

Data Structures & Algorithms

PRAWIT

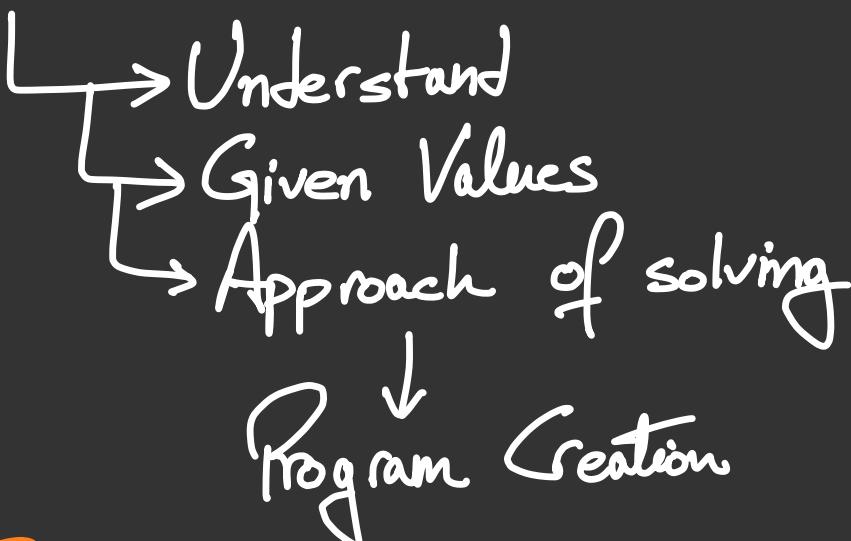
Modi



Data Structures & Algorithms

⇒ Problem Solving

Problem



Problem → Solution

Rough Soln → flowchart / pseudocode



Code

Program in High Level Language / src code



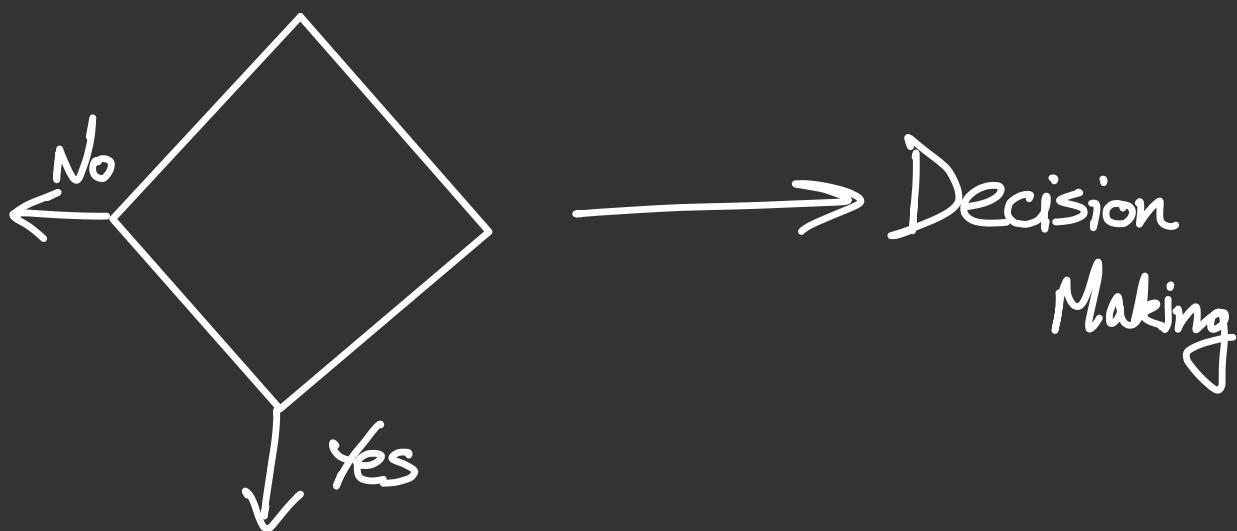
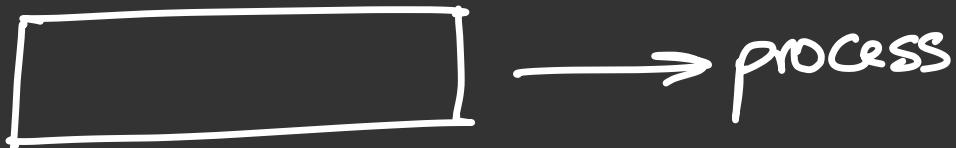
Convert

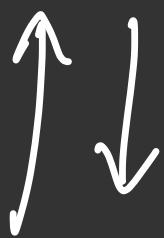
Machine Understandable format

Flowchart

↳ diagrammatic representation of an approach

Components of flowchart





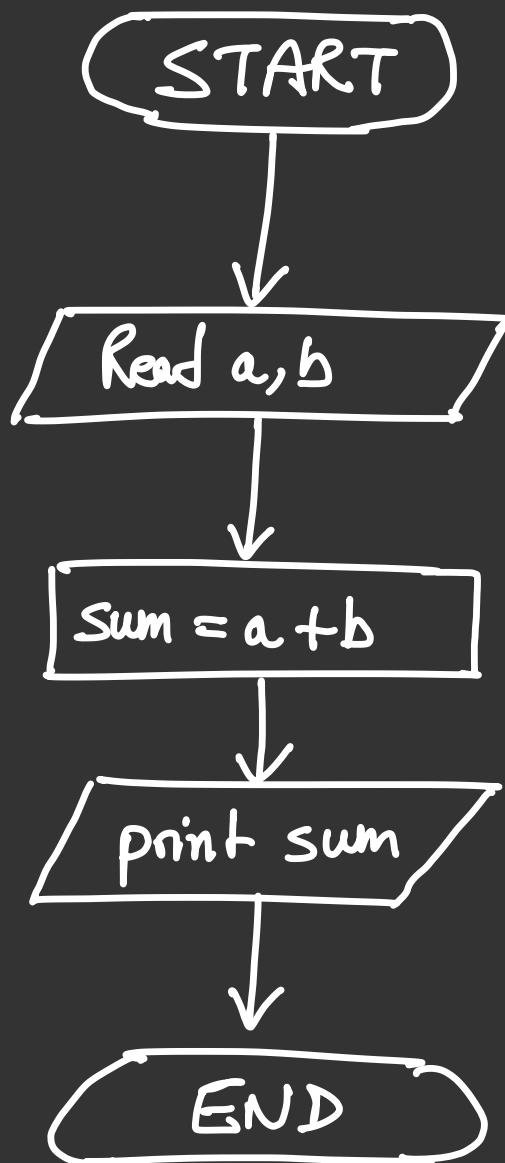
— Arrows

(to showcase the flow and connect components)



→ Connector

eg: Sum of two numbers
given a, b



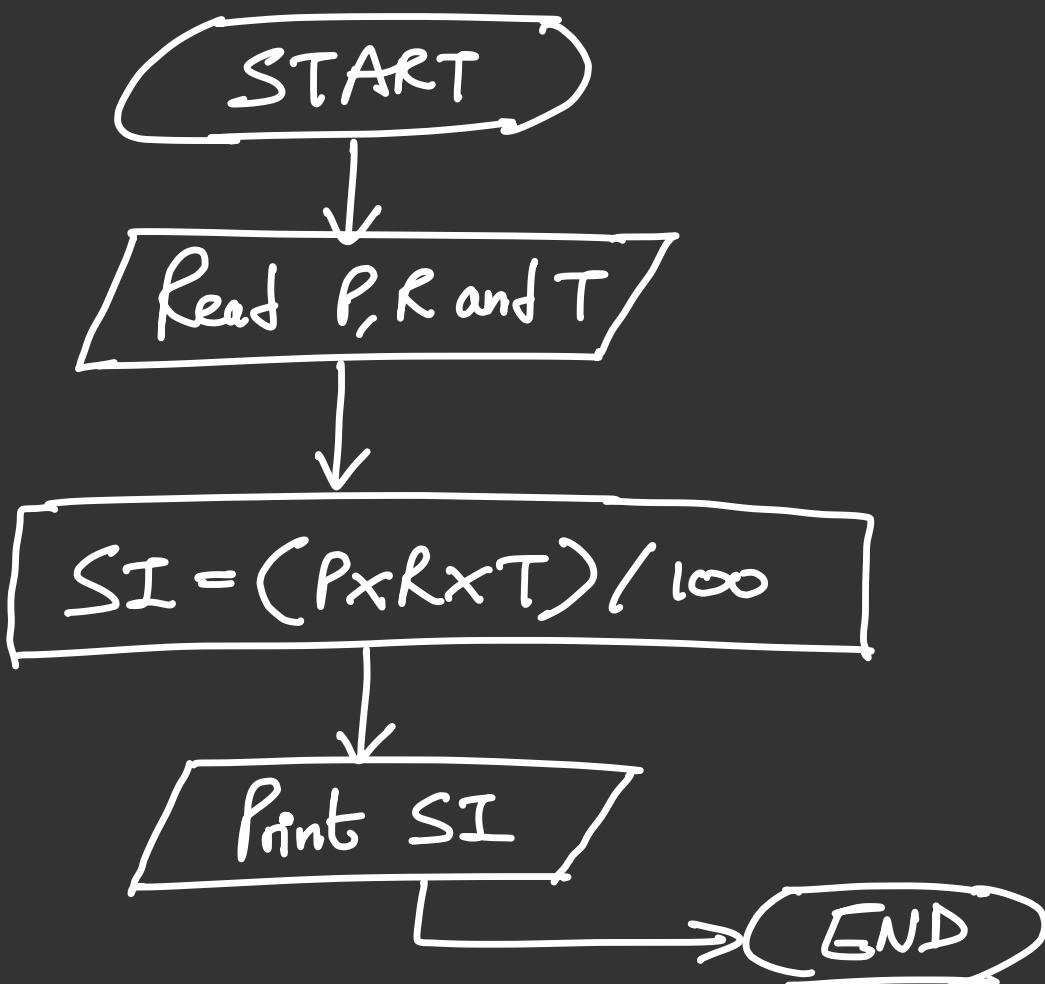
Pseudo Code

↳ way of representing logic
↳ generic irrespective of programming language

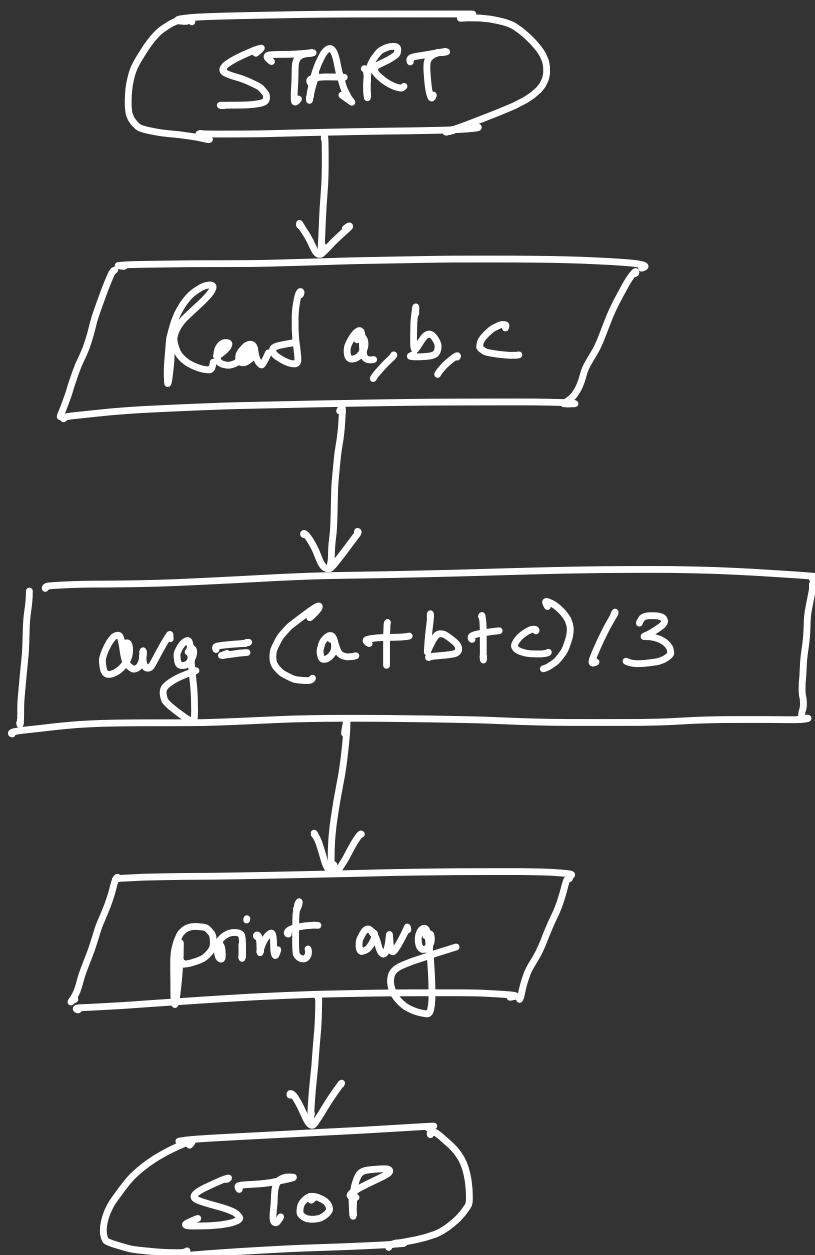
eg: Sum of two numbers

- ① Read a, b
- ② sum = a + b
- ③ print sum

Question : Flow chart for Simple Interest

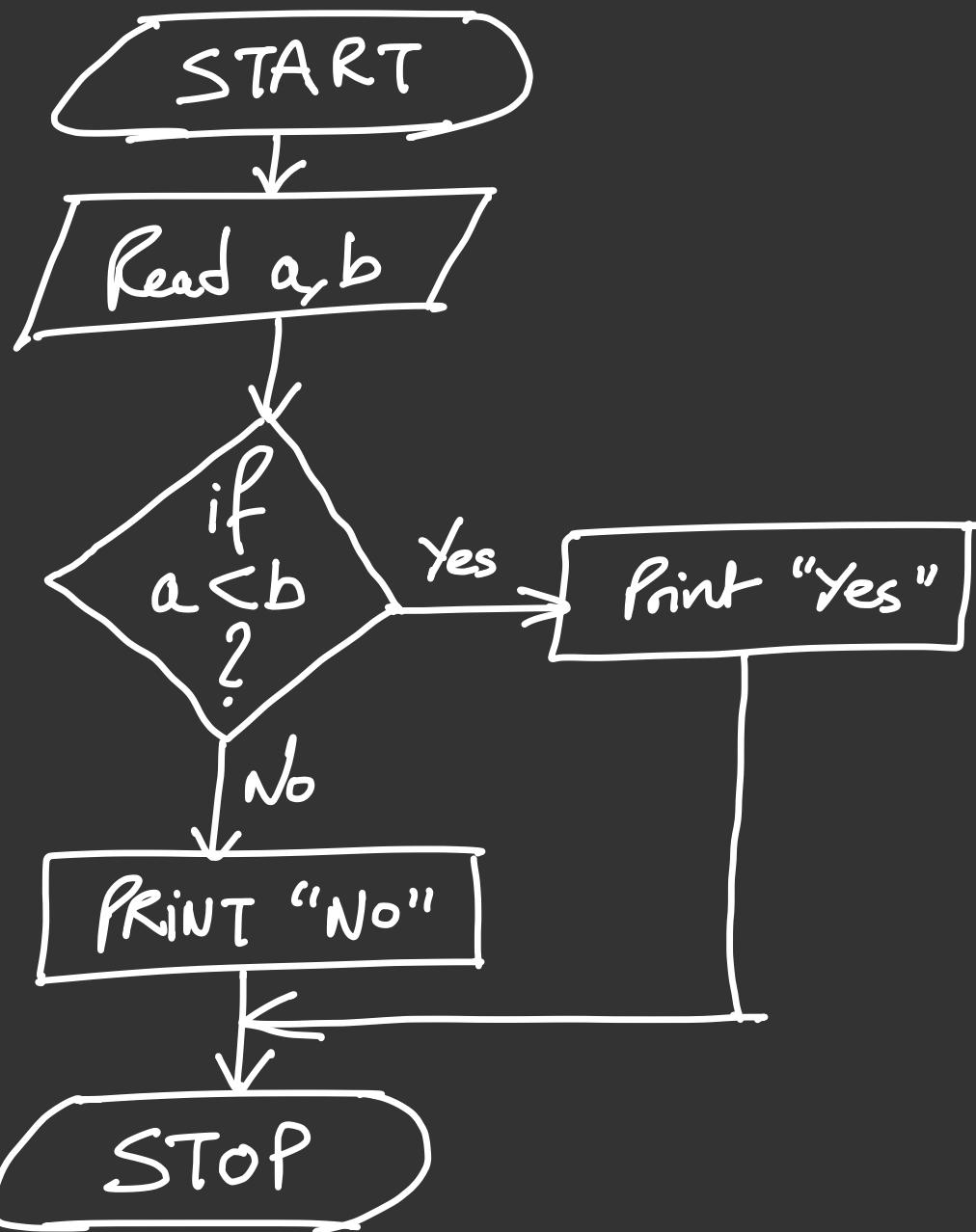


eg: Average of three numbers



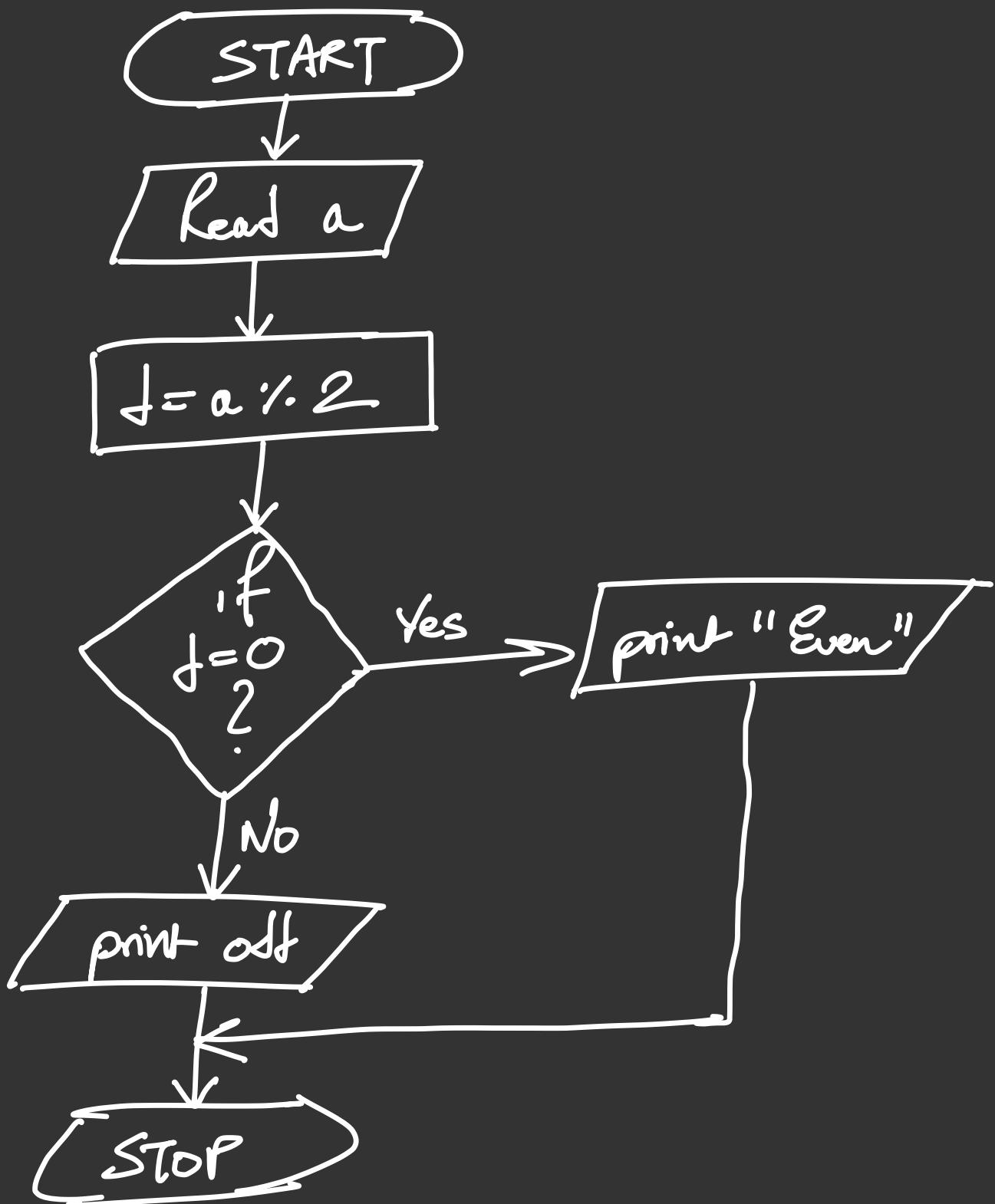
- Read a,b,c
- $\text{avg} = (a+b+c)/3$
- Print avg

Question : Check if $a < b$?



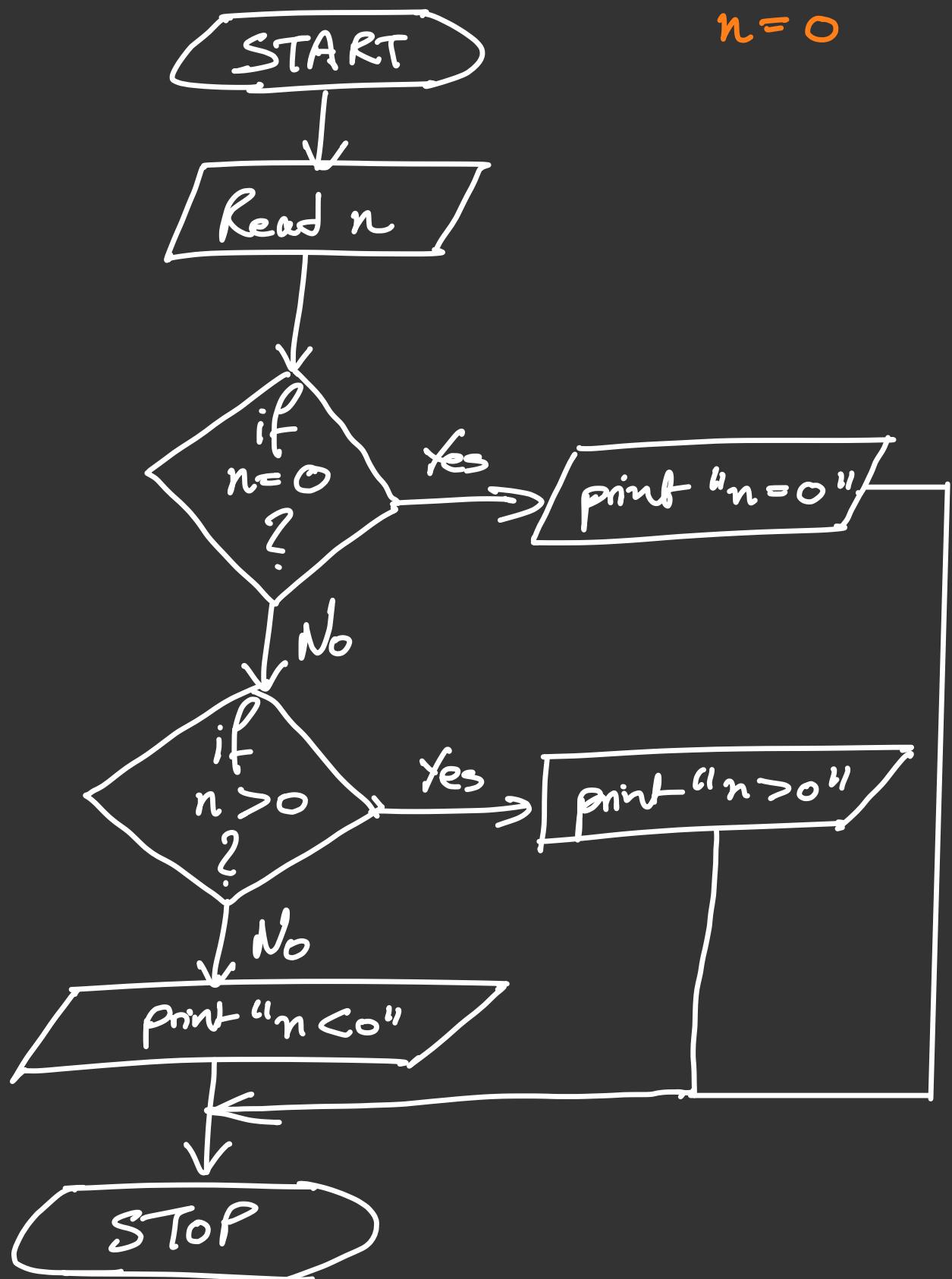
→ Read a, b
→ if $a < b$
 Print "Yes"
→ else
 Print "No"

Question: Check if a number is even or odd

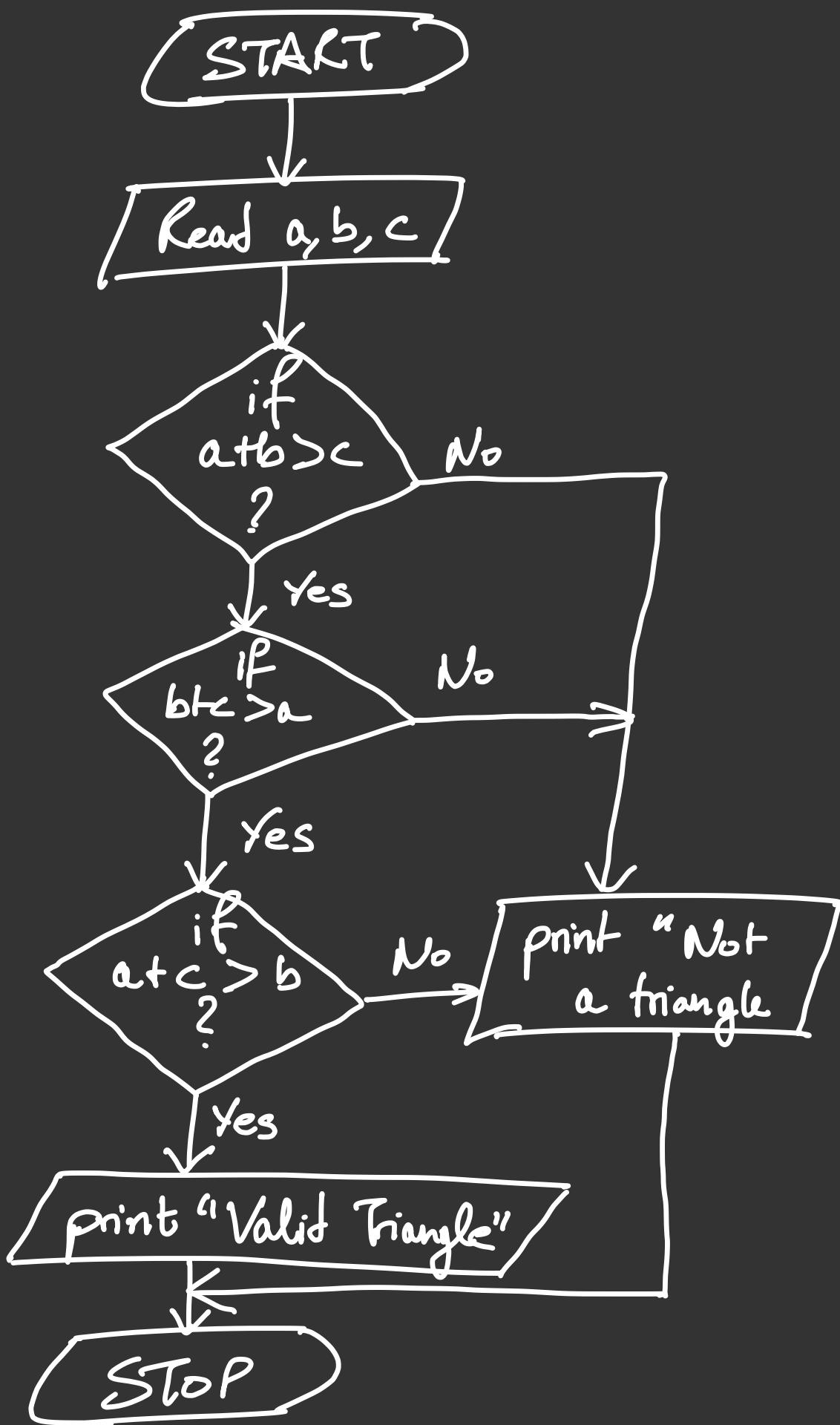


Question : Check if the number is

$n > 0$
 $n < 0$
 $n = 0$

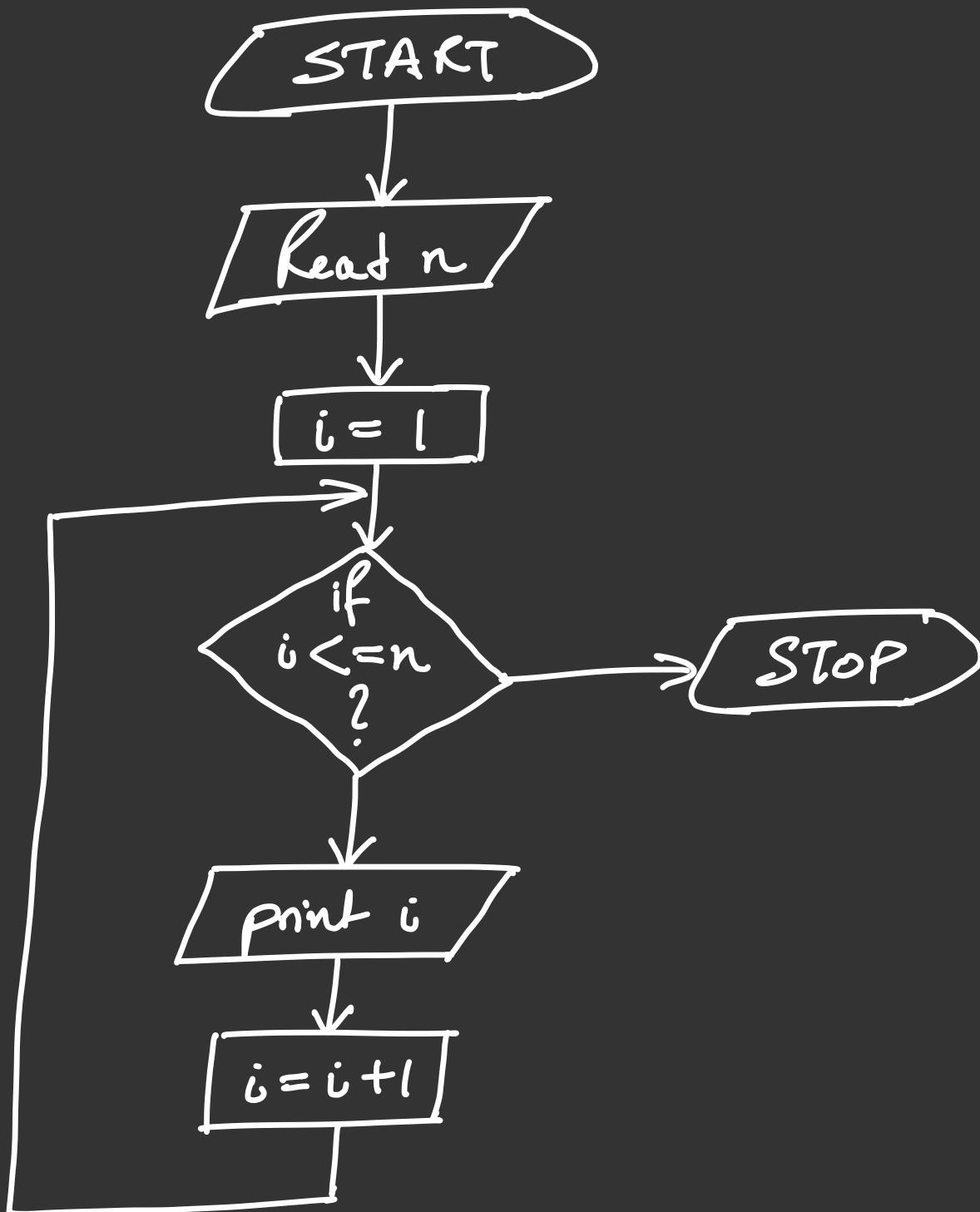


Question: Sum of two sides greater than the third → Check for Validity

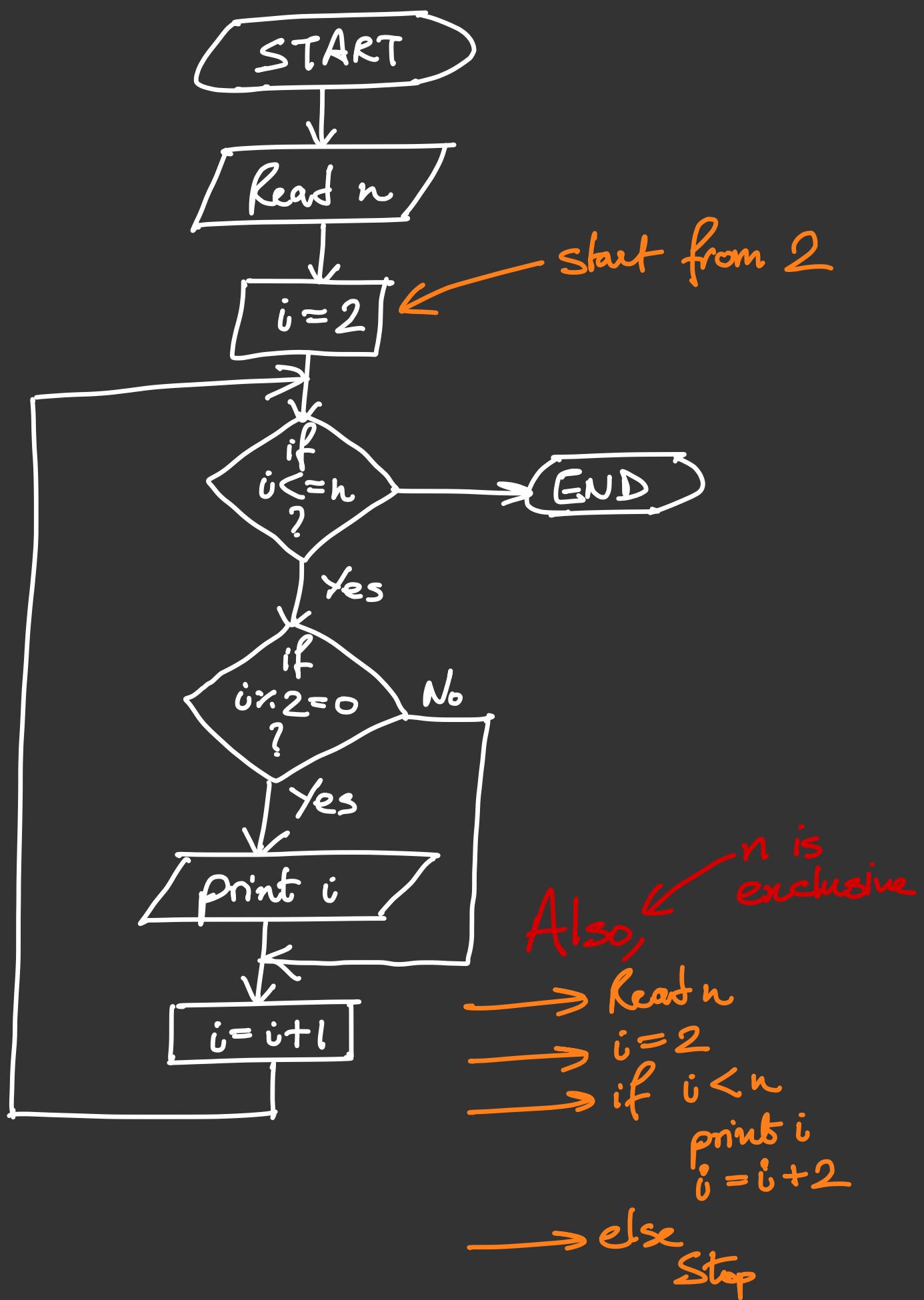


Loops

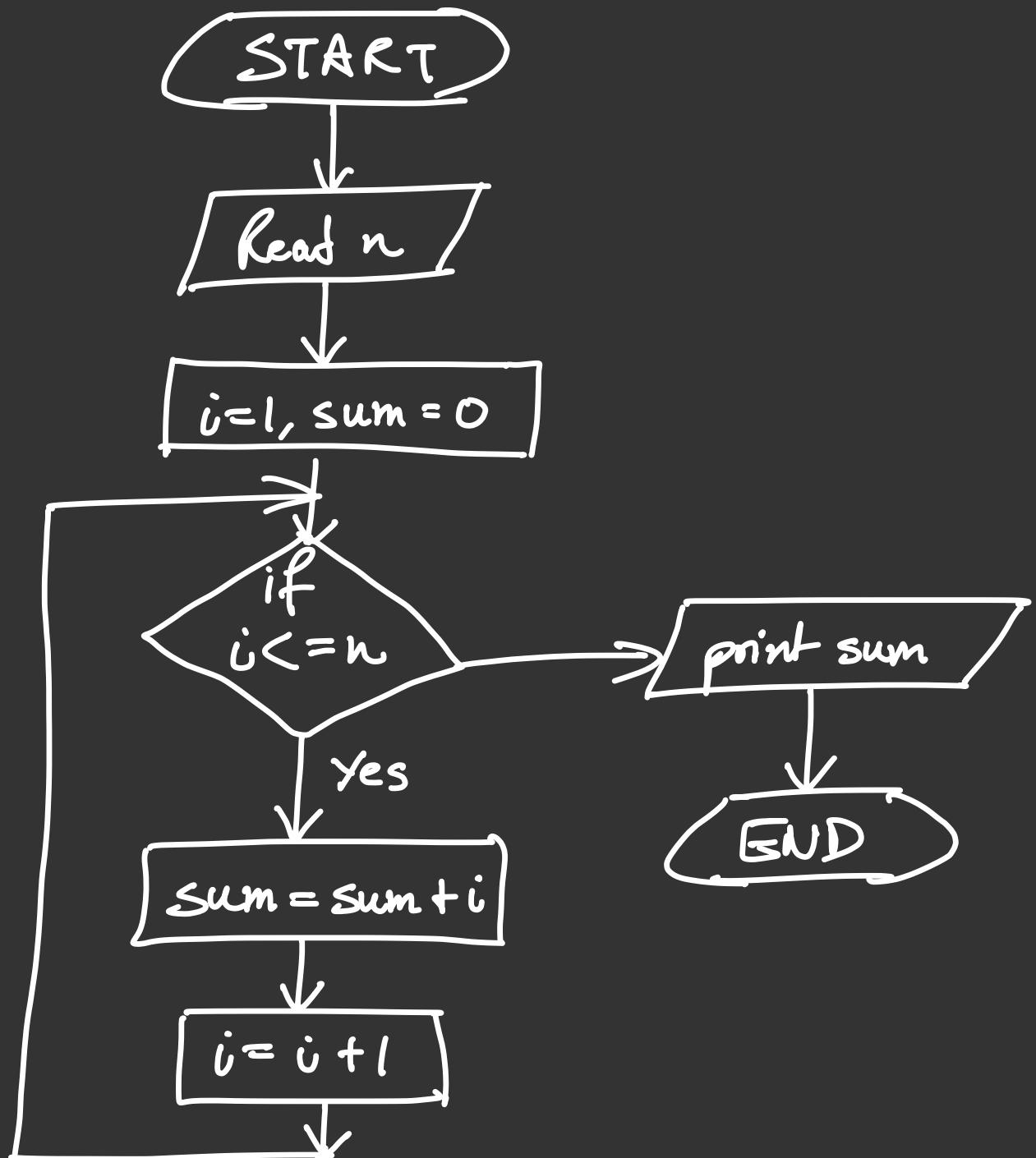
Question : Print 1 to N



Question : Prints all even numbers from 1 to n.



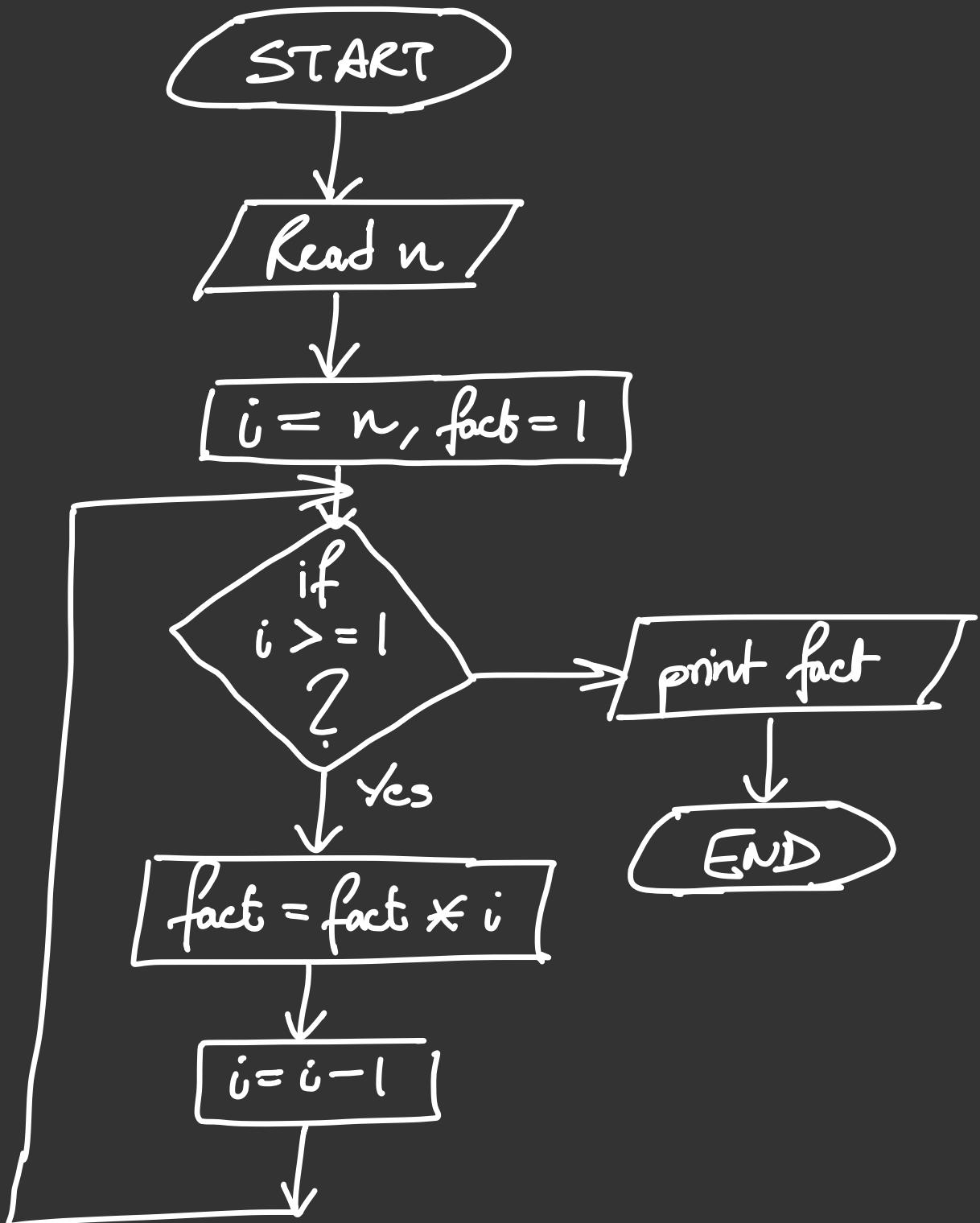
Question : find sum 1 to n (Inclusive)



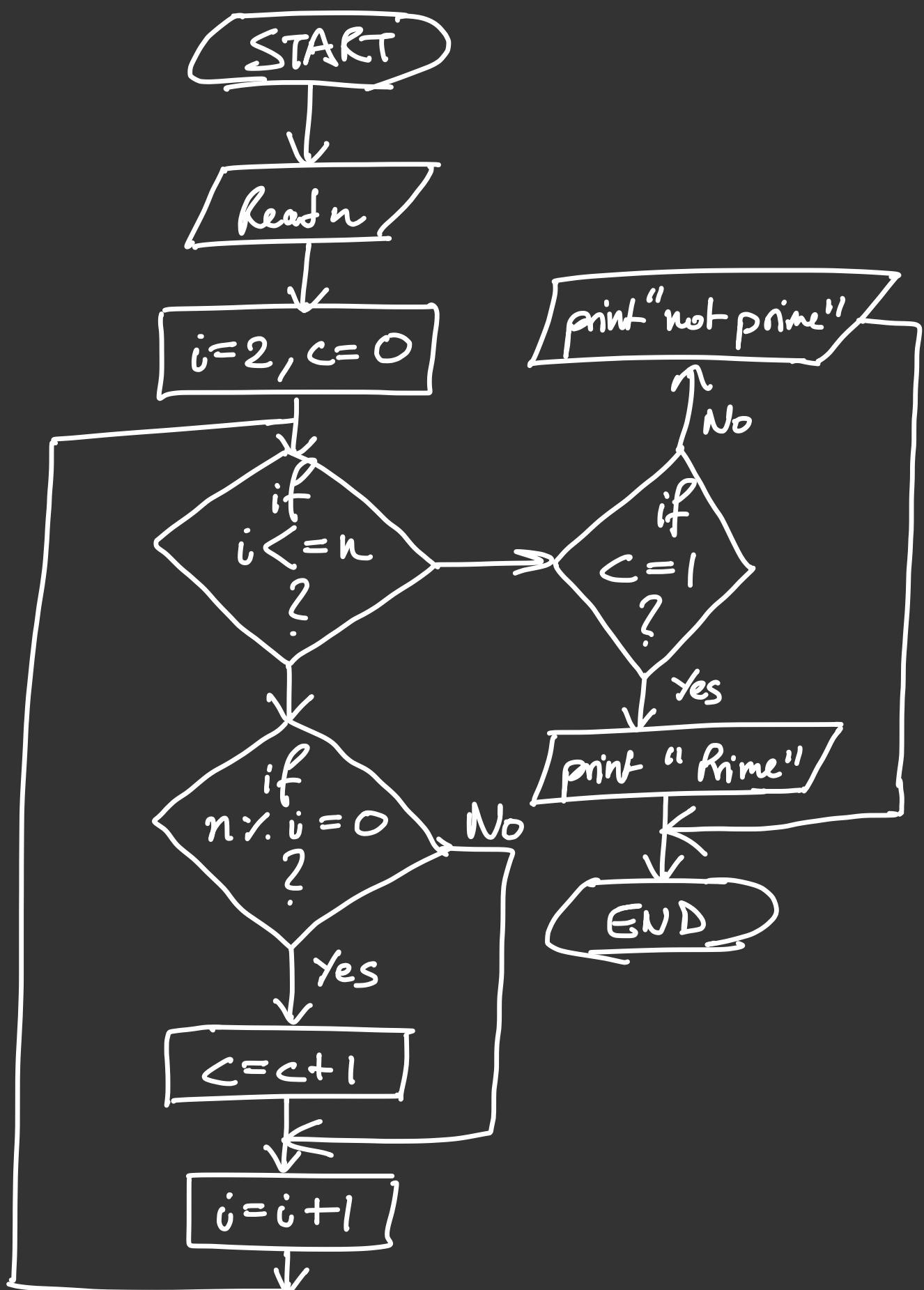
Question: factorial of n

eg: $n = 5$

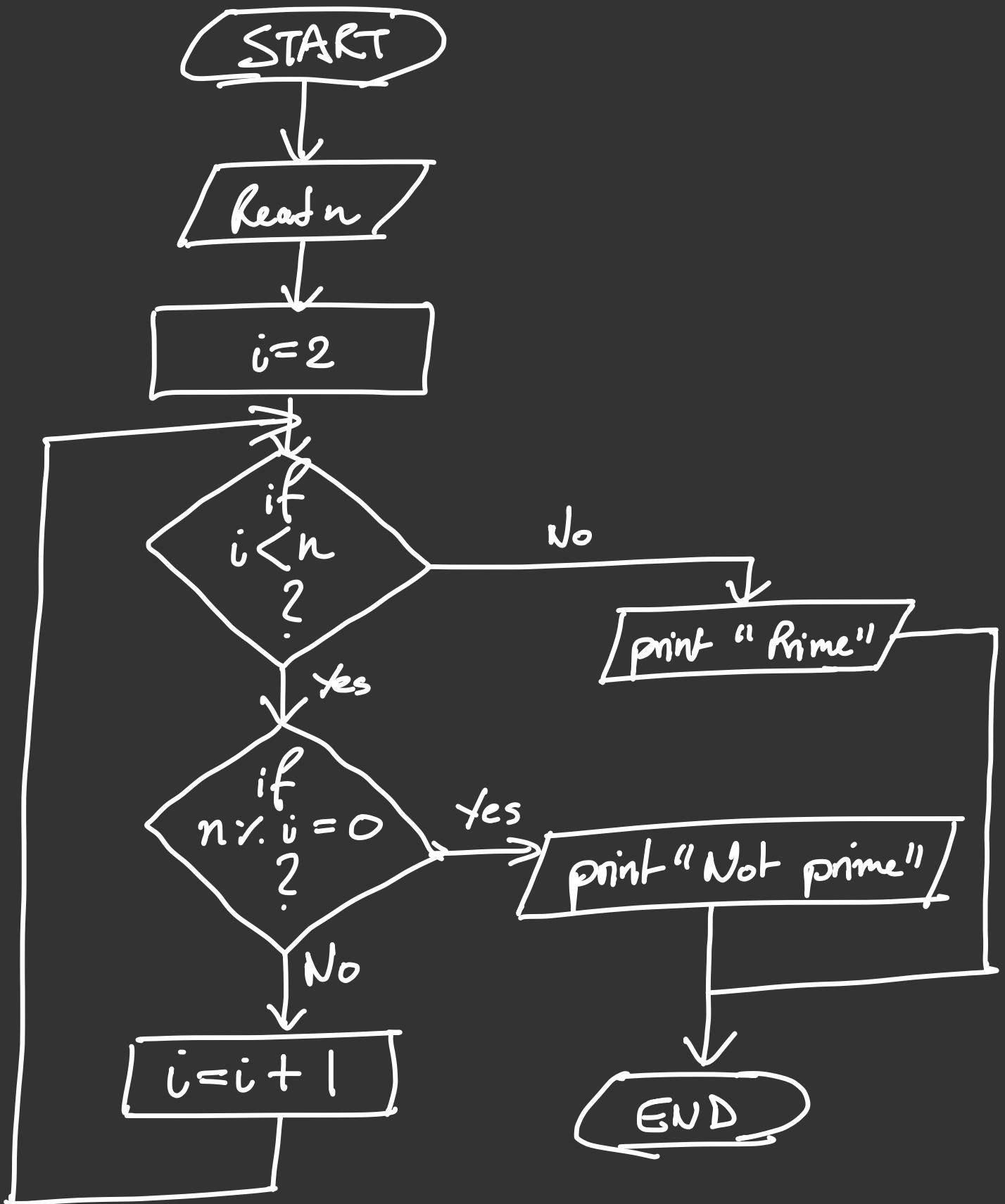
$$\text{fact} = 5 \times 4 \times 3 \times 2 \times 1$$



Question : Check for prime

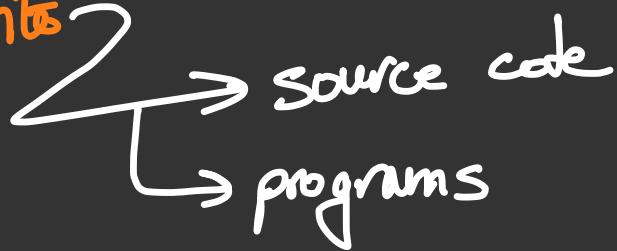


Better Logic →

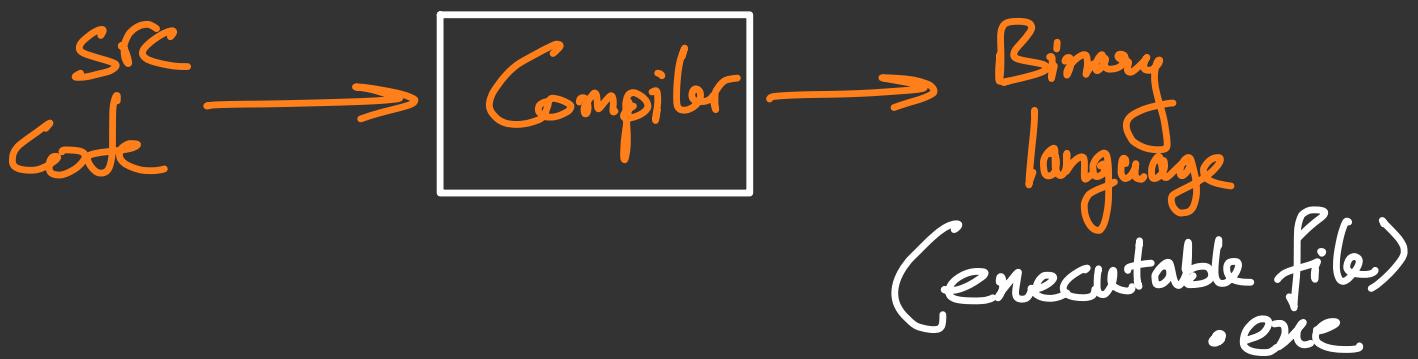
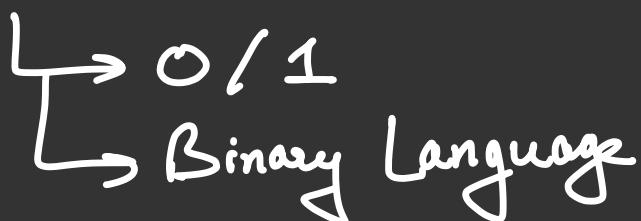


Programming Languages?

What we writes



What computer understands

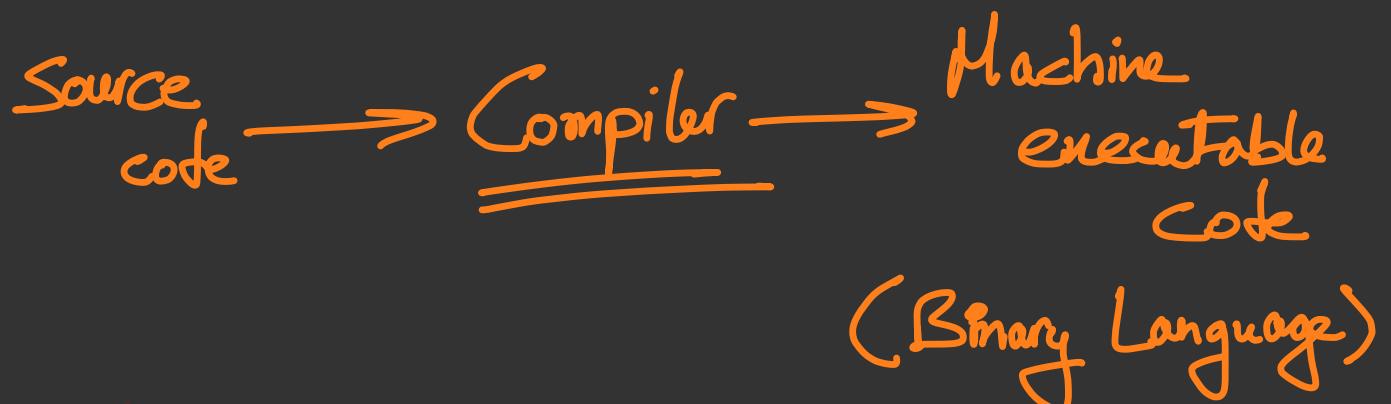


→ a way to communicate
with a computer.

eg: C, C++, Python, R, Java

→ Every language must be written
following some rules called
Syntax of that language

Lecture 2:



Compiler

- ↳ Translation from src code to binary code
- ↳ find errors

IDE → Integrated Development Environments

Programs in C++



Printing → cout << "Namaste Dunia"
 << endl

Default Code:

```
#include <iostream>
using namespace std;
int main()
{
```


 }

→ 'iostream' is a file which includes
cout

→ We want to use the namespace which is std, C++ has multiple namespaces.

↙ for output
↙ to display / write.

endl ↗ takes cursor to the new line.

↗ Other way, '\n'

∅ cout

eg: cout << "Namaste Duniya \n";

cout << "Namaste Duniya" << '\n';

cout << "Namaste Duniya" << endl;

Semicolon (;) ↗ to end the code line

Data Types and Variables

Integer: int \rightarrow 4 bytes = 32 bits

int a = 5;

a - variable name
datatype - integer
↓
memory needed = 4 bytes

Character: ch \rightarrow 1 byte = 8 bits

char ch = 'a'; \rightarrow within single inverted commas.
 $ch \neq 'ab'$

Boolean: bool \rightarrow True, 1
 \rightarrow False, 0

bool b = 1;

\rightarrow 1 bit

\rightarrow While printing, if
true \rightarrow 1 is printed
false \rightarrow 0

Float : float \rightarrow 8 Bytes = 64 bits

float f = 1.2;

Double : double \rightarrow 8 Bytes

double d = 1.23;

Variable Naming Rules

\rightarrow Don't start with numbers

\rightarrow You can use numbers, alphabets, underscore

\rightarrow You can start naming with alphabets or underscore.

* sizeof()

\hookrightarrow returns the size of the variable

e.g. int size = sizeof(a); a \rightarrow int

Thus, size = 4

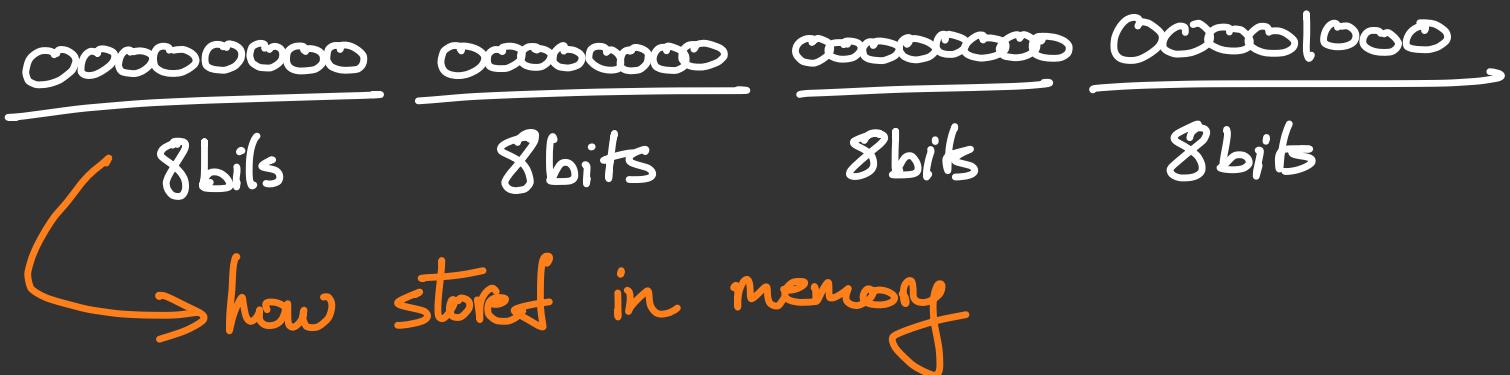
How Data is Stored?

int a = 8;

$$8_{(10)} \rightarrow 1000_{(2)}$$

↓
4 bits

but memory allocated = 32 bits



* for negative number?

ASCII Chart

space = 32

A-Z = 65 to 90

a-z = 97 to 122

0-9 = 48 to 57

fullstop(.) = 46

Comma(,) = 44

Colon(:) = 58

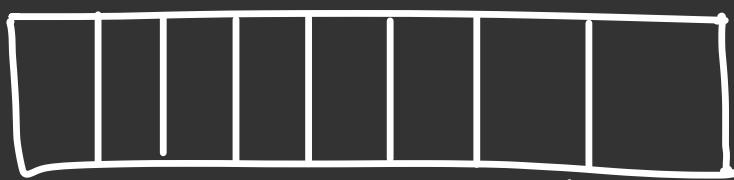
Semicolon(;) = 59

In Memory,

character's ASCII value is

converted to ~~binary~~ and

that is stored in ~~Memory~~.



8 bits = 1 byte

datatype helps us to identify
that the given bytes in the
memory are what.

Type Casting

→ char to int

```
int a = 'a';  
cout << a << endl; # 97
```

→ int to char

```
char ch = 98;  
cout << ch << endl; # b
```

What if we wants to type cast
from int to char but the value is too
large to be stored in char?

int → 4 bytes = 32 bits
 $2^{32} - 1 = \text{max}$
 $0 = \text{min}$

char → 1 byte = 8 bits

$2^8 - 1 = \text{max}$
 $0 = \text{min}$

eg:

char ch = 123456;



4 bytes



last byte gets converted to
char, which is coming to be
64 in this case.

Thus, 64 → @

Cout << ch << endl; # @

How negative numbers are stored?

First Bit

↳ 0 - +ve
↳ 1 - -ve

eg: -5

Storage of negative 5

- ① Ignore the One sign
- ② Converts into binary
- ③ Take 2's complement and store it

5 → 00000000 00000000 00000000 00000001

1's compliment

→ 11111111 11111111 11111111 11111010

2's compliment

→ add 1 to 1's compliments

11111111 11111111 11111111 11111011

This will be
stored

To display the stored value \rightarrow

① Take 2's compliment of the stored number

1 1111111 11111111 11111111 11111011

→ this tells us negative value

for 2's compliment, first do 1's compliment



0000000 0000000 0000000 00000100

2's compliment



00000000 0000000 0000000 00000101

$\hookrightarrow 5$

& negative sign above

$\Rightarrow -5$

Storage to Integers

(i) Negative

- Ignore the \ominus ve sign
- Convert the number to binary
- Take 2's compliment
 - 1's compliment
 - Add one in the end

(ii) Positive

- Convert it into Binary
- Stop

* Thus, while displaying a stored value

- if first bit is 1 \rightarrow negative
- if first bit is 0 \rightarrow positive

Converting Decimal / Integer to Binary

eg: 57

Method 1:

$$\begin{array}{r} 0 \quad 0 \quad 1 \quad 1 \quad 1 \quad 0 \quad 0 \quad 1 \\ \hline 128 \quad 64 \quad 32 \quad 16 \quad 8 \quad 4 \quad 2 \quad 1 \end{array}$$

Method 2:

2	57	
2	28	1
2	14	0
2	7	0
2	3	1
2	1	1
1	0	1

⇒ 111001

* Why 2's complement?

Integer range is

$$\hookrightarrow -(2^{31}-1) \text{ to } 2^{31}-1$$

But, in here
 $\rightarrow 0$ and -0 both are counted

So, to treat both of them as
one value \hookrightarrow 2's Complement

New Range: $-(2^{31})$ to $2^{31}-1$

* Unsigned Values

\hookrightarrow Range: 0 to $2^{31}-1$

eg: unsigned int i = 112; ✓

unsigned int i = -112;

cout << i << endl; # big value

→ it will store as negative value
that is in 2's compliment, but
Compiler will treat it as unsigned value
thus converts the whole thing to its
equivalent positive decimal number.

Operators

int/int = int

double/int = double

float/int = float

eg:

int a = 5/2; // 2

double d = 5/2; // 2

double dl = 5/2.0; // 2.5



Relational Operators

=, >, <, >=, <=, !=

To check equality

↳ $a == b$

Logical Operator

& — AND

|| — OR

! —
 ↑ True to False
 ↳ False to true

e.g.: int a = 2;

int b = 0;

cout << !a << endl; // 0

cout << !b << endl; // 1

! of anything other than zero
is 0.

Lecture 3:

Conditional & Loops

If Statements

```
if( )  
{
```

```
==== }  
{
```

if the condition
is true, then
these code statements
will be executed.

If-Else

```
if(condition)  
{
```

```
==== } if condition is true
```

```
else
```

```
{
```

```
==== } if condition is false
```

* <in>> n

↳ for inputs

Question: (number_positive.cpp)

Get an inputs from the user and check if
the number is positive or not?

* if <in>>a>>b;

↳ runs for 1 enter 2 enter ("\\n")
↳ runs for 1 tab 2 ("\\t")
↳ runs for 1 space 2 ("_")

* <in>.get()

Eg: int a;

a = <in>.get();

↳ It takes the character

So, for 1 → ASCII value of 1
= 49

Thus, 49 gets stored in a.

Nested if - else

```
if( )  
{  
    ==  
    ==  
    ==  
}  
else  
{  
    if( )  
    {  
        ==  
        ==  
        ==  
    }  
    else  
{  
        ==  
        ==  
    }  
}
```

Question: (which-character.cpp)

char ch;

if 'A' to 'Z' → upper case

if 'a' to 'z' → lower case

if '0' to '9' → numbers

While-loop

while (condition)

{

}



} till the condition is true, these codes will be executed multiple times.

Question:

① Print numbers from 1 to n.

print-1-to-n.cpp

② Sum of numbers from 1 to n.

Sum-1-to-n.cpp

③ Whether a number is prime or not
prime_no_cr_not.cpp

PATTERNS

①

* * * *
* * * * *
* * * *
* * * *

→ pattern1.cpp

②

Same pattern as above, but user gives input of rows and columns.

→ pattern1-5.cpp

③

1 1 1 → 1st row

2 2 2 → 2nd column

user → 3(n)

3 3 3 → 3rd row

→ pattern2.cpp

* → first while for rows

→ second while inside first while for columns of each row.

Lecture 4:

★ => After seeing the pattern,
first observe ki how rows and
columns are affecting the pattern.

④ 1 2 3 4 user → n
1 2 3 4
1 2 3 4 → pattern3.cpp
1 2 3 4

⑤ 1 2 3 4 user → 4(n)
1 2 3
1 2
1 → pattern3-5.cpp

⑥ 3 2 1 user → 3(n)
3 2 1
3 2 1
 → pattern3-75.cpp

⑦

1 2 3 user → 3(n)
4 5 6
7 8 9 → pattern4.cpp

⑧

*
* *
* * *
* * * * user → 4(n)
→ pattern5.cpp

⑨

1
2 3
4 5 6 → pattern6.cpp
7 8 9 10

⑩

1
2 3
3 4 5 → pattern7.cpp
4 5 6 7

⑪

1
2 1
3 2 1
4 3 2 1

12

A
B B
C C C
D D D D

$n \rightarrow 4$

→ pattern 9 - cpp

13 A B C
D E F → practice > test_pattern4.cpp
G H I

A collection of handwritten letters in orange ink on a dark background. The letters are arranged in three rows: the first row contains 'A', 'B', and 'C'; the second row contains 'D', 'E', and 'F'; the third row contains 'G', 'H', and 'I'. Each letter is written in a different style, some with loops and some with more linear strokes.

1s A B C
D E F
G H I J

16

D
C D
B C D
A B C D

* D is not the end goal → starts from such a character that it reaches D.

17

— — — *

— — * *

— * * *

* * * *

→ practice >
test_pattern5.cpp

18

* * * *

* * *

* *

*

practice >
test_pattern6.cpp

19

* * * *

* * *

* *

*

20

1 1 1 1
2 2 2
3 3
4

21

1
2 2
3 3 3
4 4 4 4

22

1 2 3 4
2 3 4
3 4
4

23

1
2 3
4 5 6
7 8 9 10

24

— — — 1
— — 2 1 2
— 3 2 1 2 3
4 3 2 1 2 3 4

25

—	—	—	1			
—	—	1	2	1		
—	1	2	3	2	1	
1	2	3	4	3	2	1

26

$n = 5$

	1	2	3	4	5	6	7	8	9	10
1	1	2	3	4	5	5	4	3	2	1
2	1	2	3	4	8	8	4	3	2	1
3	1	2	3	8	8	8	8	3	2	1
4	1	2	8	8	8	8	8	2	1	
5	1	8	8	8	8	8	8	8	1	

→ pattern - dabangg.cpp

Lecture 5:

Bitwise Operator \rightarrow they work at bit level

AND $\rightarrow \&$

OR $\rightarrow |$

NOT $\rightarrow \sim$

XOR $\rightarrow \wedge$

AND

$\&\&$ \rightarrow logical operator

$\&$ \rightarrow bitwise operator

e.g.: $a=2, b=3$

$$\begin{array}{rcl} a \& \& b \rightarrow 2 = 10 \\ & & 3 = \overline{11} \\ (1 \cdot 1) (0 \cdot 1) \rightarrow & \overline{10} & \rightarrow \textcircled{2} \end{array}$$

$$z = a \& b$$

a	b	z
0	0	0
0	1	0
1	0	0
1	1	1

OR

a	b	z
0	0	0
0	1	1
1	0	1
1	1	1

eg: $a=3, b=6$

$$\begin{array}{r} 11 \\ 100 \\ \hline 111 \end{array} \rightarrow 7$$

NOT

x	3
1	0
0	1

eg: $a = 2 \rightarrow \text{int} = 4 \text{ bytes} = 32 \text{ bits}$

$\rightarrow 0000000000000000000000000010$

$\sim a \rightarrow 1111111100000000000000001101$

→ negative

for printing $\sim a$

→ 1's compliment

$0000000000000000000000000010$

→ 2's compliment

$0000000000000000000000000010$
+1
—————

$0000000000000000000000000011$

→ 3

Since, the number was negative = -3

XOR

a	b	y
0	0	0
0	1	1
1	0	1
1	1	0

→ 1 for odd no. of 1's
 → 0 for even no. of 1's

eg: $a=2 \rightarrow 010$
 $b=4 \rightarrow \begin{array}{r} 100 \\ \hline 110 \end{array}$ $\rightarrow \underline{a \wedge b}$

0	0000	8	1000
1	0001	9	1001
2	0010	10	1010 (A)
3	0011	11	1011 (B)
4	0100	12	1100 (C)
5	0101	13	1101 (D)
6	0110	14	1110 (E)
7	0111	15	1111 (F)

eg : $a=5 \rightarrow 101$
 $b=3 \rightarrow 011$ Z \rightarrow \text{bitwise_op_cpp}

$$\Rightarrow a \& b \rightarrow \begin{array}{r} 101 \\ 011 \\ \hline 001 \end{array} \rightarrow 1$$

$$\Rightarrow a | b \rightarrow \begin{array}{r} 101 \\ 011 \\ \hline 111 \end{array} \rightarrow 7$$

$$\Rightarrow \sim a \rightarrow \begin{array}{r} 000 \dots 0101 \\ \downarrow \\ 111 \dots 1010 \\ \rightarrow 000 \dots 0101 \\ + 1 \\ \hline 000 \dots 0110 \end{array} \rightarrow -6$$

$$\Rightarrow \sim b \rightarrow \begin{array}{r} 0000 \dots 011 \\ \downarrow \\ 1111 \dots 100 \\ \rightarrow 0000 \dots 011 \\ + 1 \\ \hline 000 \dots 100 \end{array} \rightarrow -4$$

$$\Rightarrow a^b \rightarrow \begin{array}{r} 101 \\ \times 011 \\ \hline 110 \end{array} \rightarrow 6$$

Left & Right Operator

\Rightarrow Left Shift

$$\text{eg: } 5 \ll 1 \quad 5 \times 2 = 10$$

$$5 \rightarrow \begin{array}{r} 000 \\ \times 1 \\ \hline 101 \end{array} \rightarrow 10$$

$$\text{eg: } 3 \ll 2 \quad 3 \times 2 \times 2 = 12$$

$$3 \rightarrow \begin{array}{r} 000 \\ \times 2 \\ \hline 1100 \end{array} \rightarrow 12$$

$\cancel{\times} 2 \rightarrow$ not everytime, but most of the time

$\cancel{\times}$ for big numbers, this might create negative numbers

$$\text{eg: } 0100 \dots 0010$$

$$\cancel{0}0000 \dots 0100$$

\rightarrow negative number

⇒ Right Shift

eg: $5 \gg 2$

$$\frac{5}{2} = \frac{2}{2} = 1$$



for positive \oplus ve \rightarrow

padding is always with zero.

\hookrightarrow ie if new bits need to be added, they will be 0 only.

for \ominus ve

\hookrightarrow padding \rightarrow compiler dependant

eg:

$$17 \gg 1 \rightarrow 8 \quad \left. \begin{array}{l} \\ \end{array} \right\} \div 2$$

$$17 \gg 2 \rightarrow 4$$

$$19 \ll 1 \rightarrow 38 \quad \left. \begin{array}{l} \\ \end{array} \right\} \times 2$$

$$21 \ll 2 \rightarrow 84$$

\Rightarrow practice > test3.cp

int a = -5 $5 = 101$

$$\begin{array}{r} 000 \text{ -- } 000101 \\ \rightarrow 111 \text{ -- } 111010 \\ + 1 \\ \hline 111 \text{ -- } 111011 \end{array}$$

int b = 6 $000 \text{ -- } 000110$

$$\begin{array}{r} 1111 \text{ -- -- -- } 111011 \\ 0000 \text{ -- -- -- } 000110 \end{array}$$

$a \& b = 0000 \text{ -- -- -- } 000010$ $\hookrightarrow 2$

$a | b = \underline{1111 \text{ -- -- -- } 111111}$ \hookrightarrow while printing treated as negative number

$$\begin{array}{r} 0000 \text{ -- -- -- } 0000000 \\ + 1 \\ \hline 0000 \text{ -- -- } 0000001 \end{array}$$

add the negative sign $\hookrightarrow -1$

$$a \wedge b = \underline{1111 \text{ --- } 11101}$$

→ while printing treated as negative number

$$\begin{array}{r} \rightarrow 0000 \text{ --- } 000010 \\ + 1 \\ \hline 0000 \text{ --- } 000011 \\ \rightarrow -3 \end{array}$$

$$a = 111 \text{ --- } 111011$$

$$\sim a = 000 \text{ --- } 000100$$

→ 4

$$b = 000 \text{ --- } 000110$$

$$\sim b = \underline{111 \text{ --- } 111001}$$

$$\begin{array}{r} \rightarrow 000 \text{ --- } 000110 \\ + 1 \\ \hline 000 \text{ --- } 000111 \\ \rightarrow -7 \end{array}$$

$$a = 111 _ _ _ 11011$$

$$a \ll 1 = 111 _ _ _ 110110$$

$$\begin{array}{r} \hookrightarrow 000 _ _ 001001 \\ +1 \\ \hline \end{array}$$

$$000 _ _ 001010$$

$$\hookrightarrow \textcircled{-10}$$

$$a \ll 2 = 111 _ _ _ 101100$$

$$\begin{array}{r} \hookrightarrow 000 _ _ 010011 \\ +1 \\ \hline 000 _ _ 010100 \end{array}$$

$$(1 \times 2^2) + (2^4 \times 1)$$

$$= 4 + 16 = 20$$

$$\longrightarrow \textcircled{-20}$$

$$b \gg 1 = 000 _ _ _ _ _ 0000011$$

$$\hookrightarrow \textcircled{3}$$

Increments and Decrement operators

Increments

$i++;$ → post-increment
 $++i;$ → pre-increment

Decrement

$i--;$ → post-decrement
 $--i;$ → pre-decrement

$$i = i + 1 \rightarrow i + = 1;$$

$$i = i - 1 \rightarrow i - = 1;$$

eg: $i = 8;$

$$a = (i++) + (--i) + i + (-i);$$

`cout << i << endl;`

`cout << a << endl;`

8
8
8
7

$$8 + 8 + 8 + 7 = 31$$

eg: $\left\{ \begin{array}{l} \text{if}(a) \\ \quad \quad \quad \text{true : } a \neq 0 \\ \quad \quad \quad \text{false : } a = 0 \end{array} \right. \quad \equiv \quad \left\{ \begin{array}{l} \\ \\ \end{array} \right.$

```
#include <iostream>
using namespace std;
int main()
{
    int a = 1;           a = !0
    int b = 2;           b = 2 3
    if(a-- > 0 && ++b > 2 ){
        cout << "Stage1 - Inside If ";
    } else{
        cout << "Stage2 - Inside else ";
    }
    cout << a << " " << b << endl;
}
```

\Rightarrow Stage1 - Inside If
 $0 \quad 3$

```
#include <iostream>
using namespace std;
int main()
{
    int number = 3; // 4
    cout << (25 * (++number) );
}
```

$\rightarrow 100$

```
#include <iostream>
using namespace std;
int main()
{
    int a = 1;           a = !2 3
    int b = a++;         b = 1
    int c = ++a;         c = 3
    cout << b ;
    cout << c;
}
```

$a = !2 3$
 $b = 1$
 $c = 3$

$\rightarrow \frac{1}{3}$

For Loop → has iterations

Syntax:

```
for (initiation; condition; incre/decrements)  
{  
    _____  
    _____  
    _____  
    _____  
}  
_____
```

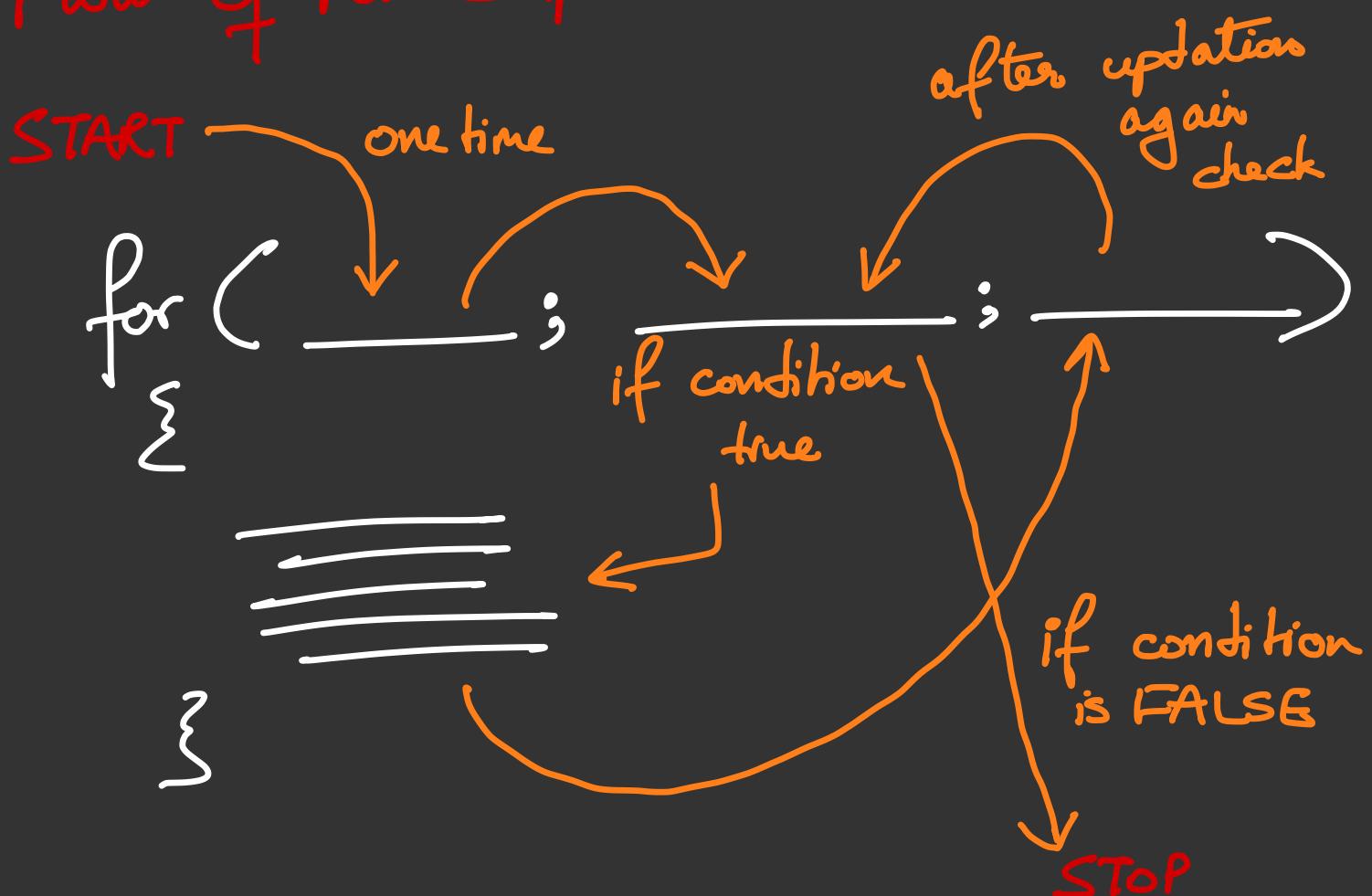
break; → gets you out of
the current loop

Question:

Print 1 to n using non-parameterized
for loop.

→ for-loop-no-parameter.cpp

Flow of For Loop



Question:

Fibonacci Series

↳ 0, 1, 1, 2, 3, 5, 8, 13

→ fibonacci_series.cpp

Prime Number or not

↳ prime_or_no.cpp

Continue; ➡ to skip all the code below this statement for current iteration.

Output Questions:

```
#include<iostream>
using namespace std;
int main() {

    for(int i = 0; i<=5; i++) {
        cout<< i << " ";
        i++;
    }
}
```

Two times
increments

i = 0 1 2 3 4 5 6

0 2 4

```

#include<iostream>
using namespace std;
int main() {

    for(int i = 0; i<=15; i += 2) {
        cout << i << " ";
        if( i&1 ){
            continue;
        }
        i++;
    }
}

```

X
Odd
number & 1 = 1

i = 0 2 4 6 8 10 12 14 16 18 20 22 24 26 28 30

OK 1 → 0

3 & 1 → 0011

$$\begin{array}{r} 0001 \\ \hline 0001 \end{array}$$

 0001 → 1

5 & 1 → 0101

$$\begin{array}{r} 0001 \\ \hline 0001 \end{array}$$

 0001 → 1

7 & 1 → 1

0	0000
1	0001
2	0010
3	0011
4	0100
5	0101
6	0110
7	0111
8	1000
9	1001
10	1010
11	1011
12	1100
13	1101
14	1110
15	1111

Output :

0 3 5 7 9 11 13 15

```
#include<iostream>
using namespace std;
int main() {

    for(int i=0;i<5;i++) {
        for(int j=i;j<=5;j++) {
            cout<<i << " " << j << endl;
        }
    }
}
```

0 0 4 4
0 1 4 5
0 2 5 5
0 3 5 5
0 4 5 5
0 5 5 5
1 1 2
1 2
1 3
1 4
1 5
2 2
2 3
2 4
2 5
3 3
3 4
3 5

→ i cannot
be 5

```
#include<iostream>
using namespace std;
int main() {

    for(int i=0;i<5;i++) {
        for(int j=i;j<=5;j++) {
            if(i+j == 10) {
                break;
            }
            cout<<i << " " << j << endl;
        }
    }
}
```

0	0		
0	1		
0	2		
0	3		
0	4		
0	5		
1	1	4	4
1	2	4	5
1	3		
1	4		
1	5		
2	2		
2	3		
2	4		
2	5		
3	3		
3	4		
3	5		

Scope of Variables

```
int main()
```

```
{  
    int a = 3;
```

```
if (true)
```

cout << a; → this will work

=====

```
    int b = 3;
```

```
}
```

int a = 1; → will give error
"redefinition of a"

```
} cout << b;
```

→ will show error

"use of undeclared identifier 'b'"

* If a variable is defined inside a block, then its presence is limited to inside that block only. But cannot define again in same block.

int a = 2; \rightarrow Defining

int b;

b = 3; \rightarrow Assigning

Operator Precedence

\rightarrow use brackets

Question: Number of 1's (LEET CODE)

1:

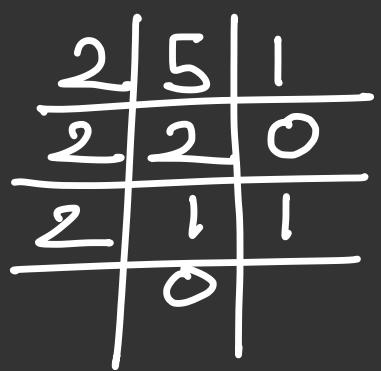
$$\begin{array}{r} 00000 \quad \text{---} \quad \text{---} \quad \text{---} \quad | 01 \\ \qquad \qquad \qquad \qquad \qquad \text{AND } 1 \\ \hline & & & & 1 \rightarrow \text{TRUE} \end{array}$$

\downarrow
count++

Right Shift

00000 $\quad \text{---} \quad \text{---} \quad \text{---} \quad | 01$

\rightarrow This needs to happen till the number becomes zero
i.e. no 1's left

2:  just keep dividing
by 2 and
keep changing
n and counting
1's.

Thus,

Right Shift is equivalent to
division by 2.

$$n \gg 1 = n/2$$

eg: $7 = 0111$

$$\begin{array}{r} 7/2 = 3 & 0111 \\ & \downarrow RS \\ & 0011 \end{array}$$

$$3 = 0011$$

$$3/2 = 1 \quad 0011 \xrightarrow{RS} 0001$$

$$1 = 0001$$

Lecture 6

Binary and Decimal Number System

Decimal to Binary

Method 1 \rightarrow decimal-to-binary
- method1.cpp

$$n = 10$$

2	1	0	0	
2	5	1		
2	2	0		
2	1			
	0			

$$10_{(10)} \rightarrow 1010_{(2)}$$

Steps

- \rightarrow divide by 2
- \rightarrow store remainder
- \rightarrow repeat step 2 until $n \neq 0$
- \rightarrow reverse the remainders

~~If~~ If $n \& 1 = 1 \rightarrow n$ is odd

else if $n \& 1 = 0 \rightarrow n$ is even

Thus, for last bit, just AND 1,
if result is 1 \rightarrow then bit was 1
else bit was 0.

Method 2 \rightarrow decimal-to-binary-method2.cpp

binary = XXXXX = n

\rightarrow for last digit ($n \& 1$)

$\rightarrow n = n \gg 1;$ = Right Shift

How to store these bits?

101 \rightarrow |
 | 01
 | 101

$\Rightarrow res = 0; count = 0;$

$res = (10^{count} \times digit) + res;$

$count++;$

~~pow()~~ pow() should be used
as double variable.

If needed typecast it to int.

Digits

flow of input

1, 2, 3

reverse flow

$ans = 0; c = 0;$
 $ans = (10^c \times digit) + ans;$
 $c++;$
 $return ans;$

Same flow

$ans = 0;$
 $ans = (ans * 10) + digit;$
 $return ans;$

Negative number to binary form
 $n = -6$ \hookrightarrow neg-decimal to
 -binary.cpp

- ① Ignore the sign
- ② Take 2's compliment
 - \rightarrow 1's compliment
 - $\rightarrow +1$

Negative Binary to Decimal *

- ① Check if first bit = 1, means number is binary
- ② Take 2's compliment of the number

Binary to Decimal

eg: 101 \hookrightarrow binary-to-decimal.cpp

$$\begin{array}{r} 1 \quad 0 \quad 1 \\ 2^2 + 2^1 + 2^0 \\ \Rightarrow (1 \times 2^2) + (1 \times 2^1) \\ \Rightarrow 4 + 1 \Rightarrow 5_{(10)} \end{array}$$

~~X~~ $n = 101011$

Last digit can be taken out by
two ways →

① int d = n % 10;
 $n = n / 10;$

② int d = n & 1; \times if the
 $n = n \gg 1;$ inputs (binary)
taken as int,
cannot use this.

This, works will last bit of the
decimal number.

Lecture 7

INT_MAX
INT_MIN } → represents the extremes of integer data type

4 Complement Base 10 Integer

Given = 5

→ 0000 — 0101

Want = 0000 — 0010

→ 2

Mask 1 = $\sim n = 1111 \dots 1010$

Mask 2 =
$$\frac{1000\dots0111}{0000\dots0010}$$

→ 2



```

int nl = ~n;
int mask = 0;
while(n != 0)
{

```

$n = n \gg 1;$ Right Shift
 $mask = mask \ll 1;$ Left Shift
 $mask = mask | 1;$

At the end we will need 1 at the last

int c = n & mask;

cout << "Compliment is: " << c << endl;

LeetCode Question - 231

Power of 2

↳ power-of-2.cpp

Method 1:

```
n → number  
j = 0; c = 0;  
while (j <= n)  
{  
    j = pow(2, c);  
    if (j == n)  
        cout << "Yes";  
    return 0;  
  
    c++;  
}  
cout << "No"
```

Method 2:

Set Bits

0 - 0000	
$2^0 = 1 - 0001$	1 —
$2^1 = 2 - 0010$	1 —
3 - 0011	
$2^2 = 4 - 0100$	1 —
5 - 0101	
6 - 0110	
7 - 0111	
$2^3 = 8 - 1000$	1 —
⋮	
$2^4 = 16 - 10000$	1 —

Set Bits = no. of 1 bits in
the binary of the
integer

* for all $2^k =$ no. of set bits
 $= 1$
no. of 1's = 1

Code:

$n \rightarrow \text{number}$

Count = 0;

while ($n! = 0$)

{

 if ($n \& 1$)

 Count++;

}

$n = n \gg 1$;

Checking for
last bit if
it is 1.

Right Shift

Lecture 8

Switch - Case → int or char

Switch (expression)

{

Case :

break;

Case :

break;

Default :

}

* Default not mandatory

* If break not written after a case, it check for other cases as well

Thus, if no breaks throughout,
Defaults will always be printed

Nested switch also allowed

* If else if's can be converted
to switch case and vice-versa.

* exit(0);

↳ terminates the program

break;

↳ helps you get out of
switch case or any loop.

* Continue; → cannot be used with switch case.

Calculator program

a, b
operator = *, /, +, - } perform
using switch case.

→ mini-calculator.cpp

Homework Question

Total Amount = ₹ x

```
graph TD; A((₹ x)) --> B((₹ 100 note)); A --> C((₹ 50 note)); A --> D((₹ 20 note)); A --> E((₹ 1 note))
```

→ Using switch case.

→ money-split.cpp

* Use switch()

{

Case 1: ≡≡≡

Case 2: ≡≡≡

Case 3: ≡≡≡

}

⇒ all the cases
will be executed

Functions

→ to stop bulkiness of
the code
(reduce LOC)

→ reusability of code

Syntax:

return-type FunctionName (Argument)
{
 =====
 return (→);
}

return-type → void
 → any other
 data type

Power a^b

↳ power-a-b.cpp

is Even?

↳ even-odd.cpp

Any number

$$n! \cdot k! = 1$$

then, $n = \text{odd number}$

$${}^n C_r = \frac{n!}{r! \times (n-r)!}$$

↳ nCr.cpp

In case of void

↳ return; can be used
without any value

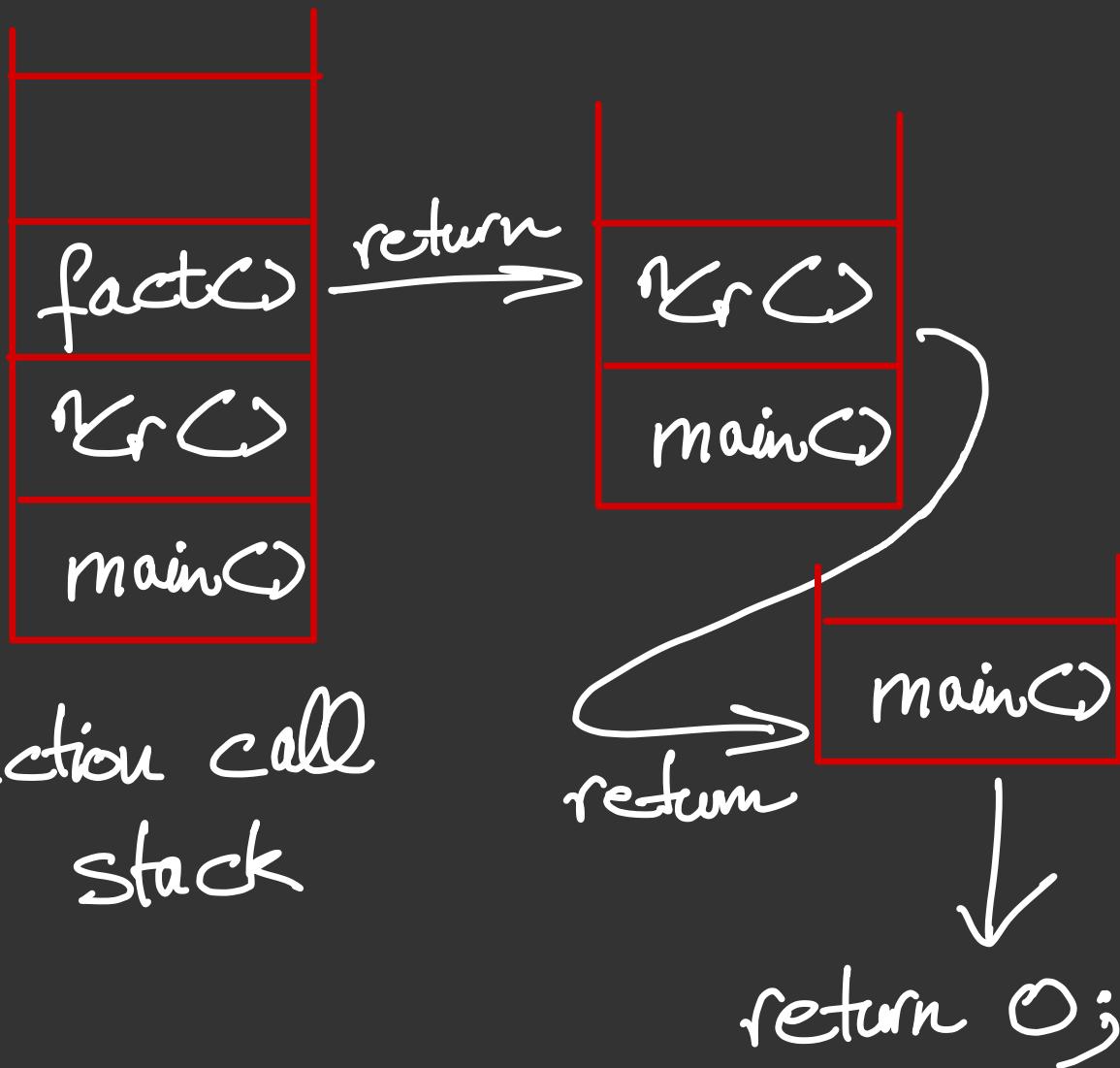
```

main()
{
    ans = nCr(n,r)
    {
        factorial(n)
        return();
    }
}

```

nCr Σ factorial
 factorial(n)
 return();
 {
 }

Function Call Stack



Pass by value

Example:

Main C)

{

n=15;

dummy(n);

cout << n;

}

dummy(int n)

{

n++;

cout << n;

}

Output → 16
15

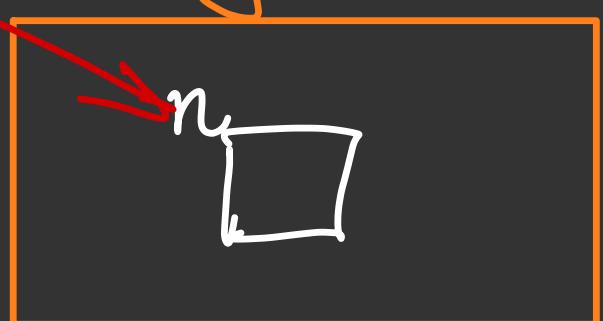
Because

main

Different

dummy

its just that
(there name is
same)



* Variable 'n' in dummy is diff.
and 'n' in main() is different.

Its just while calling
dummy the value of 'n' in
main is assigned to variable
'n' in dummy.

Output Questions

```
1 void update(int a) {  
2     a = a / 2;  
3 }  
4 int main() {  
5     int a = 10;  
6     update(a);  
7     cout << a << endl;  
8 }  
9
```

10

```
1 int update(int a){  
2     a -= 5;  
3     return a;  
4 }  
5  
6 int main() {  
7     int a = 15;  
8     update(a);  
9     cout << a << endl;  
10 }  
11
```

error
functions
returns a
value and
not assigned to
a variable.

```
1 int update(int a){  
2     int ans = a * a;  
3     return ans;  
4 }  
5  
6 int main() {  
7     int a = 14;  
8     a = update(a);  
9     cout << a << endl;  
10 }  
11
```

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Homework Question

① $AP = 3 \times n + 7$

② $a \& b \rightarrow$ total no. of set bits

$$a = 2 \rightarrow 10$$

$$b = 3 \rightarrow \underline{11}$$

no. of 1's $\rightarrow 3$

③ Fibonacci

n^{th} elements

0, 1, 1, 2, 3, 5, 8 - -

→ homework.cpp

