Linear Measurements vs Matrix-Vector Products

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- Trace can be computed exactly with ***one*** linear measurement

- Requires $\Omega(n)$ matrix-vector products for exact trace

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Upper Bounds