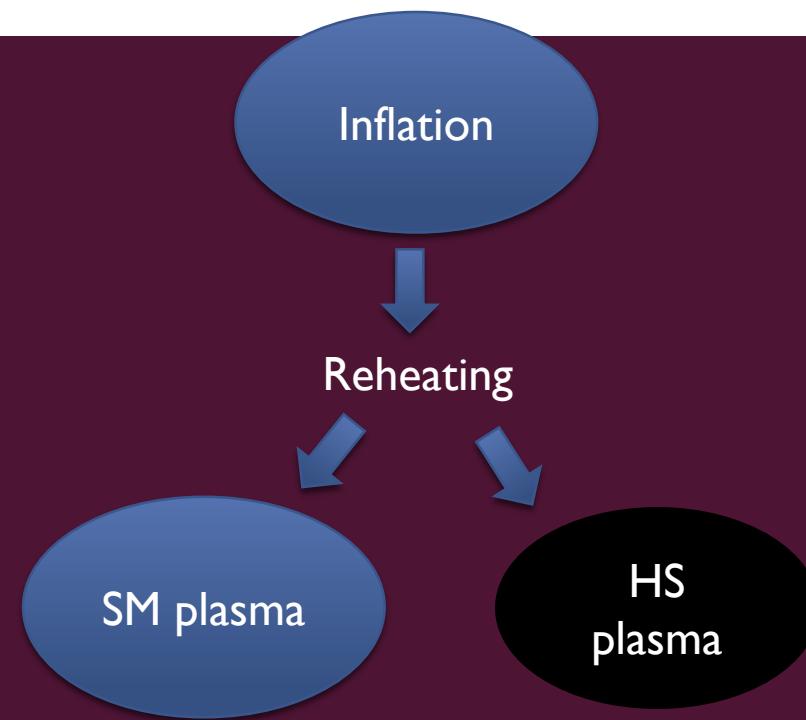

TWO SECTOR REHEATING

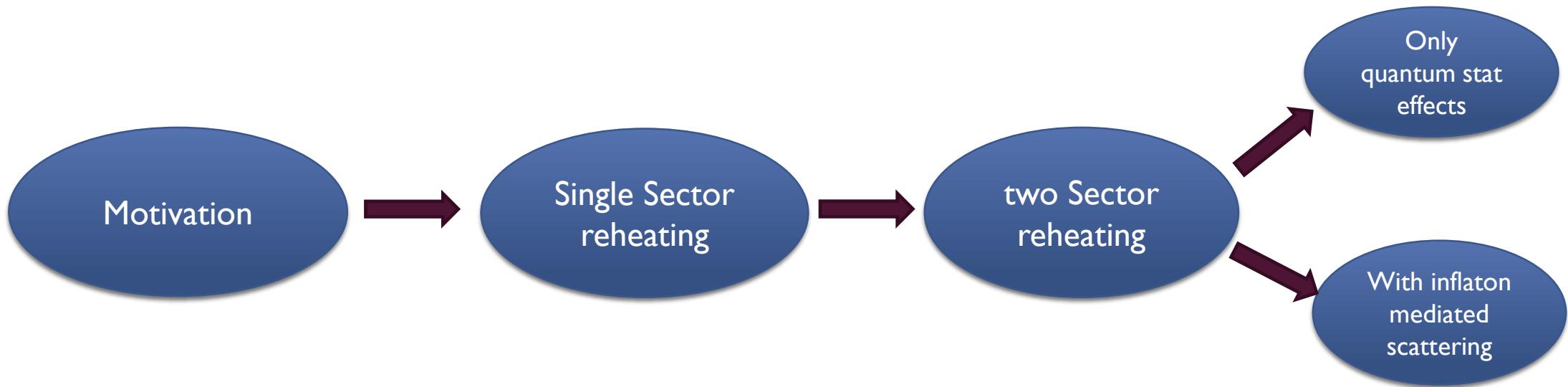
- PRANJAL RALEGANKAR, UIUC

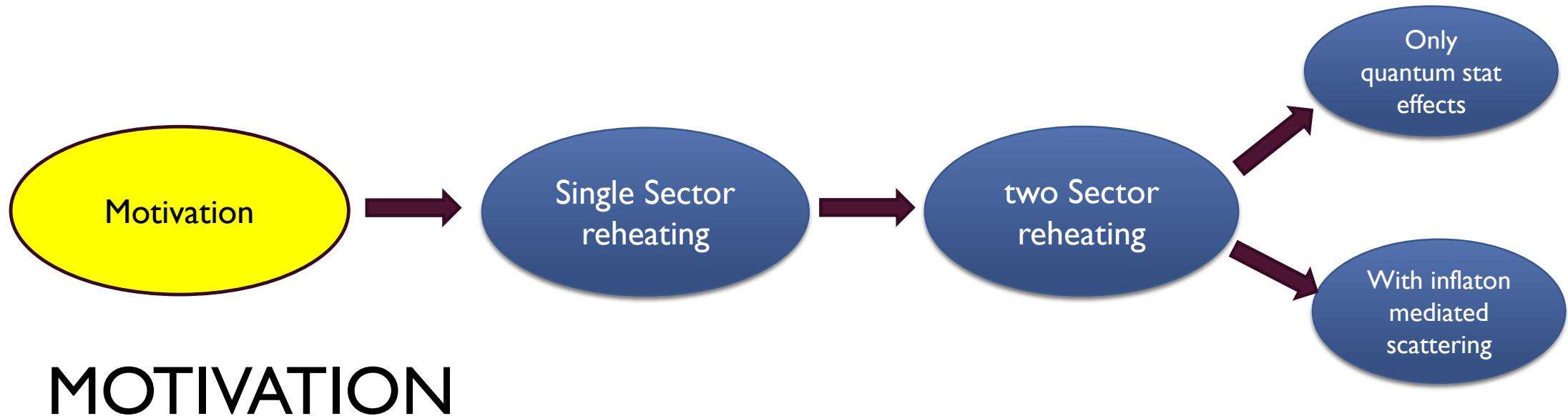
TWO SECTOR REHEATING

- PRANJAL RALEGANKAR, UIUC



CONTENTS

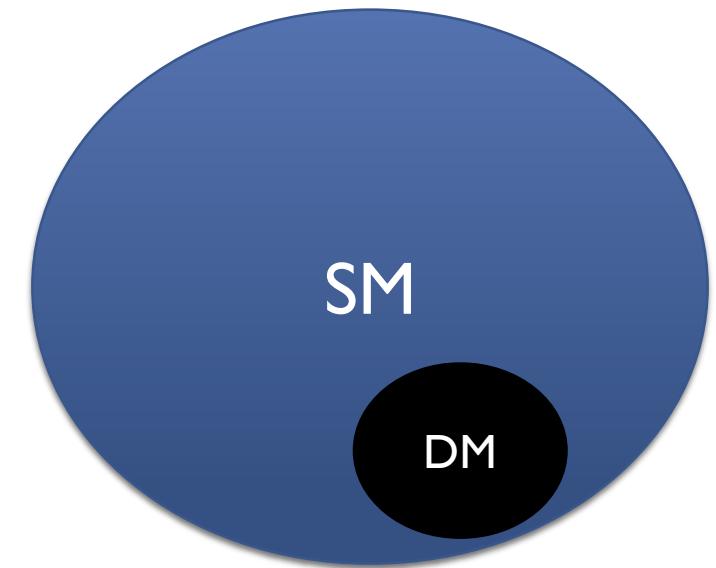




MOTIVATION

- WHY DO WE NEED A HIDDEN SECTOR (HS)?
- WHY TWO SECTOR REHEATING?

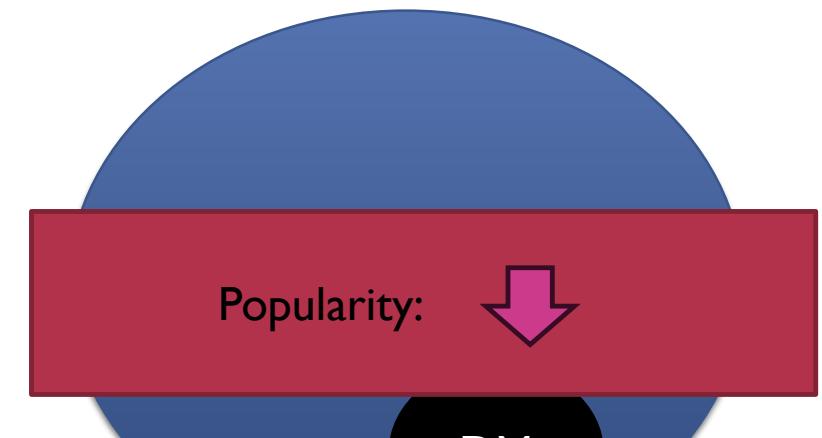
NEED FOR A HIDDEN SECTOR: Traditional DM scenario



WIMP scenario

NEED FOR A HIDDEN SECTOR: Traditional DM scenario

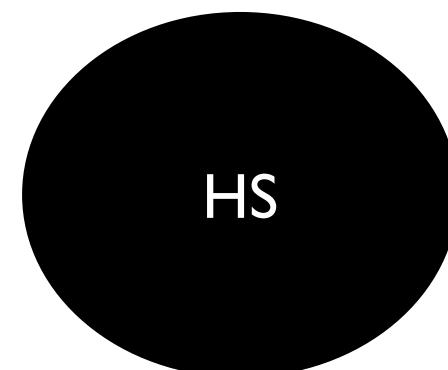
- Dearth of signals in collider, direct and indirect detection experiments reducing the parameters space for traditional WIMP scenario



WIMP scenario

NEED FOR A HIDDEN SECTOR: HS as an alternative

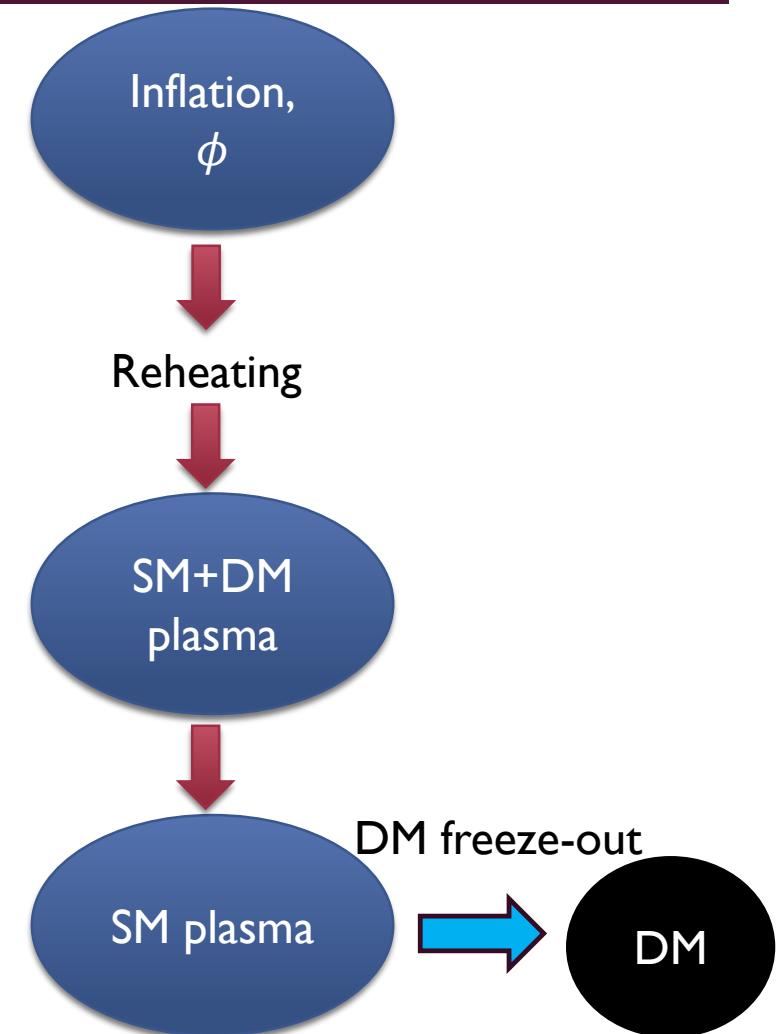
- Dearth of signals in collider, direct and indirect detection experiments reducing the parameters space for traditional WIMP scenario
- A complete sector with its own host of particles decoupled from SM as a possible alternative



POPULATING THE HIDDEN SECTOR: How?

POPULATING THE HIDDEN SECTOR: Traditional DM production

- WIMP DM populated by freeze out mechanism

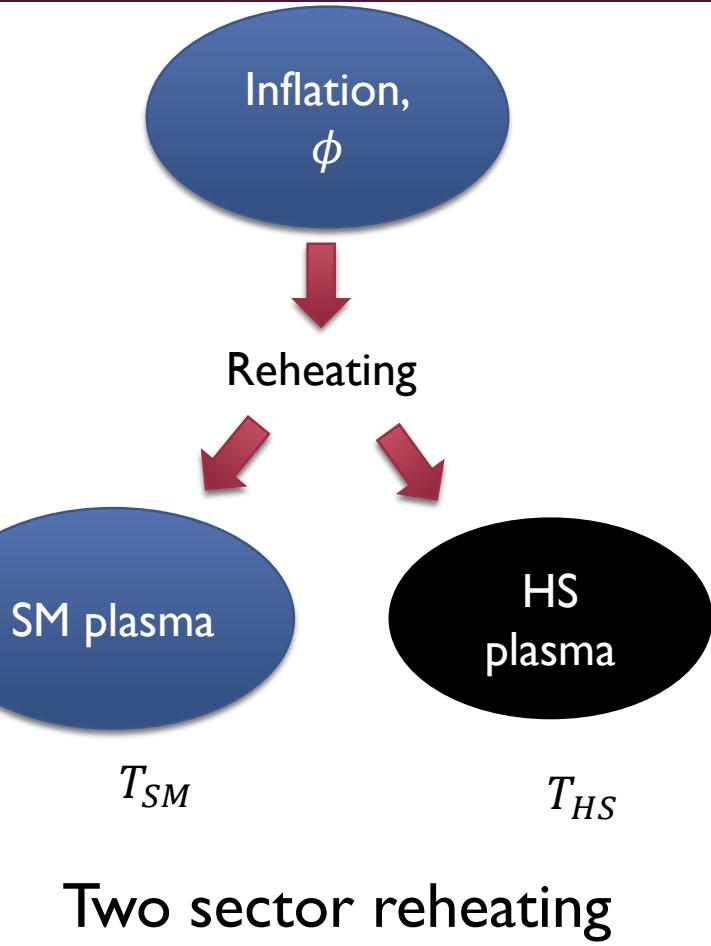


POPULATING THE HIDDEN SECTOR: Asymmetric reheating

- One straightforward way to populate the HS is directly during reheating
- Asymmetric reheating helps in avoiding the stringent N_{eff} constraints

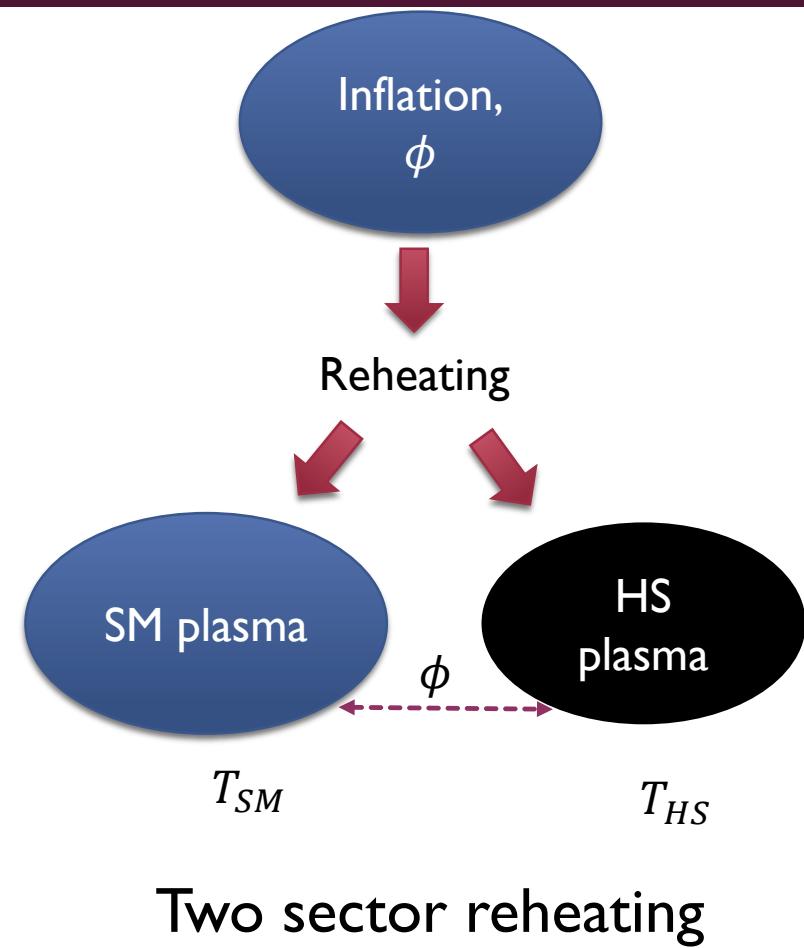
$$\Delta N_{eff} = g_{HS} \left(\frac{T_{HS}}{T_{DM}} \right)^4 \leq 0.46$$

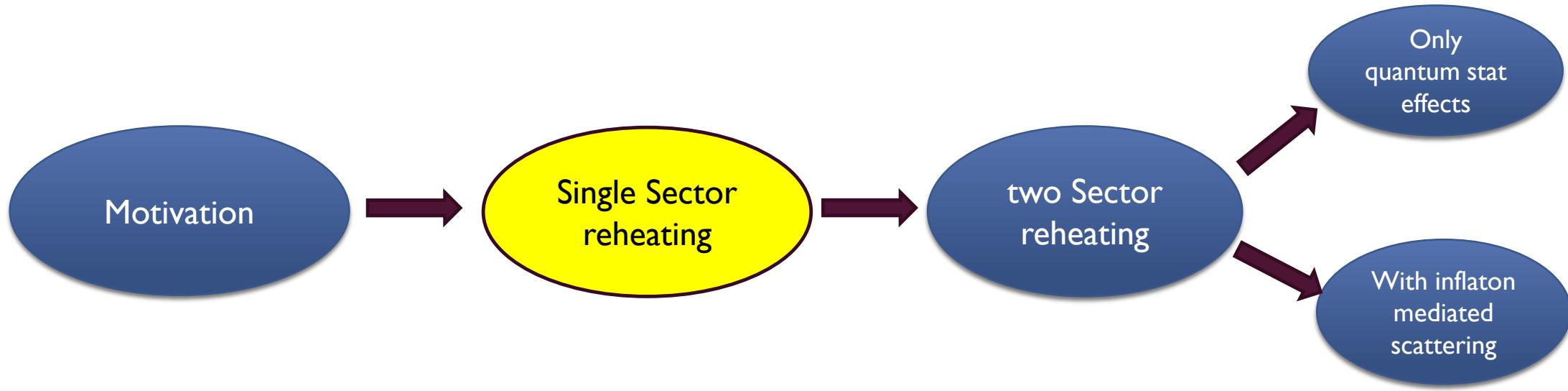
Relativistic degrees of freedom



PRIMARY GOAL: Finding temperature asymmetry

- Inflaton mediated interactions can thermalize the two sectors
Adshead, Cui and Shelton (2016).
- Primary aim to determine the temperature ratio $x = \frac{T_{HS}}{T_{SM}}$
- A first step towards this goal.
Limit to simple perturbative reheating scenario...





REVIEW OF SINGLE SECTOR PERTURBATIVE REHEATING

- UNDERSTAND PERTURBATIVE REHEATING PROCESS
- DEMONSTRATE MODIFICATION DUE TO QUANTUM STATISTICS

SINGLE SECTOR REHEATING: Boltzmann equations and assumptions

Post inflation Boltzmann Equations:

$$\frac{d\rho_\phi}{dt} + 3H\rho_\phi = -\Gamma_\phi\rho_\phi$$

Inflaton density

$$\frac{d\rho}{dt} + 4H\rho = \Gamma_\phi\rho_\phi$$

radiation density

$$H = \frac{1}{\sqrt{3}M_{pl}}\sqrt{\rho_\phi + \rho}$$

Hubble rate

Inflaton decay width

- Generic model independent scenario in perturbative limit
- Post inflaton, inflaton condensate evolves like a cold matter.
- Assume instantaneous thermalization in matter sector $\rho = \alpha T^4$

SINGLE SECTOR REHEATING: Reheating conditions

Post inflation, reheating Boltzmann Equations:

Inflaton density $\rightarrow \frac{d\rho_\phi}{dt} + 3H\rho_\phi \approx 0$

radiation density $\rightarrow \frac{d\rho}{dt} + 4H\rho = \Gamma_\phi \rho_\phi$ Inflaton decay width

Hubble rate $\rightarrow H \approx \frac{1}{\sqrt{3}M_{pl}} \sqrt{\rho_{\phi,I}} a^{-3/2}$

- Initial conditions: $\rho_{\phi,I}$ large non zero value; $\rho_I = 0$.
- Perturbative reheating era:
 $H \gg \Gamma_\phi$
- Reheating ends when
 $H \sim \Gamma_\phi$

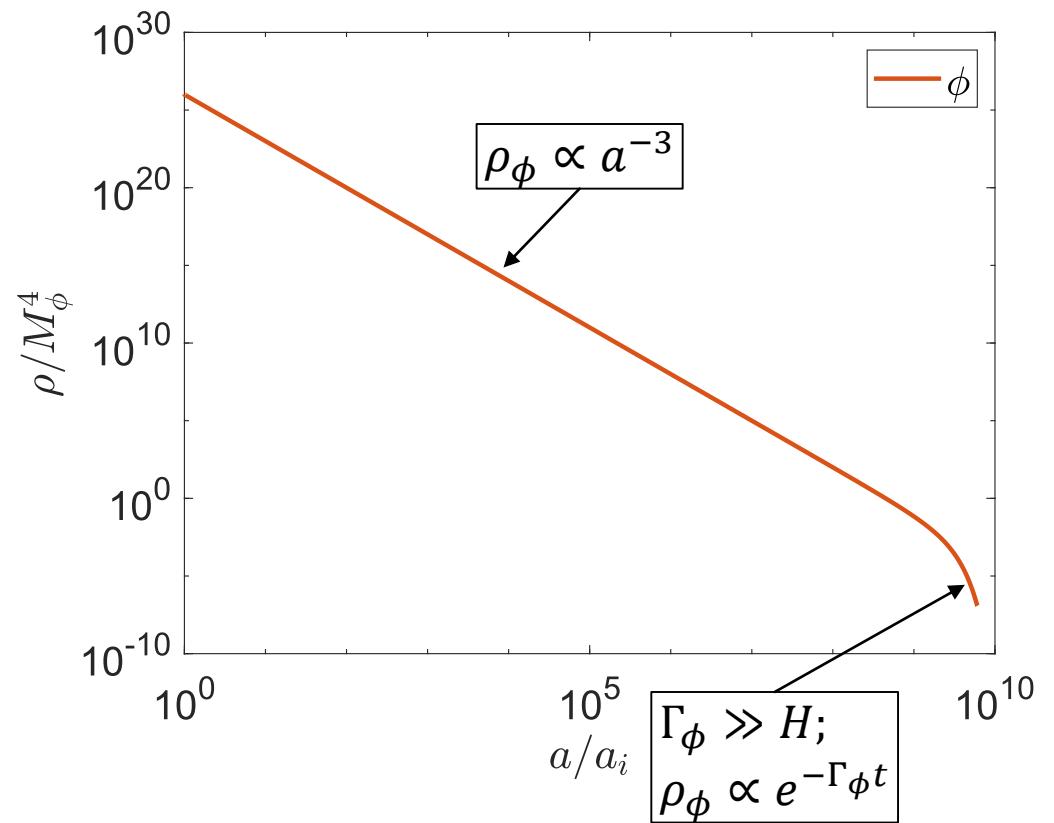
SINGLE SECTOR REHEATING: Inflaton condensate evolves like cold matter

Post inflation, reheating Boltzmann Equations:

$$\frac{d\rho_\phi}{dt} + 3H\rho_\phi \approx 0$$

$$\frac{d\rho}{dt} + 4H\rho = \Gamma_\phi \rho_\phi$$

$$H \approx \frac{1}{\sqrt{3}M_{pl}} \sqrt{\rho_{\phi,I}} a^{-3/2}$$



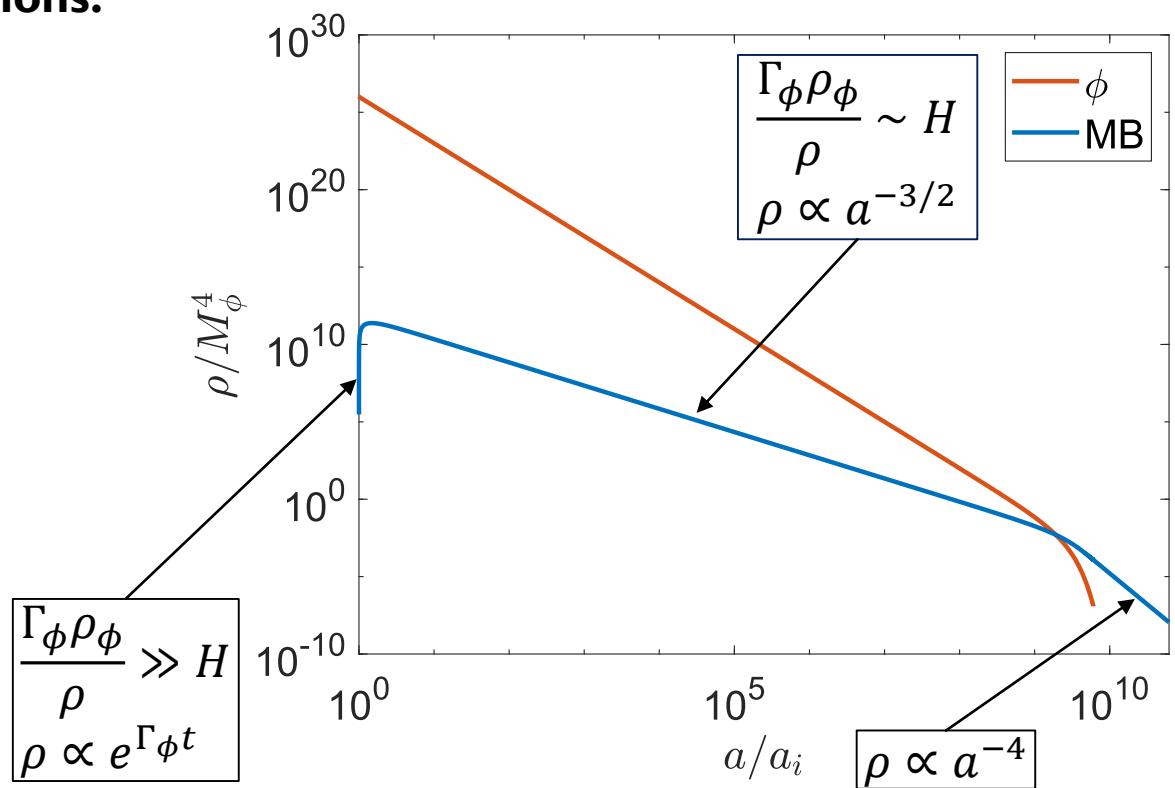
SINGLE SECTOR REHEATING: Radiation evolution non-adiabatic

Post inflation, reheating Boltzmann Equations:

$$\frac{d\rho_\phi}{dt} + 3H\rho_\phi \approx 0$$

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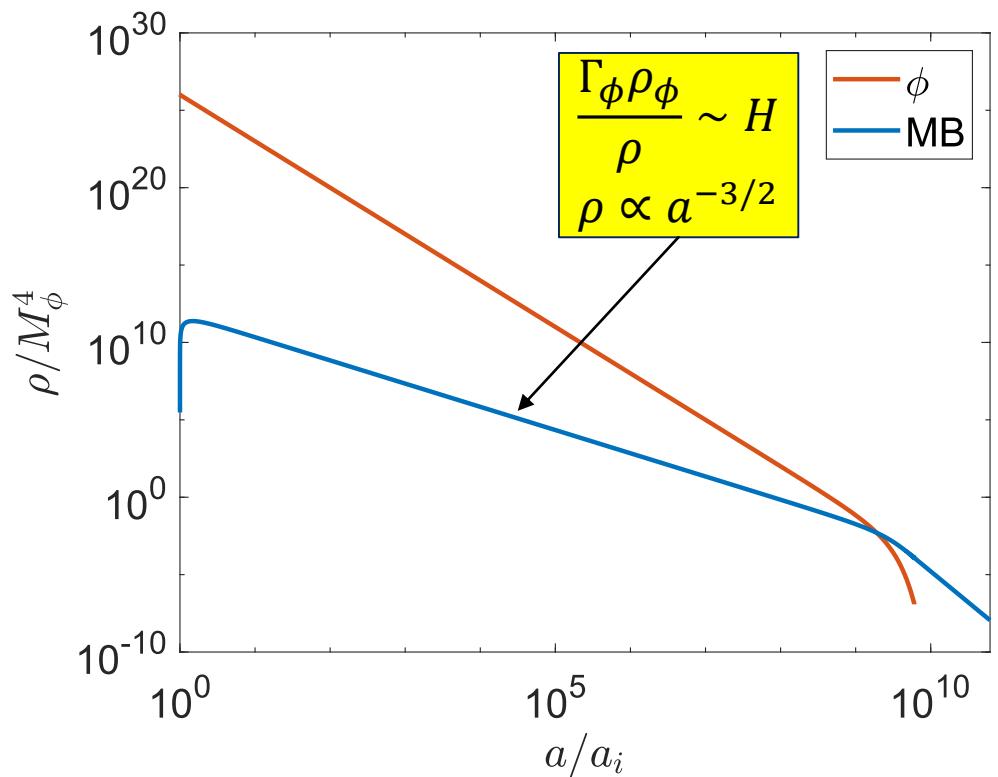


SINGLE SECTOR REHEATING: Attractor solution!

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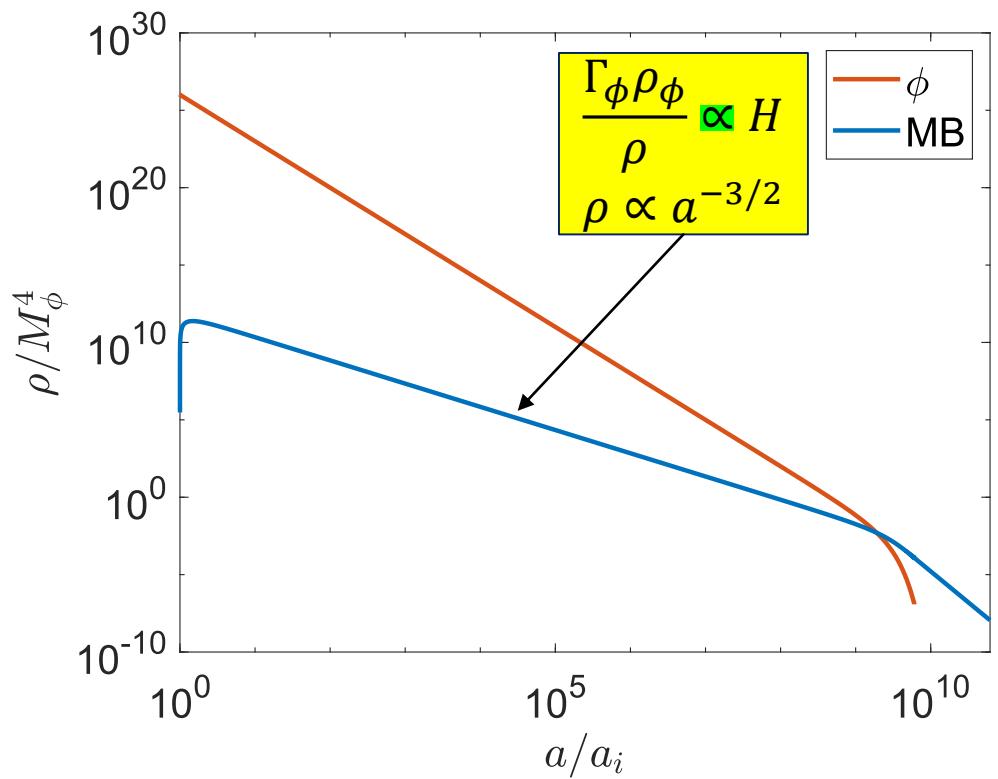


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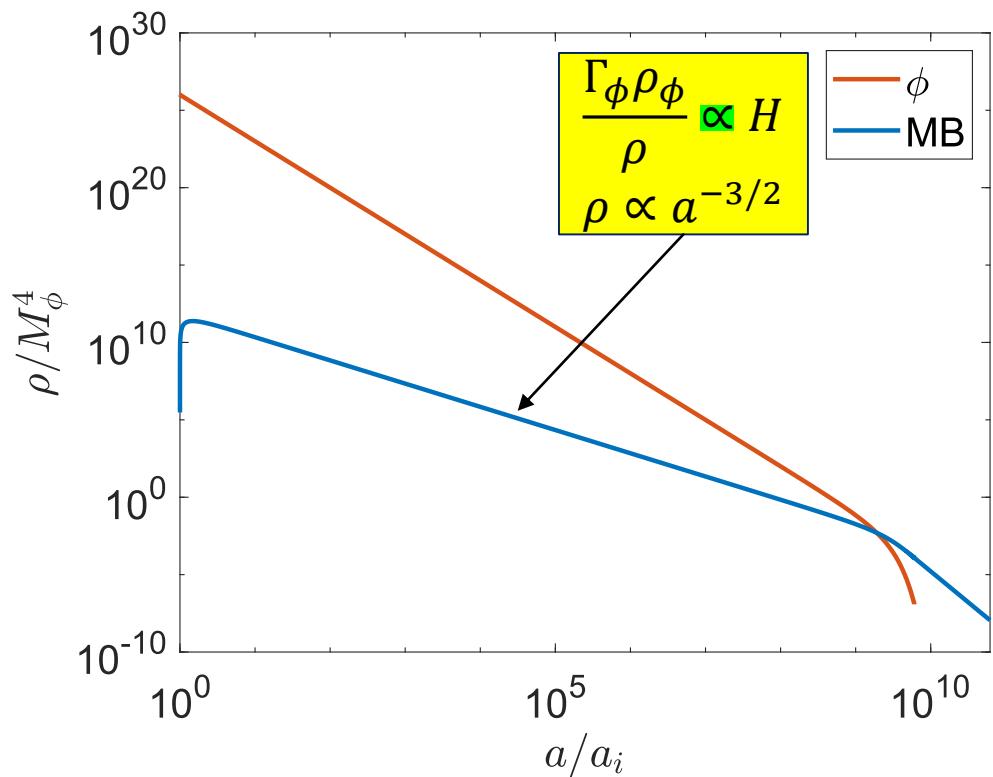
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$$T = \frac{2\sqrt{3}}{5\alpha} \frac{M_{pl}}{M_\phi} \Gamma_\phi \sqrt{\rho_{\phi,I}} \left(\frac{a}{a_I}\right)^{-3/8}$$

No dependence on temperature history



SINGLE SECTOR REHEATING: Attractor solution!

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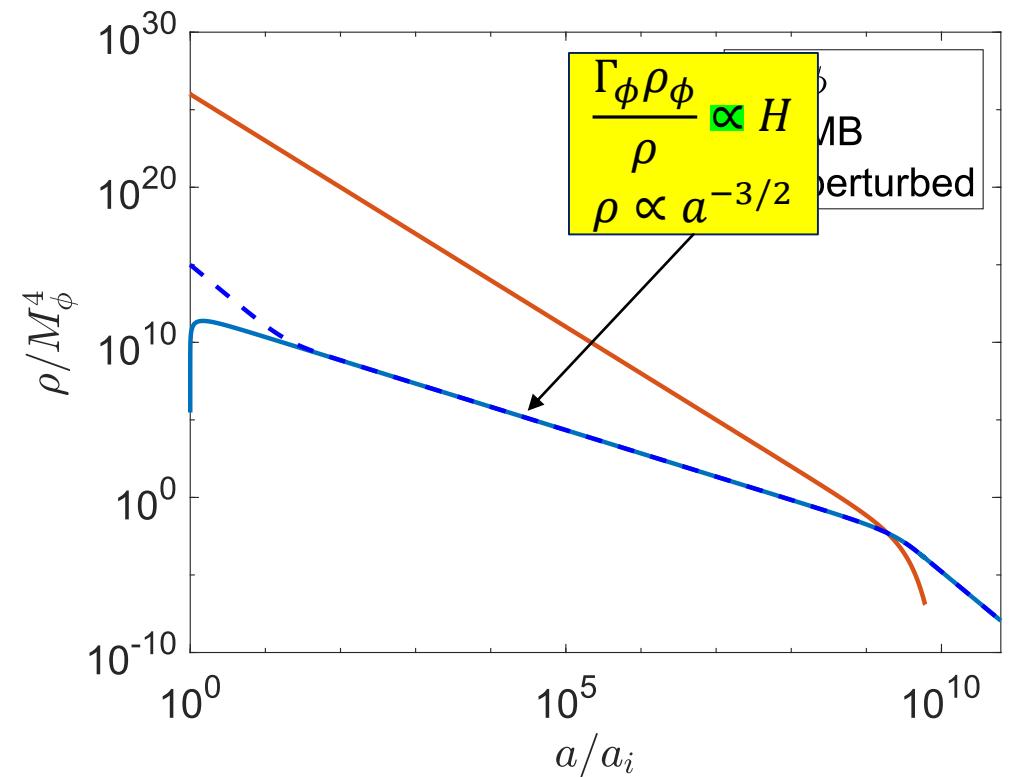
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SINGLE SECTOR REHEATING: Reheat temperature independent of initial conditions

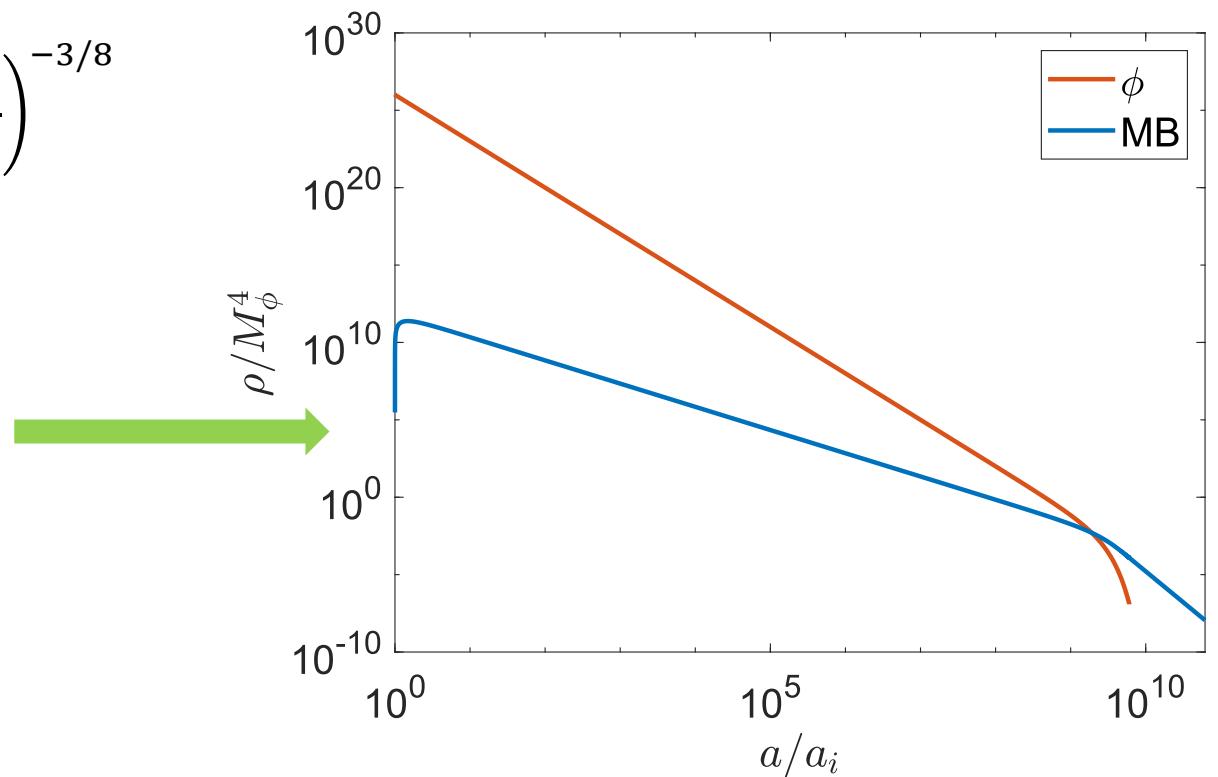
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Input arbitrary initial condition of inflaton and radiation bath



SINGLE SECTOR REHEATING: Reheat temperature independent of initial conditions

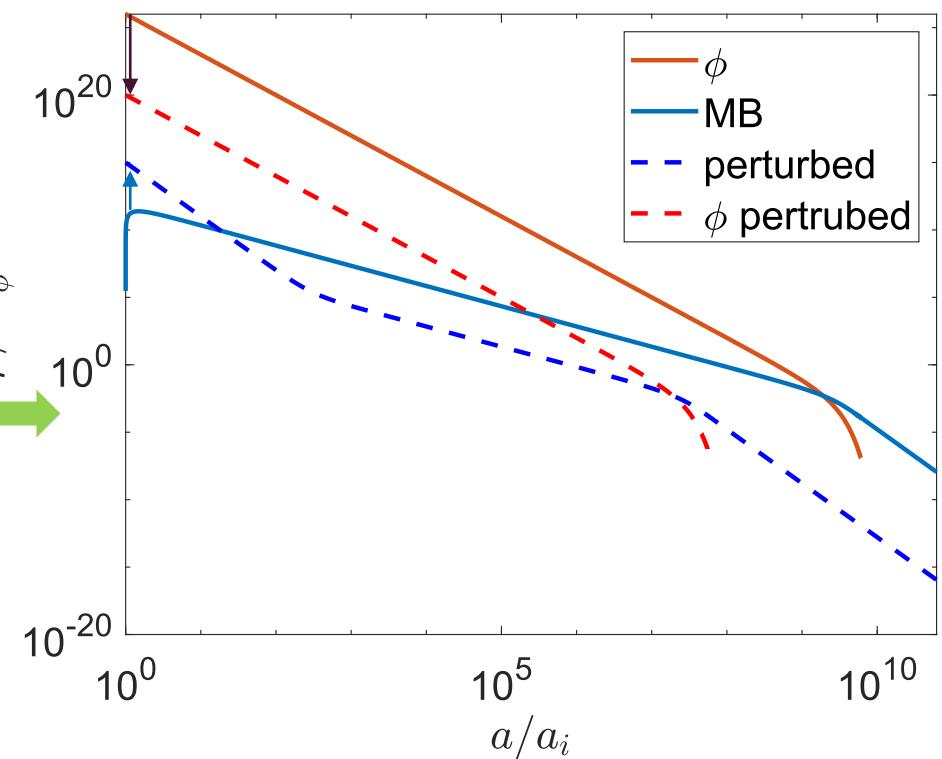
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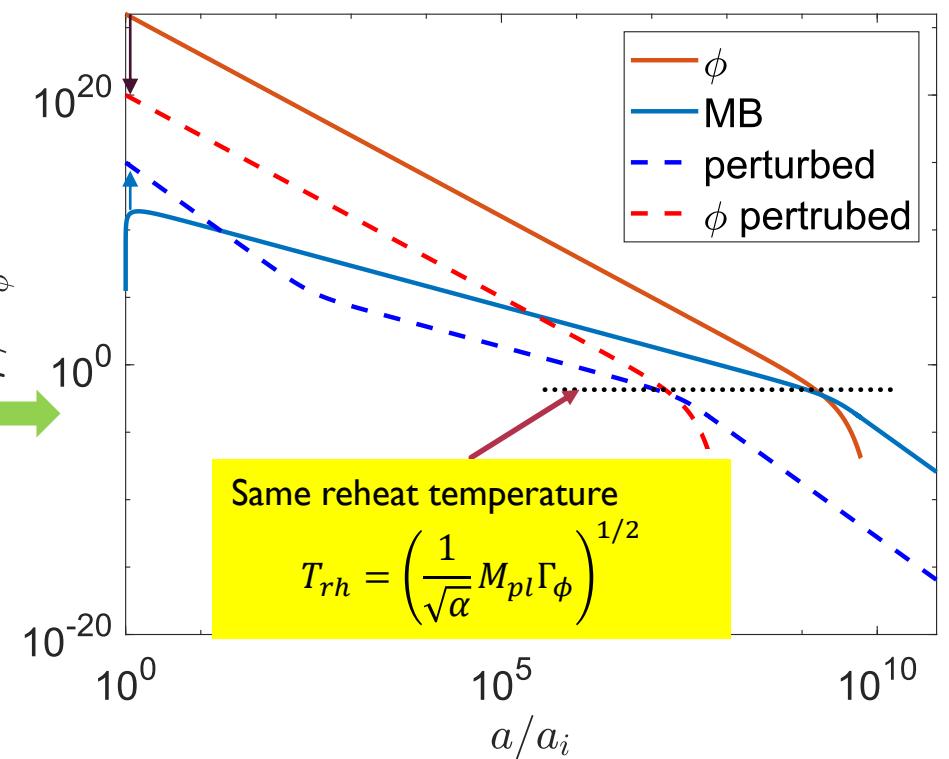
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Input arbitrary initial condition of inflaton and radiation bath

Chung, Kolb and Riotto, (1999)

$$\rho/M_\phi^4$$



SINGLE SECTOR REHEATING: Temperature dependence in Γ_ϕ

$$\frac{d\rho_\phi}{dt} + 3H\rho_\phi \approx 0$$

$$\frac{d\rho}{dt} + 4H\rho = \Gamma_\phi\rho_\phi$$

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- Feedback from Bose enhancement or Pauli Blocking alters inflaton decay width

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- Feedback from Bose enhancement or Pauli Blocking alters inflaton decay width

Bosons

$$\Gamma_\phi(T) = \Gamma_0 \frac{e^{M_\phi/2T} + 1}{e^{M_\phi/2T} - 1}$$

Fermions

$$\Gamma_\phi(T) = \Gamma_0 \frac{e^{M_\phi/2T} - 1}{e^{M_\phi/2T} + 1}$$

SINGLE SECTOR REHEATING: Temperature dependence in Γ_ϕ

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- Feedback from Bose enhancement or Pauli Blocking alters inflaton decay width

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$T \gg M_\phi$

$$\Gamma_\phi(T) \approx 4\Gamma_0 T / M_\phi$$

$T \ll M_\phi$

$$\Gamma_\phi(T) \approx \Gamma_0$$

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SINGLE SECTOR REHEATING: Temperature dependence in Γ_ϕ

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Bose-enhancement

Fermions

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Pauli-blocking

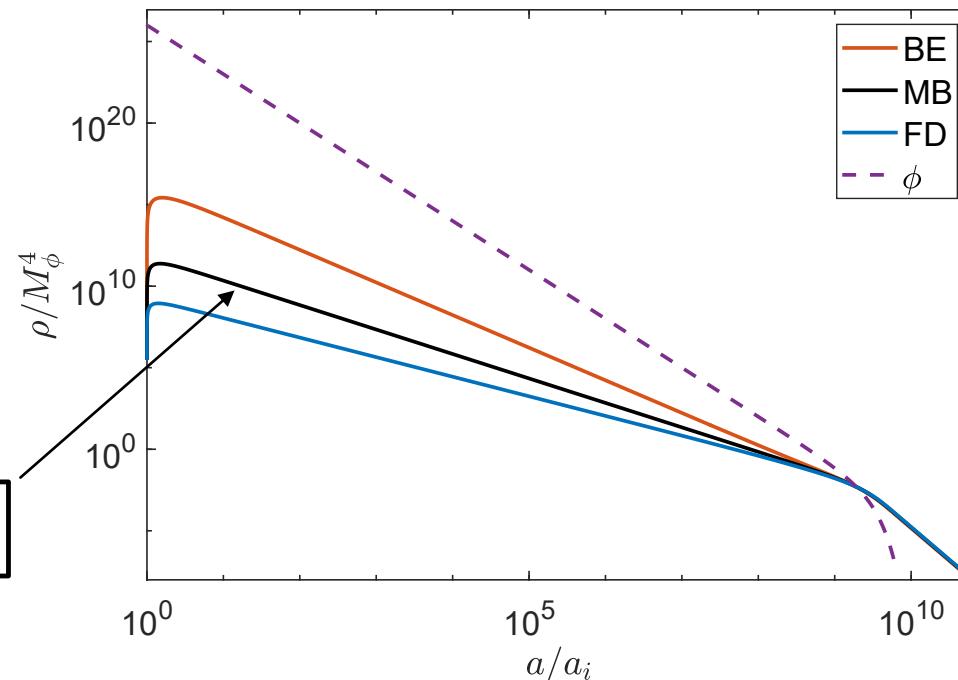
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$$\frac{\Gamma_0 \rho_\phi}{\rho} \propto H$$



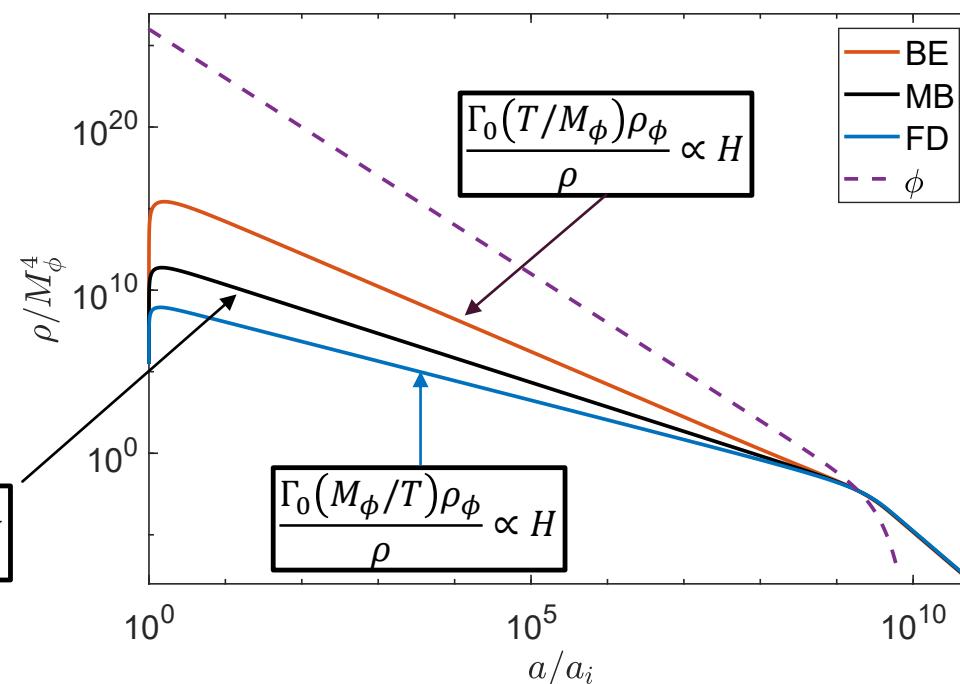
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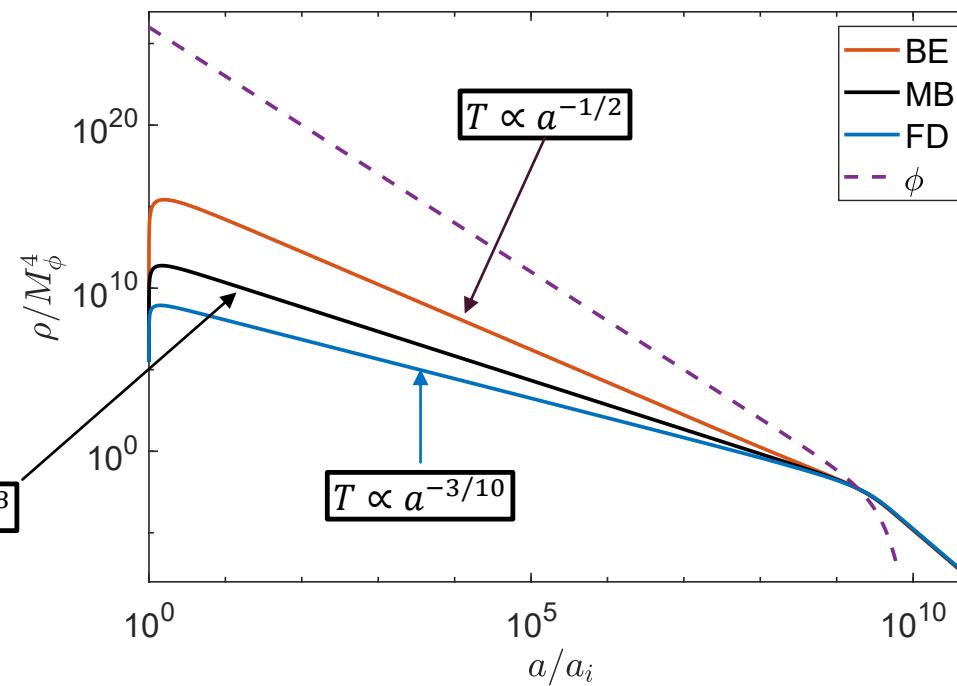
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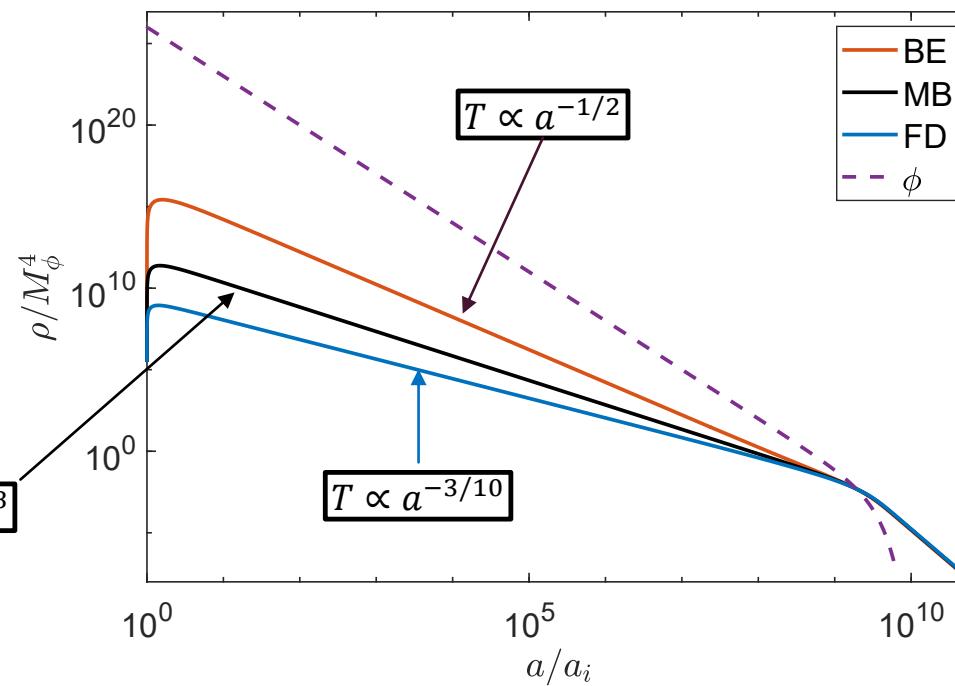
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This is for $T_{rh} < M_\phi$

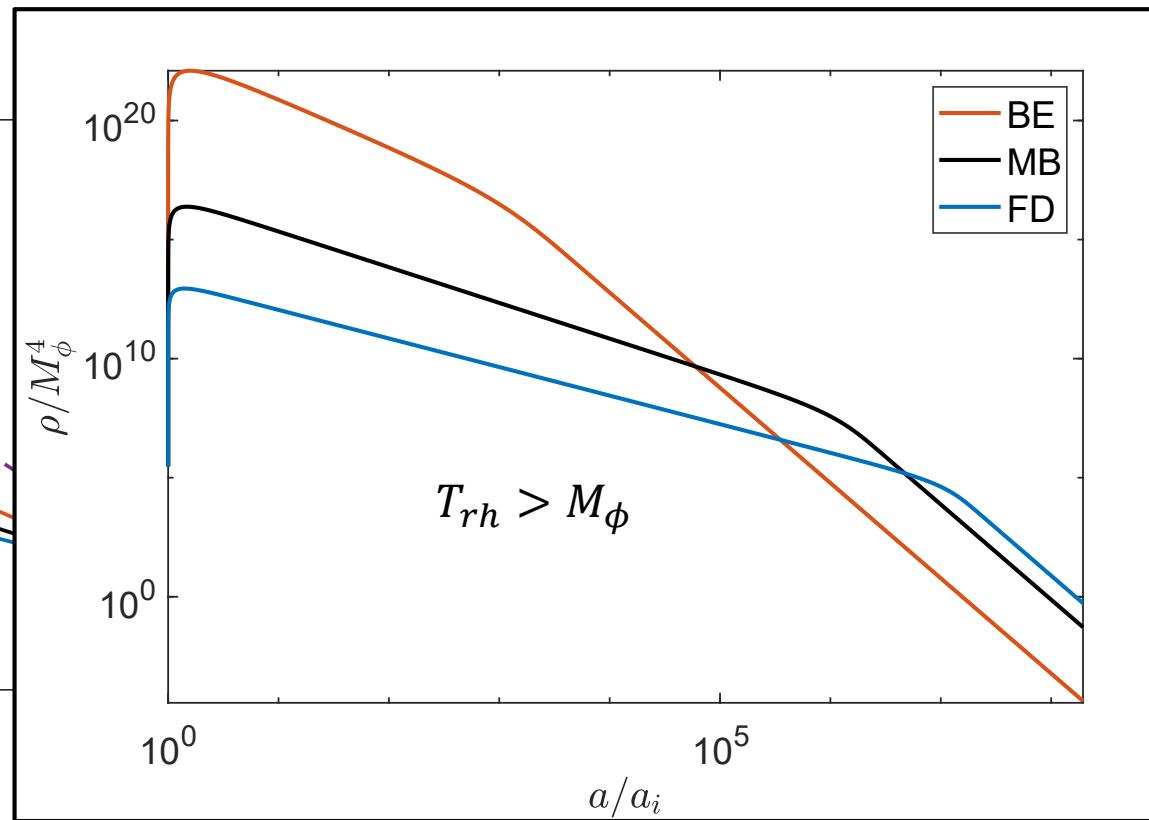
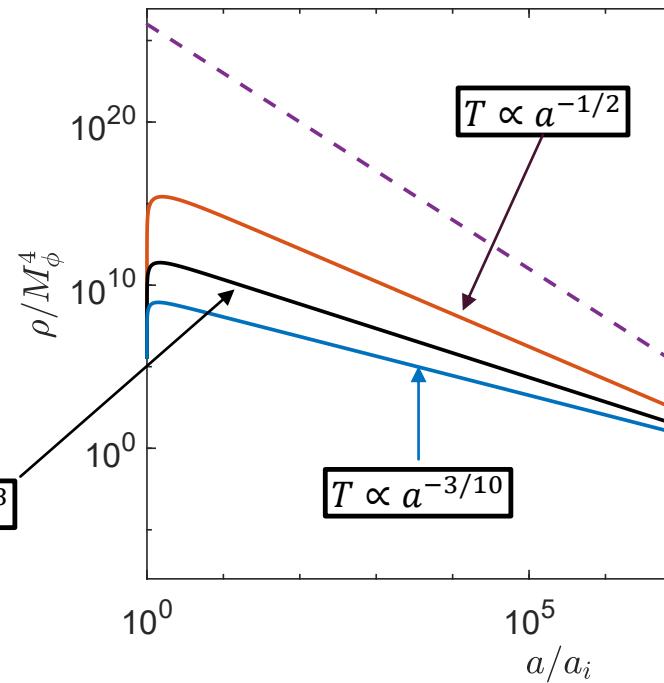
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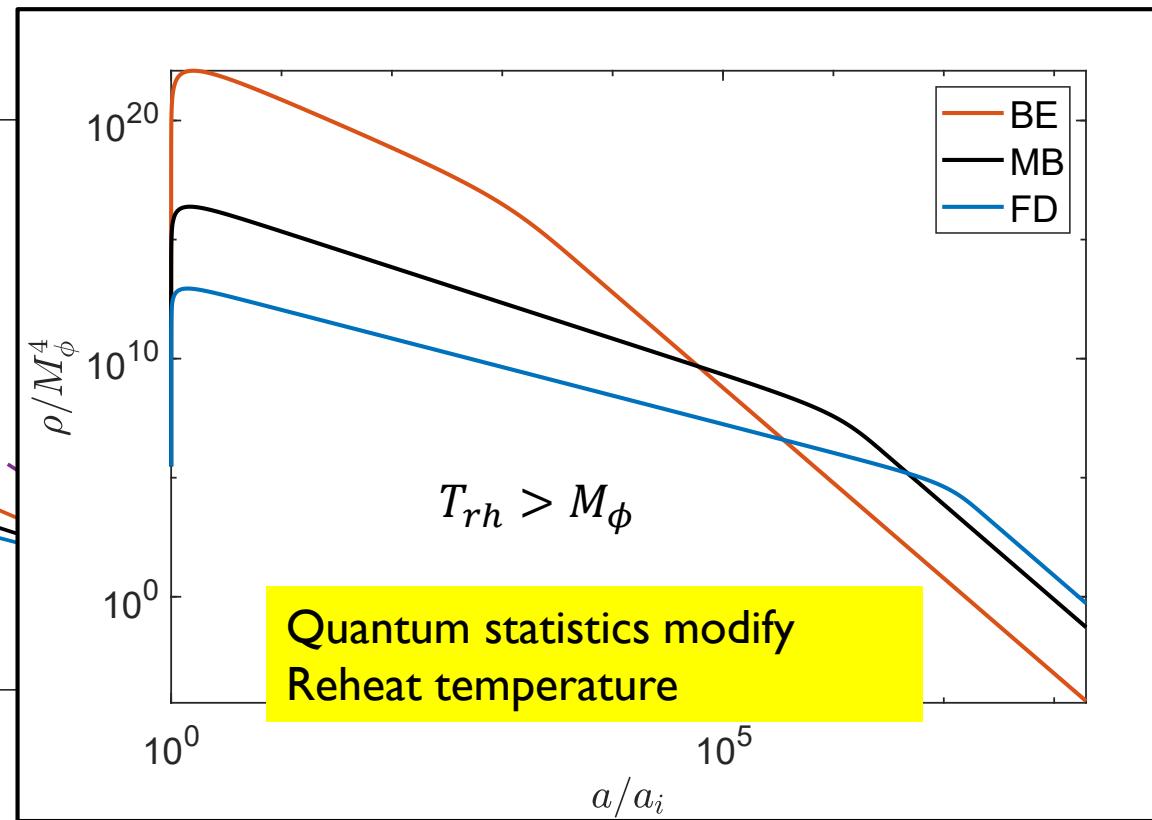
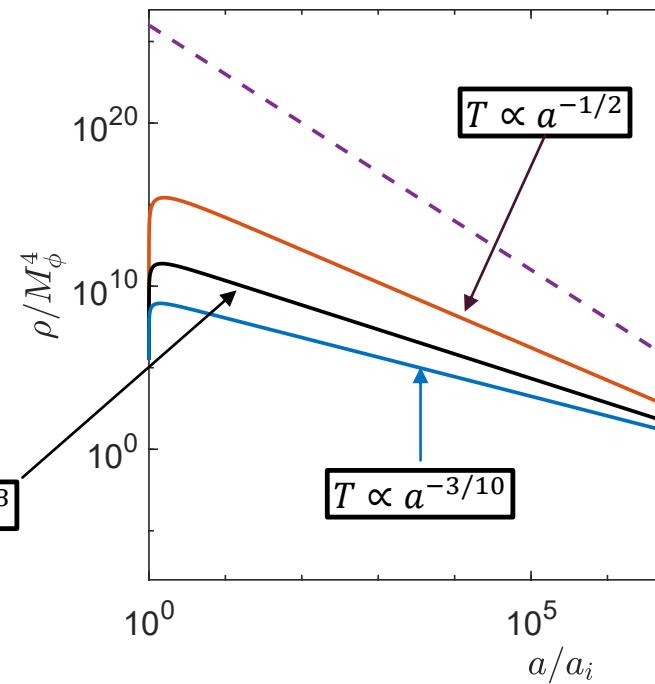
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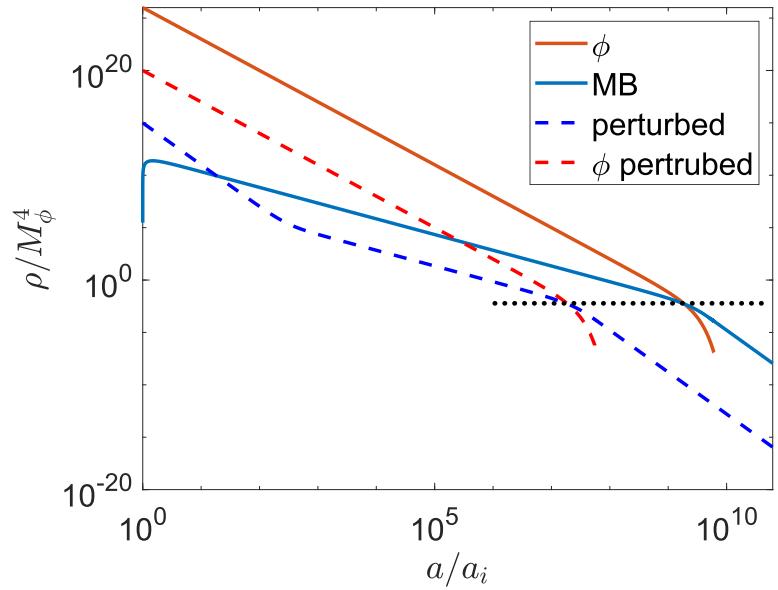
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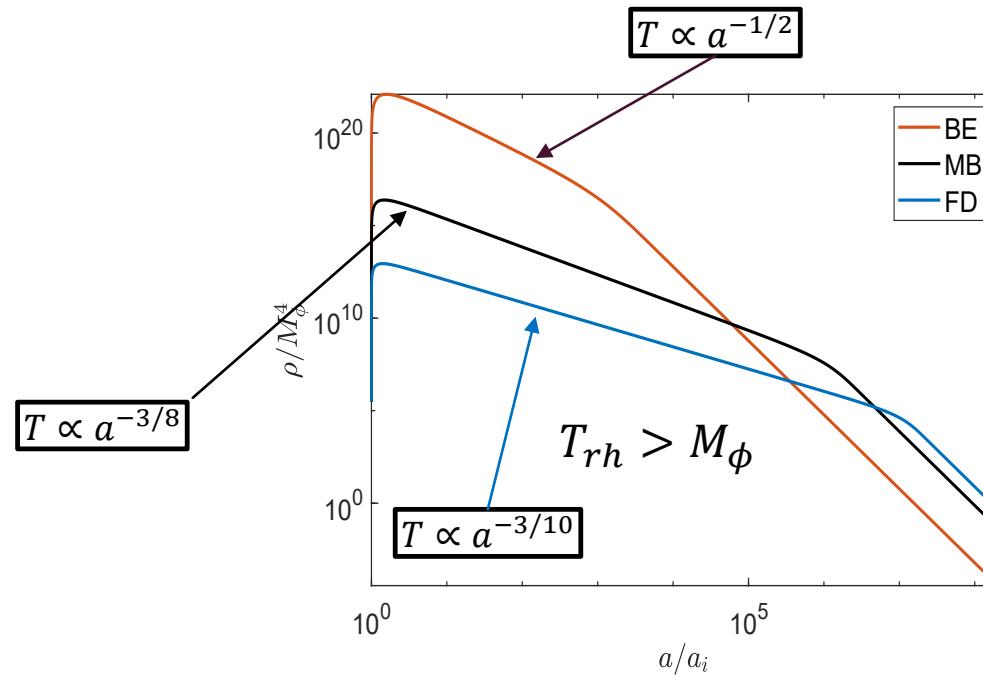
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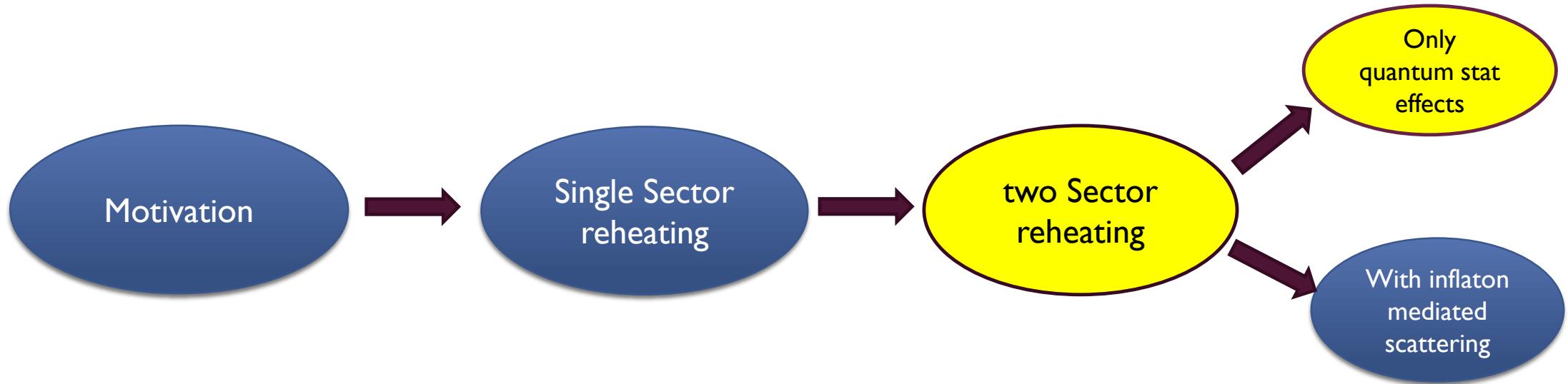
SINGLE SECTOR REHEATING: Summary



Reheat temperature independent of initial conditions



Quantum statistics can modify reheat temperature



TWO SECTOR REHEATING

- EFFECTS FROM QUANTUM STATISTICS- NEGLECT INFLATON MEDIATED INTERACTIONS
- EFFECTS FROM INFLATON MEDIATED INTERACTIONS
- REVIEW OF ASSUMPTIONS

NON INTERACTING SECTORS: Boltzmann equations

Post inflation, reheating Boltzmann Equations:

$$\frac{d\rho_\phi}{dt} + 3H\rho_\phi \approx 0$$

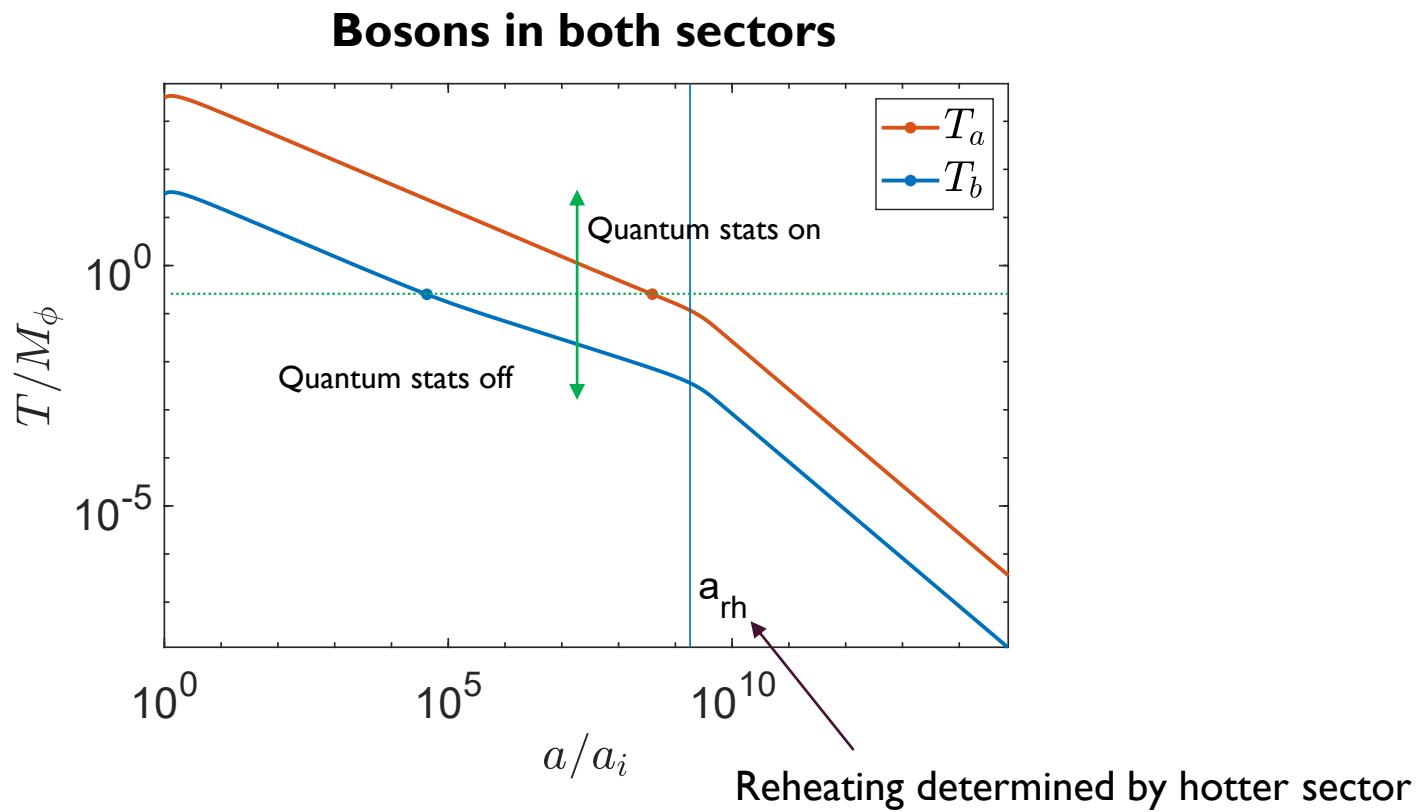
$$\frac{d\rho_a}{dt} + 4H\rho_a = \Gamma_{\phi,a}\rho_\phi$$

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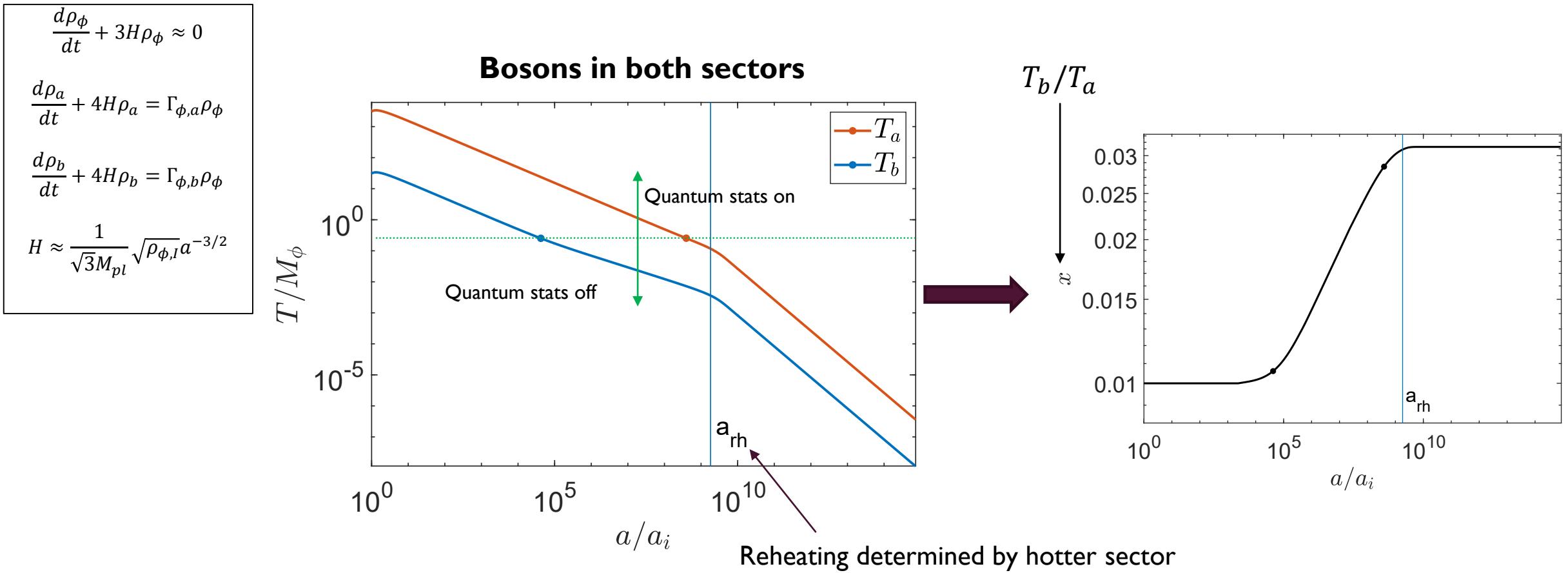
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NON INTERACTING SECTORS: Final temperature ratio fixed after reheating

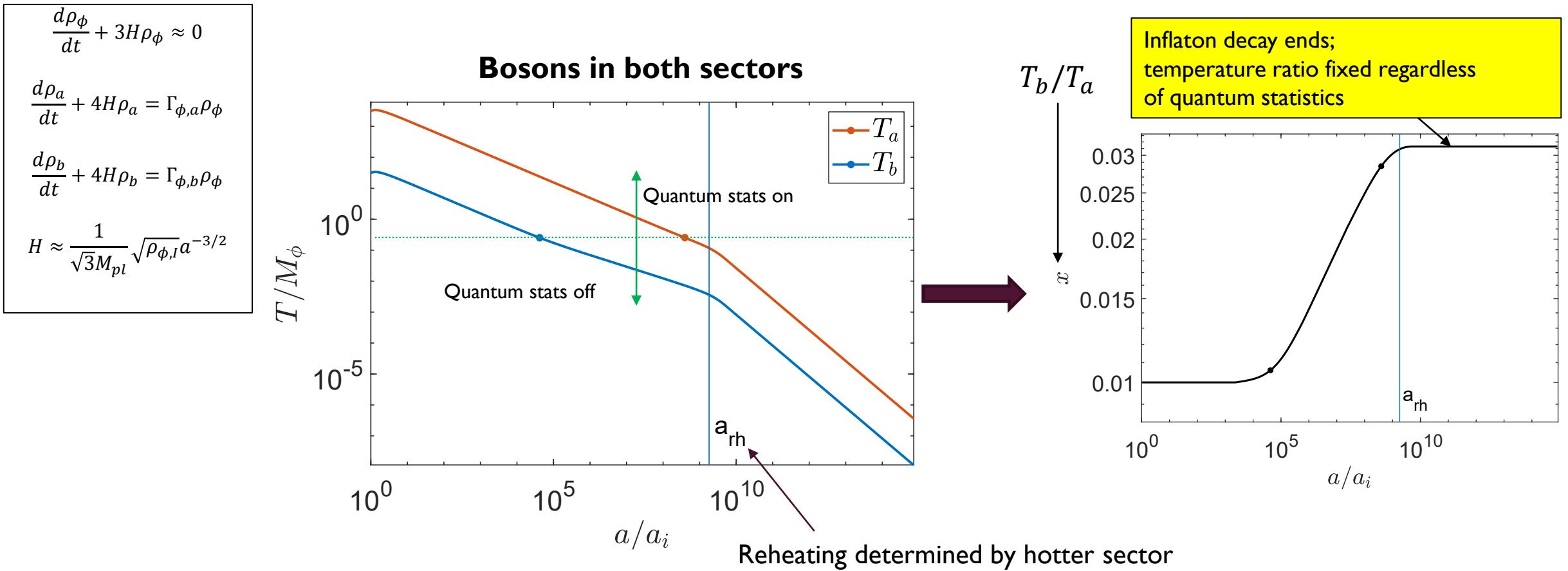
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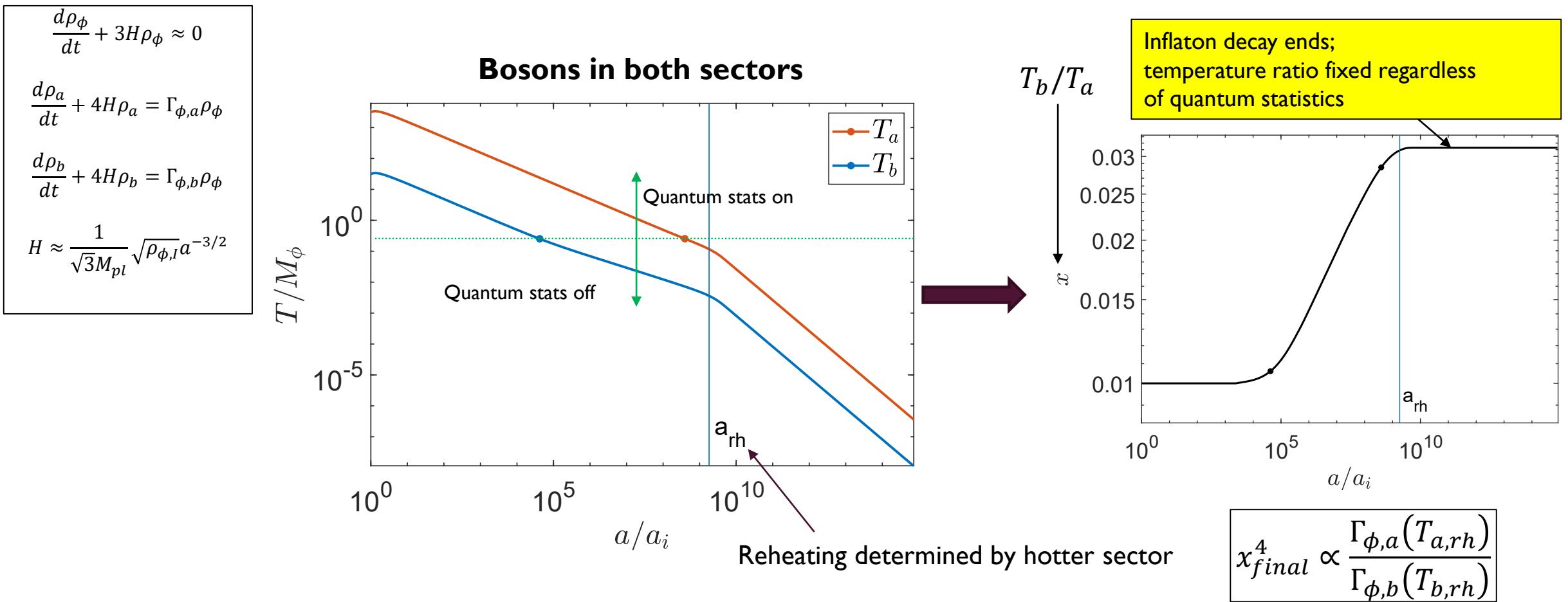
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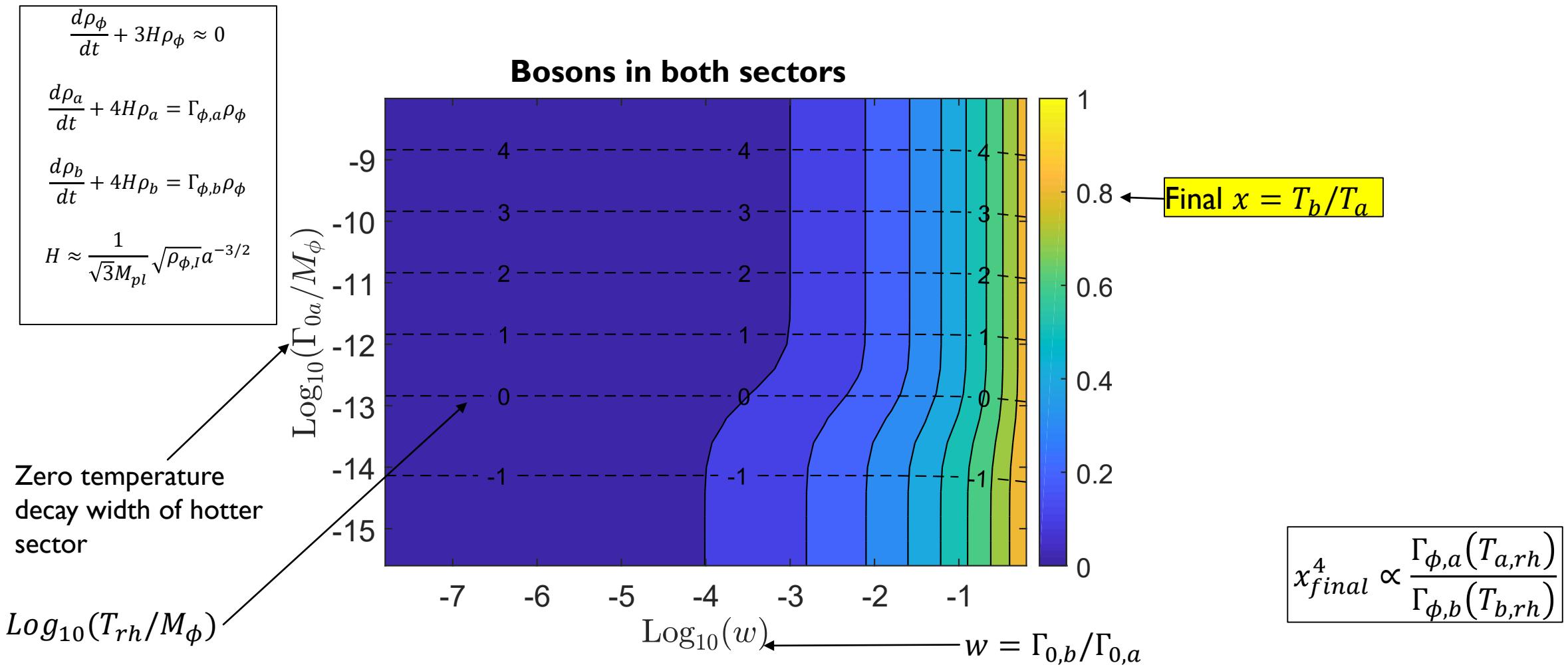
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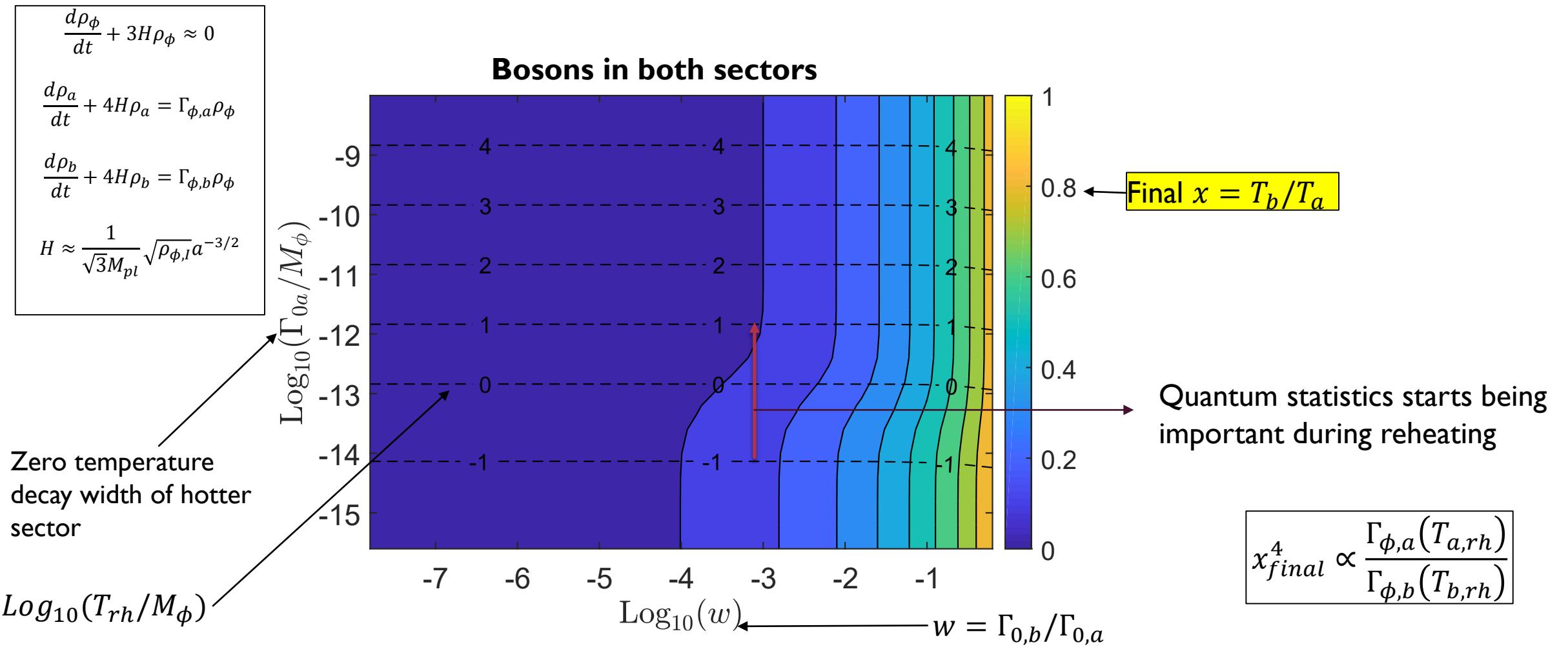
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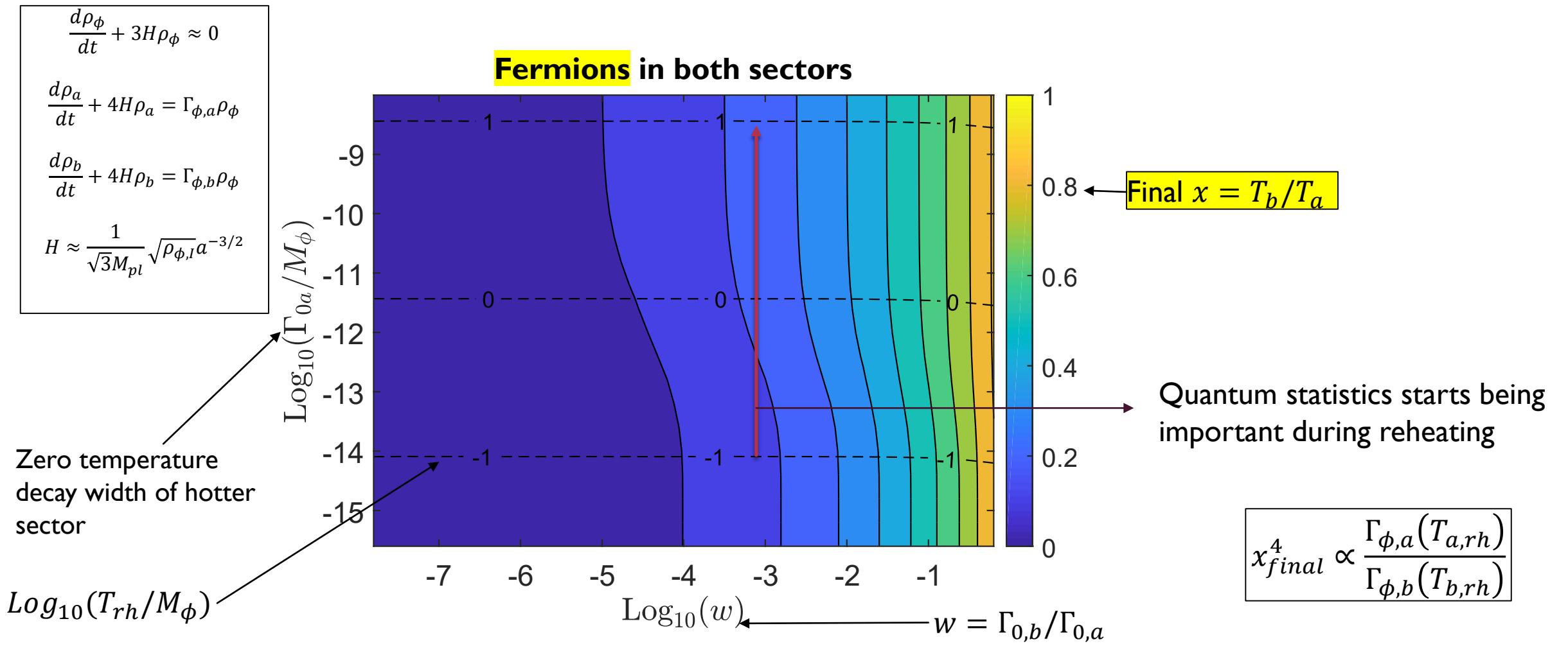
NON INTERACTING SECTORS: Quantum statistics shift final temperature ratio



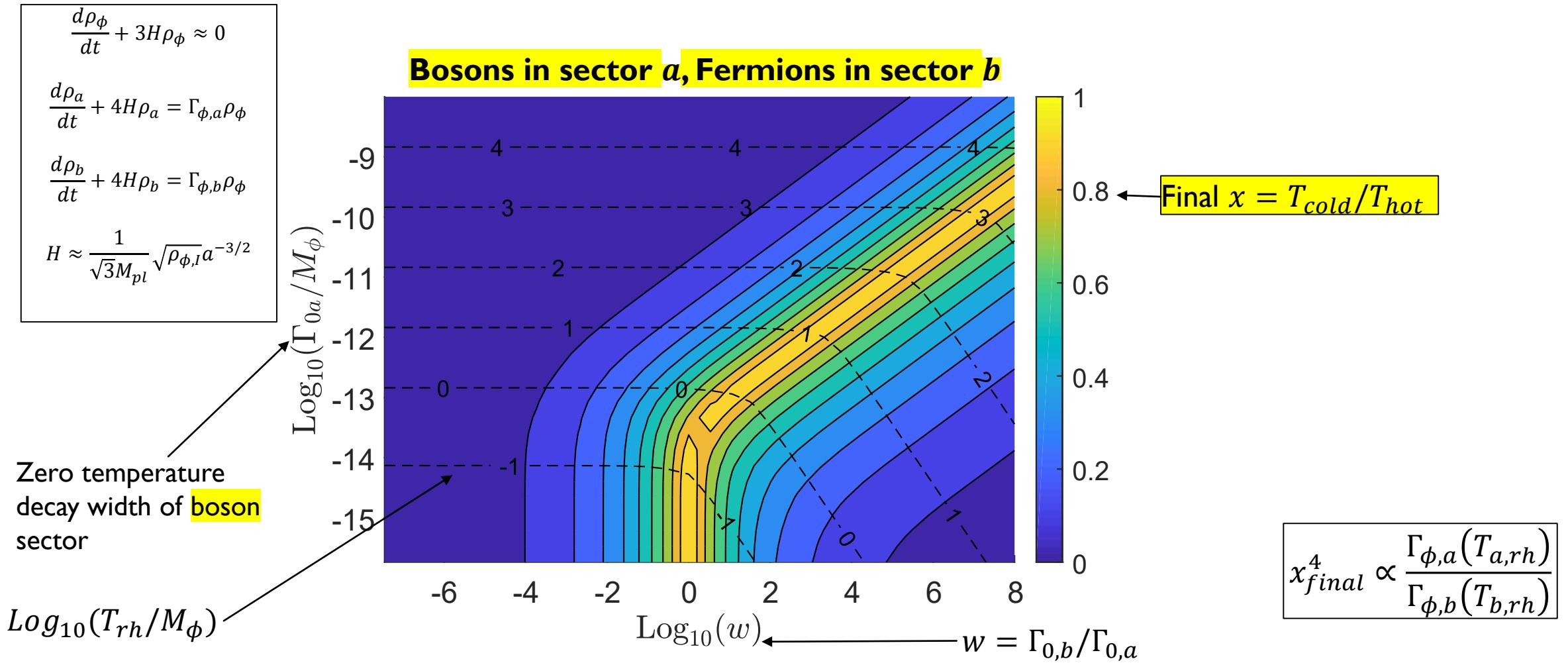
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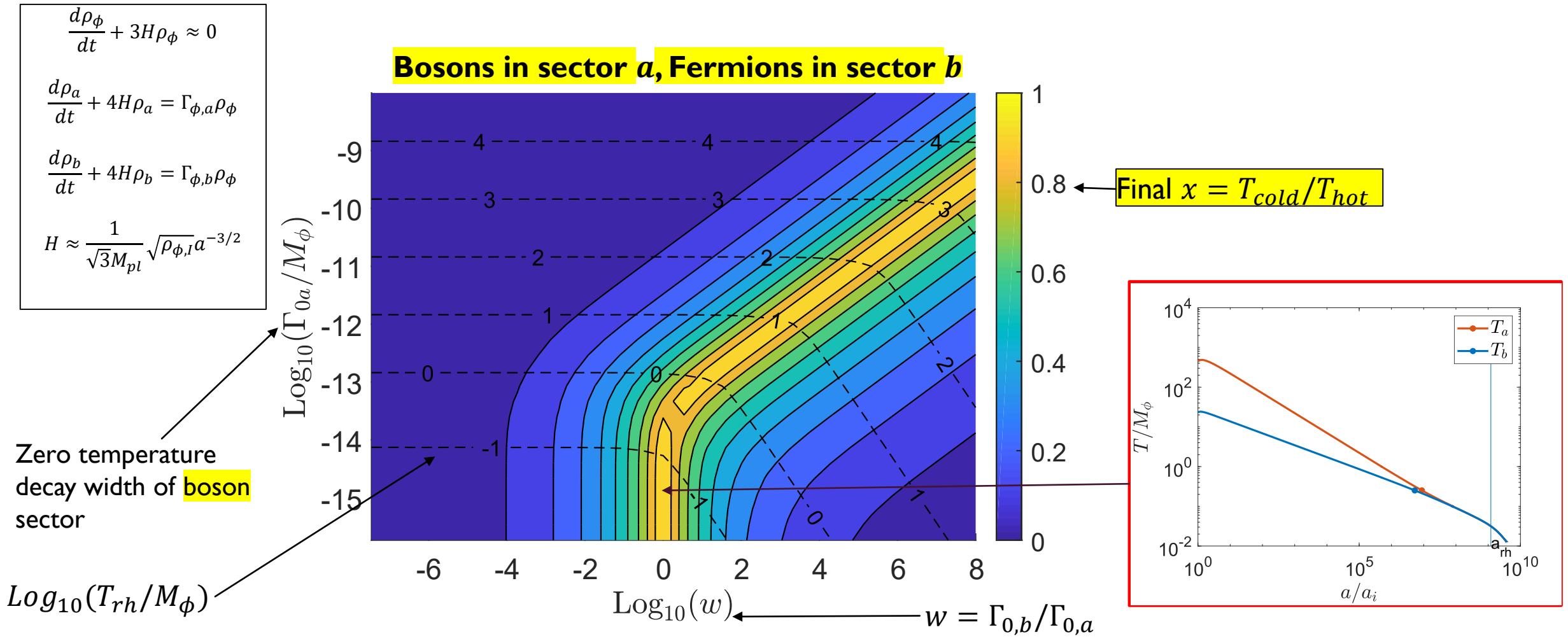
NON INTERACTING SECTORS: Quantum statistics shift final temperature ratio



NON INTERACTING SECTORS: Non trivial structure when different quantum statistics



NON INTERACTING SECTORS: Non trivial structure when different quantum statistics



NON INTERACTING SECTORS: Non trivial structure when different quantum statistics

$$\frac{d\rho_\phi}{dt} + 3H\rho_\phi \approx 0$$

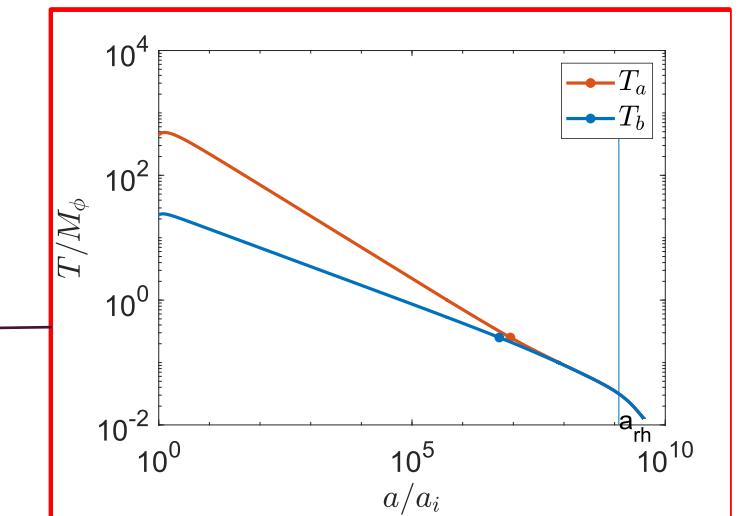
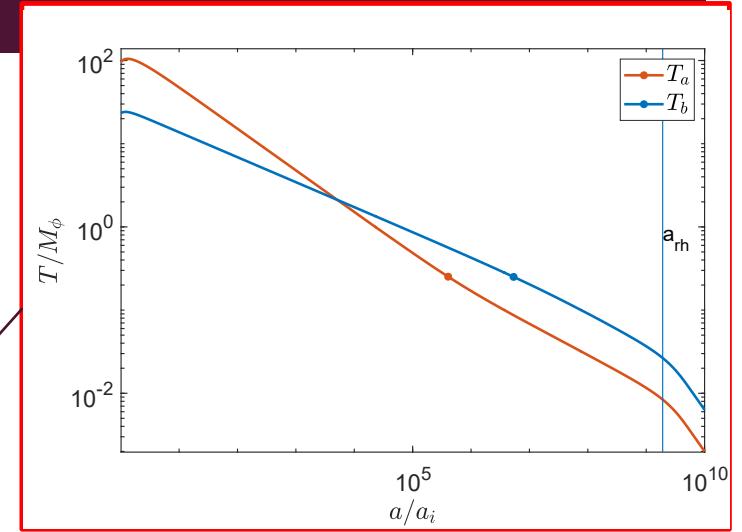
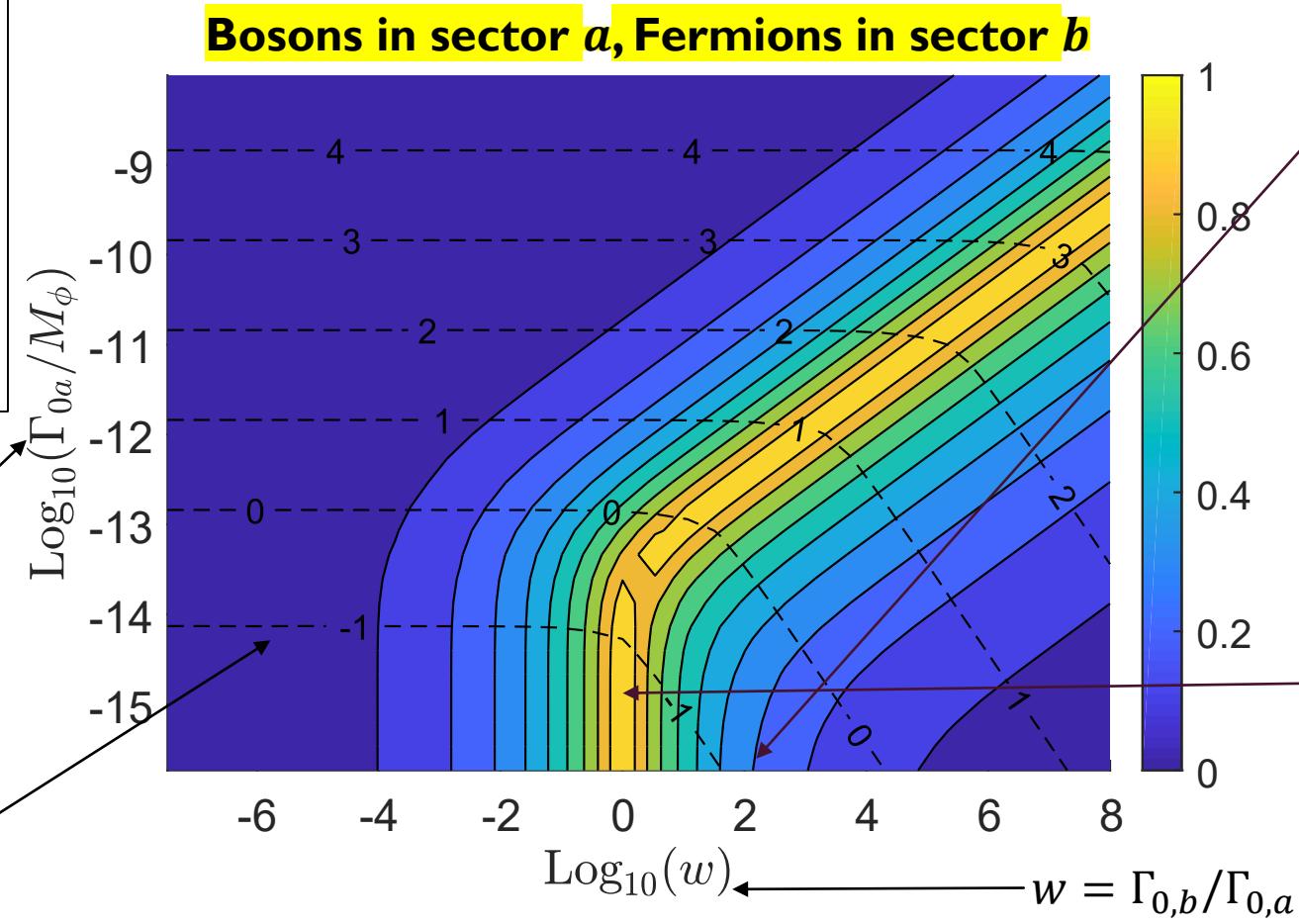
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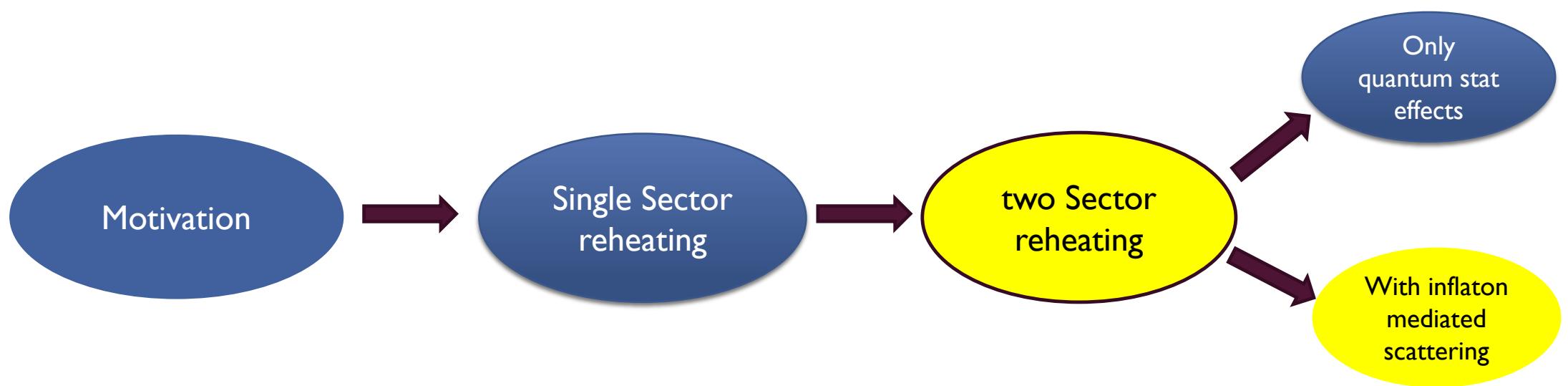
$$\frac{d\rho_b}{dt} + 4H\rho_b = \Gamma_{\phi,b}\rho_\phi$$

$$H \approx \frac{1}{\sqrt{3}M_{pl}}\sqrt{\rho_{\phi,I}}a^{-3/2}$$

Zero temperature decay width of boson sector

$\text{Log}_{10}(T_{rh}/M_\phi)$





INFLATON MEDIATED SCATTERING BETWEEN SECTORS: Boltzmann equations

Post inflation, reheating Boltzmann Equations:

$$\frac{d\rho_\phi}{dt} + 3H\rho_\phi = (\Gamma_{\phi,a} + \Gamma_{\phi,b})\rho_\phi$$

$$\frac{d\rho_a}{dt} + 4H\rho_a = \Gamma_{\phi,a}\rho_\phi - C_E$$

$$\frac{d\rho_b}{dt} + 4H\rho_b = \Gamma_{\phi,b}\rho_\phi + C_E$$

$$H \approx \frac{1}{\sqrt{3}M_{pl}} \sqrt{\rho_\phi + \rho_a + \rho_b}$$

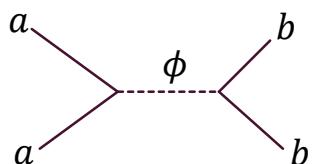
INFLATON MEDIATED SCATTERING BETWEEN SECTORS:Analytic form for collision term

$$\frac{d\rho_\phi}{dt} + 3H\rho_\phi = (\Gamma_{\phi,a} + \Gamma_{\phi,b})\rho_\phi$$

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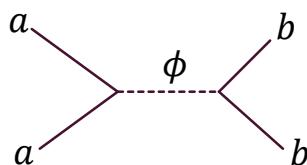
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$$\begin{aligned} C_E = & \int \frac{d^3 p_1}{2E_1(2\pi)^3} \frac{d^3 p_2}{2E_2(2\pi)^3} \frac{d^3 p_3}{2E_3(2\pi)^3} \frac{d^3 p_4}{2E_4(2\pi)^3} (2\pi)^4 \delta^4(p_1 + p_2 - p_3 + p_4) |\mathcal{M}|^2 \hat{S} \\ & \times (E_1 + E_2)[f_1(p_1)f_2(p_2)(1 \pm f_3(p_3))(1 \pm f_4(p_4)) - f_3(p_3)f_4(p_4)(1 \pm f_1(p_1))(1 \pm f_2(p_2))]. \end{aligned}$$

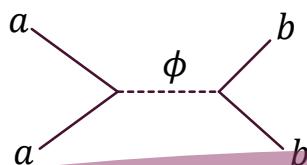
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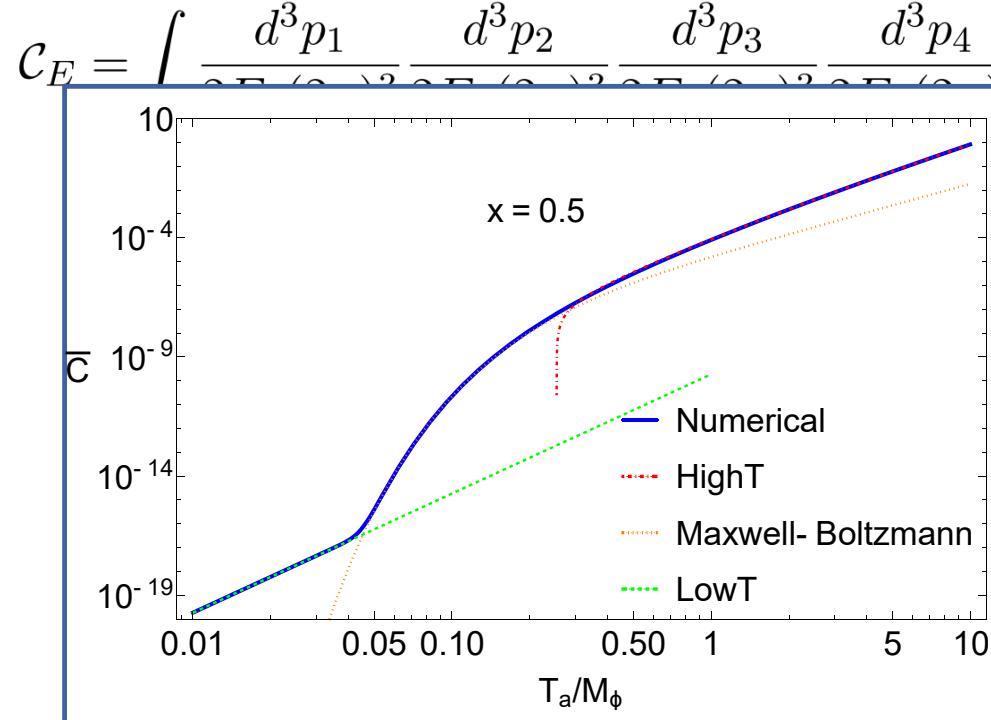
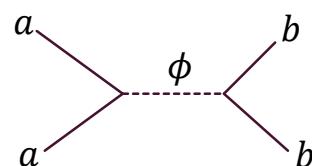
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Derived analytic expression for non-equilibrium energy transfer between two sectors at different temperatures including quantum statistics.

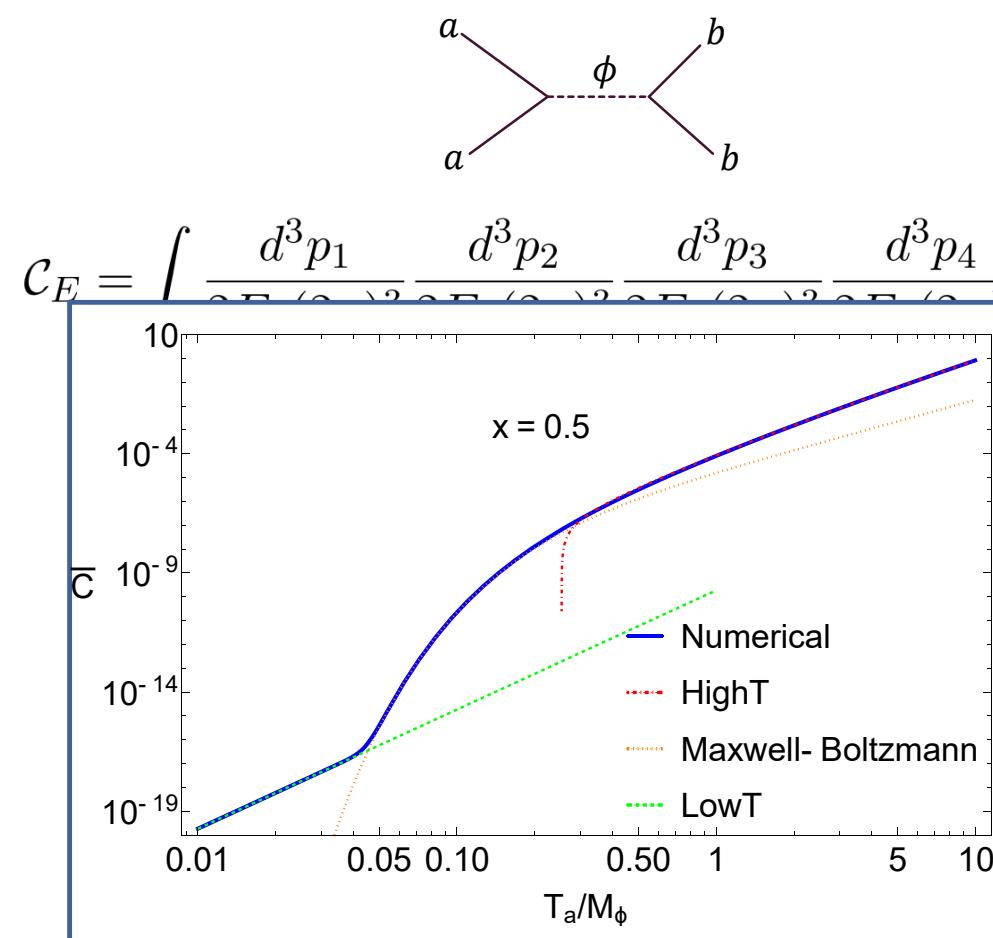
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$$H \approx \frac{1}{\sqrt{3}M_{pl}}\sqrt{\rho_{\phi,I} + \rho_a + \rho_b}$$



$$C_E = \int \frac{d^3 p_1}{(2\pi)^3} \frac{d^3 p_2}{(2\pi)^3} \frac{d^3 p_3}{(2\pi)^3} \frac{d^3 p_4}{(2\pi)^3} (2\pi)^4 \delta^4(p_1 + p_2 - p_3 + p_4) |\mathcal{M}|^2 \hat{S}$$

$$\pm f_4(p_4)) - f_3(p_3)f_4(p_4)(1 \pm f_1(p_1))(1 \pm f_2(p_2))].$$

Derived analytic expression for non-equilibrium energy transfer between two sectors at different temperatures including quantum statistics.

Birell, Yang and Rafelski (2014)

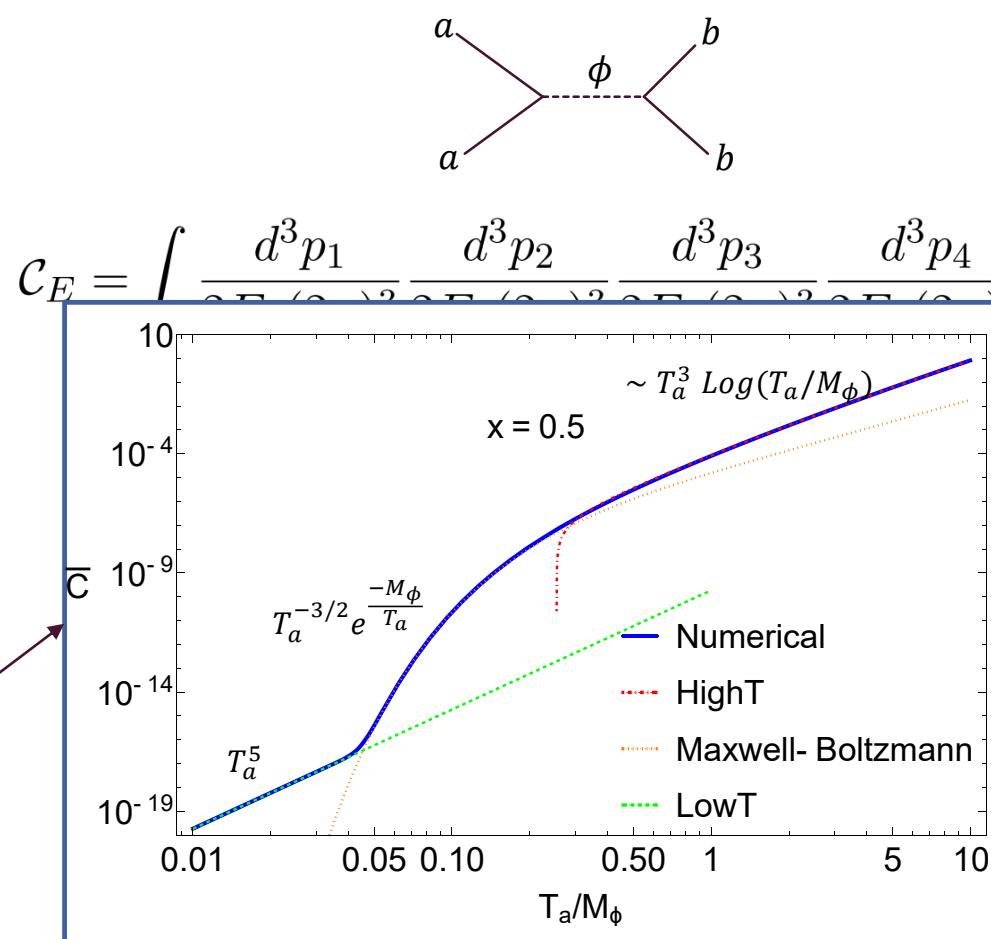
INFLATON MEDIATED SCATTERING BETWEEN SECTORS: Collision term for scalar trilinear coupling with inflaton

$$\frac{d\rho_\phi}{dt} + 3H\rho_\phi = (\Gamma_{\phi,a} + \Gamma_{\phi,b})\rho_\phi$$

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$$H \approx \frac{1}{\sqrt{3}M_{pl}}\sqrt{\rho_{\phi,I} + \rho_a + \rho_b}$$



$$C_E = \int \frac{d^3 p_1}{(2\pi)^3} \frac{d^3 p_2}{(2\pi)^3} \frac{d^3 p_3}{(2\pi)^3} \frac{d^3 p_4}{(2\pi)^3} (2\pi)^4 \delta^4(p_1 + p_2 - p_3 + p_4) |\mathcal{M}|^2 \hat{S}$$

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Derived analytic expression for non-equilibrium energy transfer between two sectors at different temperatures including quantum statistics.

s-channel collision term for scalar trilinear couplings of inflaton in both sectors

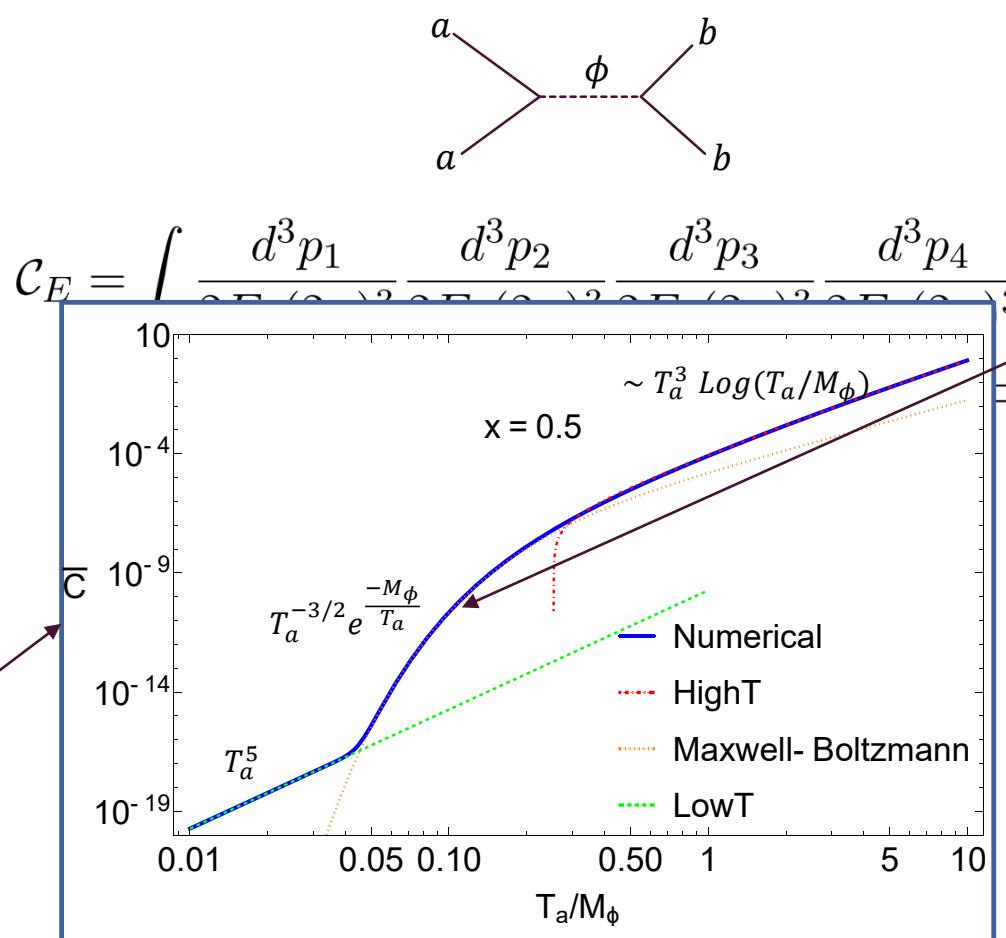
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$$H \approx \frac{1}{\sqrt{3}M_{pl}}\sqrt{\rho_{\phi,I} + \rho_a + \rho_b}$$



s-channel collision term for scalar trilinear couplings of inflaton in both sectors

$$C_s = \int \frac{d^3 p_1}{(2\pi)^3} \frac{d^3 p_2}{(2\pi)^3} \frac{d^3 p_3}{(2\pi)^3} \frac{d^3 p_4}{(2\pi)^3} (2\pi)^2 \hat{S} |^2 \hat{S} \pm f_4(p_4)) - J_3(p_3)J_4(p_4)(1 \pm J_1(p_1))(1 \pm f_2(p_2))].$$

Resonance boost in s-channel

Derived analytic expression for non-equilibrium energy transfer between two sectors at different temperatures including quantum statistics.

INFLATON MEDIATED SCATTERING BETWEEN SECTORS: Scattering becomes effective after reheating

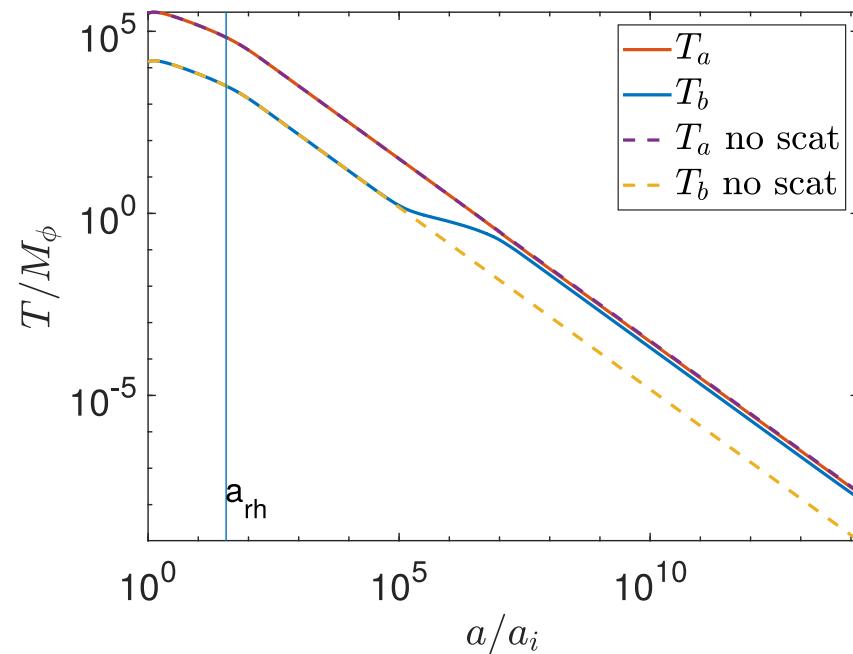
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$$H \approx \frac{1}{\sqrt{3}M_{pl}}\sqrt{\rho_{\phi,I} + \rho_a + \rho_b}$$

Inflaton with trilinear coupling to relativistic scalars in both sectors



For $\alpha_a \sim \alpha_b$, inflaton mediated scattering is usually never strong enough to overcome the Hubble rate before reheating for the interaction theories we consider.

INFLATON MEDIATED SCATTERING BETWEEN SECTORS: C_E attractor curve

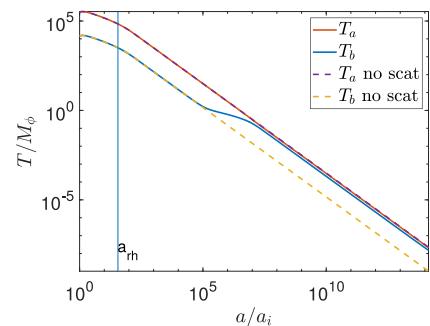
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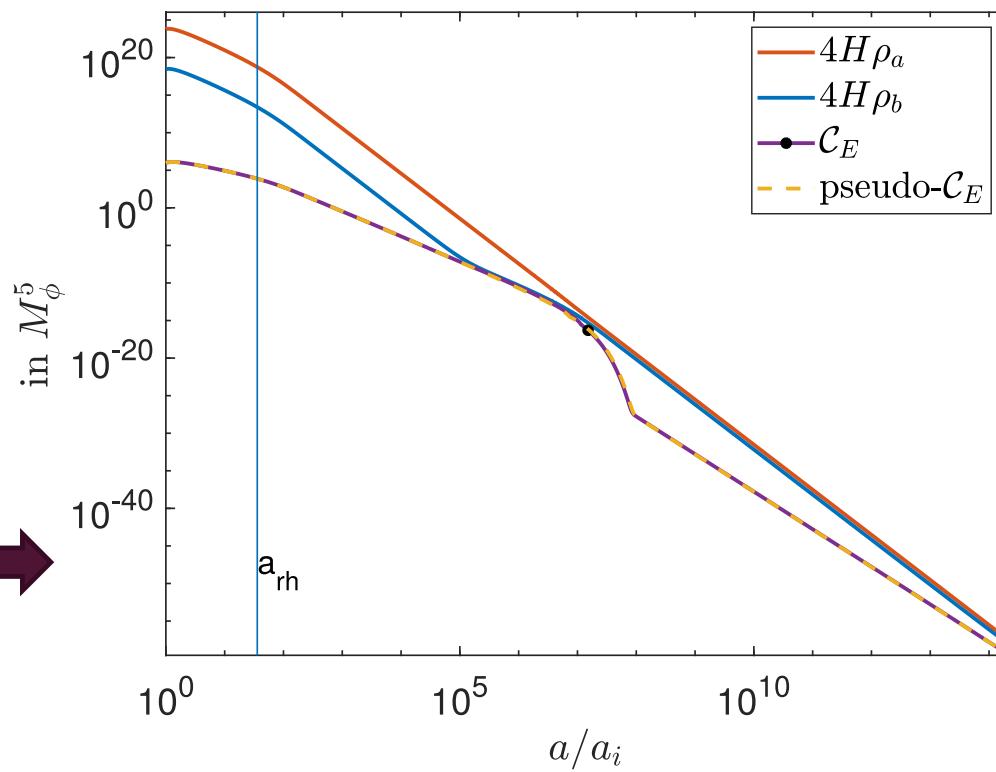
$$\frac{d\rho_b}{dt} + 4H\rho_b = \Gamma_{\phi,b}\rho_\phi + C_E$$

$$H \approx \frac{1}{\sqrt{3}M_{pl}}\sqrt{\rho_{\phi,I} + \rho_a + \rho_b}$$

Inflaton with trilinear coupling to relativistic scalars in both sectors



A better representation of thermalization process



INFLATON MEDIATED SCATTERING BETWEEN SECTORS: C_E attractor curve

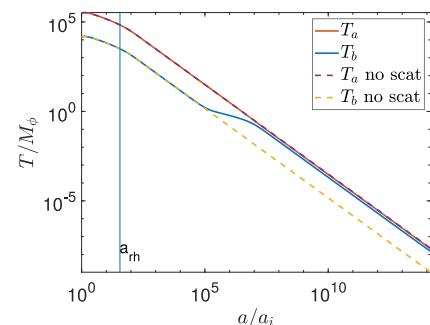
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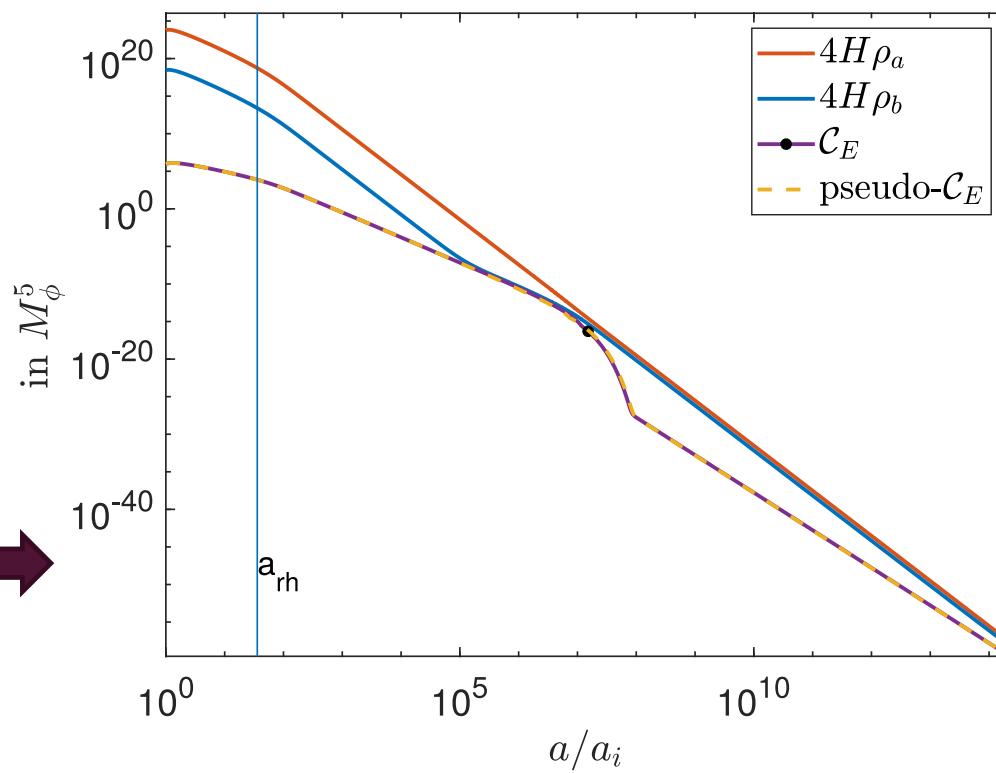
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$$H \approx \frac{1}{\sqrt{3}M_{pl}}\sqrt{\rho_{\phi,I} + \rho_a + \rho_b}$$

Inflaton with trilinear coupling to relativistic scalars in both sectors



A better representation of thermalization process



$$x^4 \sim \frac{4H\rho_b}{4H\rho_a}$$

INFLATON MEDIATED SCATTERING BETWEEN SECTORS: C_E attractor curve

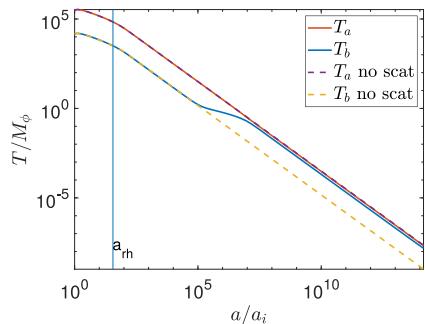
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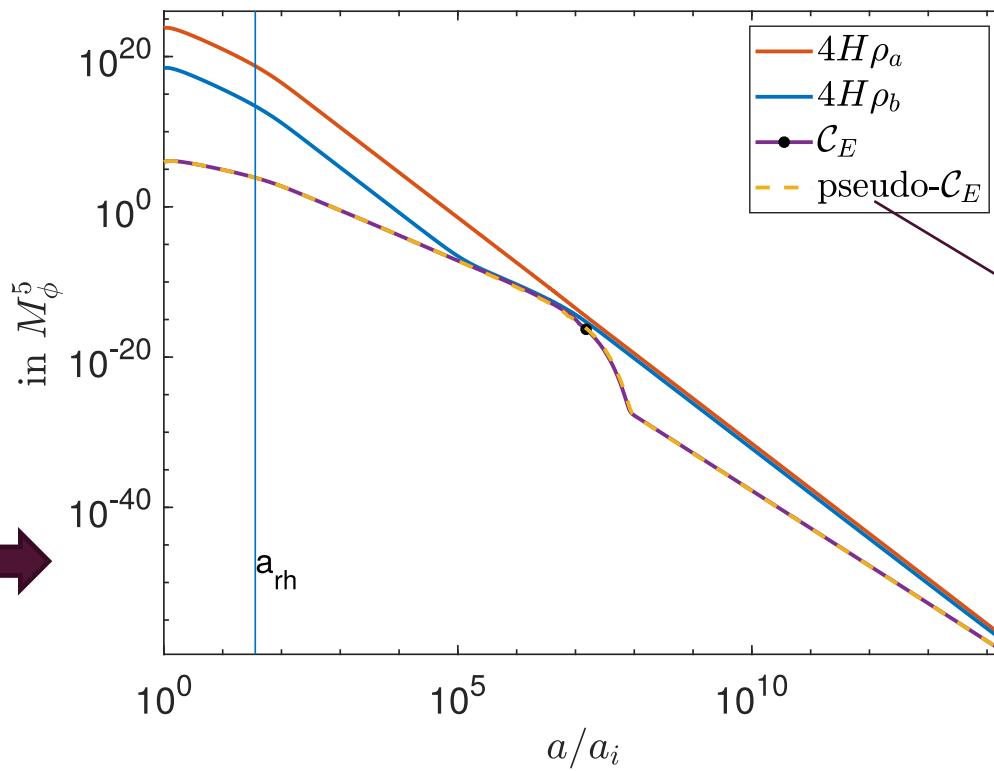
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Inflaton with trilinear coupling to relativistic scalars in both sectors



A better representation of thermalization process



$$\chi^4 \sim \frac{4H\rho_b}{4H\rho_a}$$

Collision term
neglecting feedback from
colder sector during
thermalization process

INFLATON MEDIATED SCATTERING BETWEEN SECTORS: C_E attractor curve

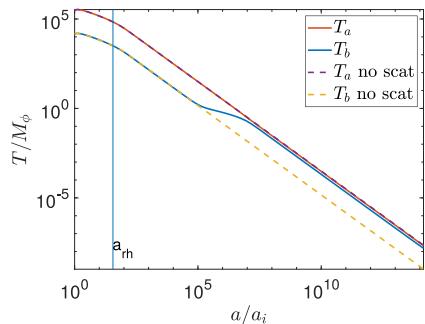
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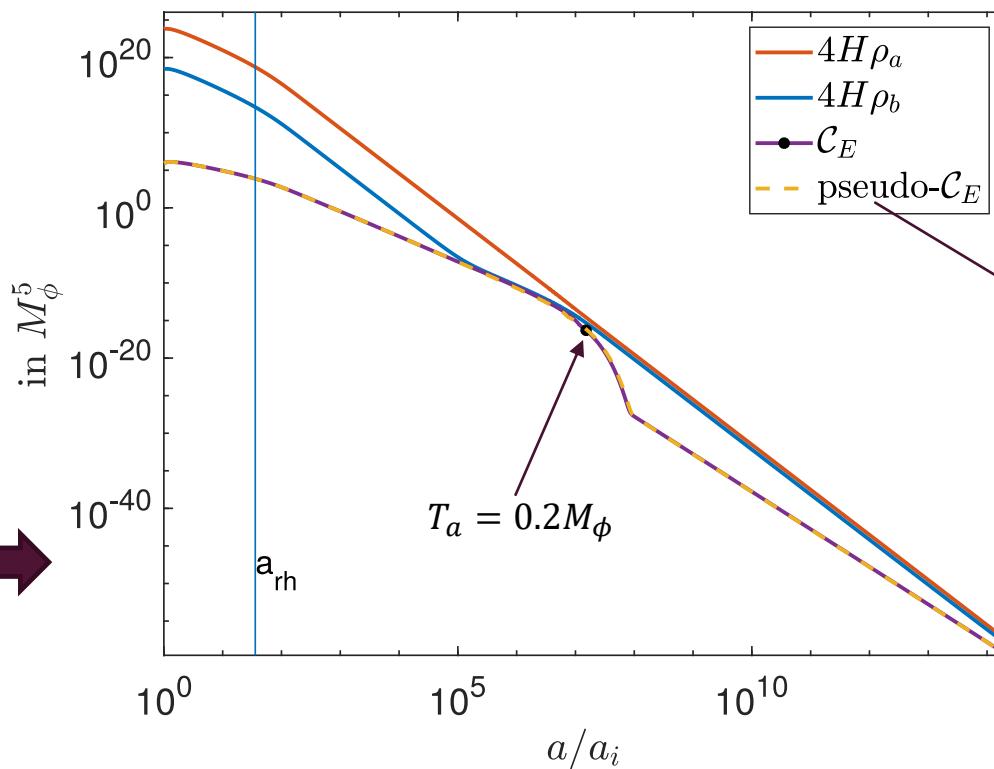
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Inflaton with trilinear coupling to relativistic scalars in both sectors



A better representation of thermalization process



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Collision term
neglecting feedback from
colder sector during
thermalization process

INFLATON MEDIATED SCATTERING BETWEEN SECTORS: C_E attractor curve

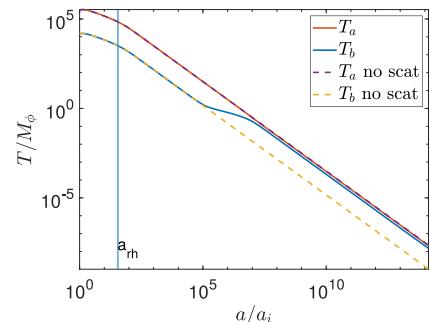
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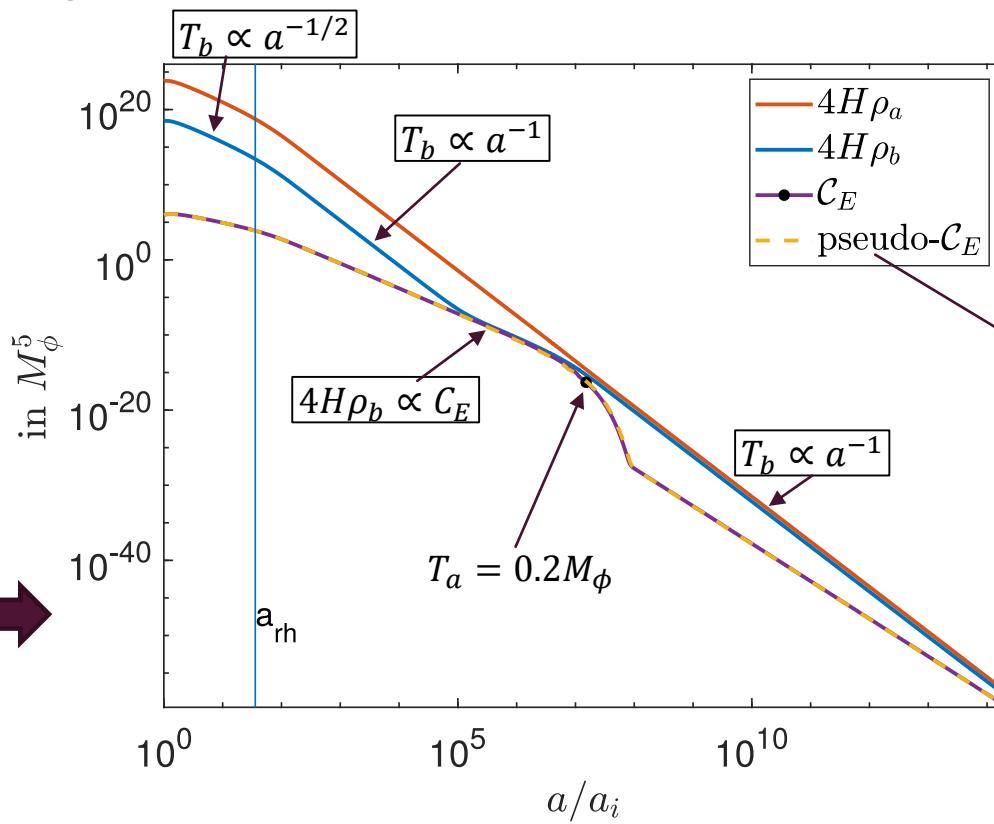
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Inflaton with trilinear coupling to relativistic scalars in both sectors



A better representation of thermalization process



$$\chi^4 \sim \frac{4H\rho_b}{4H\rho_a}$$

Collision term
neglecting feedback from
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INFLATON MEDIATED SCATTERING BETWEEN SECTORS: C_E attractor curve

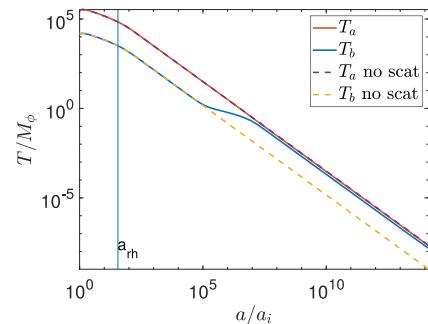
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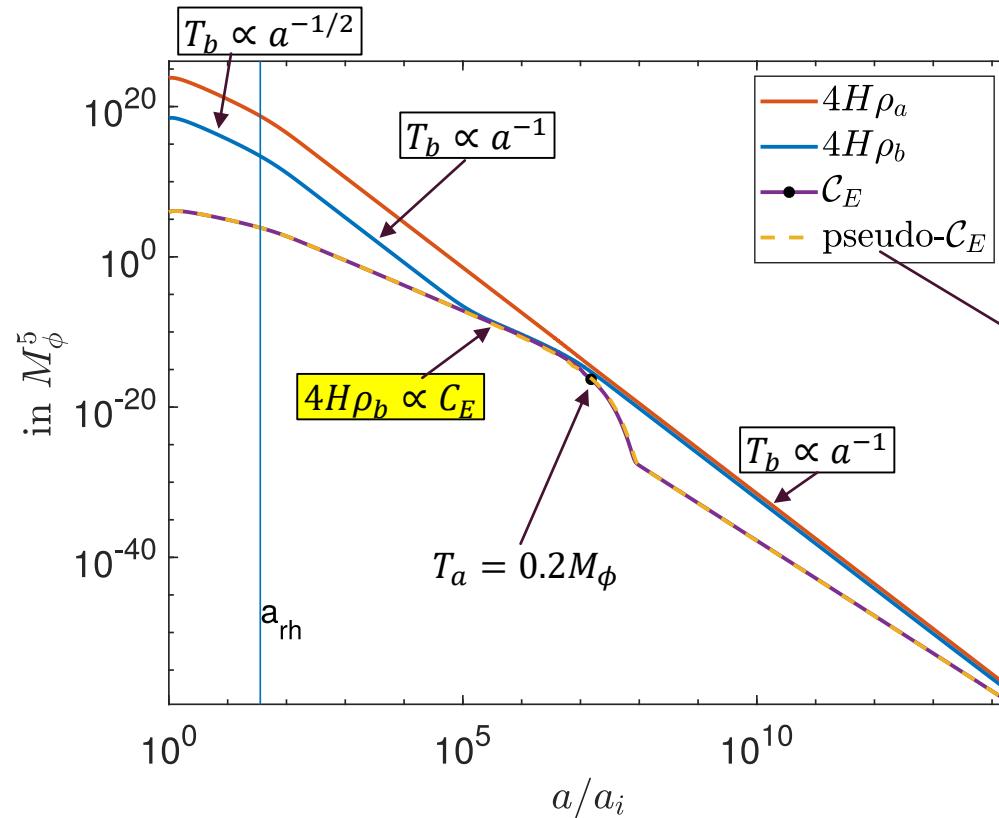
$$\frac{d\rho_b}{dt} + 4H\rho_b = \Gamma_{\phi,b}\rho_\phi + C_E$$

$$H \approx \frac{1}{\sqrt{3}M_{pl}}\sqrt{\rho_{\phi,I} + \rho_a + \rho_b}$$

Inflaton with trilinear coupling to relativistic scalars in both sectors



Energy injection from the hotter sector imposes another attractor solution!



$$x^4 \sim \frac{4H\rho_b}{4H\rho_a}$$

Collision term neglecting feedback from colder sector during thermalization process

INFLATON MEDIATED SCATTERING BETWEEN SECTORS: χ independent of initial history

$$\frac{d\rho_\phi}{dt} + 3H\rho_\phi = (\Gamma_{\phi,a} + \Gamma_{\phi,b})\rho_\phi$$

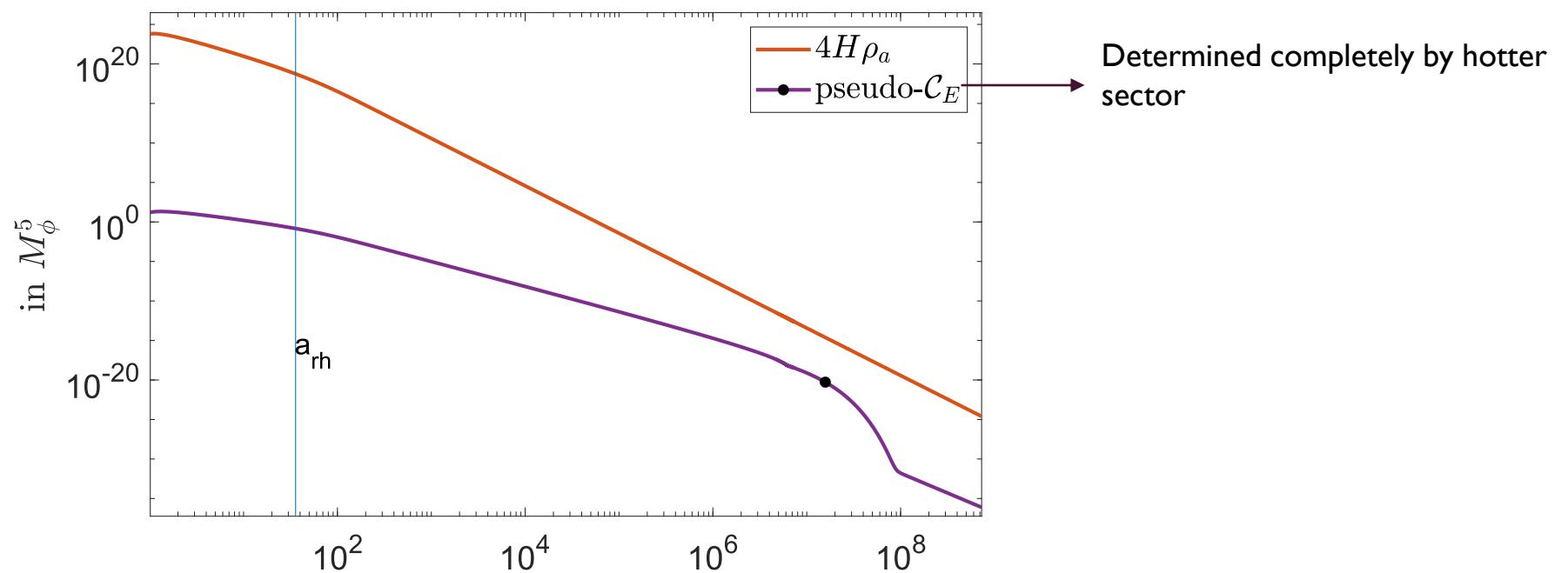
$$\frac{d\rho_a}{dt} + 4H\rho_a = \Gamma_{\phi,a}\rho_\phi - C_E$$

$$\frac{d\rho_b}{dt} + 4H\rho_b = \Gamma_{\phi,b}\rho_\phi + C_E$$

$$H \approx \frac{1}{\sqrt{3}M_{pl}}\sqrt{\rho_{\phi,I} + \rho_a + \rho_b}$$

Inflaton with trilinear coupling to relativistic scalars in both sectors

$$\chi^4 \sim \frac{4H\rho_b}{4H\rho_a}$$



INFLATON MEDIATED SCATTERING BETWEEN SECTORS: χ independent of initial history

$$\frac{d\rho_\phi}{dt} + 3H\rho_\phi = (\Gamma_{\phi,a} + \Gamma_{\phi,b})\rho_\phi$$

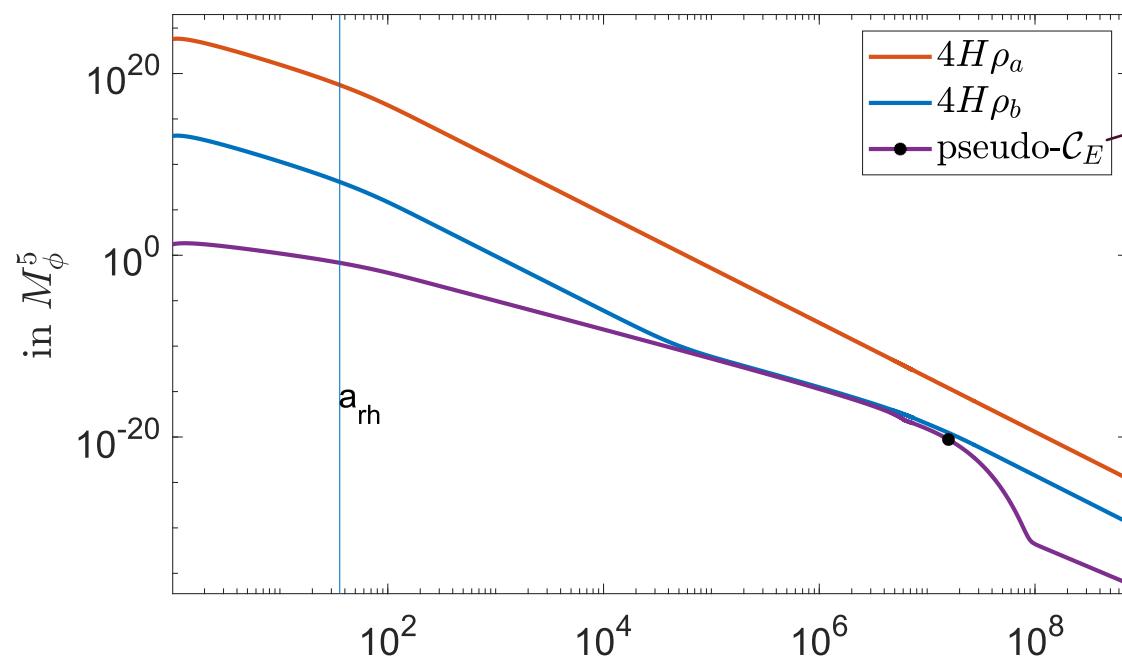
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$$H \approx \frac{1}{\sqrt{3}M_{pl}}\sqrt{\rho_{\phi,I} + \rho_a + \rho_b}$$

Inflaton with trilinear coupling to relativistic scalars in both sectors

$$\chi^4 \sim \frac{4H\rho_b}{4H\rho_a}$$



Determined completely by hotter sector

INFLATON MEDIATED SCATTERING BETWEEN SECTORS: χ independent of initial history

$$\frac{d\rho_\phi}{dt} + 3H\rho_\phi = (\Gamma_{\phi,a} + \Gamma_{\phi,b})\rho_\phi$$

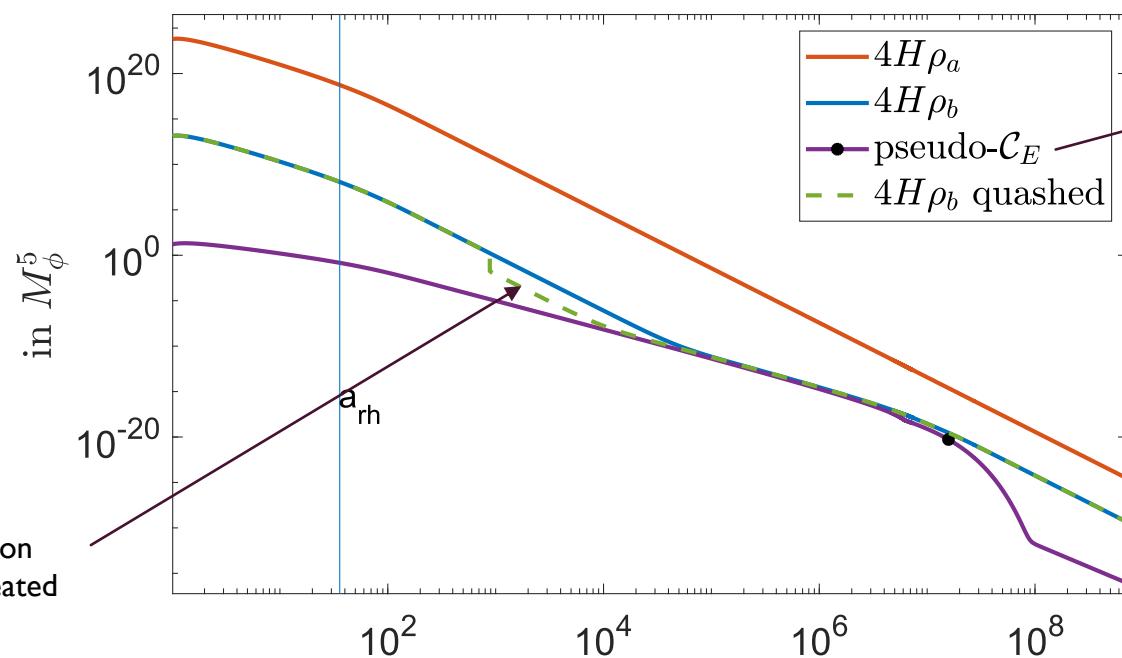
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$$H \approx \frac{1}{\sqrt{3}M_{pl}}\sqrt{\rho_{\phi,I} + \rho_a + \rho_b}$$

Inflaton with trilinear coupling to relativistic scalars in both sectors

$$\chi^4 \sim \frac{4H\rho_b}{4H\rho_a}$$



Quashed colder sector gets on the attractor curve and is heated to same temperature

INFLATON MEDIATED SCATTERING BETWEEN SECTORS: χ independent of initial history

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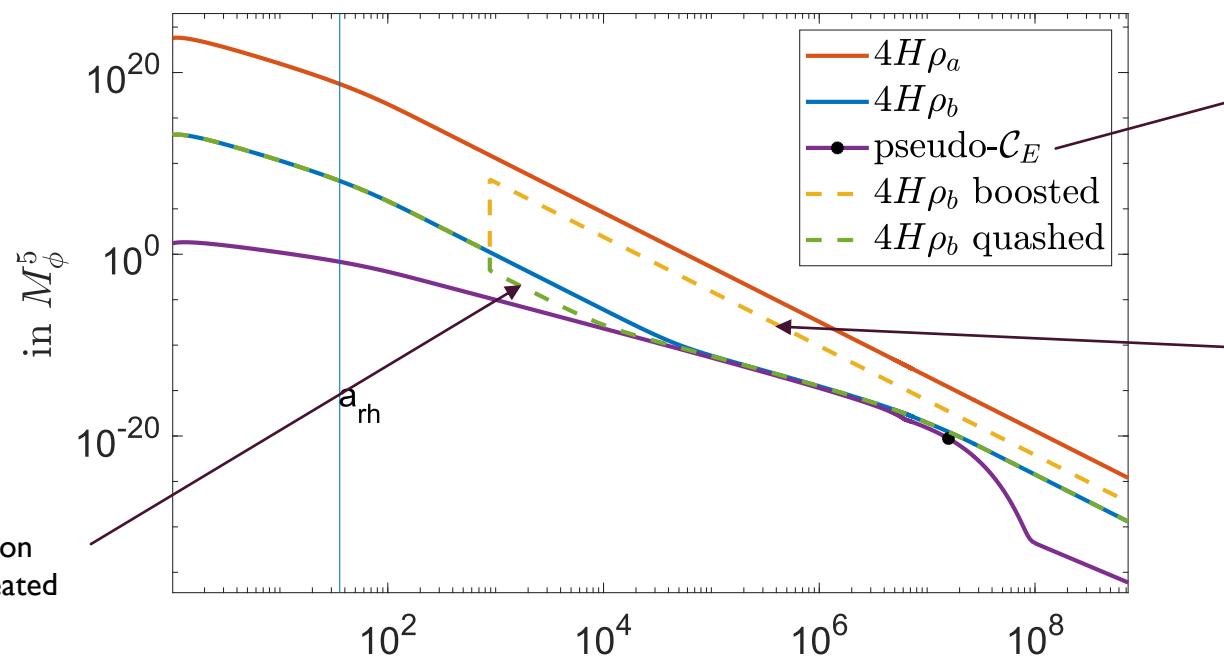
$$\frac{d\rho_b}{dt} + 4H\rho_b = \Gamma_{\phi,b}\rho_\phi + C_E$$

$$H \approx \frac{1}{\sqrt{3}M_{pl}}\sqrt{\rho_{\phi,I} + \rho_a + \rho_b}$$

Quashed colder sector gets on the attractor curve and is heated to same temperature

Inflaton with trilinear coupling to relativistic scalars in both sectors

$$\chi^4 \sim \frac{4H\rho_b}{4H\rho_a}$$



Determined completely by hotter sector

Boosted colder sector is unable to get on the attractor curve before $T_a \sim 0.2M_\phi$

INFLATON MEDIATED SCATTERING BETWEEN SECTORS: x (almost) independent of initial history

$$\frac{d\rho_\phi}{dt} + 3H\rho_\phi = (\Gamma_{\phi,a} + \Gamma_{\phi,b})\rho_\phi$$

$$\frac{d\rho_a}{dt} + 4H\rho_a = \Gamma_{\phi,a}\rho_\phi - C_E$$

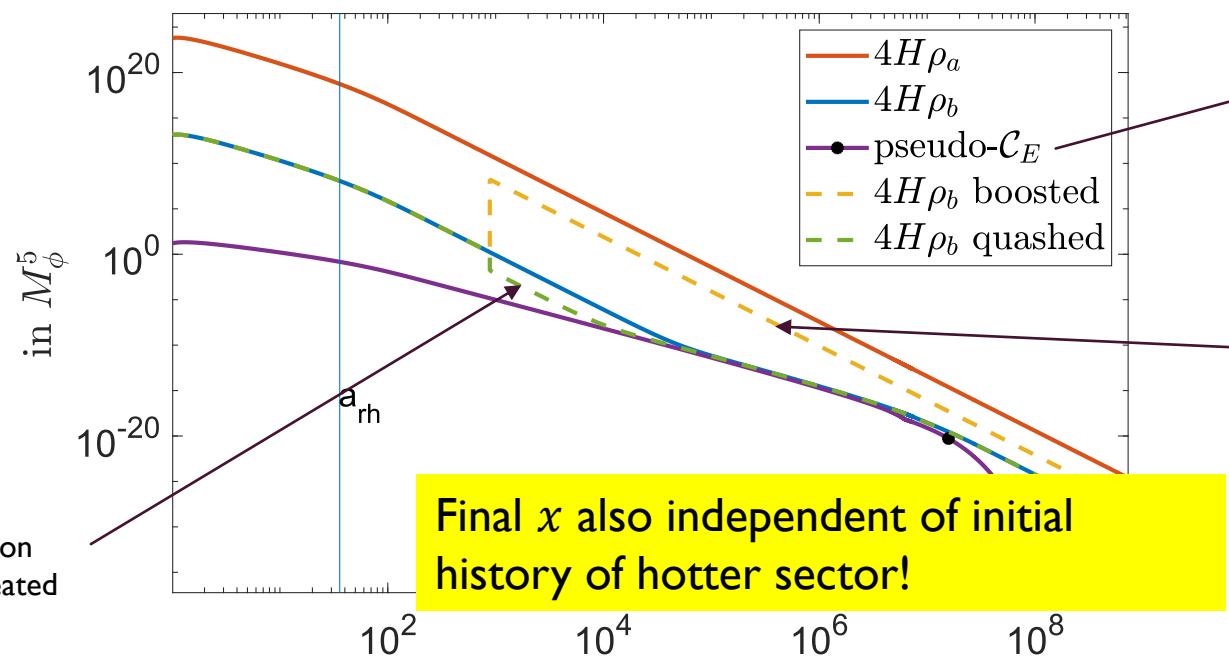
$$\frac{d\rho_b}{dt} + 4H\rho_b = \Gamma_{\phi,b}\rho_\phi + C_E$$

$$H \approx \frac{1}{\sqrt{3}M_{pl}}\sqrt{\rho_{\phi,I} + \rho_a + \rho_b}$$

Quashed colder sector gets on the attractor curve and is heated to same temperature

Inflaton with trilinear coupling to relativistic scalars in both sectors

$$x^4 \sim \frac{4H\rho_b}{4H\rho_a}$$



Determined completely by hotter sector

Boosted colder sector is unable to get on the attractor curve before $T_a \sim 0.2M_\phi$

INFLATON MEDIATED SCATTERING BETWEEN SECTORS: Finding x analytically

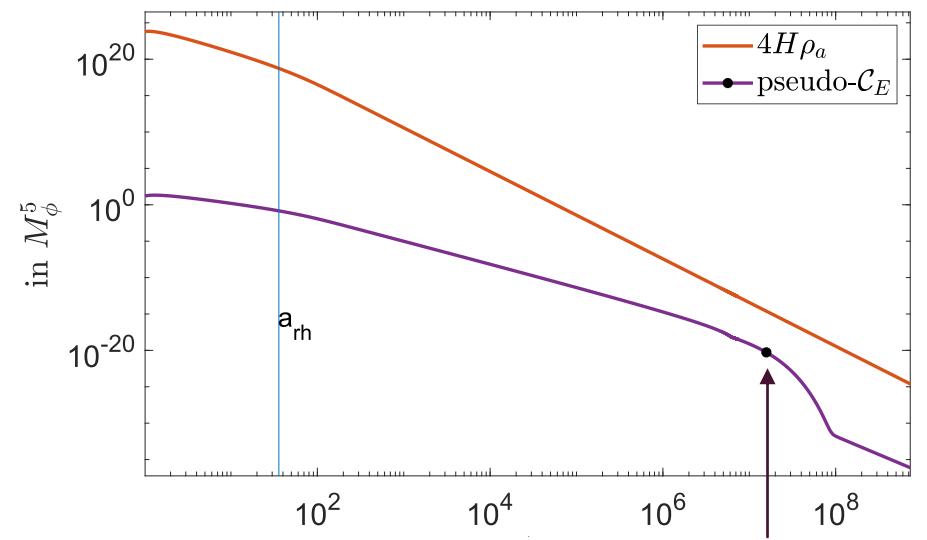
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$$\frac{d\rho_a}{dt} + 4H\rho_a = \Gamma_{\phi,a}\rho_\phi - C_E$$

$$\frac{d\rho_b}{dt} + 4H\rho_b = \Gamma_{\phi,b}\rho_\phi + C_E$$

$$H \approx \frac{1}{\sqrt{3}M_{pl}}\sqrt{\rho_{\phi,I} + \rho_a + \rho_b}$$

Inflaton with trilinear coupling to relativistic scalars in both sectors



Integrate around $T_a \sim 0.2M_\phi$ to find x_{sc} assuming colder sector gets on the attractor curve.

$x = x_{sc}$ only when $x_{rh} < x_{sc} < 1$.

$$x_{sc}^4 \sim \frac{4H\rho_b}{4H\rho_a} \sim \left[\frac{C_E}{4H\rho_a} \right]_{T_a \sim 0.2M_\phi}$$

INFLATON MEDIATED SCATTERING BETWEEN SECTORS: Numerical final x contour plot

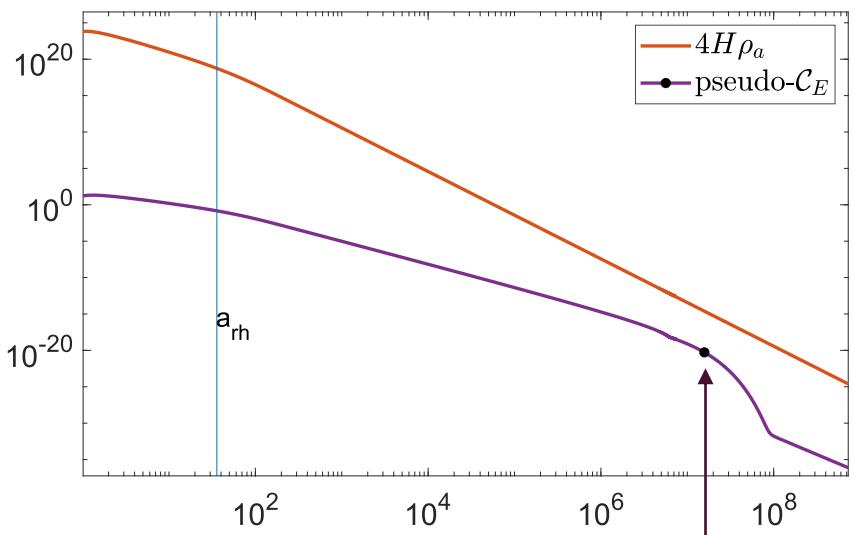
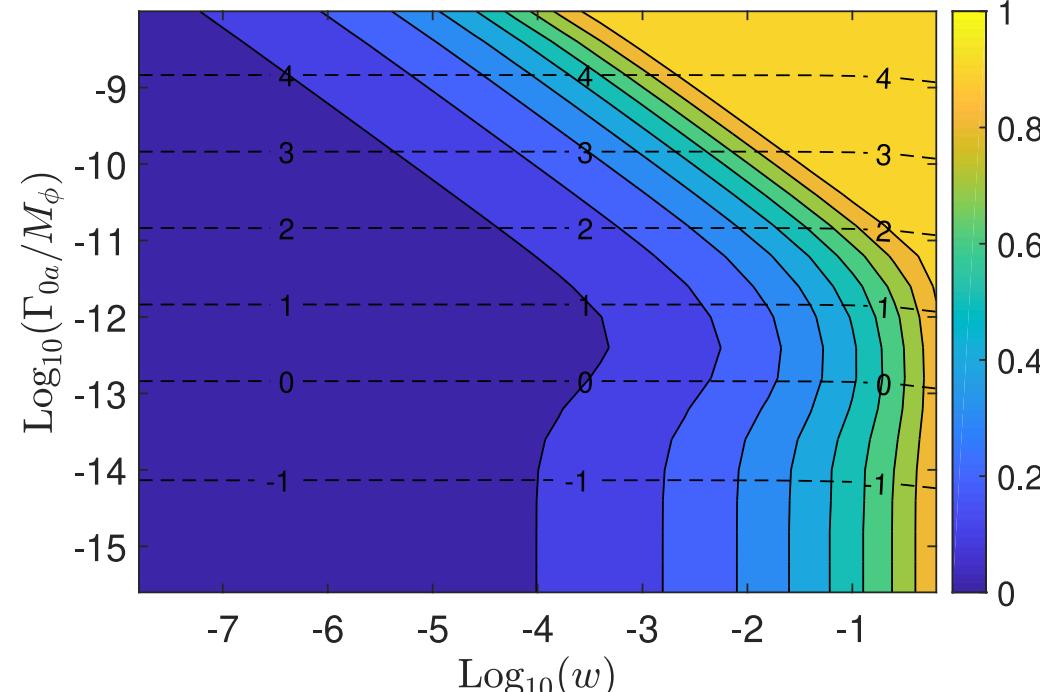
$$\frac{d\rho_\phi}{dt} + 3H\rho_\phi = (\Gamma_{\phi,a} + \Gamma_{\phi,b})\rho_\phi$$

$$\frac{d\rho_a}{dt} + 4H\rho_a = \Gamma_{\phi,a}\rho_\phi - C_E$$

$$\frac{d\rho_b}{dt} + 4H\rho_b = \Gamma_{\phi,b}\rho_\phi + C_E$$

$$H \approx \frac{1}{\sqrt{3}M_{pl}}\sqrt{\rho_{\phi,I} + \rho_a + \rho_b}$$

Inflaton with trilinear coupling to relativistic scalars in both sectors



Integrate around $T_a \sim 0.2M_\phi$ to find x_{sc} assuming colder sector gets on the attractor curve.

$x = x_{sc}$ only when $x_{rh} < x_{sc} < 1$.

$$x_{sc}^4 \sim \frac{4H\rho_b}{4H\rho_a} \sim \left[\frac{C_E}{4H\rho_a} \right]_{T_a \sim 0.2M_\phi}$$

INFLATON MEDIATED SCATTERING BETWEEN SECTORS: Numerical final x contour plot

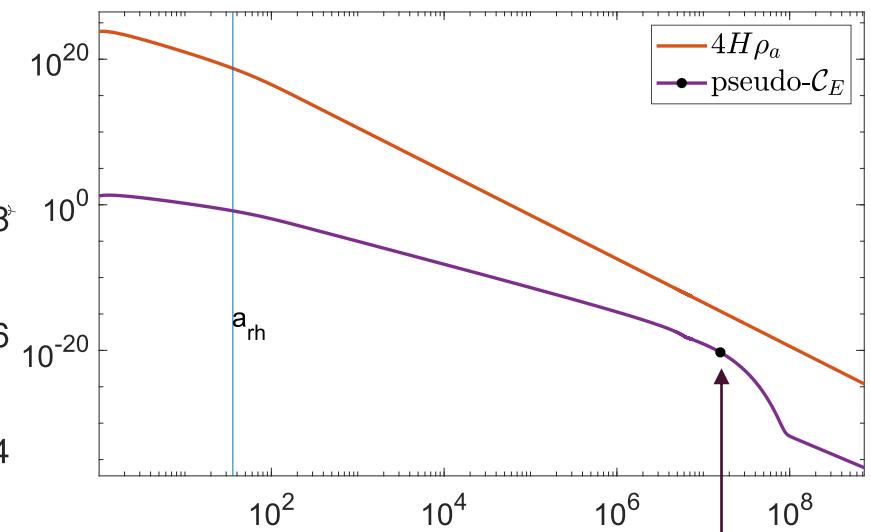
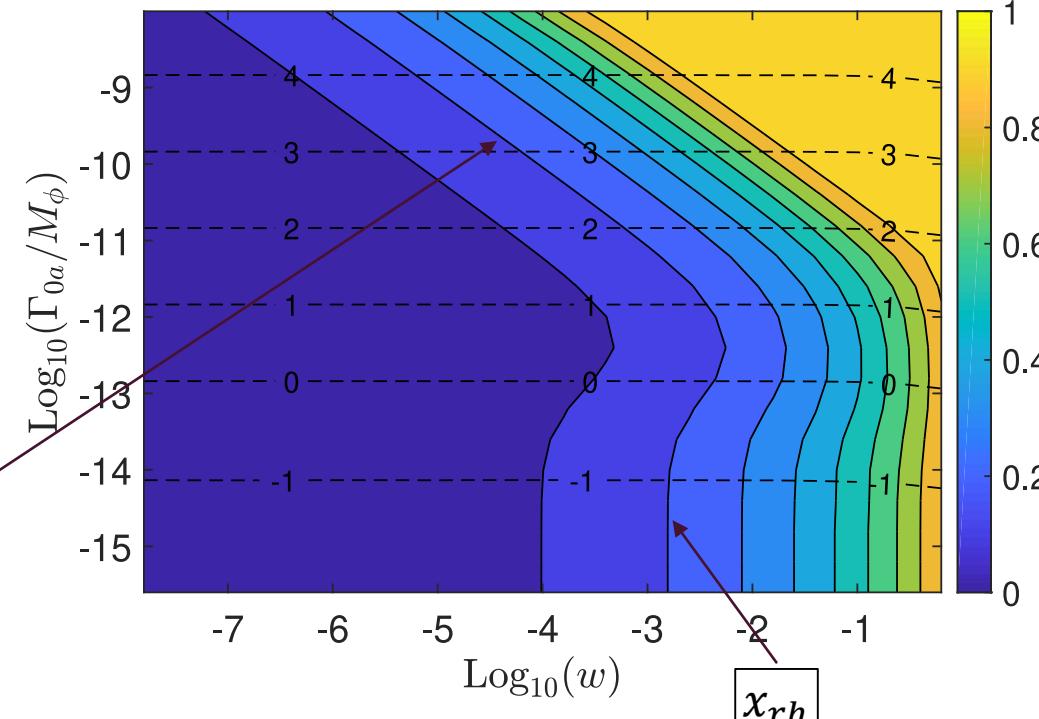
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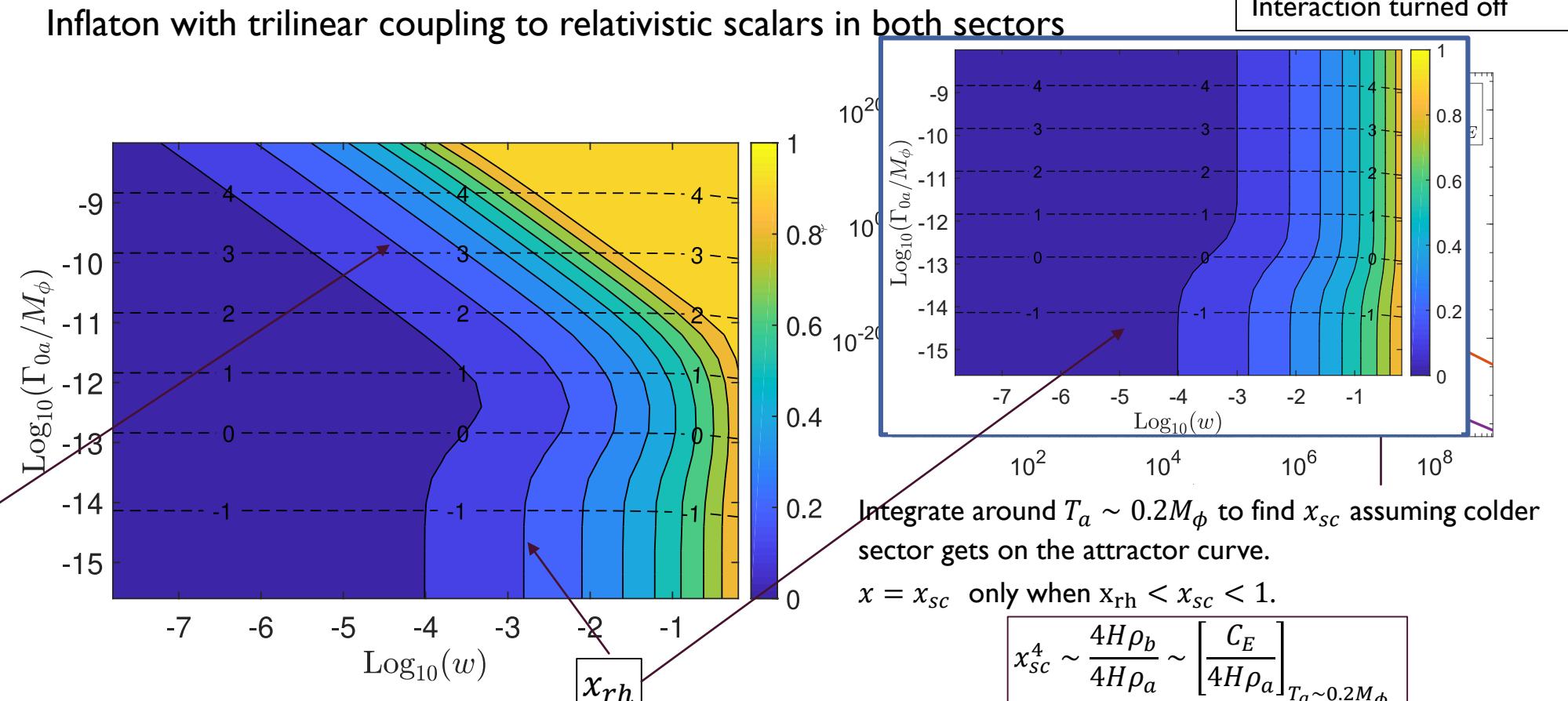
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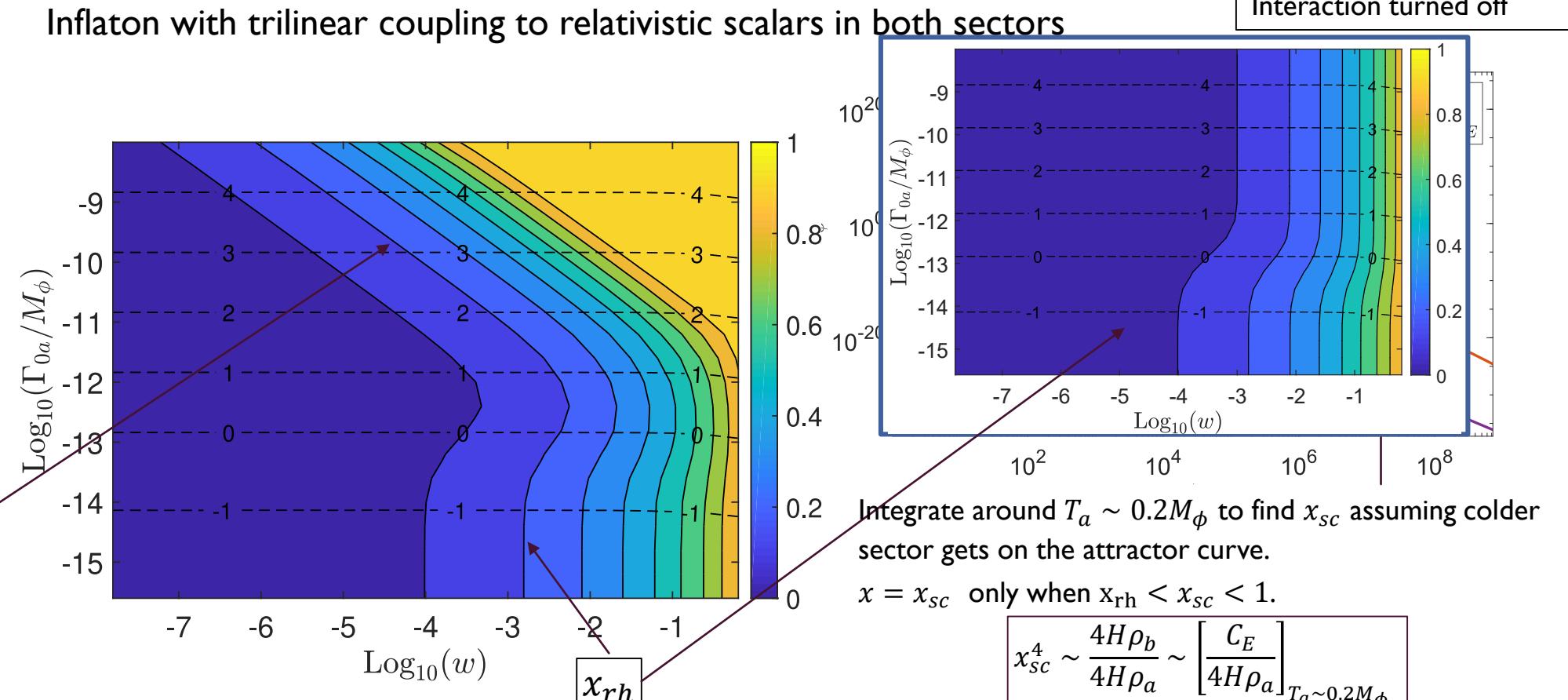
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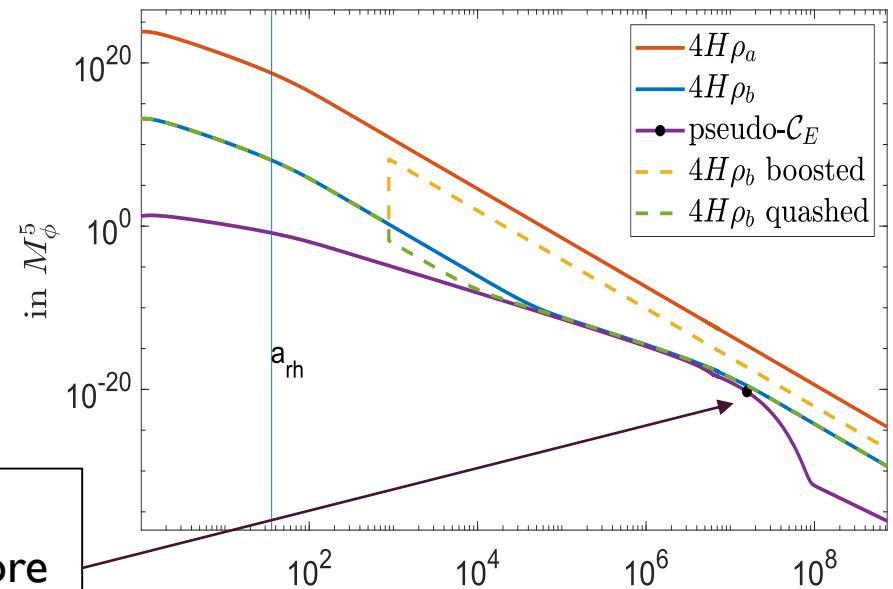
REVIEW OF MAJOR ASSUMPTIONS

- Instantaneous thermalization
- Neglected preheating
- Neglected thermal effects in plasma

REVIEW OF MAJOR ASSUMPTIONS: Robust lower bound on temperature ratio

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Inflaton mediated scattering provides a robust floor for temperature ratio at $T_a \sim 0.2M_\phi$ given above effects end before this temperature scale.



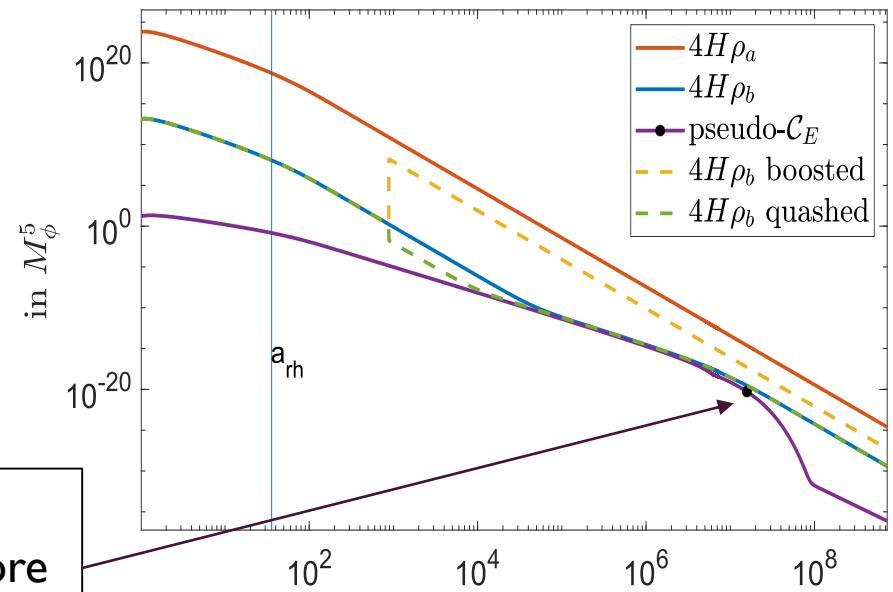
$$x^4 \geq \left[\frac{\mathcal{C}_E}{4H\rho_a} \right]_{T_a \sim 0.2M_\phi}$$

REVIEW OF MAJOR ASSUMPTIONS: Robust lower bound on temperature ratio

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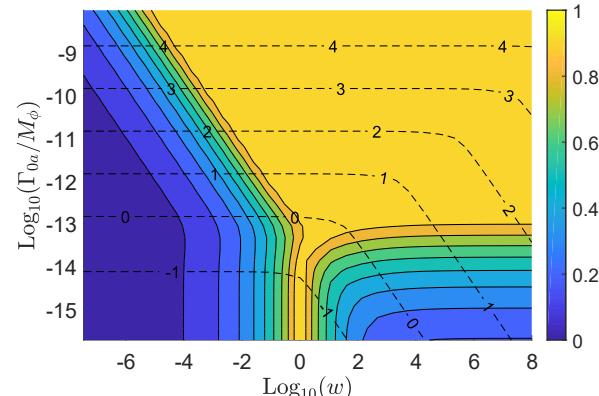
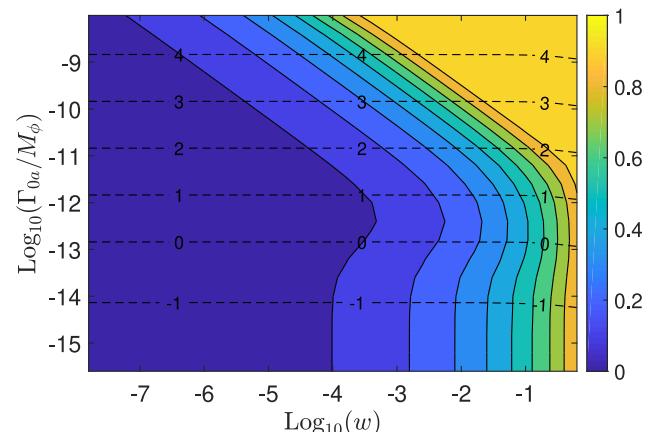
Inflaton mediated scattering provides a robust floor for temperature ratio at $T_a \sim 0.2M_\phi$ given above effects end before this temperature scale.

$T_{rh} > 0.2M_\phi$ necessary condition!



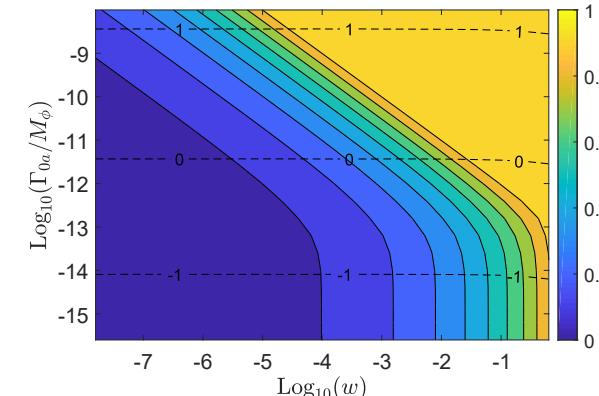
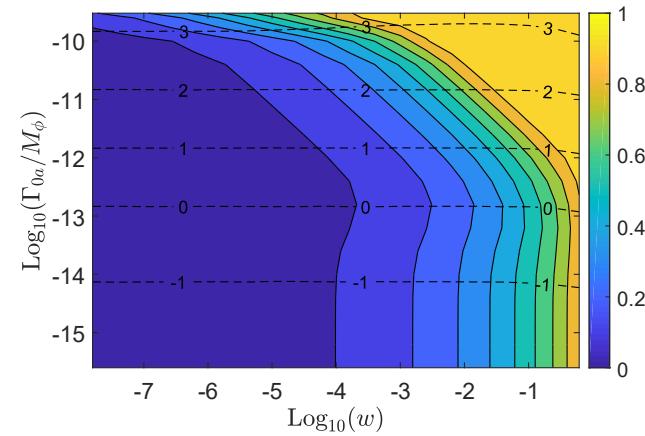
TWO SECTOR REHEATING: Final temperature ratio in other theories

Scalar bosons



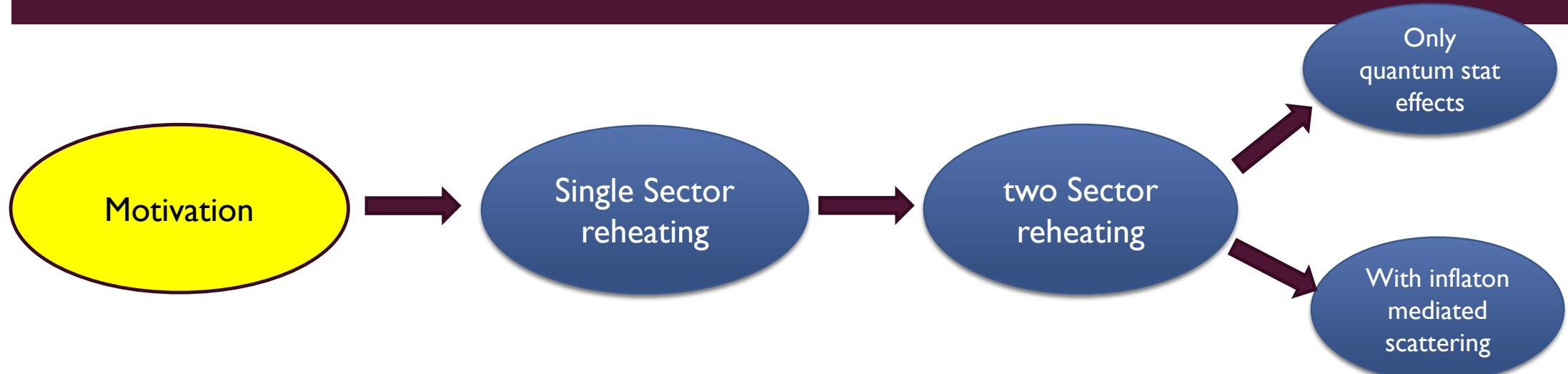
Fermions and scalar bosons

Gauge bosons



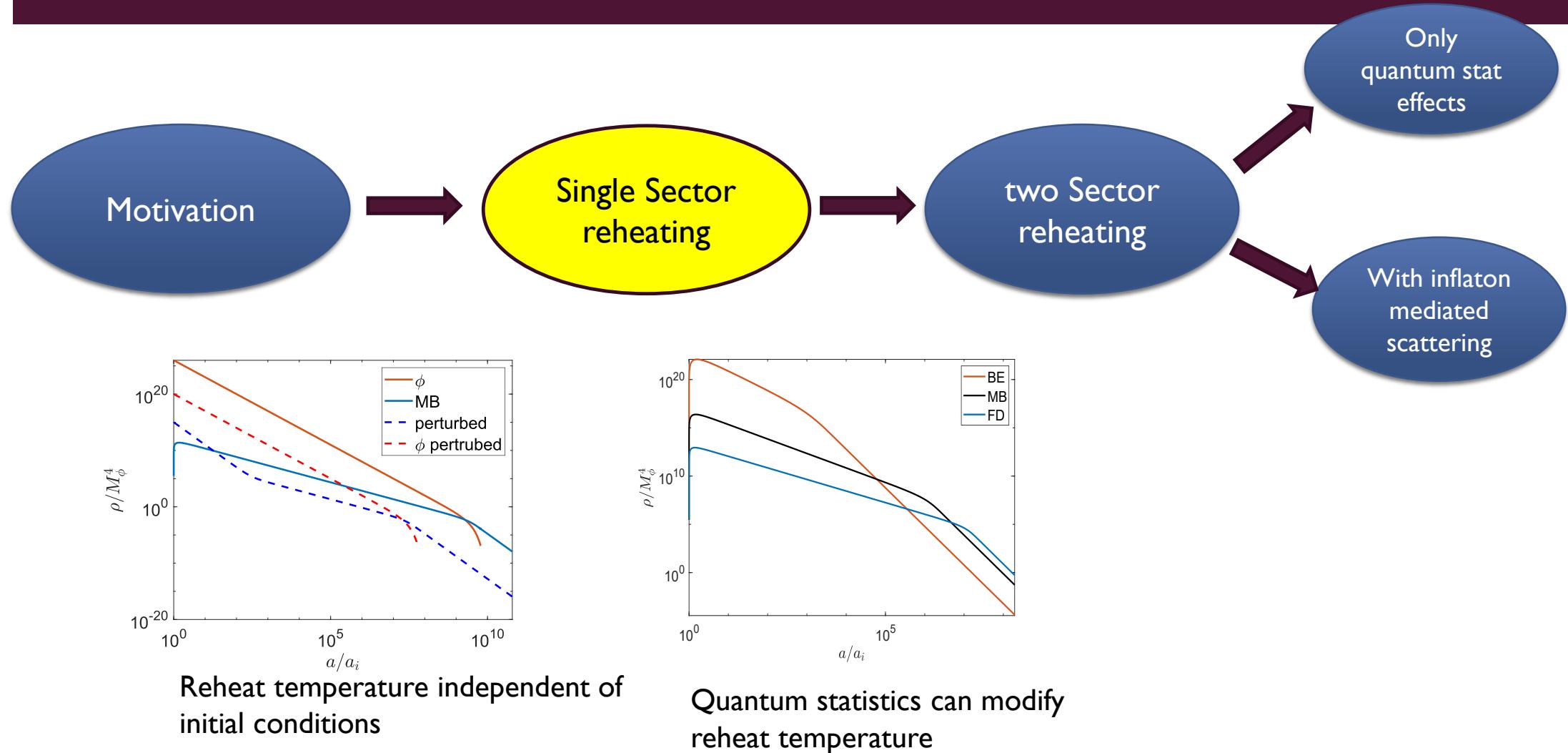
Fermions

SUMMARY

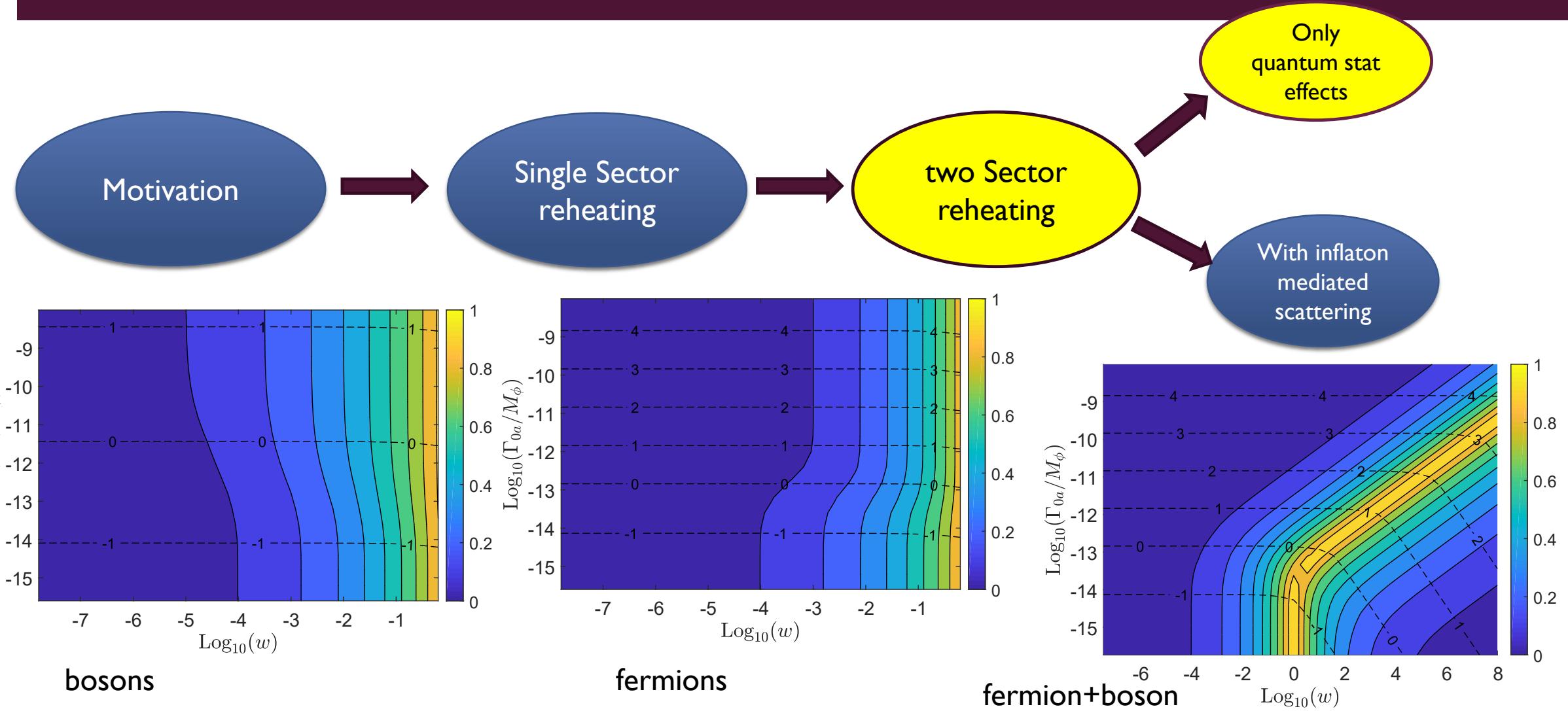


- WIMP searches null result
- Two sector reheating allows large temperature asymmetry

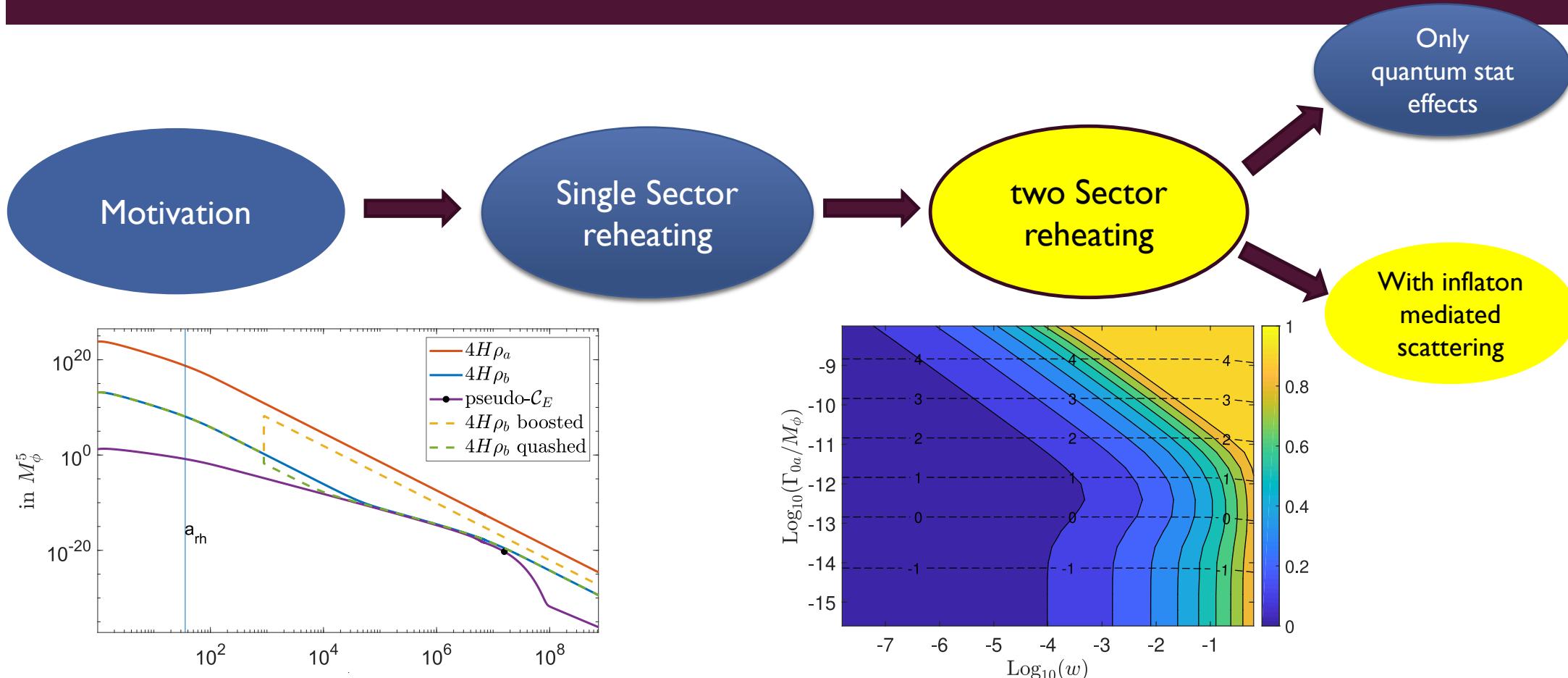
SUMMARY



SUMMARY

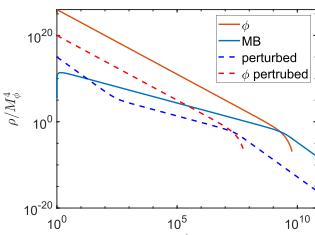


SUMMARY



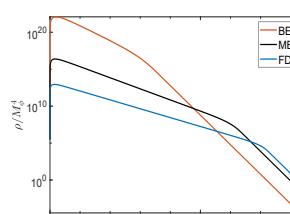
SUMMARY: QUESTIONS?

Motivation



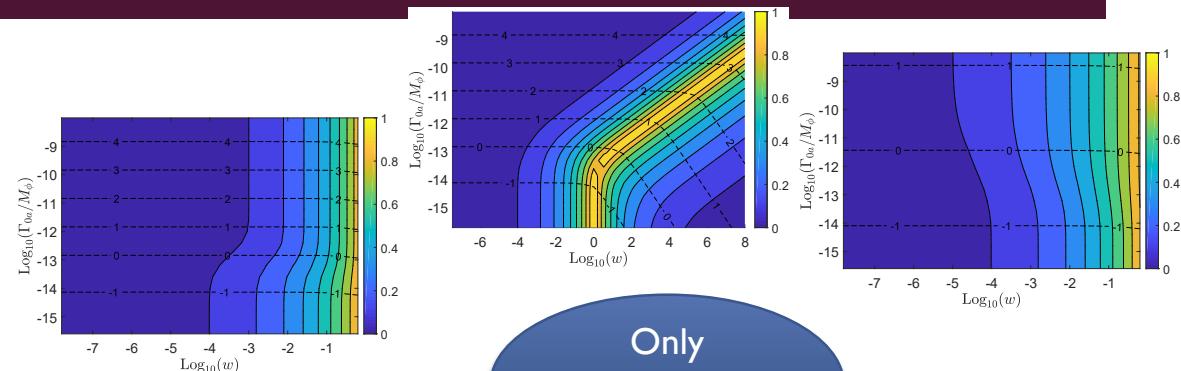
Reheat temperature (almost) independent of history before reheating.

Single Sector
reheating



Quantum statistics
can modify reheat
temperature

two Sector
reheating



Only
quantum stat
effects

With inflaton
mediated
scattering

Final temperature ratio
(almost) independent of
history before $T_a \sim 0.2 M_\phi$

