

Honors Precalculus with Trigonometry (OM013)

Problem Set 1

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Please show all work because you will be graded on the clarity of your explanation as well as the correctness of your work. An answer with no work/explanation will receive zero credit.

1. Find the center-radius form of the equation of the circle with center at $(-7, -4)$ and tangent to the x-axis. (Hint: A line tangent to a circle touches it at exactly one point.)

$$(x-h)^2 + (y-k)^2 = r^2$$

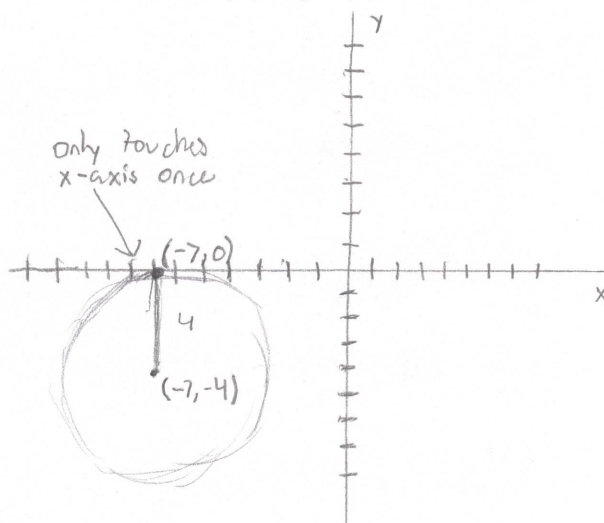
$$(h,k) = (-7, -4)$$

$$(x+7)^2 + (y+4)^2 = r^2$$

Radius is 4 \longrightarrow

$$(x+7)^2 + (y+4)^2 = 4^2$$

$$\boxed{(x+7)^2 + (y+4)^2 = 16}$$



The radius needs to be the lowest distance that the circle only touches the x-axis once and that distance is 4.

2. Decide whether or not the equation has a circle as its graph. If it does, give the center and the radius. If it does not, describe the graph: $x^2 + y^2 + 6x - 8y + 26 = 0$

$$x^2 + y^2 + 6x - 8y + 26 = 0$$

$$(x^2 + 6x) + (y^2 - 8y) + 26 = 0$$

$$(x^2 + 6x + 9) + (y^2 - 8y + 16) + 1 = 0$$

$$(x+3)^2 + (y-4)^2 + 1 = 0$$

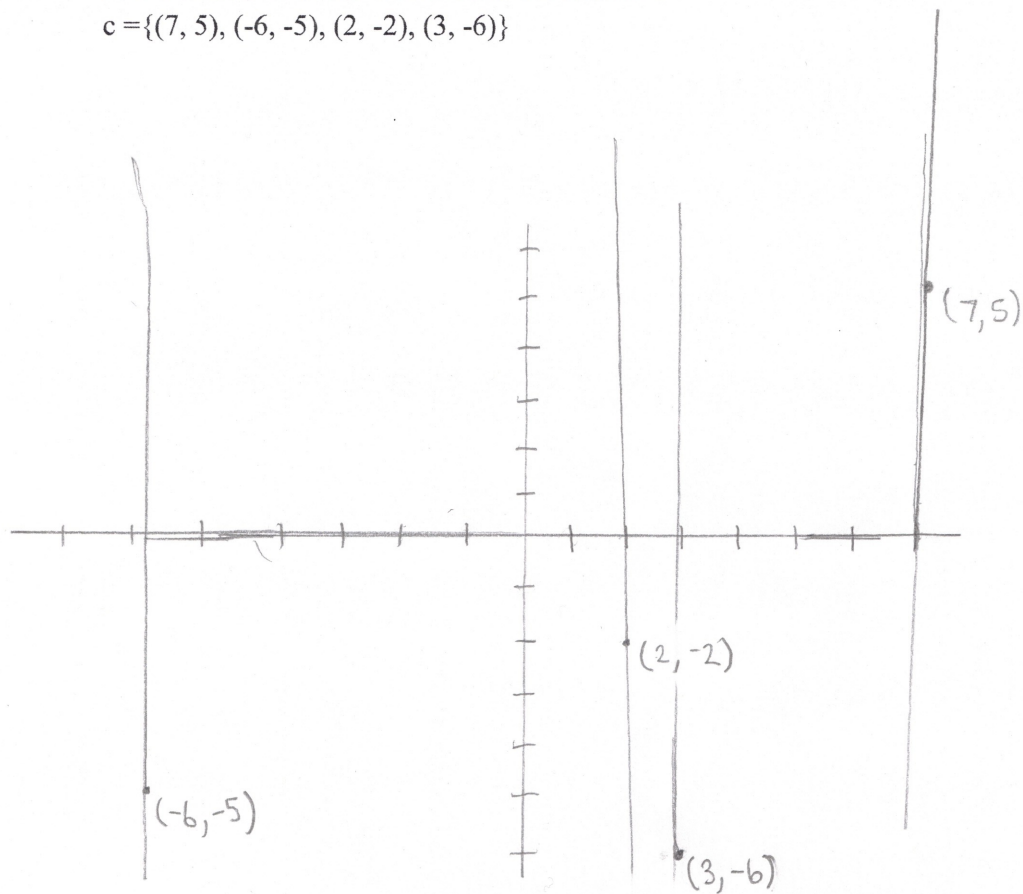
$$(x+3)^2 + (y-4)^2 = -1$$

center $(-3, 4)$, radius $\sqrt{-1}$

Since $\sqrt{-1}$ is an imaginary number, the graph is empty - \emptyset

3. Determine whether the relation is a function.

$$c = \{(7, 5), (-6, -5), (2, -2), (3, -6)\}$$



passes vertical line test - each input has exactly one output

C is a function