

Project Reading

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This file contains the important and relevant things from the reading resources for the project. It also contains doubts which are unresolved. Last edited: *[2025-05-10 Sat]*

1 Converging point method

The method is beautifully explained in this website: <https://physics.weber.edu/palen/clearinghouse/labs/hyades/disthyad.html>.

2 Reading Paper:

2.1 4. Membership determination:

Using Gaia DR2, data proper-motion is plotted as Vector Point Diagram (VPD). And the cluster members are assigned by choosing stars which form a dense cluster of points in VPD.

The centre of the circular region confining the probable cluster members was determined by maximum density method in the proper motion plane which is found to lie at (x, y) (cos,) (0.13, 3.37) mas yr⁻¹. The radius of the circle was derived by plotting the stellar density as a function of radial distance in the proper motion plane as illustrated in Fig. 2. We fit the

stellar density profile with a function similar to the one used to characterize the radial profiles of star clusters in the galaxies.

2.1.1 Membership probability

$$P_{\mu}(i) = \frac{n_c \cdot \phi_c^v(i)}{n_c \cdot \phi_c^v(i) + n_f \cdot \phi_f^v(i)}$$

$$\phi_c^v(i) = \frac{1}{2\pi \sqrt{(\sigma_{xc}^2 + \epsilon_{xi}^2)(\sigma_{yc}^2 + \epsilon_{yi}^2)}} \exp \left\{ -\frac{1}{2} \left[\frac{(\mu_{xi} - \mu_{xc})^2}{\sigma_{xc}^2 + \epsilon_{xi}^2} + \frac{(\mu_{yi} - \mu_{yc})^2}{\sigma_{yc}^2 + \epsilon_{yi}^2} \right] \right\}$$

$$\phi_f^v(i) = \frac{1}{2\pi \sqrt{1 - \gamma^2} \sqrt{(\sigma_{xf}^2 + \epsilon_{xi}^2)(\sigma_{yf}^2 + \epsilon_{yi}^2)}} \exp \left\{ -\frac{1}{2(1 - \gamma^2)} \left[\frac{(\mu_{xi} - \mu_{xf})^2}{\sigma_{xf}^2 + \epsilon_{xi}^2} - \frac{2\gamma(\mu_{xi} - \mu_{xf})(\mu_{yi} - \mu_{yf})}{\sqrt{(\sigma_{xf}^2 + \epsilon_{xi}^2)(\sigma_{yf}^2 + \epsilon_{yi}^2)}} + \frac{(\mu_{yi} - \mu_{yf})^2}{\sigma_{yf}^2 + \epsilon_{yi}^2} \right] \right\}$$

$$\gamma = \frac{(\mu_{xi} - \mu_{xf})(\mu_{yi} - \mu_{yf})}{\sigma_{xf}\sigma_{yf}}$$