# CAT SWARM OPTIMIZATION: THEORY AND APPLICATION TO DIRECT AND INVERSE MODELING

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## OUTLINE

- Cats' behavior
- Cat Swarm Optimization
- Direct Modeling
- > Inverse Modeling
- > Simulation Results
- Conclusion

## CATS' BEHAVIOR

- Chu and Tsai (2007)
- Rest indolently most of the time when they are awake.
- Move speedily when they are tracing some targets.
- Curious about all kinds of moving things.

### CAT SWARM OPTIMIZATION

- > Solution Set -- Cats:
  - M-dimensional Position.
  - Velocities for each dimension.
  - A fitness value.
  - Seeking/Tracing flag.

## CAT SWARM OPTIMIZATION

#### > Sub-models:

#### - Seeking Mode:

•To model the situation where the cat is resting, looking around and seeking the next position to move to.

#### - Tracing Mode:

To model the situation where the cat is tracing some targets.

### CAT SWARM OPTIMIZATION

- Initialize the position matrix for N-cats (NxM) where M is the number of variables to be optimized and values are in the range (0,1)
- Initialize the velocity matrix (NxM) with values in the range (0,1)
- 3. Evaluate the fitness value of each of the N cats.
- 4. Cat with best fitness acts as the gbest
- 5. Define a Mixture ratio (MR) between 0 and 1 (say 0.2)
  - It means that
    - 80% (i.e 0.8 N) randomly selected will be in seeking mode
    - Rest 20% (i.e 0.2 N) will be in tracing mode

#### 4. Seeking Mode Operation

- Copy (SMP) number of cats out of a single cat. [SMP : Seeking Memory Pool]
  - o SMP: It is the number of copies of a cat to be produced in seeking mode.
- Out of these cats, randomly choose a cat and go to one (if CDC = 1) of its random dimension (variable). [CDC : Counts of Dimensions to Change]
  - CDC : Out of M dimensions of a cat, CDC dimensions are randomly changed. In the present case CDC=1.
- Change the magnitude of that dimension by (SRD) percentage: Mutation. [SRD: Seeking Range of selected Dimension]
  - SRD: It is the maximum difference between the new and old values in the dimension selected for mutation
- Repeat it for all the copied cats.
- Evaluate the fitness value of each position modified cats.
- The best fitted cat is retained and the remaining are discarded.
- Repeat it for all seeking mode cats.
- In this way, again 0.8N new cats are created out of seeking operations.

#### 5. Tracing Mode Operation

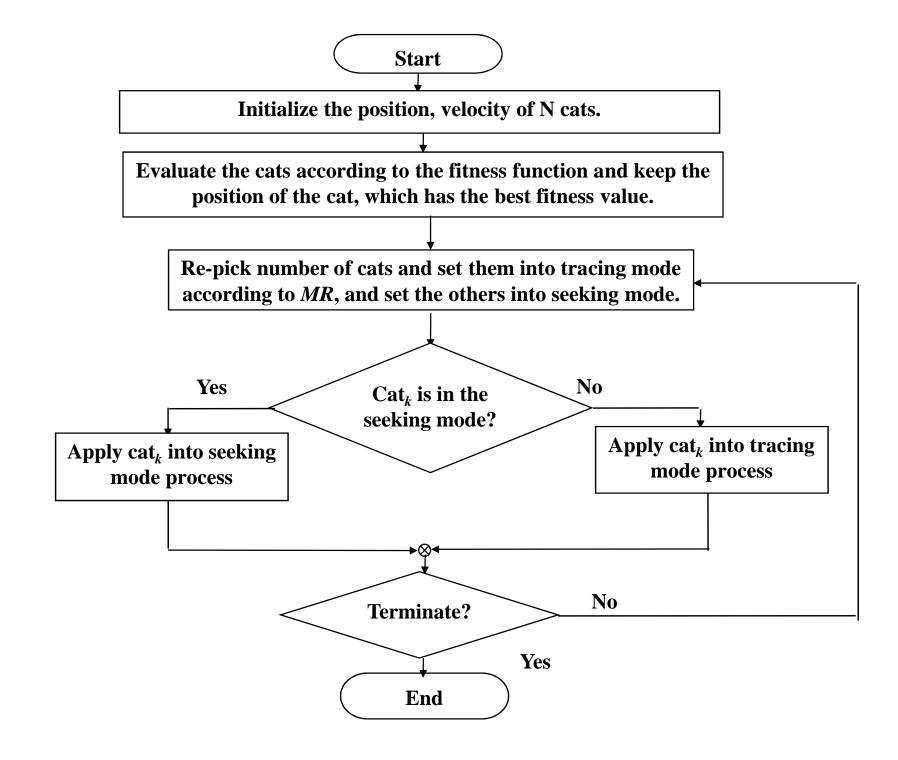
- The remaining 0.2N are under tracing mode.
- They follow PSO steps without using personal best (Pbest) values.
- Evaluate the fitness value of each of 0.2N cats
- Find the global best position (gbest) of these cats.
- Using initial positions and gbest value, update the velocity of each cat [Update velocity matrix]

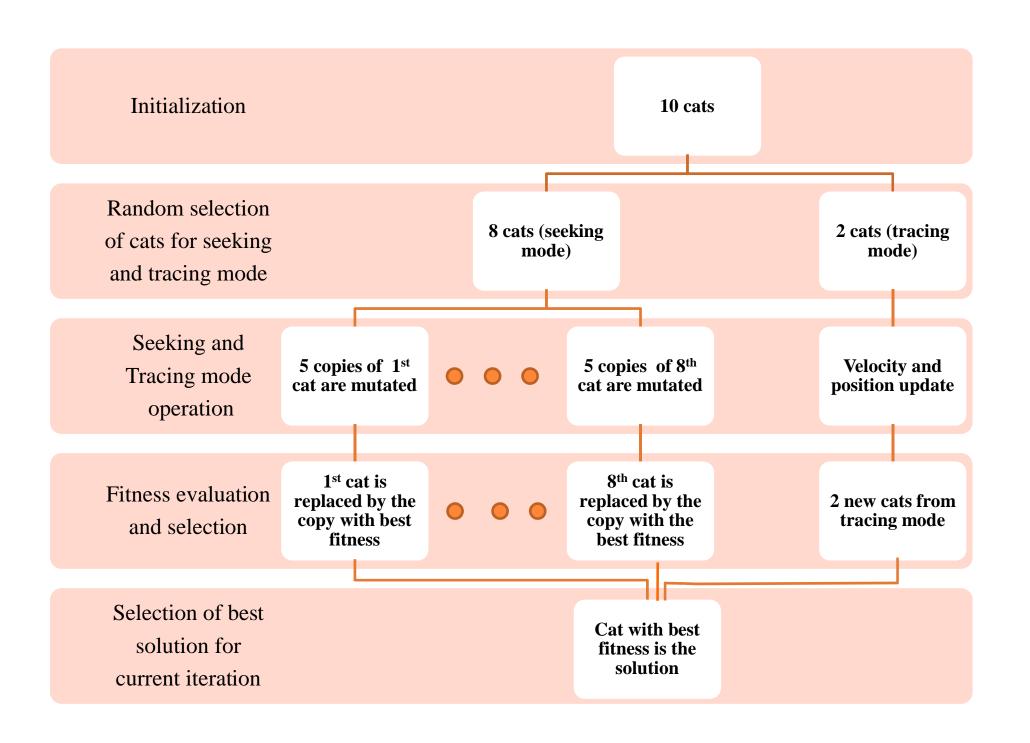
$$v_{k,d} = v_{k,d} + r_1 \times c_1 \times \left(x_{gbest,d} - x_{k,d}\right)$$

- $\circ r_1$  A random variable belongs to [0,1].
- $\circ c_1$  A constant, which is set to 2 in the experiments.
- Update the position of each particle using the modified velocity value.

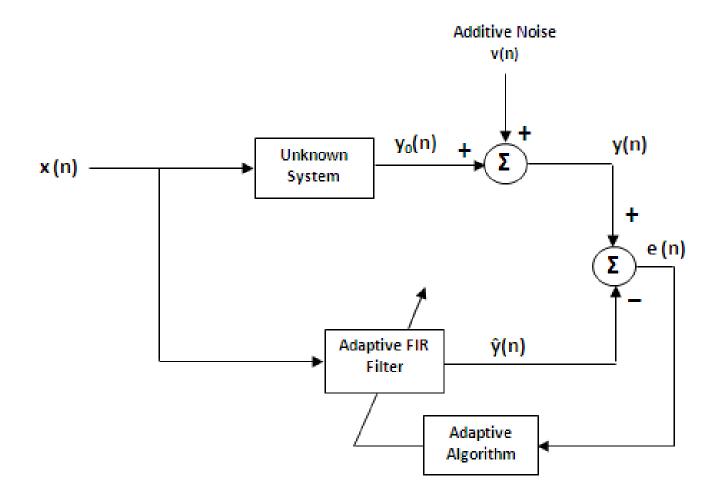
$$x_{k,d} = x_{k,d} + v_{k,d}$$

- 6. Create the new population by combining (0.8N + 0.2N) cats obtained from seeking and tracing mode respectively.
- 7. Evaluate the fitness value of each of the new N cats.
- 8. Update the gbest
- 9. Check the termination condition, if satisfied, terminate the program. Otherwise repeat steps 4 to 8.

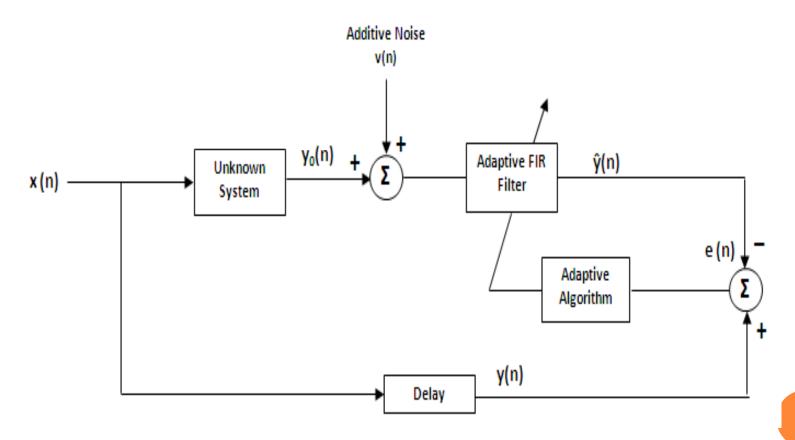




## DIRECT MODELING



## INVERSE MODELING



#### SIMULATION STUDY

Transfer function of the benchmark plant

$$H(z) = 0.26 + 0.93 z^{-1} + 0.26 z^{-2}$$

- 4 different cases for simulation study:
  - a) Direct modeling of the plant
  - b) Inverse modeling of the plant
  - c) Direct modeling of the plant with nonlinearity
  - d) Inverse modeling of the plant with nonlinearity
- Nonlinearity = hyperbolic tangent function{tanh(x)}

#### PARAMETER SETTINGS

#### **Parameter settings for CSO**

Parameter	Value or Range
SMP	5
SRD	20%
CDC	80%
MR	2%
$c_{_{I}}$	2.0
$r_1$	[0, 1]

#### **Parameter settings for PSO**

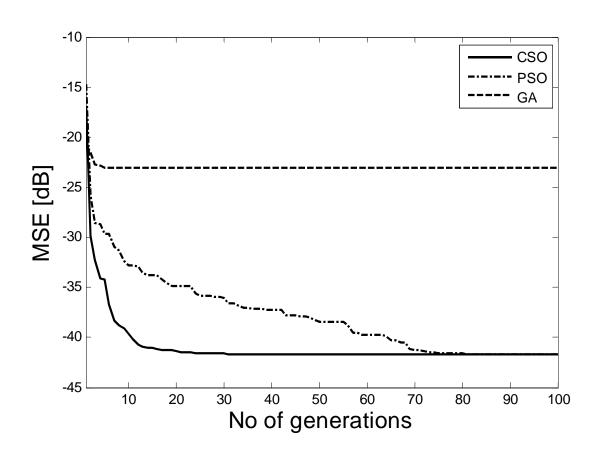
Parameter	Value or Range
Initial Weight	0.9
Final Weight	0.4
$c_{I}$	2.0
$c_2$	2.0
$r_1$	[0, 1]
$r_2$	[0,1]

#### PARAMETER SETTINGS

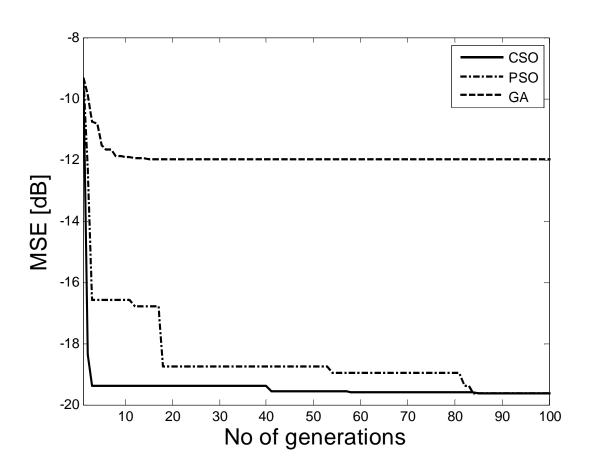
#### **Parameter settings for GA**

Parameter	Value or Range	
Pc	0.8	□ Population Size: 50
Pm	0.1	-
No of bits	10	□ Rounds for Average: 50

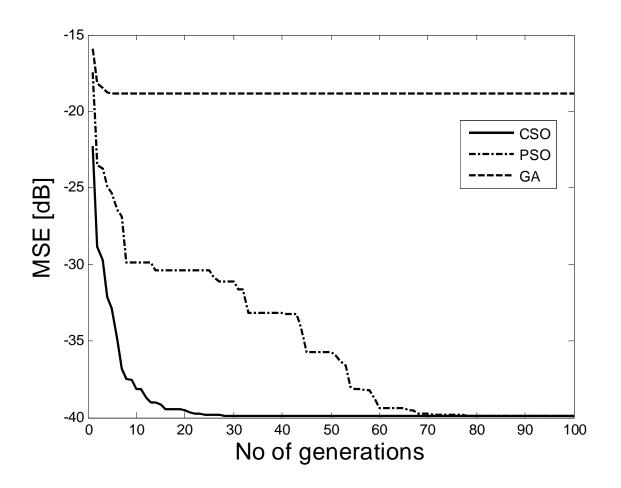
## CONVERGENCE CHARACTERISTIC FOR DIRECT MODELING



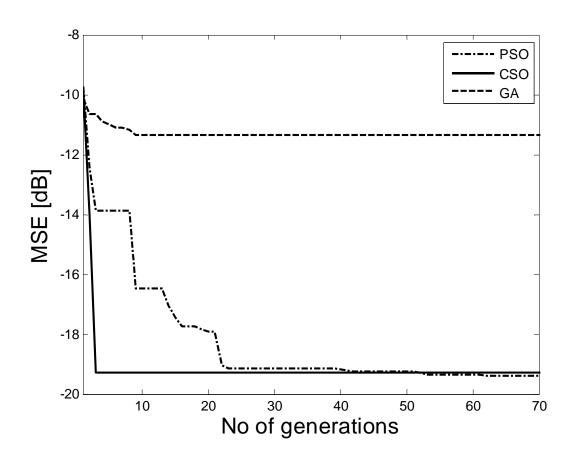
## CONVERGENCE CHARACTERISTIC FOR INVERSE MODELING



## CONVERGENCE CHARACTERISTIC FOR DIRECT MODELING WITH NONLINEARITY



## CONVERGENCE CHARACTERISTIC FOR INVERSE MODELING WITH NONLINEARITY



### IIR SYSTEM IDENTIFICATION

2<sup>nd</sup> Order IIR System: 
$$H_s(z) = \frac{0.05 - 0.4z^{-1}}{1 - 1.1314z^{-1} + 0.25z^{-1}}$$

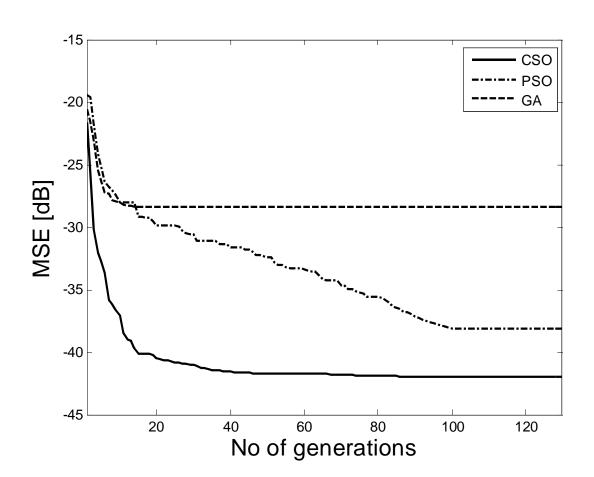
**Equal Order Modeling** 

$$H_s(z) = \frac{a_0 + a_1 z^{-1}}{1 - b_1 z^{-1} - b_2 z^{-1}}$$

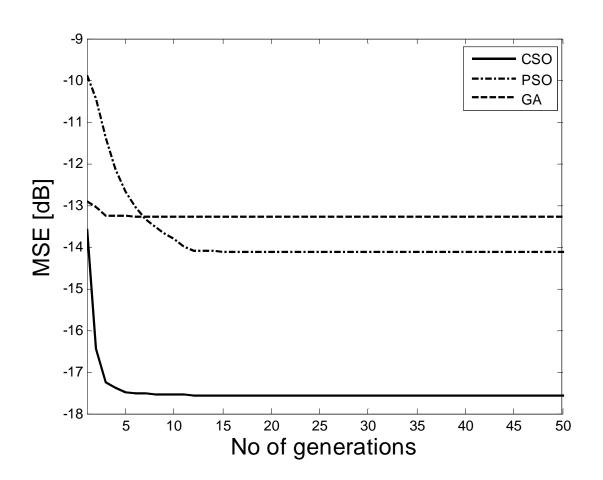
Reduced Order Modeling

$$H_{s}(z) = \frac{a_0}{1 - b_1 z^{-1}}$$

## CONVERGENCE CHARACTERISTIC FOR EQUAL ORDER MODELING OF IIR SYSTEM



### CONVERGENCE CHARACTERISTIC FOR REDUCED ORDER MODELING OF IIR SYSTEM



### **CONCLUSION**

- A new algorithm, Cat Swarm Optimization, is presented by modeling the behaviors of cat for solving the optimization problems.
- The experimental results indicate that CSO is a better candidate for finding the global best solutions in comparison to GA and PSO.

#### REFERENCES

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- Pyari Mohan Pradhan, Ganpti Panda, Solving multiobjective problems using cat swarm optimization, Expert Systems with Applications, Volumn 39, 15 February 2012 Pages 2956-2964, ISSN 0957-4174, 10.1016/j.eswa.2011.08.057
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