Unit-1

Binary Systems

<u>Digital System</u>

- It is a system that manipulates (processes) discrete elements of information.

- A digital system is a discrete information processing system.

- For e.g. calculator, digital voltmeters, general purpose computer etc.

- In such systems, all quantities are represented using two values i.e. 0 and 1.

<u>Analog System</u>

- It is a system that manipulate physical quantities that are represented in analog form i.e continuous range of values.

- For e.g. voltmeter, speedometer, analog thermometer etc.

Block Diagram of Digital Computer

A digital computer is a programmable machine which read the binary instruction and processes the data which are presented in binary form.

The digital computer takes the binary data at input, processes according to the set of instructions called program and produces the digital output.

Working principles of digital computer:

1. Memory unit stores programs as well as input, output and intermediate data.
2. The control unit supervises the flow of information between various units and retrieve the instructions stored in memory unit.
3. After getting control signal memory unit sends the data to the processor.
4. For each instruction control unit informs the processor to execute the operation according to the instruction.
5. After getting control signal processor sends the process information to memory unit and memory unit sends those information to the output unit.

Advantages of digital system

- In case of digital system large number of ICs are available for performing various operations hence digital systems are highly reliable, accurate, small in size and speed of operation is very high.

- Computer controls digital system can be controlled by software that allows new function to be added without changing hardware.

- Less expensive

- Easy to manipulate

Disadvantages of digital system

- It is difficult to install digital system because it required many more complex electronic circuits and ICs.

- In digital systems, if a single piece of data lost, large blocks of related data can completely change.

Number System

In general, in any number system there is an ordered set of symbols known as digits with rules defined for performing arithmetic operations like addition, multiplication etc. A collection of these digits makes a number in general has two parts- integer and fractional. Set apart by a radix point (.).

- There are mainly four number system which are used in digital electronics platform.

1. Decimal number system:

- The decimal number system contains ten unique digits from 0 to 9.

- The base or radix is 10.

2. Binary number system:

- The binary number system contains two unique digits 0 and 1.

- The base or radix is 2.

3. Octal number system:

- The octal number system contains eight unique digits from 0 to 7.

- The base or radix is 8.

4. Hexadecimal number system:

- The hexadecimal number system contains sixteen unique digits: 0 to 9 and six letters A, B, C, D, E and F.

- The base or radix is 16.

1. Convert decimal fraction to binary number

Most Significant Bit (MSB)			Decimal Point			Least Significant Bit (LSB)
10^2	10^1	10^0		10^{-1}	10^{-2}	10^{-3}
100	10	1	.	0.1	0.01	0.001

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Let's take an example for n = 4.47 , k = 3
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Step 1: Conversion of 4 to binary

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1. 4/2 : Remainder = 0 : Quotient = 2
2. 2/2 : Remainder = 0 : Quotient = 1
3. 1/2 : Remainder = 1 : Quotient = 0
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So equivalent binary of integral part of decimal is 100.

Step 2: Conversion of .47 to binary

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1. 0.47 * 2 = 0.94, Integral part: 0
2. 0.94 * 2 = 1.88, Integral part: 1
3. 0.88 * 2 = 1.76, Integral part: 1
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So equivalent binary of fractional part of decimal is .011

Step 3: Combined the result of step 1 and 2.

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Final answer can be written as:
100 + .011 = 100.011
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Example-2: The number 2020.50 is interpreted as:-

$= (2020.50)_{10}$
$= (1024 + 512 + 256 + 128 + 64 + 32 + 4 + (1/2))_{10}$
$= (2^{10}x1+2^{9}x1+2^{8}x1+2^{7}x1+2^{6}x1+2^{5}x1+2^{4}x0+2^{3}x0+2^{2}x1+2^{1}x0+2^{0}x0+2^{-1}x1)_{10}$
$= (11111100100.1)_2$

2. Convert binary fraction to decimal number

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Let's take an example for n = 110.101
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Step 1: Conversion of 110 to decimal
=> 110₂ = (1*2²) + (1*2¹) + (0*2⁰)
=> 110₂ = 4 + 2 + 0
=> 110₂ = 6
So equivalent decimal of binary integral is 6.

Step 2: Conversion of .101 to decimal
=> 0.101₂ = (1*1/2) + (0*1/2²) + (1*1/2³)
=> 0.101₂ = 1*0.5 + 0*0.25 + 1*0.125
=> 0.101₂ = 0.625
So equivalent decimal of binary fractional is 0.625

Step 3: Add result of step 1 and 2.
=> 6 + 0.625 = 6.625
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Convert a negative decimal into a binary

Consider you have to represent -23

23= 0001 0111

To represent it we have 3 ways you can use any but compliment representation is generally preferred

1. 1001 0111 signed magnitude representation 1st bit 1 means negative 0 for positive
2. 1110 1000 1's compliment representation
3. 1110 1001 2's compliment representation

Convert a negative binary into a decimal

If it is positive, simply convert it to decimal. If it is negative, make it positive by inverting the bits and adding one. Then, convert the result to decimal. The negative of this number is the value of the original binary.

- Interpret 11011011 as a two's complement binary number, and give its decimal equivalent.
    1. First, note that the number is negative, since it starts with a 1.
    2. Change the sign to get the magnitude of the number.

$$\begin{array}{ccccccccc} & 1 & 1 & 0 & 1 & 1 & 0 & 1 & 1 \\ \neg & 0 & 0 & 1 & 0 & 0 & 1 & 0 & 0 \\ + & & & & & & & & 1 \\ \hline & 0 & 0 & 1 & 0 & 0 & 1 & 0 & 1 \end{array}$$

3. Convert the magnitude to decimal: $00100101_2 = 25_{16} = 2 \times 16 + 5 = 37_{10}$.
4. Since the original number was negative, the final result is -37.

Complements

Complements are used in digital computers for simplifying the subtraction operation and for logical manipulations.

There are two types of complements for each base-r system:

a) The r's complement and

b) The $(r-1)$'s complement.

□ r's complement is known as 10's complement in base 10 and 2's complement in base 2.

□ $(r-1)$'s complement is known as 9's complement in base 10 and 1's complement in base 2.

- ***r*'*s*** complement

Given a positive number N in base r with an integer part of n digits, the r's complement of N is defined as

The r's complement of $N = \begin{cases} r^n - N, \text{if } N \neq 0 \\ 0, \text{if } N = 0 \end{cases}$

E.g.

10's complement of 52520 = 105-52520 = 47480

10's complement of 0.3267 = 100-0.3267 = 0.6733

10's complement of 25.639 = 102-25.639 = 74.361

2's complement of $(101100)_2 = (26)_{10}-(101100)_2 = (1000000-101100)_2 = 010100$

2's complement of $(0.0110)_2 = (20)_{10}-0.0110 = 0.1010$

- $(\boldsymbol{r} - \mathbf{1})$'$\boldsymbol{s}$ complement Given a positive number N in base r with an integer part of n digits and a fractional part of m digits, the $(r - 1)$'s complement of N is defined as: The $(r - 1)$'s complement of $N = r^{n} - r^{-m} - N$

E.g.
9's complement of (52520)10 = (105 -100 -52520) = 47479

9's complement of (0.3267)10 is (100 -10-4 -0.3267) = 0.6732

9's complement of (25.693)10 is (102 -10-3 -25.693) = 74.306

1's complement of (101100)2 is (26 -2 0)10-(101100)2 = 111111-101100 = 010011

1's complement of (0.0110)2 is (1-2 -4)10-(0.0110)2 = 0.1001

Subtraction with Complements

 Subtraction with r's Complements
Subtraction of two positive numbers $(M - N)$, both of base r, may be done as follows:
Step-1: Add the minuend M to the r's complement of subtrahend N.
Step-2: Inspect the result obtained in step 1 for an end carry:
(a) If an end carry occurs, discard it.
(b) If an end carry does not occur, take the r's complement of the number obtained in step 1 and place a negative sign in front.

 Subtraction with (r-1)'s Complements

The subtraction of $M - N$, both positive number in base r, may be calculated in the following manner:
Step-1: Add the minuend M to the $(r - 1)$'s complement of the subtrahend N.
Step-2: Inspect the result obtained in step 1 for an end carry.
(a) If an end carry occurs, add 1 to the list significant digit (end-round carry)
(b) If an end carry does not occurs, take the $(r - 1)$'s complement of the number obtained in step 1 and place a negative sign in front.

Binary Codes

When numbers, letters or words are represented by a special group of binary symbols/combinations, we say that they are being encoded and the group of symbols is called a code. Some familiar binary codes are: Decimal Codes, Error-detection Codes, The Reflected Code, Alphanumeric Codes etc.

Decimal Codes

The representation of decimal digits by binary combinations is known as decimal codes. Binary codes from decimal digits require minimum of four bits. Numerous different codes can be obtained by arranging four or more bits in ten distinct possible combinations. Some decimal codes are-

- BCD
- Excess-3

 Binary-Coded-Decimal (BCD) Code

If each digit of a decimal number is represented by its binary equivalent, the result is a code called binary coded decimal (BCD). It is possible to assign weights to the binary bits according to their positions. The weights in the BCD code are 8,4,2,1.

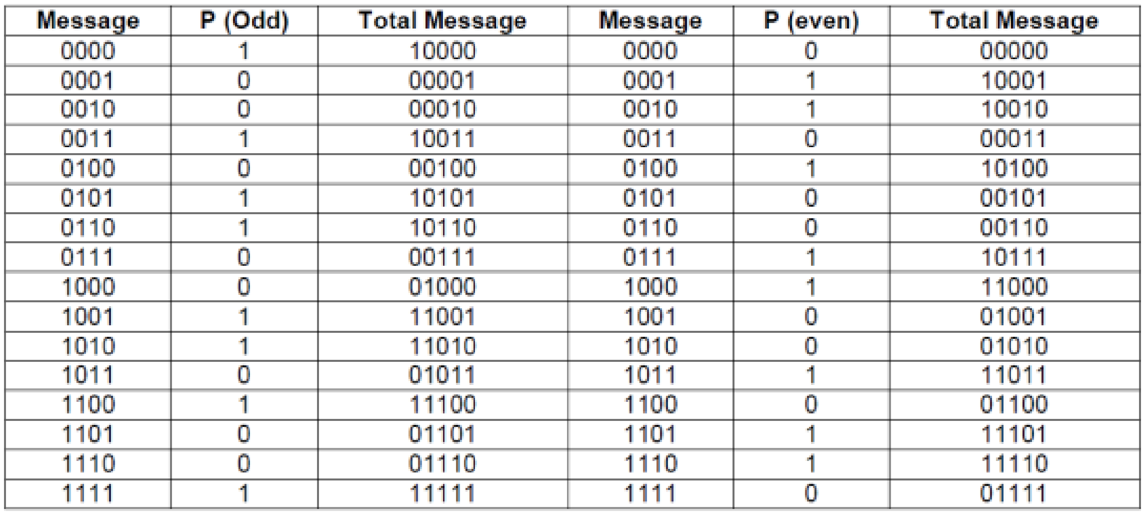
 Excess-3 Code (XS-3)

This is an unweighted code. Its code assignment is obtained from the corresponding value of BCD after the addition of 3.

Decimal	BCD 8 4 2 1	Excess-3 BCD + 0011
0	0 0 0 0	0 0 1 1
1	0 0 0 1	0 1 0 0
2	0 0 1 0	0 1 0 1
3	0 0 1 1	0 1 1 0
4	0 1 0 0	0 1 1 1
5	0 1 0 1	1 0 0 0
6	0 1 1 0	1 0 0 1
7	0 1 1 1	1 0 1 0
8	1 0 0 0	1 0 1 1
9	1 0 0 1	1 1 0 0

Error-detection Codes

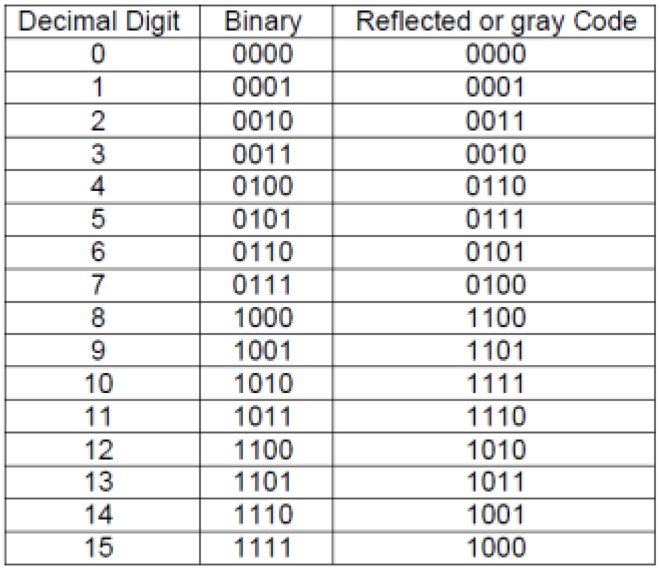
- An error detection codes can be used to detect errors during transmission. A parity bit is an extra bit included with a message to make the total number of 1’s either odd or even.
- For a message of four bits parity (P) is chosen so that the sum of all 1’s is odd (in all five bits) or the sum of all 1’s is even. In the receiving end, all the incoming bits (in this case five) are applied to a “parity-check” network for checking.
- An error is detected if the check parity does not correspond to the adopted one. The parity method detects the presence of one, three or any odd combination of errors. An even combination of errors is undetectable. Additional error-detection schemes may be needed to take care of an even combination of errors.



Message	P (Odd)	Total Message	Message	P (even)	Total Message
0000	1	10000	0000	0	00000
0001	0	00001	0001	1	10001
0010	0	00010	0010	1	10010
0011	1	10011	0011	0	00011
0100	0	00100	0100	1	10100
0101	1	10101	0101	0	00101
0110	1	10110	0110	0	00110
0111	0	00111	0111	1	10111
1000	0	01000	1000	1	11000
1001	1	11001	1001	0	01001
1010	1	11010	1010	0	01010
1011	0	01011	1011	1	11011
1100	1	11100	1100	0	01100
1101	0	01101	1101	1	11101
1110	0	01110	1110	1	11110
1111	1	11111	1111	0	01111

The Reflected Code/Gray Code

- The Reflected code, also called Gray code is unweighted and is not an arithmetic code; that is, there are no specific weights assigned to the bit positions.
- It is a binary numeral system where two successive values differ in only one bit (binary digit).
- For instance, in going from decimal 3 to decimal 4, the Gray code changes from 0010 to 0110, while the binary code changes from 0011 to 0100, a change of three bits. The only bit change is in the third bit from the right in the Gray code; the others remain the same.



Decimal Digit	Binary	Reflected or gray Code
0	0000	0000
1	0001	0001
2	0010	0011
3	0011	0010
4	0100	0110
5	0101	0111
6	0110	0101
7	0111	0100
8	1000	1100
9	1001	1101
10	1010	1111
11	1011	1110
12	1100	1010
13	1101	1011
14	1110	1001
15	1111	1000

Alphanumeric Code

- In order to communicate, we need not only numbers, but also letters and other symbols. In the strictest sense, alphanumeric codes are codes that represent numbers and alphabetic characters (letters). Most such codes, however, also represent other characters such as

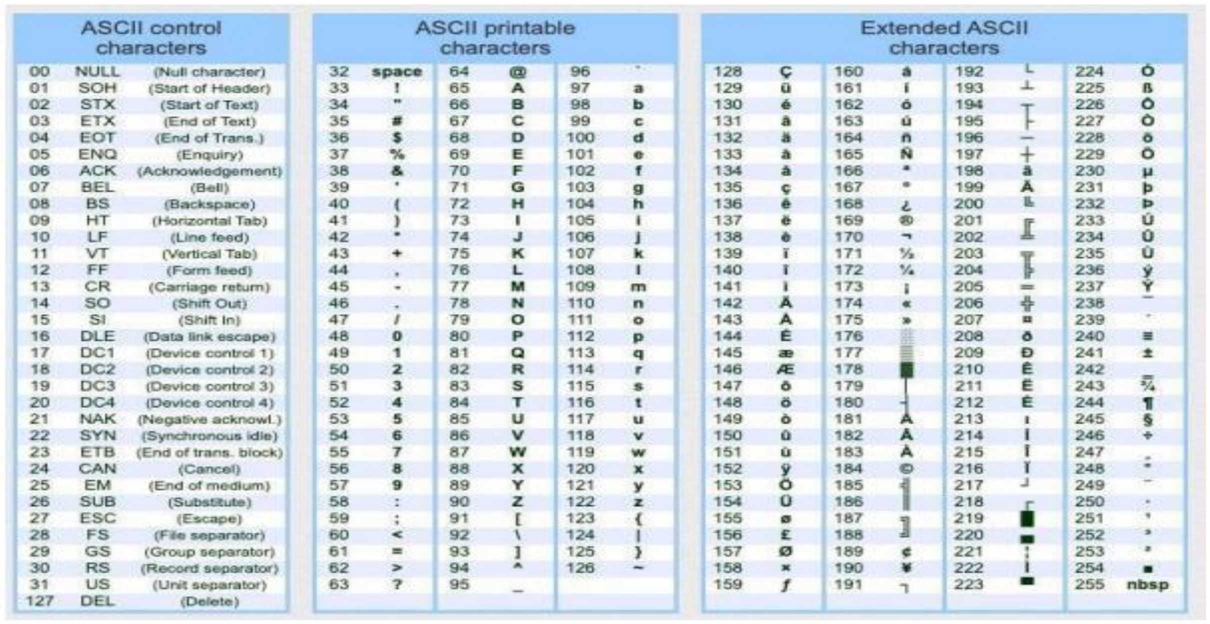
symbols and various instructions necessary for conveying information.
- The ASCII is the most common alphanumeric code.

ASCII Code

ASCII is the abbreviation for American Standard Code for Information Interchange.
ASCII is a universally accepted alphanumeric code used in most computers and other electronic equipment. Most computer keyboards are standardized with the ASCII. When we enter a letter, a number, or control command, the corresponding ASCII code goes into the computer.
- ASCII has 128 characters and symbols represented by a 7-bit binary code. Actually, ASCII can be considered an 8-bit code with the MSB always 0. This 8-bit code is 00 through 7F in hexadecimal.
- The first thirty-two ASCII characters are non-graphic commands that are never printed or displayed and are used only for control purposes. Examples of the control characters are ""null," "line feed," "start of text," and "escape."
- The other characters are graphic symbols that can be printed or displayed and include the letters of the alphabet (lowercase and uppercase), the ten decimal digits, punctuation signs and other commonly used symbols.

Extended ASCII characters

In addition to the 128 standard ASCII characters, there are an additional 128 characters that were adopted by IBM for use in their PCs (personal computers). Because of the popularity of the PC, these particular extended ASCII characters are also used in applications other than PCs and have become essentially an unofficial standard. The extended ASCII characters are represented by an 8-bit code series from hexadecimal 80 to hexadecimal FF.



ASCII control characters		
00	NULL	(Null character)
01	SOH	(Start of Header)
02	STX	(Start of Text)
03	ETX	(End of Text)
04	EOT	(End of Trans.)
05	ENQ	(Enquiry)
06	ACK	(Acknowledgement)
07	BEL	(Bell)
08	BS	(Backspace)
09	HT	(Horizontal Tab)
10	LF	(Line feed)
11	VT	(Vertical Tab)
12	FF	(Form feed)
13	CR	(Carriage return)
14	SO	(Shift Out)
15	SI	(Shift In)
16	DLE	(Data link escape)
17	DC1	(Device control 1)
18	DC2	(Device control 2)
19	DC3	(Device control 3)
20	DC4	(Device control 4)
21	NAK	(Negative acknowl.)
22	SYN	(Synchronous idle)
23	ETB	(End of trans. block)
24	CAN	(Cancel)
25	EM	(End of medium)
26	SUB	(Substitute)
27	ESC	(Escape)
28	FS	(File separator)
29	GS	(Group separator)
30	RS	(Record separator)
31	US	(Unit separator)
127	DEL	(Delete)

ASCII printable characters					
32	space	64	@	96	`
33	!	65	A	97	a
34	"	66	B	98	b
35	#	67	C	99	c
36	$	68	D	100	d
37	%	69	E	101	e
38	&	70	F	102	f
39	'	71	G	103	g
40	(	72	H	104	h
41	)	73	I	105	i
42	*	74	J	106	j
43	+	75	K	107	k
44	,	76	L	108	l
45	-	77	M	109	m
46	.	78	N	110	n
47	/	79	O	111	o
48	0	80	P	112	p
49	1	81	Q	113	q
50	2	82	R	114	r
51	3	83	S	115	s
52	4	84	T	116	t
53	5	85	U	117	u
54	6	86	V	118	v
55	7	87	W	119	w
56	8	88	X	120	x
57	9	89	Y	121	y
58	:	90	Z	122	z
59	;	91	[	123	{
60	<	92	\	124	|
61	=	93	]	125	}
62	>	94	^	126	~
63	?	95	_		

Extended ASCII characters							
128	Ç	160	á	192	└	224	Ó
129	ü	161	í	193	┴	225	ß
130	é	162	ó	194	┬	226	Ô
131	â	163	ú	195	├	227	Ò
132	ä	164	ñ	196	─	228	õ
133	à	165	Ñ	197	┼	229	Õ
134	å	166	ª	198	ã	230	µ
135	ç	167	º	199	Ã	231	þ
136	ê	168	¿	200	╚	232	Þ
137	ë	169	®	201	╔	233	Ú
138	è	170	¬	202	╩	234	Û
139	ï	171	½	203	╦	235	Ù
140	î	172	¼	204	╠	236	ý
141	ì	173	¡	205	═	237	Ý
142	Ä	174	«	206	╬	238	¯
143	Å	175	»	207	¤	239	´
144	É	176	░	208	ð	240	≡
145	æ	177	▒	209	Ð	241	±
146	Æ	178	▓	210	Ê	242	‗
147	ô	179	│	211	Ë	243	¾
148	ö	180	┤	212	È	244	¶
149	ò	181	Á	213	ı	245	§
150	û	182	Â	214	Í	246	÷
151	ù	183	À	215	Î	247	¸
152	ÿ	184	©	216	Ï	248	°
153	Ö	185	╣	217	┘	249	¨
154	Ü	186	║	218	┌	250	·
155	ø	187	╗	219	█	251	¹
156	£	188	╝	220	▄	252	³
157	Ø	189	¢	221	¦	253	²
158	×	190	¥	222	Ì	254	■
159	ƒ	191	┐	223	▀	255	nbsp