

# EE5609: Matrix Theory

## Assignment-11

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**Abstract**—This document has an example of finding the Transpose or adjoint  $T'$  of a linear operator  $T$  for a given function.

Download the latex-tikz codes from

<https://github.com/pranaya14014/EE5609/tree/master/Assignment12>

### 1 PROBLEM

Let,  $\mathbf{V}$  be the space of all  $n \times n$  matrices over a field  $\mathbf{F}$  and let  $\mathbf{B}$  be a fixed  $n \times n$  matrix. If  $T$  is the linear operator on  $\mathbf{V}$  defined by  $T(\mathbf{A}) = \mathbf{AB} - \mathbf{BA}$ , and if  $f$  is the trace function, what is  $T'f$ ?

### 2 SOLUTION

$$T'f(\mathbf{A}) = f(T(\mathbf{A})) \quad (2.0.1)$$

$$= f(\mathbf{AB} - \mathbf{BA}) \quad (2.0.2)$$

$$= \text{trace}(\mathbf{AB} - \mathbf{BA}) \quad (2.0.3)$$

using  $\text{trace}(\mathbf{AB}) = \text{trace}(\mathbf{BA})$  in (2.0.3),

$$T'f(\mathbf{A}) = \text{trace}(\mathbf{AB}) - \text{trace}(\mathbf{BA}) = 0 \quad (2.0.4)$$

Hence  $T'f = 0$