

Deep learning Day-6

* Type of loss function

Regression loss function	Binary classification loss function	Multi class classification loss function
(1) MSE (Mean Squared error) (2) MAE (Mean absolute error) (3) MSLE (Mean Squared logarithmic error) - ReLU, leaky relu, X-relu, ELU, Swish	(1) Binary cross entropy loss function (2) Hinge loss - (1) Sigmoid (2) Tanh..	(1) Multi class cross entropy loss fun or categorical cross entropy loss fun (2) Sparse Multi class cross entropy loss function or Sparse categorical cross entropy loss fun - Softmax

(1) Regression loss function

(1) MSE (Mean Squared error)

$$MSE = \frac{1}{n} \sum_{i=1}^n (y_a - y_p)^2$$

→ MSE penalize big error value so that (increases)

optimizer function can easily identify big error term.

Let's say $y_a = 5$

$$(y_a - y_p)^2$$

$$(5 - 4)^2 = 1^2 = 1$$

$$(5 - 3)^2 = 2^2 = 4$$

$$3 - 2 \left[(5 - 2)^2 = 3^2 = 9 \right] - 5 - 4 = 5$$

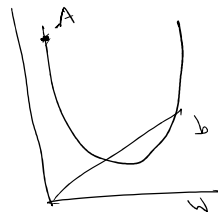
→ $y_a = 5$ $y_p = 4.9$ — 0.1
 $= 4.8$ — 0.2
 $= 4.7$ — 0.3
 $= 4.6$ — 0.4
 $= 4.55$ — 0.05
 $= 4.85$ — 0.15

1 lakh

$$(5 - 4.9)^2 = 0.1^2 = 0.01 = 4.6$$

$$(5 - 4.8)^2 = 0.2^2 = 0.04 = 4.55$$

$$(5 - 4.7)^2 = 0.3^2 = 0.09 = 4.85$$



$$(5 - 4.0)^2 = 0.32 = 0.09 = 4.85$$

$\begin{matrix} 5 \\ 4.7 \\ 4.01 \\ 0.01 \\ 0.04 \\ 0.09 \end{matrix}$

I II

→ Draw back of MSE :-

→ Since we are penalizing the big error value, we can not use MSE in case of outlier.

② MAE (mean absolute error)

$$MAE = \frac{1}{n} \sum_{i=1}^n |y_a - y_p|$$

→ We can use MSE in case of outlier.

③ MSLE (mean squared logarithmic error)

$$MSE = \frac{1}{n} \sum_{i=1}^n (y_a - y_p)^2$$

$$MSLE = \frac{1}{n} \sum_{i=1}^n (\log(y_a) - \log(y_p))^2$$

$$MSLE = \frac{1}{n} \sum_{i=1}^n (\log(y_a + 1) - \log(y_p + 1))^2$$

$$\log(100) = \dots$$

$$MSE > MSLE$$

MAE

② Classification loss function

① Binary Classification

① Binary cross entropy loss function

→ It is also called log loss

It is also called log loss function.

→ conditions for use

- ① Classification → Binary classification
- ② activation function → Sigmoid in out put layer
- ③ Dependent variable should be encoded

$$\text{log} = -\frac{1}{n} \sum_{i=1}^n [y_i \log y_i + (1-y_i) \log(1-y_i)]$$

② Hinge loss

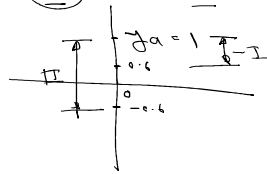
* conditions for use:-

- ① Classification → Binary
- ② Activation function → tanh used in out put layer
- ③ Dependent variable should be encoded in -1 or 1

$$\text{Hinge loss} = \max(0, 1 - y_a y_p)$$

tanh — Range → $\begin{pmatrix} -1 \\ 1 \end{pmatrix}$

- ① $y_a = 1$ $y_p = 0.6$
 ② $y_a = 1$ $y_p = -0.6$



Case (I) $\text{Hinge loss} = \max(0, 1 - y_a y_p)$
 $= \max(0, 1 - 1 \times 0.6)$

$$\text{Hinge loss} = 0.4$$

Case (II) $\text{Hinge loss} = \max(0, 1 - 1 \times (-0.6))$

$$\text{Hinge loss} = 1.6$$

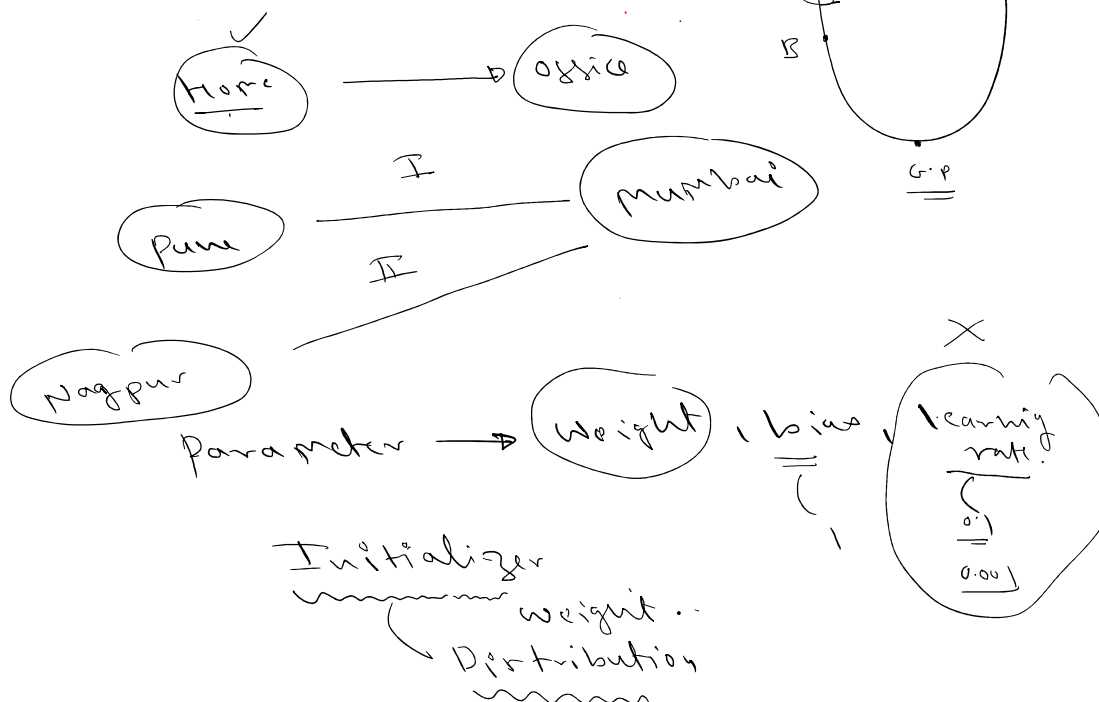
tanh — Range — -1 to 1

(1) $-0.6 \rightarrow -1$

- ① Classification → multi class
- ② Out put layer activation → Softmax
- ③ dependent variable ^{func} should be one hot encoded but loss will be calculated for 1

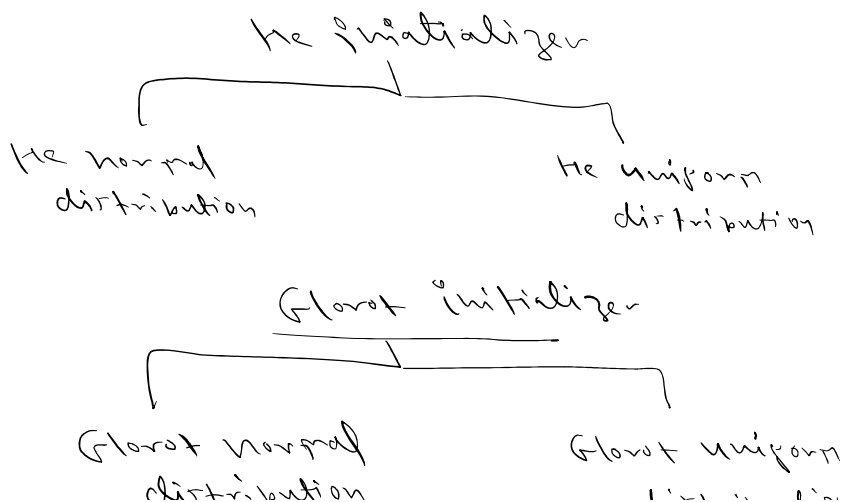
$$\text{loss} = - \sum_{i=1}^n y_i \log \hat{y}_i$$

* Initializer



* Types of Initializer

- ① He initializer
- ② Glorot initialize



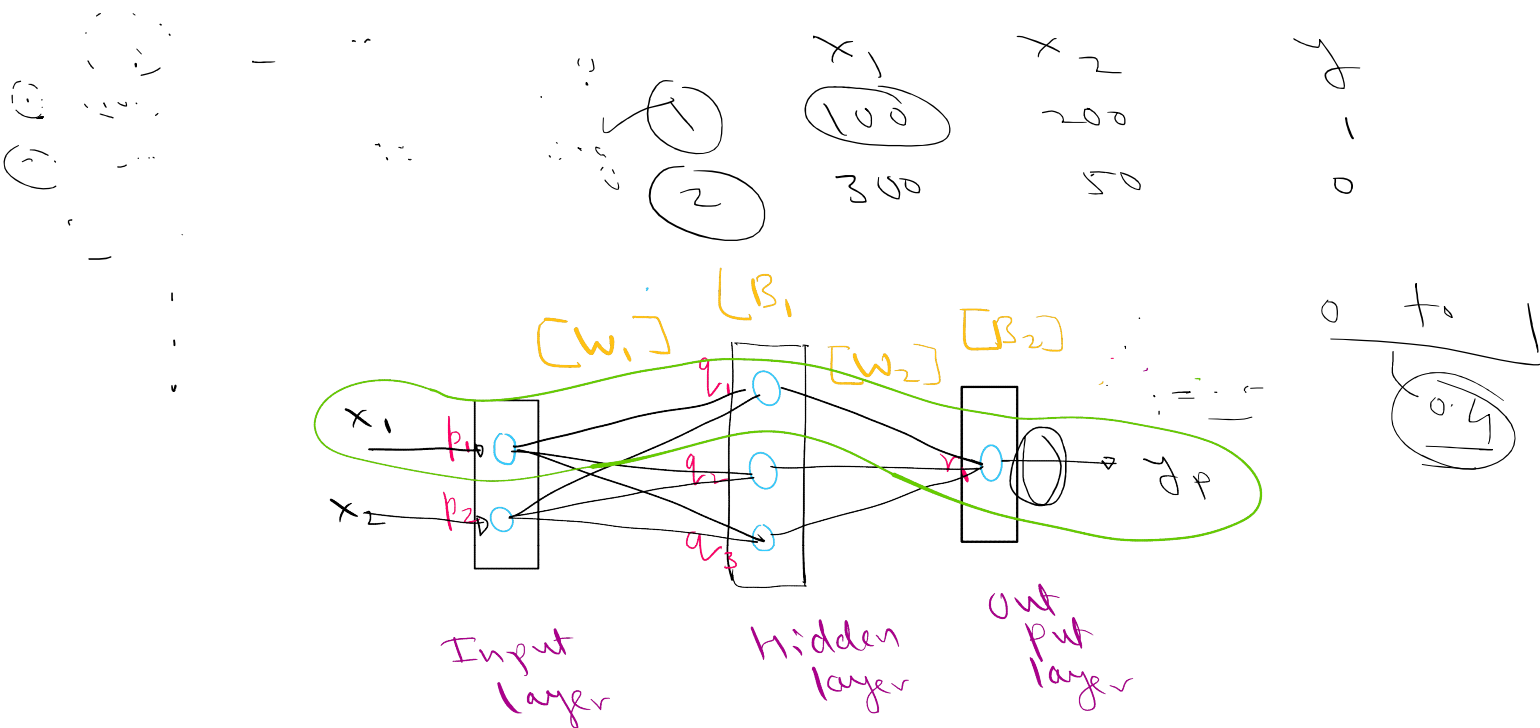
Glorot normal
distribution

Glorot uniform
distribution

General thumb rule

→ If we deal with regression problem we initializer will work good.

→ If we deal with classification problem that time Glorot work well.



$$\begin{aligned}
 (1) & \quad x_1 \rightarrow p_1 \xrightarrow{w_1} q_1 \xrightarrow{w_2} r_1 \rightarrow y_{p1} \quad 100, \\
 (2) & \quad x_1 \rightarrow p_1 \rightarrow q_2 \rightarrow r_1 \rightarrow y_{p2} \quad 100, \\
 & \quad x_1 \rightarrow p_1 \rightarrow q_3 \rightarrow r_1 \rightarrow y_{p3} \\
 & \quad x_2 \rightarrow p_2 \rightarrow q_1 \rightarrow r_1 \rightarrow y_{p4} \\
 & \quad x_2 \rightarrow p_2 \rightarrow q_2 \rightarrow r_1 \rightarrow y_{p5} \\
 & \quad x_2 \rightarrow p_2 \rightarrow q_3 \rightarrow r_1 \rightarrow y_{p6}
 \end{aligned}$$

$$x_2 \rightarrow p_2 \rightarrow q_3 \rightarrow r_1 \rightarrow y_4$$