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Control Systems

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Abstract—This manual is an introduction to control systems based on GATE problems.Links to sample Python codes are available in the text.

1 STABILITY

1.1 Bode Plot

1.1. The asymptotic Bode magnitude plot of minimum phase transfer function G(s) is show below.

Consider the following two statements.

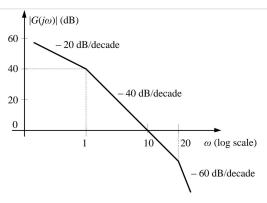


Fig. 1.1

Statement 1: Transfer function G(s) has 3 poles and one zero

Statement 2: At very high frequency

$$(\omega \to \infty)$$
, the phase angle $\angle G(j\omega) = -3\pi/2$

Which of the following is correct?

- (A) Statement 1 is true and Statement 2 is false.
- (B) Statement 1 is false and Statement 2 is true.
- (C) Both the statements are true.
- (D) Both the statements are false.

Solution:

Since, each pole corresponds to -20 dB/decade and each zero corresponds to +20 dB/decade. Therefore, from the given Bode plot we can get the Transfer equation,

$$G(s) = \frac{k}{s(1+s)(20+s)}$$
(1.1.1)

Now, from the Transfer equation we can conclude that, there are three poles (0, -1 and -20) and no zeros.

:. Statement 1 is false(1)

Calculating phase:

Since we know that,

phase ϕ is the sum of all the phases corresponding to each pole and zero. phase corresponding to pole is =

$$-tan^{-1}(\frac{imaginary}{real}) (1.1.2)$$

phase corresponding to zero is =

$$tan^{-1}(\frac{imaginary}{real})$$
 (1.1.3)

Now take,

$$s = j\omega \tag{1.1.4}$$

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$$\Rightarrow G(j\omega) = \frac{k}{j\omega(1+j\omega)(20+j\omega)}$$
 (1.1.5)

Therefore,

erefore,

$$\phi = -tan^{-1}(\frac{\omega}{0}) - tan^{-1}(\omega) - tan^{-1}(\frac{\omega}{20})$$
(1.1.6)

$$\phi = -90^{\circ} - tan^{-1}(\omega) - tan^{-1}(\frac{\omega}{20}) \qquad (1.1.7)$$

$$: \omega \to \infty \tag{1.1.8}$$

$$\phi = -90^{\circ} - 90^{\circ} - 90^{\circ} \tag{1.1.9}$$

$$\phi = -270^{\circ} \tag{1.1.10}$$

$$\phi = -3\pi/2 \tag{1.1.11}$$

:. Statement 2 is true(2) thus, from (1) and (2) option (B) is correct.

2 ROUTH HURWITZ CRITERION

- 3 Compensators
- 4 NYQUIST PLOT