

CS 325 – Asymptotic Analysis

Practice Problems

Big-O, Ω , Θ Examples

For each of the following pairs of functions, either $f(n)$ is $O(g(n))$, $f(n)$ is $\Omega(g(n))$, or $f(n) = \Theta(g(n))$. Determine which relationship is correct.

1) $f(n) = 0.00001n^3$; $g(n) = 500000n + 4000000$

1) $f(n) = \log n^3$; $g(n) = \log n + 5$

3) $f(n)=\log(\log n)$; $g(n) = \log n$

4) $f(n) = \log n^3$; $g(n) = \log^3 n$

5) $f(n)=n\log n$; $g(n) = \log(n!)$

6) $f(n)=10$; $g(n) = \log 10$

7) $f(n) = 2^n$; $g(n) = 10n^2$

8) $f(n) = 4^n$; $g(n) = 2^{2n}$; $h(n) = 2^{n+1}$

$$9) g(n) = 2^{2n}; h(n) = 2^{n^2}$$

10. Prove or disprove (with a counterexample).

If $f_1(n) = O(g_1(n))$ and $f_2(n) = O(g_2(n))$ then
 $f_1(n) + f_2(n) = O(\max\{g_1(n), g_2(n)\})$.

