

CS 325 - Activity 3

You may work in groups with up to 3 students. When submitting solutions in Gradescope select a page for each problem and the students in your group.

Written: (5 pts)

Canoe Rental Problem: There are n trading posts numbered 1 to n as you travel downstream. At any trading post i you can rent a canoe to be returned at any of the downstream trading posts j , where $j \geq i$. You are given an array $R[i, j]$ defining the costs of a canoe which is picked up at post i and dropped off at post j , for $1 \leq i, j \leq n$. Assume that $R[i, i] = 0$ and $R[i, j] = -1$ if $i > j$. Your task is to determine a sequence of rentals which start at post 1 and end at post n , and that has the minimum total cost.

a) Give a written description and pseudocode for a DP algorithm to compute the cost of the cheapest sequence of canoe rentals from trading post 1 to n . Give the recursive formula you used to fill in the table or array.

- CanoeCost(R)
- Take in n as a user input.
- Generate the $[n \times n]$ table of the costs of the canoe.
- $n \leftarrow \#rows[R]$
- $C[1] \leftarrow 0$
- for $i \leftarrow 2$ to n
- $min \leftarrow R[1, i]$
- for $k \leftarrow 2$ to $i - 1$
- if $C[k] + R[k, i] < min$
- $min \leftarrow C[k] + R[k, i]$
- $C[i] \leftarrow min$
- return $C[n]$

b) Give a written description and pseudocode for code to print the sequence of trading posts visited.

- CanoeSequence(R)
- $n \leftarrow \#rows[R]$
- $C[1] \leftarrow 0, P[1]$
- for $i \leftarrow 2$ to n
- $min \leftarrow R[1, i]$
- $P[i] \leftarrow 1$
- for $k \leftarrow 2$ to $i - 1$
- if $C[k] + R[k, i] < min$
- $min \leftarrow C[k] + R[k, i]$
- $P[i] \leftarrow k$
- $C[i] \leftarrow min$
- return P
- -----
- PrintSequence(P, i)
- if $i > 1$
- PrintSequence(P, $P[i]$)
- print "rented at $P[i]$ and dropped off at i "

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- For each of the downstream posts, subtract the highest travel cost possible from the total cost.
 - Store the index of the values in an integer array.
 - Go through the array of indexes and remove any repeats.
 - Print array.

c) What is the running time of your algorithms to find the minimum cost and to find the sequence of trading posts?

DP Problem:

$O(n*j)$ (N in the number of total trading posts, j is the number of downstream trading posts)

Print:

- $O(n*j)$?

Code: (10 pts)

Implement your algorithms for the Canoe Rental Problem in C++. The test cases have the following structure

```
Input:      4
            0 10 15 40
            -1 0 5 15
            -1 -1 0 8
            -1 -1 -1 0
```

```
Output:     23 1 3 4
```

where

Input is the number of trading posts, n , followed by an $n \times n$ table of rental costs R . $R[i][j]$ is the cost to rent a canoe at trading post i and return it to trading post j . $R[i][i] = 0$ $R[i][j] = -1$ if $i > j$.

Output the minimum cost and a list of trading posts that were stopped at.

You can use the code template 3 provided. The name of the file you submit to Gradescope must be **act3.cpp**. You may submit multiple times. Select all group members each time you submit and include the names of the group members in your comments.