# Sieve of Eratosthenes

Difficulty Level: Medium • Last Updated: 31 Mar, 2021

Given a number n, print all primes smaller than or equal to n. It is also given that n is a small number.

### **Example:**

**Input:** n = 10

**Output:** 2357

**Input:** n = 20

Output: 235711131719

The sieve of Eratosthenes is one of the most efficient ways to find all primes smaller than n when n is smaller than 10 million or so (Ref <u>Wiki</u>).

Recommended: Please solve it on "**PRACTICE**" first, before moving on to the solution.

Following is the algorithm to find all the prime numbers less than or equal to a given integer n by the Eratosthene's method:

When the algorithm terminates, all the numbers in the list that are not marked are prime.

## **Explanation with Example:**

Let us take an example when n = 50. So  $\sqrt{\phantom{a}}$  ed to print all prime numbers smaller

than or equal to 50.

We create a list of all numbers from 2 to 50.

	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50

According to the algorithm we will mark all the numbers which are divisible by 2 and are greater than or equal to the square of it.

	2	3	4	5	6	7	8	9	10
11	12	13	14	15	<mark>16</mark>	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	<mark>36</mark>	37	38	39	40
41	42	43	44	45	46	47	48	49	50

Now we move to our next unmarked number 3 and mark all the numbers which are multiples of 3 and are greater than or equal to the square of it.

	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	50

We move to our next unmarked number 5 and mark all multiples of 5 and are greater than or equal to the square of it.

	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	25	26	27	28	29	30
31	<mark>32</mark>	33	34	35	36	37	38	<mark>39</mark>	40
41	42	43	44	45	46	47	48	49	<u>50</u>

We continue this process and our final table will look like below:

	2	3	4	5	6	7	8	9	10
11	12	13	14	15	16	17	18	19	20
21	22	23	24	<mark>25</mark>	26	27	28	29	<mark>30</mark>
31	32	33	34	35	36	37	38	39	40
41	42	43	44	45	46	47	48	49	<mark>50</mark>

So the prime numbers are the unmarked ones: 2, 3, 5, 7, 11, 13, 17, 19, 23, 29, 31, 37, 41, 43, 47.

Thanks to **Krishan Kumar** for providing above explanation.

### Implementation:

Following is the implementation of the above algorithm. In the following implementation, a boolean array arr[] of size n is used to mark multiples of prime numbers.

```
C++
```

```
// C++ program to print all primes
// smaller than or equal to
// n using Sieve of Eratosthenes
#include <bits/stdc++.h>
using namespace std;
void SieveOfEratosthenes(int n)
{
    // Create a boolean array
    // "prime[0..n]" and initialize
    // all entries it as true.
    // A value in prime[i] will
    // finally be false if i is
    // Not a prime, else true.
    bool prime[n + 1];
    memset(prime, true, sizeof(prime));
    for (int p = 2; p * p <= n; p++)</pre>
        // If prime[p] is not changed,
        // then it is a prime
        if (prime[p] == true)
```

```
// Update all multiples
            // of p greater than or
            // equal to the square of it
            // numbers which are multiple
            // of p and are less than p^2
            // are already been marked.
            for (int i = p * p; i <= n; i += p)</pre>
                 prime[i] = false;
        }
    }
    // Print all prime numbers
    for (int p = 2; p <= n; p++)</pre>
        if (prime[p])
            cout << p << " ";
}
// Driver Code
int main()
{
    int n = 30;
    cout << "Following are the prime numbers smaller "</pre>
         << " than or equal to " << n << endl;</pre>
    SieveOfEratosthenes(n);
    return 0;
}
```

### Java



#### **Related Articles**

```
// prime, else true.
boolean prime[] = new boolean[n + 1];
for (int i = 0; i <= n; i++)
    prime[i] = true;

for (int p = 2; p * p <= n; p++)
{
    // If prime[p] is not changed, then it is a
    // prime
    if (prime[p] == true)</pre>
```

```
{
                // Update all multiples of p
                for (int i = p * p; i <= n; i += p)</pre>
                    prime[i] = false;
            }
        }
        // Print all prime numbers
        for (int i = 2; i <= n; i++)</pre>
        {
            if (prime[i] == true)
                System.out.print(i + " ");
    }
    // Driver Code
    public static void main(String args[])
        int n = 30;
        System.out.print(
            "Following are the prime numbers ");
        System.out.println("smaller than or equal to " + n);
        SieveOfEratosthenes g = new SieveOfEratosthenes();
        g.sieveOfEratosthenes(n);
    }
}
// This code has been contributed by Amit Khandelwal.
```

## **Python**

```
# Python program to print all
# primes smaller than or equal to
# n using Sieve of Eratosthenes
def SieveOfEratosthenes(n):
    # Create a boolean array
    # "prime[0..n]" and initialize
    # all entries it as true.
    # A value in prime[i] will
    # finally be false if i is
    # Not a prime, else true.
    prime = [True for i in range(n+1)]
    p = 2
    while (p * p <= n):
        # If prime[p] is not
        # changed, then it is a prime
        if (prime[p] == True):
```

#### C#

```
// C# program to print all primes
// smaller than or equal to n
// using Sieve of Eratosthenes
using System;
namespace prime {
public class GFG {
    public static void SieveOfEratosthenes(int n)
        // Create a boolean array
        // "prime[0..n]" and
        // initialize all entries
        // it as true. A value in
        // prime[i] will finally be
        // false if i is Not a
        // prime, else true.
        bool[] prime = new bool[n + 1];
        for (int i = 0; i < n; i++)</pre>
            prime[i] = true;
        for (int p = 2; p * p <= n; p++)</pre>
            // If prime[p] is not changed,
            // then it is a prime
            if (prime[p] == true)
                // Update all multiples of p
                for (int i = p * p; i | ; i += p)
```

```
prime[i] = false;
            }
        }
        // Print all prime numbers
        for (int i = 2; i <= n; i++)</pre>
        {
            if (prime[i] == true)
                Console.Write(i + " ");
        }
    }
    // Driver Code
    public static void Main()
        int n = 30;
        Console.WriteLine(
            "Following are the prime numbers");
        Console.WriteLine("smaller than or equal to " + n);
        SieveOfEratosthenes(n);
    }
}
}
// This code is contributed by Sam007.
```

### **PHP**

```
// php program to print all primes smaller
// than or equal to n using Sieve of
// Eratosthenes
function SieveOfEratosthenes($n)
    // Create a boolean array "prime[0..n]"
    // and initialize all entries it as true.
    // A value in prime[i] will finally be
    // false if i is Not a prime, else true.
    $prime = array_fill(0, $n+1, true);
    for (p = 2; p*p <= n; p++)
        // If prime[p] is not changed,
        // then it is a prime
        if ($prime[$p] == true)
        {
            // Update all multiples of p
            for (\$i = \$p*\$p; \$i <= \$n \cdot \$i += \$p)
                $prime[$i] = false;
```

```
}
}

// Print all prime numbers
for ($p = 2; $p <= $n; $p++)
    if ($prime[$p])
        echo $p." ";
}

// Driver Code
    $n = 30;
    echo "Following are the prime numbers "
        ."smaller than or equal to " .$n."\n";
    SieveOfEratosthenes($n);

// This code is contributed by mits
?>
```

# **Javascript**

```
<script>
// javascript program to print all
// primes smaller than or equal to
// n using Sieve of Eratosthenes
function sieveOfEratosthenes(n)
{
    // Create a boolean array
    // "prime[0..n]" and
    // initialize all entries
    // it as true. A value in
    // prime[i] will finally be
    // false if i is Not a
    // prime, else true.
    prime = Array.from({length: n+1}, (_, i) => true);
    for (p = 2; p * p <= n; p++)
    {
        // If prime[p] is not changed, then it is a
        // prime
        if (prime[p] == true)
            // Update all multiples of p
            for (i = p * p; i <= n; i += p)</pre>
                prime[i] = false;
        }
    }
    // Print all prime numbers
    for (i = 2; i <= n; i++)</pre>
```

#### Output

```
Following are the prime numbers smaller than or equal to 30 2 3 5 7 11 13 17 19 23 29
```

Time complexity : O(n\*log(log(n)))

You may also like to see :

- How is the time complexity of Sieve of Eratosthenes is n\*log(log(n))?
- Segmented Sieve.
- Sieve of Eratosthenes in O(n) time complexity

Attention reader! Don't stop learning now. Get hold of all the important DSA concepts with the **DSA Self Paced Course** at a student-friendly price and become industry ready. To complete your preparation from learning a language to DS Algo and many more, please refer **Complete Interview Preparation Course**.

In case you wish to attend live classes with industry experts, please refer <u>Geeks</u> <u>Classes Live</u> and <u>Geeks Classes Live USA</u>



Like 0

Previous

### RECOMMENDED ARTICLES

using Sieve of Eratosthenes

Sum of all Primes in a given range  $\bigcap \Box$ 

Segmented Sieve (Print Primes in a Range)

**Page: 1** 2

24, Nov 15

How is the time complexity of Sieve of Eratosthenes is n\*log(log(n))?

**n\*log(log(n))?** 15, Jan 20 O6 Sieve of Sundaram to print all primes smaller than n

12, Jan 16

O3 Sieve of Eratosthenes in O(n) time 07 complexity

22, Jan 17

17, Oct 18

Number of unmarked integers in a special sieve

29, May 18

**O4** Segmented Sieve

24, Nov 15

**Bitwise Sieve** 

26, Nov 17

# **Article Contributed By:**



# Vote for difficulty

Current difficulty: Medium



Easy Normal Medium Hard Expert

Improved By: Mithun Kumar, radhesh, shivamnayak, diwakarjaiswal880, vsasvipul,

siddhantj17, mrmgssingh, 29AjayKumar

Article Tags: GE, MAQ Software, number-theory, Prime Number, Qualcomm, sieve,

VMWare, Dynamic Programming, Mathematical

Practice Tags: VMWare, MAQ Software, Qualcomm, GE, number-theory,

Dynamic Programming, Mathematical, Prime Number, sieve

Improve Article

Report Issue

Writing code in comment? Please use ide.geeksforgeeks.org, generate link and share the link here.

**Load Comments** 



5th Floor, A-118, Sector-136, Noida, Uttar Pradesh - 201305

feedback@geeksforgeeks.org

Company	Learn
About Us	Algorithms
Careers	Data Structures
Privacy Policy	Languages
Contact Us	CS Subjects
Copyright Policy	Video Tutorials
Practice	Contribute

Courses Write an Article

Company-wise Write Interview Experience

Topic-wise Internships

How to begin? Videos

@geeksforgeeks , Some rights reserved