

Worksheet 2

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1. Simplify the following symbolic statements

(a) $(\pi > 0) \wedge (\pi < 10)$	[$0 < \pi < 10$]
(b) $(p \geq 7) \wedge (p < 12)$	[$7 \leq p < 12$]
(c) $(x > 5) \wedge (x < 7)$	[$5 < x < 7$]
(d) $(x < 4) \wedge (x < 6)$	[$x < 4$]
(e) $(y < 45) \wedge (y^2 < 9)$	[$-3 < y < 3$]
(f) $(x \geq 0) \wedge (x \leq 0)$	[$x = 0$]

3. As conjunction is associative for $\phi_1 \wedge \phi_2 \wedge \cdots \wedge \phi_n$ to be true all of the conjuncts need to be true

4. Similarly, for the statement to be false only one of the conjuncts needs to be false

5. Simplify the following symbolic statements

(a) $(\pi > 3) \vee (\pi > 10)$	[$\pi > 3$]
(b) $(x < 0) \vee (x > 0)$	[$x \neq 0$]
(c) $(x > 0) \vee (x = 0)$	[$x \geq 0$]
(d) $(x > 0) \vee (x \geq 0)$	[$x \geq 0$]
(e) $(x > 3) \vee (x^2 > 9)$	[$x^2 > 9$]

7. As disjunction is associative for $\phi_1 \vee \phi_2 \vee \cdots \vee \phi_n$ to be true only one of the disjuncts need to be true

8. Similarly, as disjunction is associative all of the disjuncts need to be false for the statement to be false

9. Simplify the following symbolic statements

(a) $\neg(\pi > 3.2)$	[$\pi \leq 3.2$]
(b) $\neg(x < 0)$	[$x \geq 0$]
(c) $\neg(x^2 > 0)$	[$x = 0$]

- (d) $\neg(x = 1)$ [$x \neq 1$]
- (e) $\neg\neg\psi$ [ψ]
11. Let D be “The dollar is strong”, Y be “The Yuan is strong”, and T be “New US-China trade agreement signed.” Represents the following statements using symbolic notation:
- (a) “Dollar and Yuan both strong” [$D \wedge Y$]
- (b) “Yuan weak despite new trade agreement, but Dollar remains strong” [$\neg Y \wedge T \wedge D$]
- (c) “Dollar and Yuan can’t both be strong at the same time” [$\neg(D \wedge Y)$]
- (d) “New trade agreement does not prevent fall in Dollar and Yuan” [$T \wedge \neg D \wedge \neg Y$]
- (e) “US-China trade agreement fails but both currencies remain strong” [$\neg T \wedge D \wedge Y$]
12. Do “Not guilty” and “ \neg guilty” mean the same?
- (a) “Not guilty” only means that they have failed to prove guilt, and not that the person is actually innocent whereas “ \neg guilty” means that person *is* innocent
13. How can you state “I was not displeased with the movie.” in formal language
- (a) You would need to introduce various other levels of pleasure such as S as satisfied, E as enthralled, and so on. Then take the disjunction of all of those.