



Other Results

• **Theorem:** For  $0 < p < 2$ , can approximate  $F_p(x)$  up to  $1 \pm \varepsilon$  using **optimal**  $O(\varepsilon^{-2} \log n)$  bits of space and  $O(\log n)$  update time

- valid only for  $\varepsilon \leq 1/n^c$

- Improves on  $O(\log^2 n \log \log n)$  update time of [KNPW'11]

- **CountSketch:** Given  $t$  and  $r$ , a streaming algorithm which can compute  $\hat{x}[i]$  such that for  $\alpha \leq 1$



• Obtained by `derandminzing[MinandPrice'14]`



- The algorithm uses  $O(tr \log(n) + \log^2 n)$  bits of space

- $O(r \log n)$  update time

$$\Pr[|x[i] - \hat{x}[i]| \geq \frac{\alpha \|x\|_2}{\sqrt{t}}] \leq 2 \exp(-\alpha^2 r) + 1/\text{poly}(n)$$

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  - Valid only for  $\varepsilon < 1/n^c$
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- **CountSketch:** Given  $t$  and  $r$ , a streaming algorithm which can compute  $\hat{x}[i]$  such that for  $\alpha \leq 1$

$$\Pr[|x[i] - \hat{x}[i]| > \alpha \frac{\|x\|_2}{\sqrt{t}}] \leq 2 \exp(-\alpha^2 r) + 1/\text{poly}(n)$$

- Obtained by derandomizing [Minton and Price '14]
- The algorithm uses  $O(tr \log(n) + \log^2 n)$  bits of space
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# Other Applications of Sketching

- **Classic**

- Ridge Regression [KW, AISTATS '20], [KW, ICML '22]
- Dimensionality Reduction for Sum-of-Distances [FKW, ICML '21]
- Reduced Rank Regression [KW, COLT '21]
- Fast and Small Subspace Embeddings [CCKW, SODA '22]
- PolySketchFormer : Linear Time Transformers obtained via sketching Polynomial Kernels [KMZ, ICML '24]
- Lower Bounds for Adaptive Matrix Recovery [KW , NeurIPS '23]
- Fast algorithms for Schatten- $p$  Low Rank Approximation [KW, '24]