

EE5609: Matrix Theory

Challenge Question

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Abstract—This document contains a proof for a theorem related to triangle. From the given,

Download the python codes from

<https://github.com/pranaya14014/EE5609/tree/master/Assignment3/code>

and latex-tikz codes from

<https://github.com/pranaya14014/EE5609/tree/master/Assignment3>

$$\|c\| (A - B)^T = \|a\| (A - C)^T \quad (2.0.6)$$

$$\|c\| (A^T - B^T) = \|a\| (A^T - C^T) \quad (2.0.7)$$

$$(\|c\| - \|a\|) A^T - \|c\| B^T + \|a\| C^T = 0 \quad (2.0.8)$$

As the A , B and C are points on the triangle and using the Linear independence in (2.0.8) we get,

$$\|c\| = \|a\| \quad (2.0.9)$$

Hence Proved

1 PROBLEM

Sides opposite to equal angles of a triangle are equal.

2 SOLUTION

Given: Consider a $\triangle ABC$ with sides AB , BC , AC . Let direction vectors of AB , BC and CA be $\mathbf{a} = (A - B)$, $\mathbf{b} = (B - C)$, and $\mathbf{c} = (A - C)$. Let $\angle ABC = \angle ACB = \theta$

Need to prove: $\|a\| = \|c\|$

Proof: Using cosine formula for $\angle ABC$,

$$\cos \theta = \frac{\mathbf{a}^T \mathbf{b}}{\|\mathbf{a}\| \|\mathbf{b}\|} \quad (2.0.1)$$

Using cosine formula for $\angle ACB$,

$$\cos \theta = \frac{\mathbf{c}^T \mathbf{b}}{\|\mathbf{b}\| \|\mathbf{c}\|} \quad (2.0.2)$$

From (2.0.1) and (2.0.2),

$$\frac{\mathbf{a}^T \mathbf{b}}{\|\mathbf{a}\| \|\mathbf{b}\|} = \frac{\mathbf{c}^T \mathbf{b}}{\|\mathbf{b}\| \|\mathbf{c}\|} \quad (2.0.3)$$

$$\frac{\mathbf{a}^T}{\|\mathbf{a}\|} = \frac{\mathbf{c}^T}{\|\mathbf{c}\|} \quad (2.0.4)$$

$$\|c\| \mathbf{a}^T = \|a\| \mathbf{c}^T \quad (2.0.5)$$

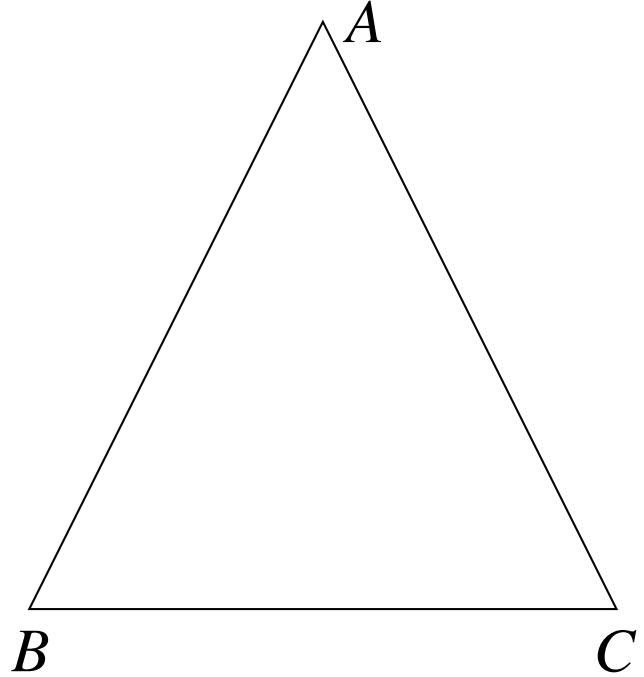


Fig. 0: Triangle