

# Control Systems

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## CONTENTS

### 1 STABILITY

#### 1.1 Bode Plot

1.1. The asymptotic Bode magnitude plot of minimum phase transfer function  $G(s)$  is show below.

Consider the following two statements.

**Statement 1:** Transfer function  $G(s)$  has 3 poles and one zero

**Statement 2:** At very high frequency ( $\omega \rightarrow \infty$ ), the phase angle  $\angle G(j\omega) = -3\pi/2$

Which of the following is correct ?

- (A) Statement 1 is true and Statement 2 is false.
- (B) Statement 1 is false and Statement 2 is true.
- (C) Both the statements are true.
- (D) Both the statements are false.

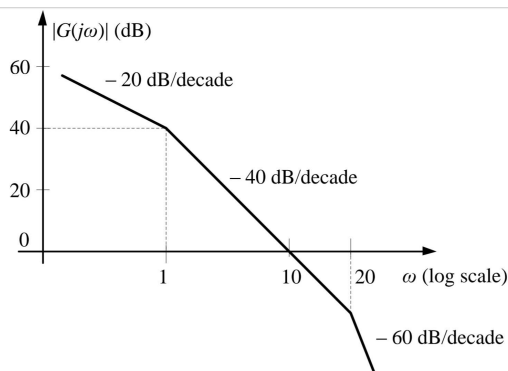


Fig. 1.1

#### Solution:

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Since, each pole corresponds to -20 dB/decade and each zero corresponds to +20 dB/decade. Therefore, from the given Bode plot we can get the Transfer equation,

$$G(s) = \frac{k}{s(1+s)(20+s)} \quad (1.1.1)$$

Now, from the Transfer equation we can conclude that, there are three poles (0, -1 and -20 ) and no zeros.

∴ Statement 1 is false .....(1)

Calculating phase

Since we know that,

phase  $\phi$  is the sum of all the phases corresponding to each pole and zero.

phase corresponding to pole is =

$$-\tan^{-1}\left(\frac{\text{imaginary}}{\text{real}}\right) \quad (1.1.2)$$

phase corresponding to zero is =

$$\tan^{-1}\left(\frac{\text{imaginary}}{\text{real}}\right) \quad (1.1.3)$$

Now take,

$$s = j\omega \quad (1.1.4)$$

$$\Rightarrow G(j\omega) = \frac{k}{j\omega(1+j\omega)(20+j\omega)} \quad (1.1.5)$$

Therefore,

$$\phi = -\tan^{-1}\left(\frac{\omega}{0}\right) - \tan^{-1}(\omega) - \tan^{-1}\left(\frac{\omega}{20}\right) \quad (1.1.6)$$

$$\phi = -90^\circ - \tan^{-1}(\omega) - \tan^{-1}\left(\frac{\omega}{20}\right) \quad (1.1.7)$$

$$\therefore \omega \rightarrow \infty \quad (1.1.8)$$

$$\phi = -90^\circ - 90^\circ - 90^\circ \quad (1.1.9)$$

$$\phi = -270^\circ \quad (1.1.10)$$

$$\phi = -3\pi/2 \quad (1.1.11)$$

∴ Statement 2 is true .....(2)

thus, from (1) and (2) option (B) is correct.

2 ROUTH HURWITZ CRITERION

3 COMPENSATORS

4 NYQUIST PLOT