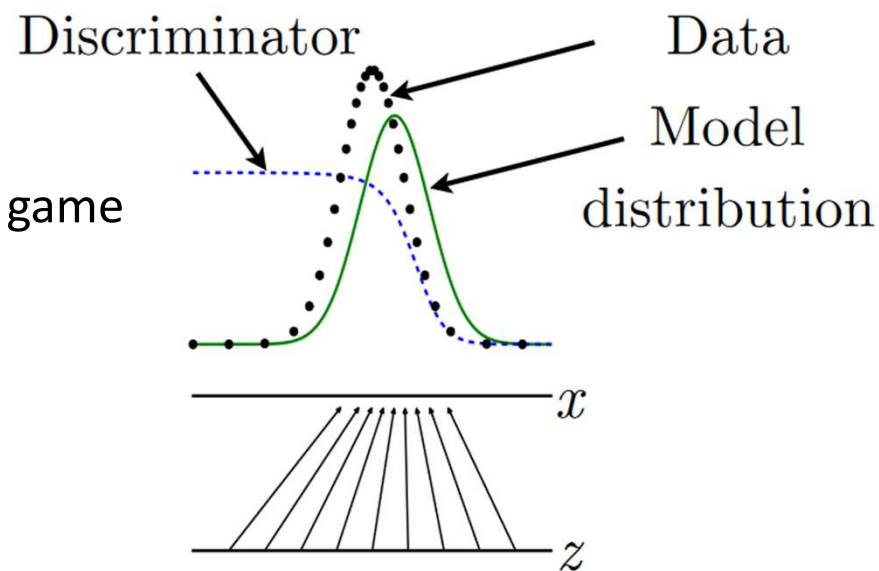
$$J^{(D)}(\theta^{(D)}, \theta^{(G)}) = -\frac{1}{2} \mathbb{E}_{x \sim p_{data}} [\log D(x)] - \frac{1}{2} \mathbb{E}_{z \sim q(z)} [\log(1 - D(G(z)))]$$

$$\frac{\partial J^D}{\partial D(x)} = 0 \rightarrow D^*(x) = \frac{P_{data}(x)}{P_{data}(x) + P_{model}(x)}$$

- The Nash Equilibrium/Saddle point of this particular game is achieved at:

- $P_{data}(x) = P_{model}(x) \forall x$
- $D(x) = \frac{1}{2} \forall x$

□ What happens with $D(G(z)) \rightarrow 0$?

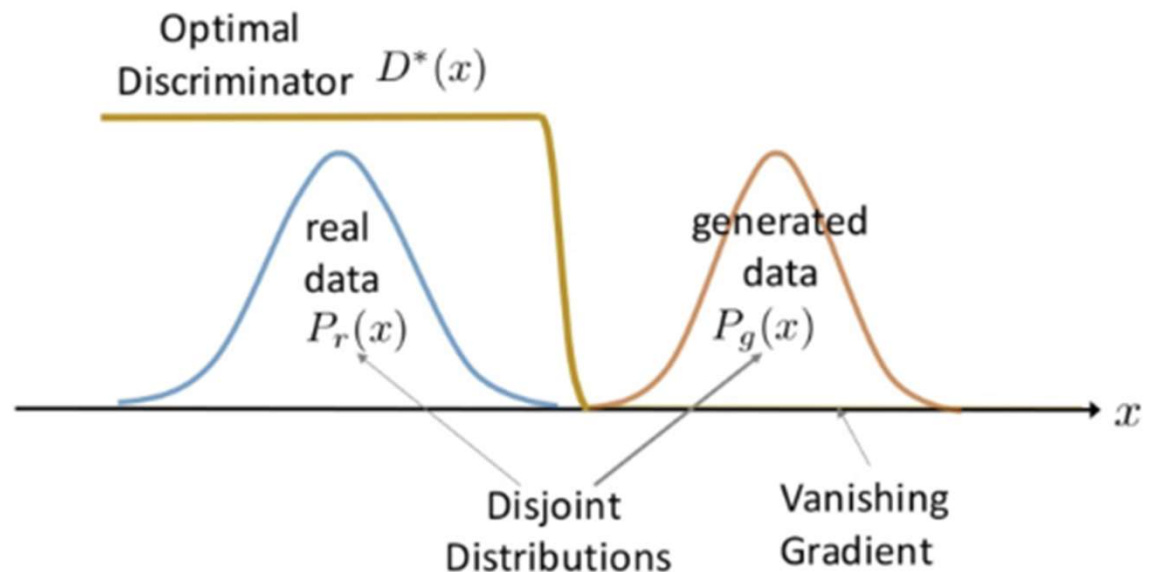


Vanishing Gradient Problem with Generator

$$J^{(D)}(\theta^{(D)}, \theta^{(G)}) = -\frac{1}{2} \mathbb{E}_{x \sim p_{data}} [\log D(x)] - \frac{1}{2} \mathbb{E}_{z \sim q(z)} [\log(1 - D(G(z)))]$$

- Gradient goes to 0 if D is confident, i.e., $D(G(z)) \rightarrow 0$

- ✓ As can be seen that whenever the discriminator becomes very confident, the loss value will be zero
- ✓ Nothing to improve for the generator



Heuristic, non-saturating game

$$J^{(D)} = -\frac{1}{2} \mathbb{E}_{x \sim p_{data}} [\log D(x)] - \frac{1}{2} \mathbb{E}_{z \sim q(z)} [\log(1 - D(G(z)))]$$

$$J^G = -\frac{1}{2} \mathbb{E}_{z \sim q(z)} \log D(G(z))$$

- Generator maximizes the log probability of the discriminator's mistake

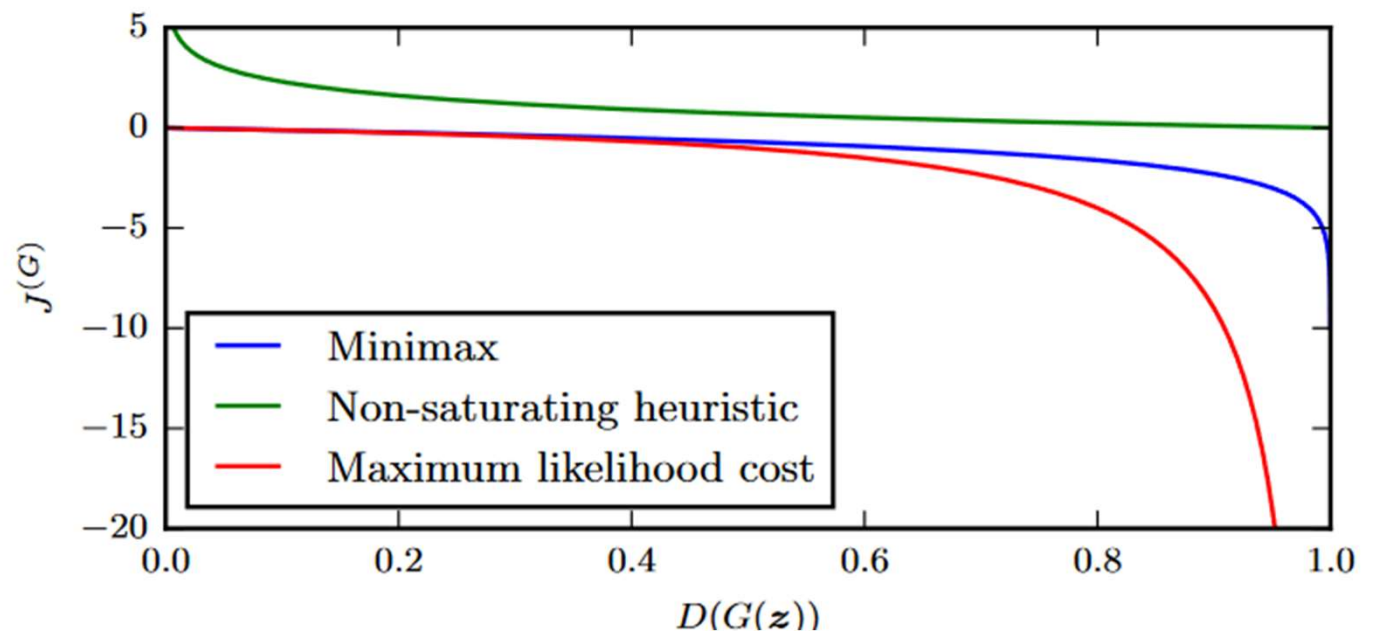
Comparison of Generator Losses

The cost that the generator receives for generating a samples $G(z)$ depends only on how the discriminator responds to that sample

$$J^G = -J^D$$

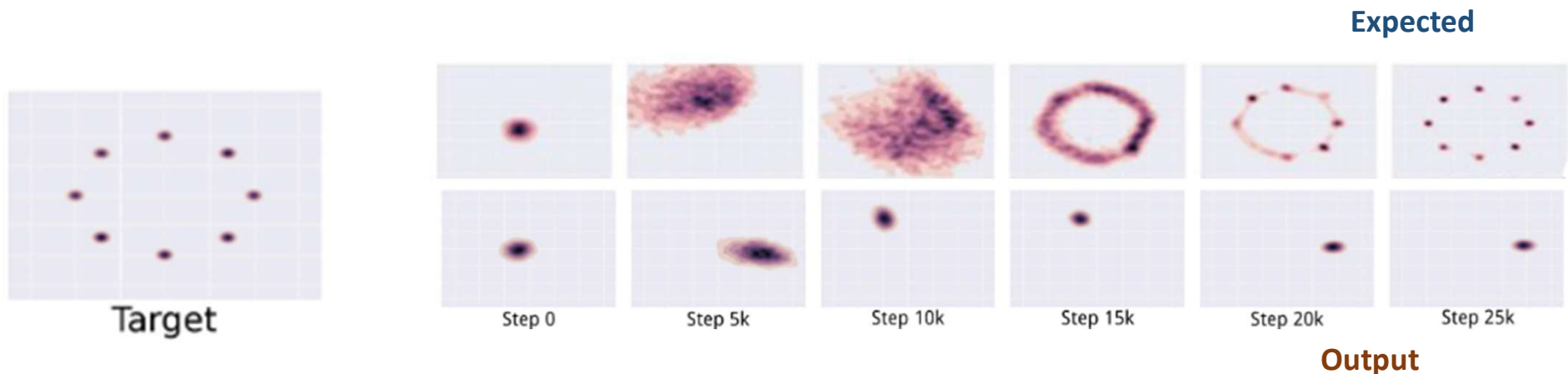
$$J^G = -\frac{1}{2} E_z \log D(G(z))$$

$$J^G = -\frac{1}{2} E_z e^{(\sigma^{-1} D(G(z)))}$$



Why GANs are hard to train?

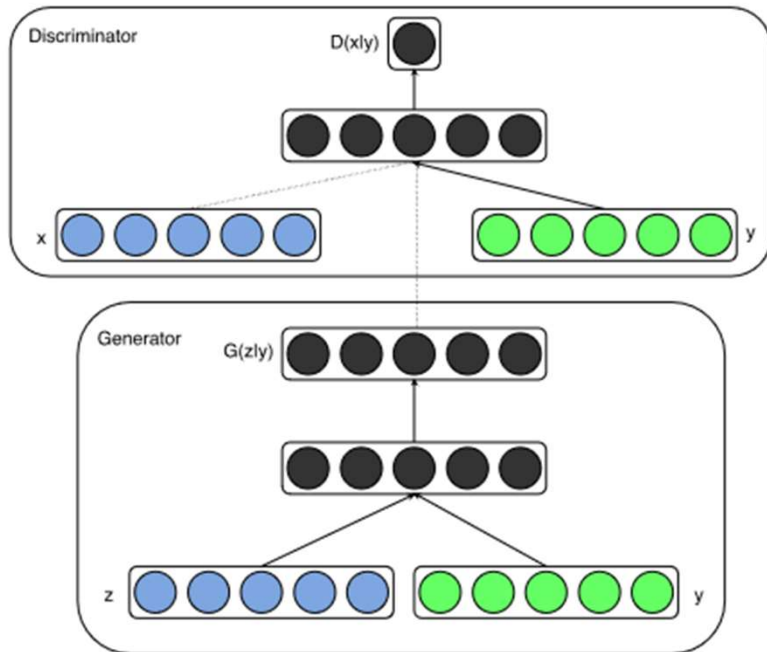
- Non-Convergence: D & G nullifies each other's learning in every iteration. The two learning tasks need to have balance to achieve stability
- Mode Collapse: Maintain trade-off of generating more accurate vs high coverage samples. Generator excels in a subspace but does-not cover entire real distribution



Tricks to train GANs

- Historical generated batches: Helps stabilize discriminator training at early stages.
[Shrivastava, Ashish, et al. "Learning from Simulated and Unsupervised Images through Adversarial Training." CVPR. Vol. 2. No. 4. 2017]
- One Side Label Smoothing: Involves modifying the labels used during the training of the discriminator. [Salimans, Tim, et al. "Improved techniques for training gans." Advances in Neural Information Processing Systems. 2016]
- Feature Matching: Generator is trained such that the expected value of statistics matches the expected value of real statistics

Few variations of GAN – Conditional GANs



- Generator Learns $P(x|z,y)$
- Discriminator Learns $P(x,y)$

$$J^D = \mathbb{E}_{x \sim p_{data}(x)} [\log D(x|y)] + \mathbb{E}_{z \sim p_x(z)} [\log(1 - D(G(z|y)))]$$

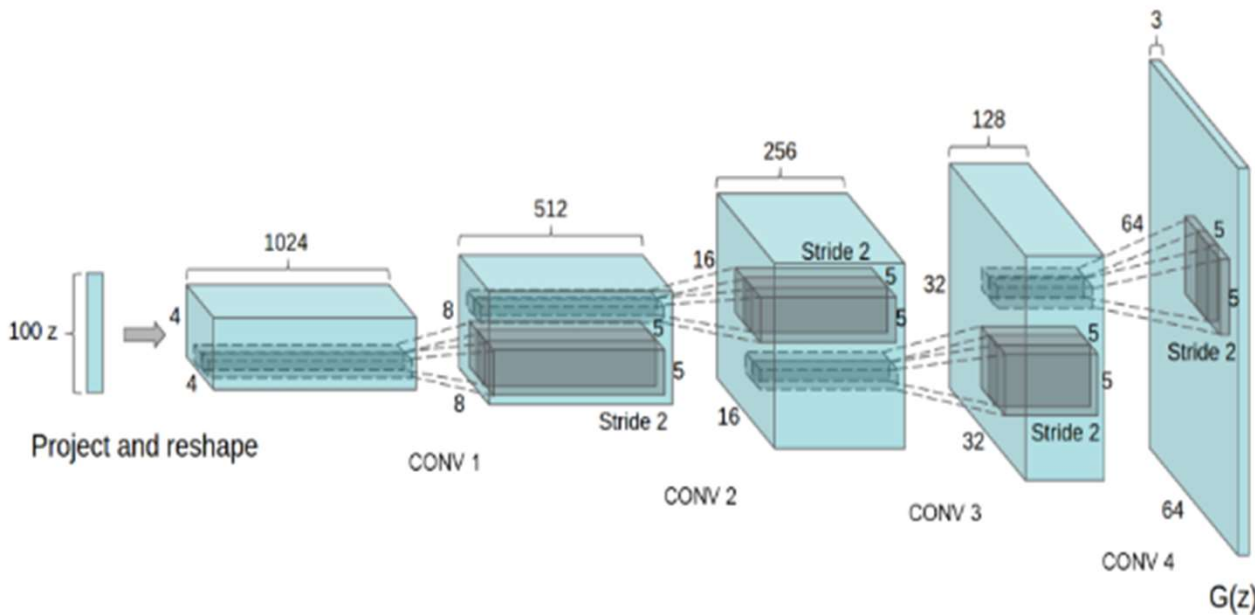
Mirza, M. and Osindero, S., 2014. Conditional generative adversarial nets. arXiv:1411.1784.

Each row is conditioned on a different label. You can use a single neural network to generate all 10 digits by telling it what digit to generate



Deep Convolutional GANs (DCGANs)

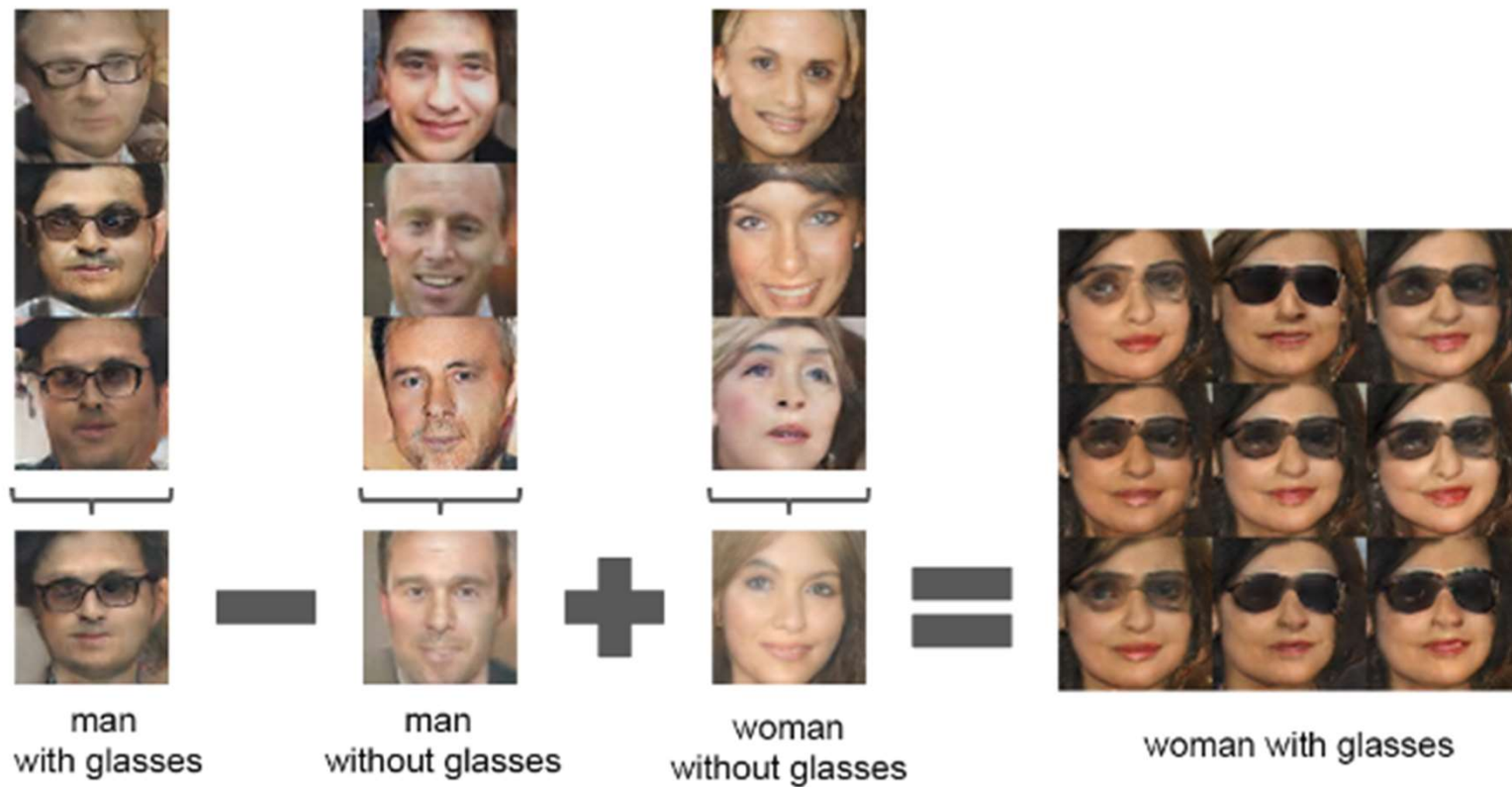
Generator Architecture



- Replace FC hidden layers with Convolutions
 - Generator: Fractional-Strided Convolutions
- Use Batch Normalization after each layer
- Inside Generator
 - Use ReLU for hidden layers
 - Use Tanh for the output layer

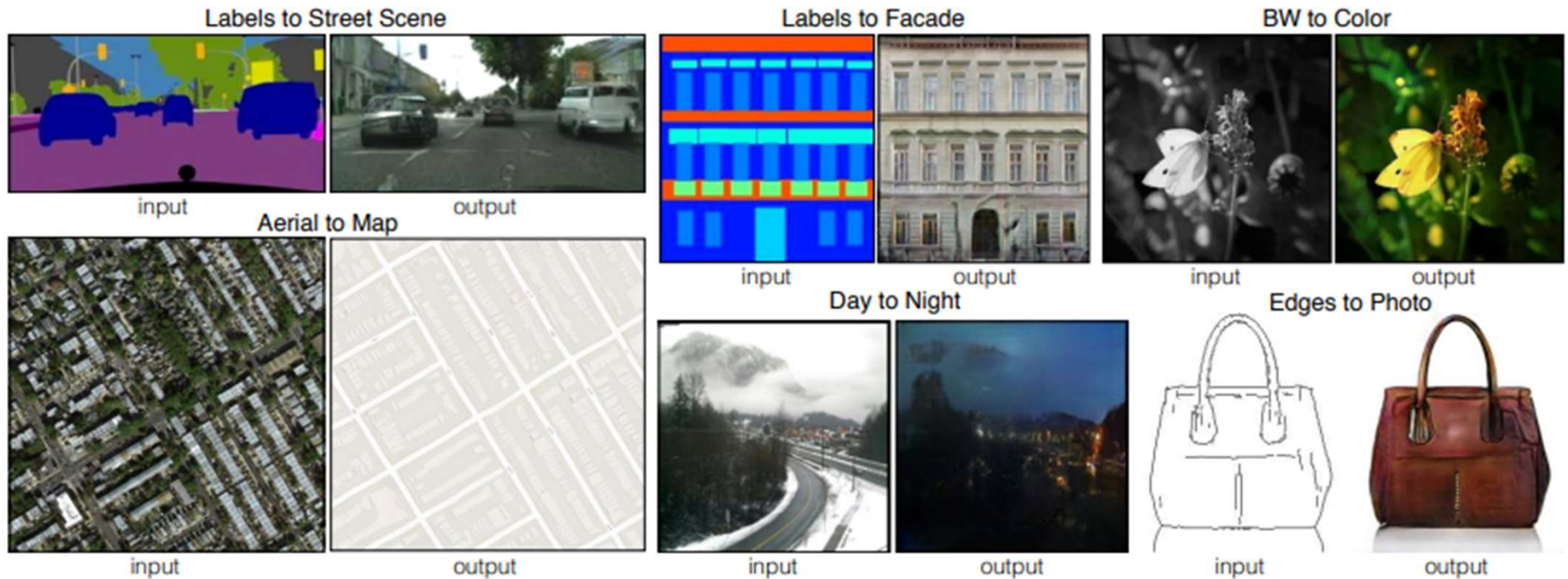
Radford, Alec, Luke Metz, and Soumith Chintala. "Unsupervised representation learning with deep convolutional generative adversarial networks." arXiv:1511.06434 (2015).

Latent vectors capture interesting patterns....



vector additions and subtractions are meaningful in this latent space

Image-to-Image Translation



[Link to an interactive demo of the paper](#)

Isola, P., Zhu, J. Y., Zhou, T., & Efros, A. A. "Image-to-image translation with conditional adversarial networks". arXiv preprint arXiv:1611.07004. (2016).

Text-to-Image Synthesis

Motivation:

- Given a text description, generate images closely associated.
- Uses a conditional GAN with the generator and discriminator being condition on “dense” text embedding

Reed, S., Akata, Z., Yan, X., Logeswaran, L., Schiele, B., & Lee, H.
“Generative adversarial text to image synthesis”. ICML (2016)

this small bird has a pink breast and crown, and black primaries and secondaries.



the flower has petals that are bright pinkish purple with white stigma



this magnificent fellow is almost all black with a red crest, and white cheek patch.



this white and yellow flower have thin white petals and a round yellow stamen



Summary

- GANs are generative models that are implemented using two stochastic neural network modules: Generator and Discriminator
- The Generator tries to generate samples from random noise as input
- The Discriminator tries to distinguish the samples from Generator and samples from the real data distribution
- Both the networks are trained adversarially to fool the other component making them better at their respective tasks
- GAN is an active area of research with a lot of work currently done in the theoretic foundation of the Network

Important Papers

- NIPS 2016 Tutorial: - [Ian Goodfellow](#),
<https://arxiv.org/search/cs?searchtype=author&query=Goodfellow,+I>
- Arjovsky, Martin, and Léon Bottou. "Towards principled methods for training generative adversarial networks." arXiv preprint arXiv:1701.04862 (2017).
- Roth, Kevin, et al. "Stabilizing training of generative adversarial networks through regularization." Advances in Neural Information Processing Systems. 2017.
- Li, Jerry, et al. "Towards understanding the dynamics of generative adversarial networks." arXiv:1706.09884 (2017).
- Kodali, Naveen, et al. "On convergence and stability of GANs." arXiv:1705.07215 (2017).
- Fedus, William, et al. "Many Paths to Equilibrium: GANs Do Not Need to Decrease a Divergence At Every Step. arXiv:1710.08446 (2017).
- <https://github.com/soumith/ganhacks#authors>
- <http://www.inference.vc/instance-noise-a-trick-for-stabilising-gan-training/>
- <https://www.araya.org/archives/1183>

Codes, Tools and Tricks

- <https://github.com/soumith/ganhacks#authors>
- <https://medium.com/@utk.is.here/keep-calm-and-train-a-gan-pitfalls-and-tips-on-training-generative-adversarial-networks-edd529764aa9>
- <https://jhui.github.io/2017/03/05/Generative-adversarial-models/>
- <https://www.kaggle.com/code/theblackmamba31/generating-fake-faces-using-gan>
- <https://realpython.com/generative-adversarial-networks/>