

# EE5609: Matrix Theory

## Assignment-8

Y.Pranaya  
AI20MTECH14014

**Abstract**—This document contains a proof to show that upper-triangular matrix is invertible if and only if diagonal elements are not 0.

Download the latex-tikz codes from

<https://github.com/pranaya14014/EE5609/tree/master/Assignment8>

### 1 PROBLEM

An  $n \times n$  matrix  $\mathbf{A}$  is called upper-triangular if  $\mathbf{A}_{ij} = 0$  for  $i > j$ , that is, if every entry below the main diagonal is 0. Prove that an upper-triangular (square) matrix is invertible if and only if every entry on its main diagonal is different from 0.

### 2 SOLUTION

Considering  $\mathbf{A}$ , an upper triangular matrix. Using the property that determinant of upper triangular matrix is the product of diagonal elements,

$$|\mathbf{A}| = \prod_{i=1}^n a_{i,i} \quad (2.0.1)$$

If  $\mathbf{A}$  be invertible then  $|\mathbf{A}| \neq 0$ . Hence from (2.0.1) we get,

$$\prod_{i=1}^n a_{i,i} \neq 0 \quad (2.0.2)$$

if any diagonal element is 0 then (2.0.2) won't be right hence no diagonal elements should be 0.  
Hence Proved.