

ORIENTATION OF BINARY:

$\angle i \rightarrow$ inclination angle

--- line of sight

$$(\theta_l, \phi_l) \hat{l} \quad \hat{n} (\theta_n, \phi_n)$$

$$\hat{l} \cdot \hat{n} = \cos i$$

$$= \cos \theta_l \cos \theta_n$$

$$+ \sin \theta_l \sin \theta_n \cos(\phi_l - \phi_n)$$

① The plus and cross polarization can be written as (for orbiting binary)

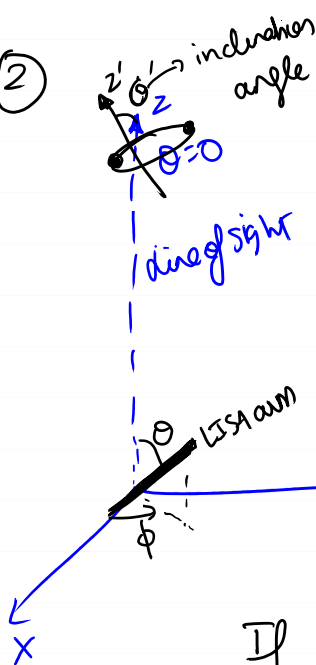
$$h_+ = \frac{-4G\mu}{c^2 r} \left(\frac{v}{c}\right)^2 \left\{ \frac{1 + (\hat{l} \cdot \hat{n})^2}{2} \right\} \cos 2\phi$$

$$= -\frac{4G\mu}{c^2 r} \left(\frac{v}{c}\right)^2 \left(\frac{1 + \cos^2 i}{2} \right) \cos 2\phi //$$

$$h_x = -\frac{4G\mu}{c^2 r} \left(\frac{v}{c}\right)^2 (\hat{l} \cdot \hat{n}) \sin 2\phi$$

$$= -\frac{4G\mu}{c^2 r} \left(\frac{v}{c}\right)^2 \cos i \sin 2\phi //$$

②



since $\theta = 0$ is the line of sight, the inclination angle is θ'

$$h_+ = -\frac{4G\mu}{c^2 r} \left(\frac{v}{c}\right)^2 \left(\frac{1 + \cos^2 \theta'}{2} \right) \cos 2\phi$$

$$h_x = -\frac{4G\mu}{c^2 r} \left(\frac{v}{c}\right)^2 \cos \theta' \sin 2\phi$$

If we define $F_+^{(+)}$ & $F_+^{(x)}$ as the antenna beam parameters we can write more accurately

$$h(t) = B(t) \cos \chi(t) \quad \text{where} \quad B(t) = \sqrt{(F_+^{(+)}(t) A_+(t))^2 + (F_+^{(x)}(t) A_x(t))^2}$$

$$\chi(t) = \phi_{gw}(t) + \phi_n(t)$$

$$\text{where } \phi_n(t) = \tan^{-1} \left[\frac{-F_+^{(x)}(t) A_x(t)}{F_+^{(+)}(t) A_+(t)} \right]$$