

## ANGLE MODULATION

### Angle modulation

frequency modulation

phase modulation

$V_m \sin \omega t$

$V_m \rightarrow$  maximum voltage

$\omega \rightarrow$  angular frequency (radian)

$\phi = \omega t + \theta$

$\theta \rightarrow$  phase deviation

$$v_c = V_c \cos(\omega t + \theta)$$

### DIRECT FREQUENCY MODULATION

Varying the frequency of constant amplitude carrier directly proportional to amplitude of modulating signal at a rate equal to the frequency of modulating signal.

### DIRECT PHASE MODULATION

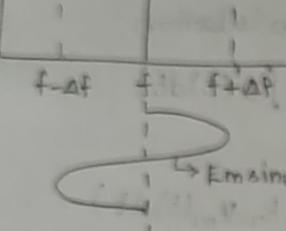
Varying the phase of constant amplitude carrier directly proportional to amplitude of modulating signal at a rate equal to the frequency of modulating signal.

$f_c$

$\frac{3}{3} / 2^3$

### INSTANTANEOUS PHASE DEVIATION: ( $\theta$ )

It is the instantaneous change in phase of carrier signal at a given instance of time and indicates how much the phase of carrier is changing with respect to the reference phase.



### INSTANTANEOUS PHASE ( $\omega t + \theta$ )

It is the precise phase of carrier at a given instance of time.

### INSTANTANEOUS FREQUENCY DEVIATION:

It is the instantaneous change in frequency of carrier and it is defined as first time derivative of instantaneous phase deviation. It is expressed as  $\theta'(t) \frac{d\theta}{dt}$ . The unit is radians per second.

### INSTANTANEOUS FREQUENCY:

It is the precise frequency of carrier at any instance of time and is defined as first time derivative of instantaneous phase. It is expressed as  $w_i(t) = w_c + \theta'(t) \frac{d}{dt} [\omega t + \theta(t)]$ . The unit is radians per second.

$$V_c \cos[\omega t + k V_m(t)] \quad \left. \begin{array}{l} \text{Modulated output of phase} \\ \text{Modulated output of frequency} \end{array} \right\}$$

$$V_c \cos[\omega t + k_1 \int V_m(t) dt]$$

The output equations are shown for carrier signal  $V_c \cos \omega t$  and modulating signal  $V_m(t)$ . If carrier signal is  $V_c \cos \omega t$  and modulating signal  $V_m \cos \omega m t$ , the the equations would be

$$V_c \cos[\omega t + k V_m \cos \omega m t]$$

$$V_c \cos[\omega t + k_1 \int V_m \cos \omega m t dt] \Rightarrow V_c \cos[\omega t + \frac{k V_m \sin \omega m t}{\omega m}]$$

Compare the above equation with  $V_c \cos(\omega t + \theta)$  base equation, Hence  $\frac{k V_m \sin \omega m t}{\omega m}$  is the phase deviation.

$$(k V_m \cos \omega m t) \cdot V_c \cos(\omega t + \theta)$$

$$(k V_m \sin \omega m t) \cdot V_c \cos(\omega t + \theta)$$

Writelab  
length

PROBLEMS:

- i) If the signal  $v(t) = 20 \sin(6.28 \times 10^6 t + 10 \sin 6.283 \times 10^9 t)$  represents a phase modulated signal, find i) carrier frequency ii) modulating frequency iii) modulation index iv) peak phase deviation.

Sol: i)  $\frac{6.283 \times 10^9}{2\pi}$  ii)  $\frac{6.28 \times 10^3}{2\pi}$  iii) 10 iv) 10

$$= \frac{6.282 \times 10^3 \times 10^3}{2\pi} \\ = 1 \text{ MHz.}$$

$$= \frac{6.28}{2\pi} \times 10^3 \\ = 1 \text{ kHz.}$$

Peak phase deviation = modulation index

The eqn is in the form of  $m(t) = V_c \sin(\omega_0 t + k_1 V_m \sin \theta)$   
where carrier frequency =  $\frac{\omega_0}{2\pi}$ ; modulating frequency =  $\frac{V_m}{2\pi}$

$$\text{Peak phase deviation } \Delta\theta = k_1 V_m \\ = 10 \text{ rad}$$

modulation index = 10

16/3/23 TUE DEVIATION SENSITIVITY:

$k \rightarrow$  sensitivity for Phase modulation;  $k_i \rightarrow$  sensitivity for Frequency modulation  
Output of PM =  $k_e V_m(t) \xrightarrow{\text{Input}} ①$  Output of FM =  $k_e V_m(t) \xrightarrow{\text{Input}} ②$   
We know that  $f = \frac{d\theta}{dt} \propto \theta'(t)$

$$\theta - \int f dt \Rightarrow \theta = \int \theta'(t) dt \rightarrow ③$$

Modulation output is given by the general equation:  $m(t) = V_c \cos(\omega_0 t + \theta)$   
For phase modulation:  $① \theta = k_e V_m(t)$

$$= V_c \cos(\omega_0 t + k_e V_m(t))$$

where  $V_c \rightarrow$  Amplitude of carrier signal

$\omega_0 \rightarrow$  Angular frequency of carrier

$k \rightarrow$  Modulating sensitivity of phase

$V_m(t) \rightarrow$  modulating signal

If input is  $V_m(t) = V_m \cos \omega_m t$

$$m(t) = V_c \cos(\omega_0 t + k_e V_m \cos \omega_m t) \rightarrow ④$$

Comparing ④ with general equation,

$$\theta = k_e V_m \cos \omega_m t$$

From this equation, peak phase deviation is given by,

$$\Delta\theta = k_e V_m$$

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Modulated wave

Deviation sensitivity

Deviation Modulating signal

Frequency modulation

$$m(t) = V_c \cos \left[ \omega_0 t + \frac{k_e V_m \sin(\omega_m t)}{f_m} \right]$$

$$m(t) = V_c \cos \left[ \omega_0 t + m \sin(\omega_m t) \right]$$

$$m(t) = V_c \cos \left[ \omega_0 t + \frac{\Delta f}{f_m} \sin(\omega_m t) \right]$$

$$k_e (\text{Hz/V})$$

$$\Delta f = k_e V_m (\text{Hz})$$

$$V_m(t) = V_m \sin(\omega_m t)$$

Phase modulation

$$m(t) = V_c \cos \left[ \omega_0 t + k_e V_m \cos(\omega_m t) \right]$$

$$m(t) = V_c \cos \left[ \omega_0 t + m \cos(\omega_m t) \right]$$

$$m(t) = V_c \cos \left[ \omega_0 t + \Delta\theta \cos(\omega_m t) \right]$$

$$k_e (\text{rad/V})$$

$$\Delta\theta = k_e V_m (\text{rad})$$

$$V_m(t) = V_m \cos(\omega_m t)$$

Modulation index

Frequency modulation

phase modulation

$$m = \frac{K_1 V_m}{f_m}$$

$$m = \frac{\Delta f}{f_m} \quad (\text{No unit})$$

$$m = k V_m \text{ (rad)}$$

$$m = \Delta \theta \text{ (rad)}$$

Modulating frequency

$$\omega_m = 2\pi f_m \text{ rad/s}$$

$$\omega_m = 2\pi f_m \text{ rad/s}$$

$$\frac{\omega_m}{2\pi} = f_m \approx \text{Hz}$$

$$\frac{\omega_m}{2\pi} = \delta_m \text{ (Hz)}$$

carrier signal

$$V_c \cos(\omega_c t)$$

$$V_c \cos(\omega_c t)$$

carrier frequency

$$\omega_c = 2\pi f_c \text{ (rad/s)}$$

$$\omega_c = 2\pi f_c \text{ (rad/s)}$$

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$$\frac{\omega_c}{2\pi} = f_c \text{ (Hz)}$$

$$\frac{\omega_c}{2\pi} = f_c \text{ (Hz)}$$

## FREQUENCY ANALYSIS / FREQUENCY SPECTRUM:

The modulated output for angle modulation is  $m(t) = V_c \cos[\omega_c t + m \cos \theta]$

According to Bessel function,  $\cos(\alpha + m \cos \beta) = \sum_{n=-\infty}^{\infty} J_n(m) \cos(\alpha + n\beta + n\pi/2) \rightarrow ②$   
where  $J_n(m)$  is called Bessel function.

Modifying ① according to Bessel function,  $\rightarrow$  RHS of ① and RHS of ② is same

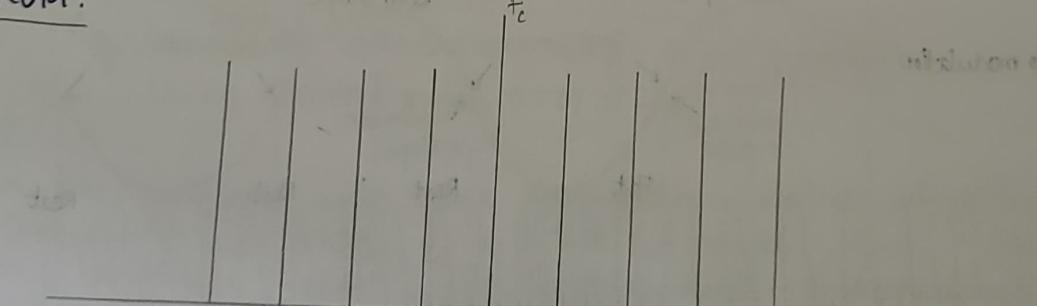
$$m(t) = \sum_{n=0}^{\infty} J_0(m) \cos(\omega_c t + n\omega_m t + 0) + \sum_{n=1}^{\infty} J_1(m) \cos(\omega_c t + n\omega_m t + \pi/2) + \dots$$

Bessel function:  $m(t) = \sum_{n=-\infty}^{\infty} J_n(m) \cos(\omega_c t + n\omega_m t + n\pi/2)$

$$J_{-1}(m) \leftarrow - (J_1(m)) \cos(\omega_c t - n\omega_m t - \pi/2), \dots$$

Final Equations:  $m(t) = J_0(m) \cdot V_c \cos \omega_c t + J_1(m) V_c \cos(\omega_c + \omega_m)t - J_1(m) \cos(\omega_c - \omega_m)t + J_2(m) V_c \cos(\omega_c + 2\omega_m)t - J_2(m) V_c \cos(\omega_c - 2\omega_m)t + \dots \infty$

SPECTRUM!



$$-f \dots f_c - 4f_m \quad f_c - 3f_m \quad f_c - 2f_m \quad f_c - f_m \quad f_c \quad f_c + f_m \quad f_c + 2f_m \quad f_c + 3f_m \quad f_c + 4f_m \dots f$$

The spectrum of angle modulation has multiple frequency components  $J_0(m), J_1(m), \dots$  are Bessel function values and these values will vary according to the value of  $m$ .

$J_0(m) \rightarrow$  Carrier frequency component;  $J_1(m) \rightarrow$  First set of side frequency

$J_2(m) \rightarrow$  Second set of side frequency.

PROBLEM:

1. Find carrier frequency, Modulating frequency, modulation index, maximum deviation for FM where  $E_{FM}(t) = 12 \sin [6 \times 10^8 t + 5 \sin(1250t)]$

$$f_c = \frac{6 \times 10^8}{2\pi} = \frac{6 \times 10^8 \times 10^6}{2\pi} = 95.5 \text{ MHz}$$

$$f_m = \frac{1250}{2\pi} = 198.94 \text{ Hz}$$

$$\text{Deviation} = \Delta f = k_i V_m$$

$$\text{Given: } \frac{k_i V_m}{f_m} = 5$$

$$\therefore \Delta f = 5 \times f_m = 5 \times 198.94 = 994.71 \text{ Hz.}$$

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MON

## FM & PM DEMODULATORS

$\Rightarrow$  PM modulator - differentiator followed by a FM modulator

$\Rightarrow$  PM demodulator - FM demodulator followed by an integrator.

$\Rightarrow$  FM modulator - Integrator followed by PM modulator

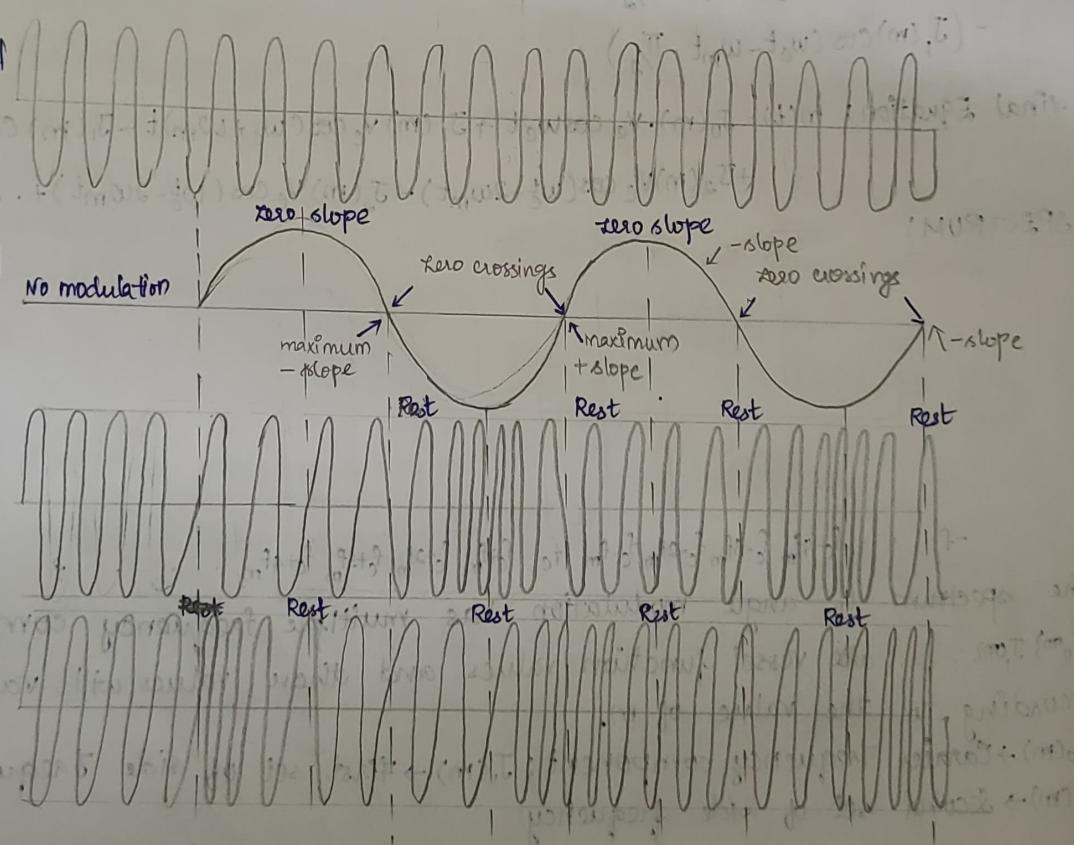
$\Rightarrow$  FM demodulator - PM demodulator followed by a differentiator

## PROBLEMS:

1. Draw FM & PM output waveforms with their input waveforms.
2. Calculate deviation ratio if maximum peak deviation is 5 kHz and modulating frequency is 2.5 kHz maximum.
3. For an FM modulator with modulation index  $m=1$ , modulating signal  $V_m(t) = V_m \sin(2\pi 1000t)$ . Then  $V_c(t) = 10 \sin(2\pi 500t)$ . Find i) No. of sets of side frequencies ii) Their amplitudes iii) Draw the frequency spectrum for the given signal.

1.

Unmodulated  
carrier  
signal



FM  
modulated  
wave

PM  
modulated  
wave

FM modulated signal  $\rightarrow$  High  $\Rightarrow$  Negative maximum input

Low  $\Rightarrow$  Positive maximum input

PM modulated signal  $\rightarrow$  High  $\Rightarrow$  Zero crossing with + slope

Low  $\Rightarrow$  Zero crossing with - slope.

$$2. \text{ Deviation ratio} = \frac{\Delta f}{f_m(\max)} = \frac{5}{2.5} = 2 \text{ (No unit)}$$

$$3. V_m(t) = V_m \sin 2\pi 1000t; V_c(t) = 10 \sin(2\pi 500t); m = 1$$

$$m(t) = J_0(m) V_c \cos(w_c t + n w_m t + n \frac{\pi}{2}) \Rightarrow \sum_{n=0}^3 J_n(m) V_c \cos(2\pi 500t + n 2\pi 1000t + n \frac{\pi}{2})$$

According to Bessel functions,

$$J_0 = 0.77; J_1 = 0.44; J_2 = 0.11; J_3 = 0.02.$$

$$m(t) = V_c [J_0(m) \cos(w_c t + J_1(m) \cos(w_c + w_m)t + J_2(m) \cos(w_c - w_m)t + J_3(m) \cos(w_c t + 2w_m t) - J_2(m) \cos(w_c t - 2w_m t) + J_3(m) \cos(w_c t + 3w_m t) - J_3(m) \cos(w_c t - 3w_m t)]$$

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TUE

### BESSEL FUNCTION TABLE:

$$J_n(m) = \left(\frac{m}{2}\right)^n \left[ 1 - \frac{(m/2)^2}{1!(n+1)} + \frac{(m/2)^4}{2!(n+2)!} + \dots \right]$$

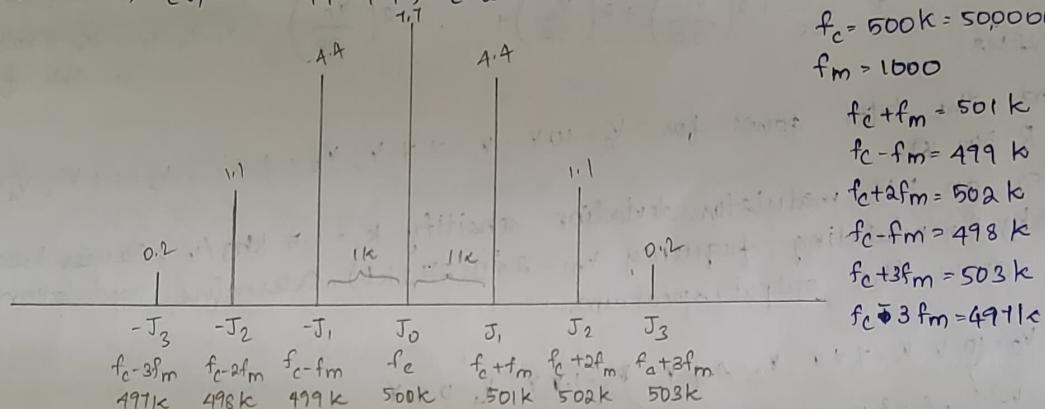
$$3. i) \text{ From bessel function table, } m=1; J_0 = 0.77; J_1 = 0.44; J_2 = 0.11; J_3 = 0.02$$

i). No. of sets of side frequencies = 3

ii) Amplitude of side frequencies =  $V_c J_n$

$$V_c J_0 = 10 \times 0.77 = 7.7 \text{ V}; V_c J_1 = 10 \times 0.44 = 4.4 \text{ V}; V_c J_2 = 10 \times 0.11 = 1.1 \text{ V}; V_c J_3 = 10 \times 0.02 = 0.2 \text{ V}$$

iii)



$$f_c = 500 \text{ kHz} = 500,000 \text{ Hz}$$

$$f_m = 1000 \text{ Hz}$$

$$f_c + f_m = 501 \text{ kHz}$$

$$f_c - f_m = 499 \text{ kHz}$$

$$f_c + 2f_m = 502 \text{ kHz}$$

$$f_c - 2f_m = 498 \text{ kHz}$$

$$f_c + 3f_m = 503 \text{ kHz}$$

$$f_c - 3f_m = 497 \text{ kHz}$$

### BANDWIDTH REQUIREMENT FOR ANGLE MODULATION:

For bandwidth calculation using bessel function,

$$BW = n \times 2f_m. \text{ Using Carson's rule, } B = 2(Af + f_m),$$

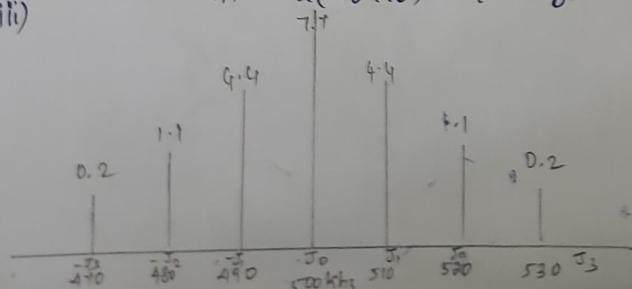
### PROBLEMS:

1. For an FM modulator with peak frequency deviation  $\Delta f = 10 \text{ kHz}$ , modulating signal frequency  $f_m = 10 \text{ kHz}$ ;  $V_c = 10 \text{ V}$  and  $f_c = 500 \text{ kHz}$ . Find i) Actual minimum bandwidth from bessel function table ii) Approximate bandwidth using Carson's rule. iii) Draw the spectrum of FM output.

Sol: i)  $BW = n \times 2f_m$

To find  $n$ ,  $m = \frac{\Delta f}{f_m} = \frac{10}{10} = 1 \therefore n = 3. BW = 3 \times 2 \times 10 = 60 \text{ kHz}$ .

ii)  $B = 2(Af + f_m) = 2(10 + 10) = 40 \text{ kHz}$ .



$$V_c J_0 = 10 \times 0.77 = 7.7 \text{ V}$$

$$V_c J_1 = 10 \times 0.44 = 4.4 \text{ V}$$

$$V_c J_2 = 10 \times 0.11 = 1.1 \text{ V}$$

$$V_c J_3 = 10 \times 0.02 = 0.2 \text{ V}$$

$$f_c = 500 \text{ kHz} f_m = 10 \text{ kHz}$$

$$f_c + f_m = 510 \text{ kHz}$$

$$f_c - f_m = 490 \text{ kHz}$$

$$f_c + 2f_m = 500 + 20 = 520 \text{ kHz}$$

$$f_c - 2f_m = 480 \text{ kHz}$$

$$f_c + 3f_m = 530 \text{ kHz}$$

$$f_c - 3f_m = 470 \text{ kHz}$$

23/3/23  
TYPERS OF FM:

Narrow band FM If modulation index  $m$  is less than 1, low index  
Wideband FM If modulation index  $m$  is between 1 and 10, medium index  
FM If modulation index  $m$  is greater than 10, high index

### POWER CALCULATION FOR PM & FM:

The output equation is given by  $m(t) = V_c \cos(\omega_c t + \theta)$   
From the above equation, average power can be calculated as  $P_t = \frac{m(t)^2}{R}$

$$P_t = \frac{V_c^2 \cos^2(\omega_c t + \theta(t))}{R} \quad \cos^2 \theta = \frac{1 + \cos 2\theta}{2}$$

$$P_t = \frac{V_c^2}{R} \left[ \frac{1 + \cos 2(\omega_c t + \theta(t))}{2} \right] \Rightarrow \frac{V_c^2}{2R} + \frac{V_c^2 \cos 2(\omega_c t + \theta(t))}{2R}$$

$$\text{Hence, } P_t = \frac{V_c^2}{2R}$$

Considering side frequencies, total power can be written as  $P_t = P_0 + P_1 + P_2 + \dots + P_n$   
where  $n$  = no. of side frequencies.

$$\therefore P_t = \frac{V_c^2}{2R} + 2\left(\frac{V_1^2}{2R}\right) + 2\left(\frac{V_2^2}{2R}\right) + \dots + 2\left(\frac{V_n^2}{2R}\right)$$

where  $V_c \rightarrow$  Carrier Voltage  
 $V_1, V_2, V_3, \dots, V_n \rightarrow$  voltage of side frequencies

### PROBLEMS:

- Find the total power for  $V_c = 10V$ ;  $V_1 = 7.7V$ ;  $V_2 = 4.4V$ ;  $V_3 = 1.1V$ ;  $V_4 = 0.2V$  and  $R = 500 \Omega$ .
- For an FM modulator, deviation sensitivity  $k_1 = 1.5 \text{ khz/V}$ ; carrier frequency = 500 khz; modulating frequency  $V_m = 2\sin(2\pi f_m t)$ . Determine modulation index and draw the output spectrum.

Sol:  $V_c = 10V$   $V_1 = 7.7V$   $V_2 = 4.4V$   $V_3 = 1.1V$   $V_4 = 0.2V$

$$P_t = \frac{V_c^2}{2R} + 2\left(\frac{V_1^2}{2R}\right) + 2\left(\frac{V_2^2}{2R}\right) + 2\left(\frac{V_3^2}{2R}\right) + 2\left(\frac{V_4^2}{2R}\right) \Rightarrow \frac{10^2}{2 \times 500} + 2\left(\frac{7.7^2}{2 \times 500}\right) + 2\left(\frac{4.4^2}{2 \times 500}\right) + 2\left(\frac{1.1^2}{2 \times 500}\right) + 2\left(\frac{0.2^2}{2 \times 500}\right)$$

$$= 0.1 + 0.11858 + 0.03872 + 0.00242 + 8 \times 10^{-5} = 0.2598 \text{ W}$$

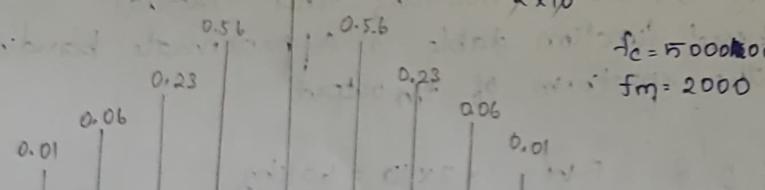
2.  $k_1 = 1.5 \text{ khz/V}$ ;  $f_c = 500 \text{ khz}$ ;  $V_m = 2\sin(2\pi f_m t)$ .

$$m = \frac{k_1 V_m}{f_m} = \frac{1.5 \times 2}{2 \times 10^3} = 0.0015 = \frac{1.5 \times 10^8 \times 2}{2 \times 10^3} = 1.5 \text{ khz}$$

when  $m = 1.5$ ,  $n = 4$

$$J_0 = 0.51 \quad J_1 = 0.56 \quad J_2 = 0.23$$

$$J_3 = 0.06 \quad J_4 = 0.01$$



$$492 \text{ khz} \quad 496 \text{ khz} \quad 498 \text{ khz} \quad 500 \text{ khz} \quad 502 \text{ khz} \quad 504 \text{ khz} \quad 506 \text{ khz} \quad 508 \text{ khz}$$

27/3/23

MORE

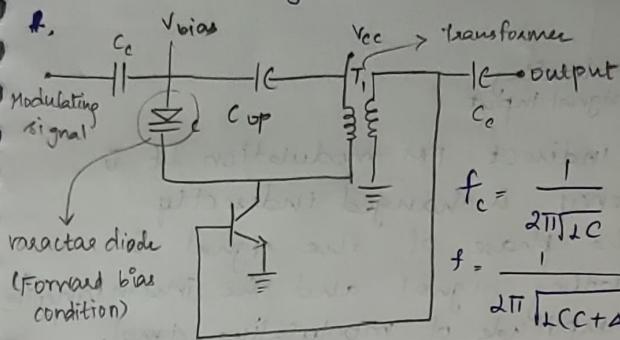
DIRECT FM MODULATORS:

There are <sup>LC</sup><sub>2</sub> common methods for producing direct FM modulation.

1. Varactor diode modulator
2. FM reactance modulator (JFET)
3. Linear integrated circuit direct FM modulator (Removes unwanted noise)

Varactor diode

$C_c$  → coupling capacitor  
(Removes unwanted noise)

PROBLEMS:

1. Determine the frequency of carrier signal and modulated output if  $L = 100 \text{ mH}$  &  $C = 1000 \text{ pF}$

$$f_c = \frac{1}{2\pi\sqrt{LC}}$$

$$\text{sol: } f_c = \frac{1}{2\pi\sqrt{LC}} = \frac{1}{2\pi\sqrt{316.22 \times 10^{-12}}} = \frac{1}{2\pi \times 316.22 \times 10^3} = 0.503 \text{ Hz}$$

$$f = \frac{1}{2\pi\sqrt{(LC+AC)}} = \frac{1}{2\pi\sqrt{100 \times 10^{-12} + 1000 \times 10^{-12}}} = 0.5001 \text{ Hz}$$

28/3/23  $Af = |f_c - f|$

TVF

In DC circuits      In AC circuits /

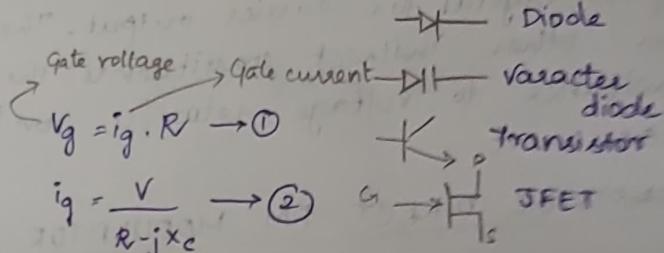
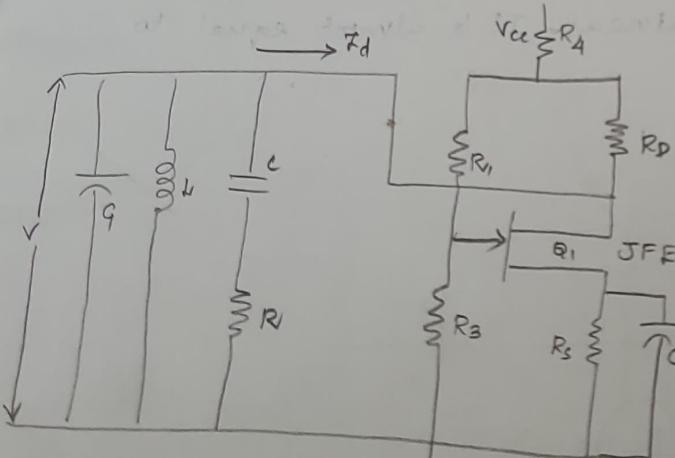
$$R = \frac{V}{I} \quad \text{Resists the flow of current}$$

$$Z = \frac{V}{I} \quad \text{Reactance}$$

Impedance

$R$  Resistance  
 $L$  Inductance  $\propto \omega$   
 $C$  capacitance  $\propto \frac{1}{\omega}$

JFET: Junction field effect transistor  
It is a type of transistor



Sub ② in ①

If Inductance,

$$R = R + jL$$

If Capacitance,

$$R = R - jXc$$

 $g_m \rightarrow \text{trans conductance} = \frac{1}{R}$ 

We know that  $i = \frac{V}{R} = V \left( \frac{1}{R} \right)$   $i_d = g_m V_g \rightarrow ④$

Sub ③ in ④

$$i_d = g_m \left( \frac{V}{R - jXc} \right) R \rightarrow ⑤$$

drain current

We need  $\text{drain impedance } Z_d = \frac{V}{i_d} \rightarrow ⑥$

$Z_d = \frac{V}{i_d} = \frac{R - jXc}{g_m}$

Rearranging ⑤

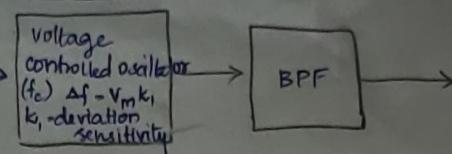
$$\frac{V}{i_d} = \frac{R - jXc}{R g_m}$$

$$\therefore Z_d = \frac{1}{g_m} \left( 1 - \frac{j}{2\pi f_m R} \right)$$

# 31/3/23 LINEAR INTEGRATED-CIRCUIT DIRECT FM MODULATORS:

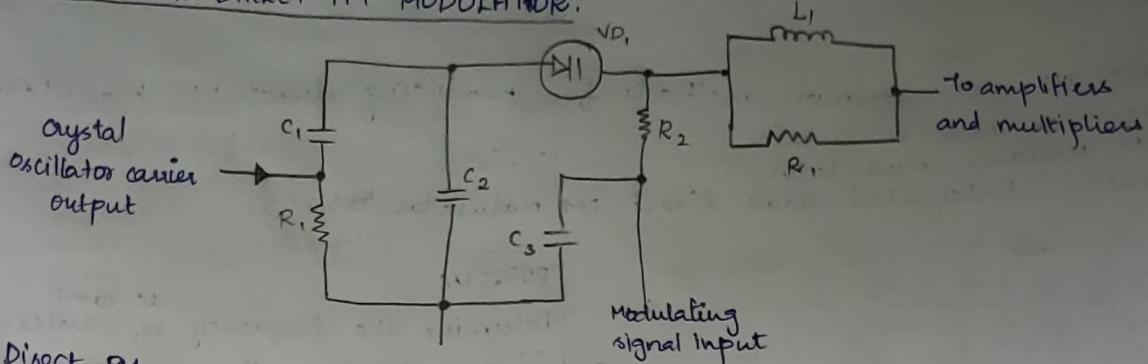
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$$V_m(t) = V_m \sin(2\pi f_m t)$$



$$\begin{aligned} \text{FM output} \\ f_o + \Delta f \\ m = \frac{\Delta f}{f_m} \\ \Delta \theta = m \end{aligned}$$

## VARACTOR DIODE DIRECT PM MODULATOR:

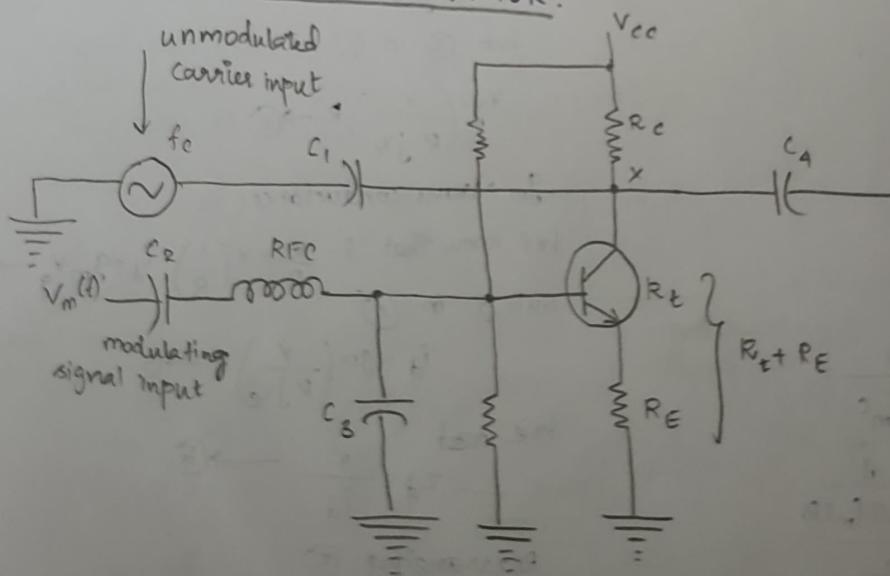


Direct PM modulation is also called indirect FM modulation. It is an angle modulation in which the frequency is changed indirectly corresponding to the modulating signal. The phase of the signal is directly changed with respect to modulating signal and the instantaneous phase is directly proportional to the amplitude of modulating signal.

The modulator circuit consists of a varactor diode combined in series with a inductor circuit (the induced coil  $L_1$ , resistor  $R_1$ ). The combined series-parallel resonance circuit appears in series with the output carrier signal of the crystal oscillator. The modulating signal input is connected to the varactor diode.

The advantage of direct PM modulator circuit is that it uses buffered crystal for easier output. The frequency is more stable than other indirect constituents. The disadvantage is that the capacitance to voltage ratio is non linear. It is almost equal to square root.

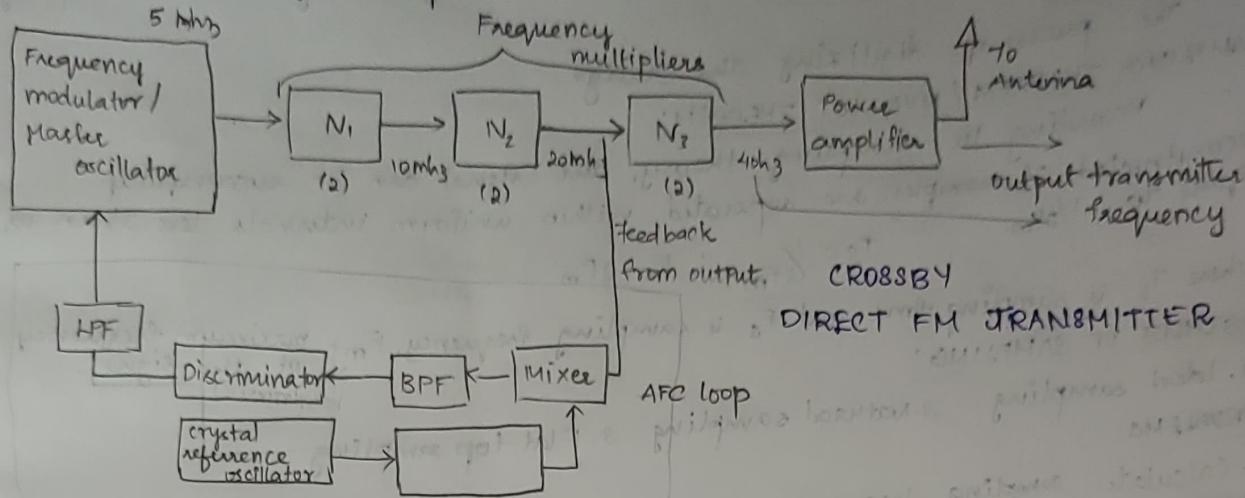
## TRANSISTOR DIRECT PM MODULATOR:



11/128 FM TRANSMITTER:

- Direct FM transmitter → Crosby direct FM transmitter
- Indirect FM transmitter → PLL/Phase lock loop direct FM transmitter
- ↳ Armstrong indirect FM transmitter

AFC - Auto frequency control ; LPF - Low pass filter ; BPF → Band pass filter  
 $N_1, N_2, N_3 \rightarrow$  frequency multipliers



### PROBLEMS:

1. For Crosby direct FM transmitter, frequency multiplication = 20 and transmit carrier frequency ( $f_c$ ) = 88.8 mhz. Determine i) Master oscillator carrier frequency ii) frequency deviation at the output of modulator if frequency deviation at antenna = 15 khz. iii) Deviation ratio at the output of modulator if  $f_m = 15$  khz. iv) Deviation ratio at the transmitter side.

Sol:  $f_c = 88.8$  mhz. multiplier = 20 (N)

$$i) f_c = \frac{88.8}{20} = 4.44 \times 10^6 \text{ khz. } ii) f_t = 15 \text{ khz } f_c = \frac{15}{20} = 3.75 \text{ khz. (frequency deviation)}$$

$$iii) \text{Deviation ratio} = \frac{\Delta f}{f_m} = \frac{3.75}{15} = 0.25 \quad iv) \text{Deviation ratio at modulator} = 0.25$$

Deviation ratio at transmitter =  $0.25 \times 20 = 5$

1. An angle modulated signal is described by  $x_c(t) = 10 \cos [2\pi(10^6)t + 0.1 \sin(10^3)\pi t]$  considering  $x_c(t)$  as PM signal with  $k_p = 10$ . Find  $m(t)$ . (Modulating signal).

$$\text{Sol: } v_m(t) = k_p v_m \cos(\omega_m t) \quad V_m = 0.1, \quad \omega_m = 10^3 \pi \quad m(t) = 10 \times 0.1 \cos(10^3 \pi t)$$

$$m(t) = \cos(10^3 \pi t)$$

2. Calculate the BW of FM signal whose frequency deviation is 75 khz and signal frequency is 2.5 khz.

$$\text{Sol: } \Delta f = 75 \text{ khz. } f_m = 2.5 \text{ khz. } \text{BW} = 2(\Delta f + f_m) = 2(75 + 2.5) = 77.5 = 155 \text{ khz.}$$

3. A 107.6 Mhz carrier is frequency modulated by a 7 khz sine wave. The resultant FM signal has a frequency deviation of 50 khz. Determine the modulation index of the FM wave.

$$\text{Sol: } f_c = 107.6 \text{ Mhz } f_m = 7 \text{ khz } \Delta f = 50 \text{ khz. } m = \frac{\Delta f}{f_m} = \frac{50}{7} = 7.142$$

10/9/23 MON

UNIT-3 DIGITAL MODULATION

11/12, 03, 04, (11/14/23)

ADVANTAGES OF DIGITAL COMMUNICATION:

1. Better noise immunity
2. flexible & adaptable
3. Multiplexing & processing becomes easier
4. Error correction & decoding becomes more effective

SAMPLING:

The process of measuring instantaneous value of continuous signal and making into discrete form. The process of digitalizing is called sampling.

QUANTIZATION:

The process of digitizing the range.

SAMPLING THEOREM / NYQUIST THEOREM:

According to sampling theory, the signal can be successfully reconstructed, if samples are separated within uniform intervals less than or equal to  $\frac{1}{2F_m}$ .

$$T_s \leq \frac{1}{2F_m} ; F_s = 2F_m \quad \text{Satisfying criteria}$$

where  $T_s$  is sampling time and  $F_s$  is sampling frequency,  $F_m$  - maximum frequency of the signal.

METHODS OF SAMPLING:

1. Ideal sampling
2. Natural sampling
3. Flat-top sampling

PROBLEMS:

1. Calculate sampling frequency & maximum frequency if samples are taken for every 3 milliseconds from the information signal of time period 15 ms.

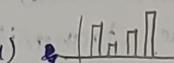
$$F_s = \frac{1}{T_s} \Rightarrow F_s = \frac{1}{3 \times 10^{-3}} = 0.333 \times 10^3 \quad F_m = \frac{1}{T} = \frac{1}{15 \times 10^{-3}} = 0.066 \text{ kHz}$$

$$= 0.333 \text{ kHz}$$

11/4/23 TUE

PULSE MODULATION TYPES:

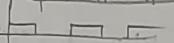
1. Pulse amplitude modulation (PAM)



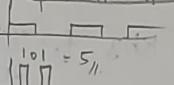
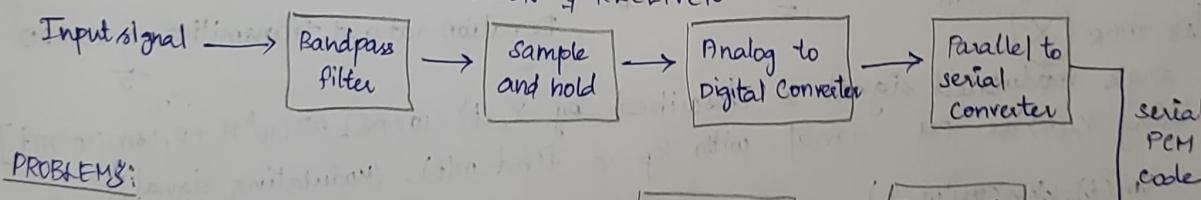
2. Pulse position modulation (PPM)



3. Pulse width modulation (PWM)



4. Pulse code modulation (PCM)

PULSE CODE MODULATION:PULSE CODE MODULATION: TRANSMITTER & RECEIVERPROBLEMS:

1. Calculate the line speed of PCM if sampling rate is 8 kHz and 8 bits are sampled for every sample.

$$\text{Line speed} = \text{sampling rate} \times \text{bits per sample}$$

$$= 8 \times 8 = 64 \text{ bits per second.}$$

