

Hausdorff distance is the maximum distance of a set to the nearest point in the other set. It is distance from set A to set B and called a maximin function, and defined as

Given two finite point sets

$$A = \{a_1, a_2, \dots, a_p\} \text{ and}$$

$$B = \{b_1, b_2, \dots, b_q\}$$

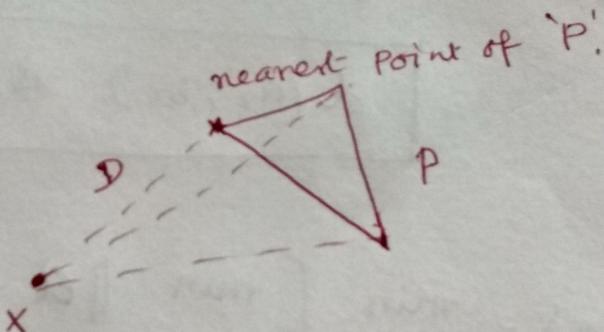
$$H(A, B) = \max(h(A, B), h(B, A))$$

where

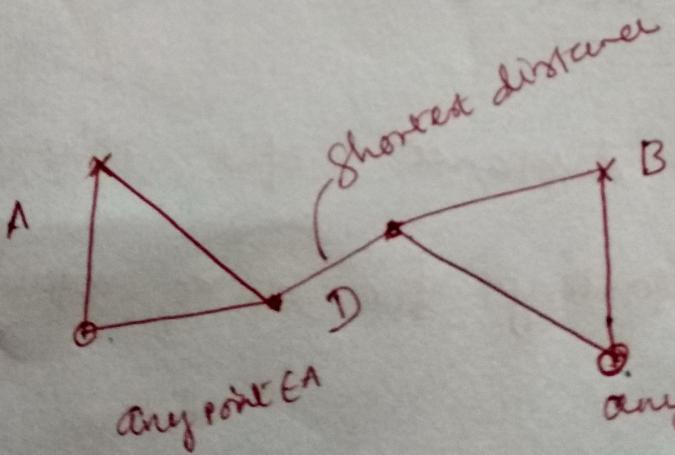
$$h(A, B) = \max_{a \in A} \left\{ \min_{b \in B} \|a - b\| \right\}$$

Shortest Distance:

Motivation: Eg : 2



Eg : 3

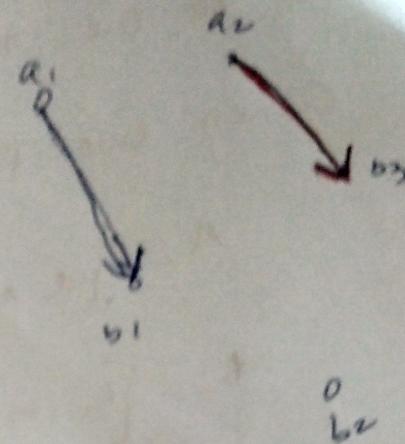
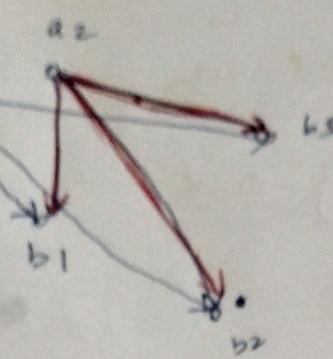


$$D(A, B) = \min_{a \in A} \left\{ \min_{b \in B} \|a - b\| \right\}$$

Consider set of points

Eg: 1

A a₁ a₂



for every point $a \in A$; for any point $b \in B$
 find one smallest distance; finally keep the
 smallest distance among all point \underline{a} .

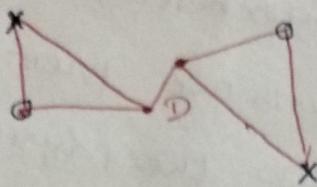
$$d(a_2, b_3) \text{ is one } D(A, B)$$

$$D(A, B) = \min_{a \in A} \left\{ \min_{b \in B} \|a - b\| \right\} \Rightarrow \text{minimum function}$$

This def of distance b/w polygons can be
 quite unsatisfactory for some applications;

Consider eq: 3 now

(2)



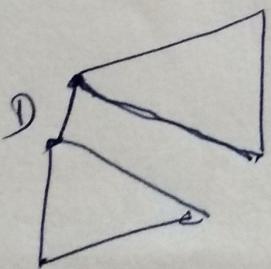
The shortest distance does not consider the whole shape

The shortest distance 'd' between these polygons means that no point of one polygon is far from the other polygon.

In this sense ; the two polygon shown are not so close ; as their furthest points 'x' could actually be very far ~~away~~ away from other polygon.

* Clearly the shortest distance is totally independent of each polygonal shape.

Another issue:



where we have same two triangles at the same shortest distance ; but in different position.

It is quite obvious that the shortest distance
concept carries very low information, as the distance
value did not change with the previous case, while
something did change with the polygon objects)

These two issues, which are ignored by the
shortest distance is handled by Hausdorff distance