Linear Measurements vs Matrix-Vector Products

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- n linear measurements are **at least** as powerful as one matrix-vector product

- Trace can be computed exactly with ***one*** linear measurement

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Upper Bounds