

CS315: Principles of Database Systems

Normalization Theory

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Database design

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- Informal
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 - No spurious tuple
- Normalization theory answers in the formal manner

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 - Changing name of project id 7 causes updates to many employees
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 - Inserting an employee immediately requires a project and vice versa
- **Delete anomaly**
 - Deleting a project may delete all its employees

Decomposition

- Must preserve **losslessness** of the corresponding join
- **Lossy decomposition**

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id	name	yob
1	A	81
2	A	83

is decomposed into

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- Try to preserve **functional dependencies**

Functional dependencies

- **Functional dependencies** (FDs) are *constraints* derived from the meaning of and relationships among attributes
- A set of attributes X **functionally determines** Y , denoted by $X \rightarrow Y$, if the value of X determines a *unique* value of Y
- For any two tuples t_1 and t_2 in any *legal* instance of $r(R)$, if $t_1.X = t_2.X$ then $t_1.Y = t_2.Y$
- Example: roll \rightarrow name
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- A FD $X \rightarrow Y$ is **trivial** if it is satisfied for *all* instances of a relation, i.e., $Y \subseteq X$
- A candidate key functionally determines all attributes
- Functional dependencies and keys define **normal forms** for relations
- Normal forms are formal measures of how “good” a database design is

Armstrong's axioms

- Given a set of FDs, additional FDs can be inferred using **Armstrong's inference rules** or **Armstrong's axioms**
 - Reflexive**: If $Y \subseteq X$, then $X \rightarrow Y$
 - Augmentation**: If $X \rightarrow Y$, then $XZ \rightarrow YZ$
 - Transitive**: If $X \rightarrow Y$ and $Y \rightarrow Z$, then $X \rightarrow Z$

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- These rules are
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- Other rules
 - Decomposition**: If $X \rightarrow YZ$, then $X \rightarrow Y$ and $X \rightarrow Z$
 - Union**: If $X \rightarrow Y$ and $X \rightarrow Z$, then $X \rightarrow YZ$
 - Pseudotransitivity**: If $X \rightarrow Y$ and $WY \rightarrow Z$, then $WX \rightarrow Z$

Properties of FDs

- **Closure** of a set F of FDs is the set F^+ of all FDs that can be inferred from F
- Closure of a set of attributes X with respect to F is the set X^+ of all attributes that are functionally determined by X using F^+

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- Two sets of FDs F and G are **equivalent** if every FD in F can be inferred from G and vice versa
- F and G are equivalent if $F^+ = G^+$
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- F and G are equivalent if $F^+ = G^+$
- F and G are equivalent if F covers G and G covers F
- A set of FDs is **minimal** if
 - Every FD in F has only a single attribute in RHS
 - Any $G \subset F$ is not equivalent to F
 - Any $F - (X \rightarrow A) \cup (Y \rightarrow A)$ where $Y \subset X$ is not equivalent to F
- Every set of FD has *at least one* equivalent minimal set

Normal forms

- The process of decomposing relations into smaller relations that conform to certain norms is called **normalization**
- Keys and FDs of a relation determine which **normal form** a relation is in
- Different normal forms
 - **1NF**: based on attributes only
 - **2NF**, **3NF**, **BCNF**: based on keys and FDs
 - **4NF**: based on keys and multi-valued dependencies (MVDs)
 - **5NF** or **PJNF**: based on keys and join dependencies
 - **DKNF**: based on all constraints

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- A relation is in 1NF if
 - Every attribute must be atomic
- Phone numbers
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1	A	{3, 4}
2	B	{5}

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- Nested relations

Id	Name	Project		
		ProjId	Hrs	
1	A	1	30	should be broken into
1	A	2	20	
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Prime attribute, full functional dependency and transitive functional dependency

- A **prime attribute** must be a member of some candidate key
 - Example: roll
- A **non-prime attribute** is not a member of any candidate key
 - Example: gender

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- A FD $X \rightarrow Y$ is a **full functional dependency** if the FD does not hold when any attribute from X is removed
 - Example: (roll) \rightarrow (name)
- It is a **partial functional dependency** otherwise
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- It is a **partial functional dependency** otherwise
 - (roll, gender) \rightarrow (name)
- A FD $X \rightarrow Y$ is a **transitive functional dependency** if it can be derived from two FDs $X \rightarrow Z$ and $Z \rightarrow Y$
 - Example: (roll) \rightarrow (hod) since (roll) \rightarrow (deptid) and (deptid) \rightarrow (hod) hold
- It is **non-transitive** otherwise
 - Example: (roll) \rightarrow (name)

Second normal form (2NF)

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 $(Id, ProjId) \rightarrow (Hrs)$; $(Id) \rightarrow (Name)$; $(ProjId) \rightarrow (ProjName)$

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 - (Id, Name) with FD: $(Id) \rightarrow (Name)$
 - (ProjId, ProjName) with FD: $(ProjId) \rightarrow (ProjName)$

Third normal form (3NF)

- A relation is in 3NF if
 - It is in 2NF, and
 - No non-prime attribute is transitively functionally dependent on the candidate keys
- Alternatively, for every FD $X \rightarrow Y$, either
 - It is trivial, or
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Example

- $L = (\underline{\text{Id}}, \text{Dist}, \text{Lot}, \text{Area}, \text{Price}, \text{Rate})$ with FDs:
 - $(\text{Id}) \rightarrow (\text{Dist}, \text{Lot}, \text{Area}, \text{Price}, \text{Rate})$
 - $(\text{Dist}, \text{Lot}) \rightarrow (\text{Id}, \text{Area}, \text{Price}, \text{Rate})$
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 - $(\text{Area}) \rightarrow (\text{Price})$

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 - $(\text{Dist}, \text{Lot}) \rightarrow (\text{Id}, \text{Area}, \text{Price}, \text{Rate})$
 - $(\text{Dist}) \rightarrow (\text{Rate})$
 - $(\text{Area}) \rightarrow (\text{Price})$
- L is not in 2NF because (Rate) depends partially on (Dist)
- $L_1 = (\underline{\text{Id}}, \text{Dist}, \text{Lot}, \text{Area}, \text{Price})$ with FDs:
 - $(\text{Id}) \rightarrow (\text{Dist}, \text{Lot}, \text{Area}, \text{Price})$
 - $(\text{Dist}, \text{Lot}) \rightarrow (\text{Id}, \text{Area}, \text{Price})$
 - $(\text{Area}) \rightarrow (\text{Price})$
- $L_2 = (\underline{\text{Dist}}, \text{Rate})$ with FD:
 - $(\text{Dist}) \rightarrow (\text{Rate})$

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 - $(\text{Dist}, \text{Lot}) \rightarrow (\text{Id}, \text{Area}, \text{Price})$
 - $(\text{Area}) \rightarrow (\text{Price})$
- $L_2 = (\underline{\text{Dist}}, \text{Rate})$ with FD:
 - $(\text{Dist}) \rightarrow (\text{Rate})$
- L_1 is in 2NF but not 3NF because (Price) depends on (Id) through (Area)

Example

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 - $(\text{Id}) \rightarrow (\text{Dist}, \text{Lot}, \text{Area}, \text{Price}, \text{Rate})$
 - $(\text{Dist}, \text{Lot}) \rightarrow (\text{Id}, \text{Area}, \text{Price}, \text{Rate})$
 - $(\text{Dist}) \rightarrow (\text{Rate})$
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- L is not in 2NF because (Rate) depends partially on (Dist)
- $L_1 = (\underline{\text{Id}}, \text{Dist}, \text{Lot}, \text{Area}, \text{Price})$ with FDs:
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 - $(\text{Dist}, \text{Lot}) \rightarrow (\text{Id}, \text{Area}, \text{Price})$
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- L_2 is in 2NF and in 3NF

Example (contd.)

- $L_1 = (\underline{\text{Id}}, \text{Dist}, \text{Lot}, \text{Area}, \text{Price})$ with FDs:
 - $(\text{Id}) \rightarrow (\text{Dist}, \text{Lot}, \text{Area}, \text{Price})$
 - $(\text{Dist}, \text{Lot}) \rightarrow (\text{Id}, \text{Area}, \text{Price})$
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 - $(\text{Area}) \rightarrow (\text{Price})$
- L_1 is in 2NF but not 3NF because (Price) depends on (Id) through (Area)
- $L_{11} = (\underline{\text{Id}}, \text{Dist}, \text{Lot}, \text{Area})$ with FDs:
 - $(\text{Id}) \rightarrow (\text{Dist}, \text{Lot}, \text{Area})$
 - $(\text{Dist}, \text{Lot}) \rightarrow (\text{Id}, \text{Area})$
- $L_{12} = (\underline{\text{Area}}, \text{Price})$ with FD:
 - $(\text{Area}) \rightarrow (\text{Price})$

Example (contd.)

- $L_1 = (\underline{\text{Id}}, \text{Dist}, \text{Lot}, \text{Area}, \text{Price})$ with FDs:
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 - $(\text{Dist}, \text{Lot}) \rightarrow (\text{Id}, \text{Area})$
- $L_{12} = (\underline{\text{Area}}, \text{Price})$ with FD:
 - $(\text{Area}) \rightarrow (\text{Price})$
- L_{11} and L_{12} are in 3NF

Boyce-Codd normal form (BCNF)

- A relation is in BCNF
 - If $X \rightarrow Y$ is a non-trivial FD, then X is a superkey of R
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 - Loses $(Dist, Lot) \rightarrow (Id, Area)$

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- Remedy
 - BCNF: Decompose and set up a relation for each nonkey attribute with attributes functionally dependent on it

Lossless decomposition

- BCNF decomposition is not always possible
- (town, state, dist) with FDs:
 $(\text{town}, \text{state}) \rightarrow (\text{dist}); (\text{dist}) \rightarrow (\text{state})$

town	state	dist
iit	up	east
iit	wb	mdp
prayag	up	east
prayag	wb	dinaj
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- However, the decomposition is *not* lossless
- Also, (town, state) and (town, dist) is lossy
- Only (town, dist) and (state, dist) is lossless
- Losslessness *must* be preserved

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- Modification anomalies are still there
 - Inserting a new teacher for db requires two tuples
- Better design if (course, teacher) and (course, book)

Multi-valued dependency (MVD)

- A **multi-valued dependency (MVD)** $X \twoheadrightarrow Y$ holds for a relation schema R if for all *legal* relations $r(R)$, if for a pair of tuples t_1 and t_2 , $t_1.X = t_2.X$, then there exists another pair of tuples t_3 and t_4
 - $t_1.X = t_2.X = t_3.X = t_4.X$
 - $t_3.Y = t_1.Y$
 - $t_3.R - Y - X = t_2.R - Y - X$
 - $t_4.Y = t_2.Y$
 - $t_4.R - Y - X = t_1.R - Y - X$

	X	Y	R - Y - X
t_1	a	b	c
t_2	a	d	e
t_3	a	b	e
t_4	a	d	c

- Example: $(\text{course}) \twoheadrightarrow (\text{teacher})$ in $(\text{course}, \text{teacher}, \text{book})$
 - If $(\text{db}, \text{ab}, \text{fdb})$ and $(\text{db}, \text{sg}, \text{dbm})$ exist, then $(\text{db}, \text{ab}, \text{dbm})$ and $(\text{db}, \text{sg}, \text{fdb})$ must exist
 - Otherwise, ab has something to do with fdb

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- **Closure** of a set of MVDs is the set of all MVDs that can be inferred using the following rules

Inference rules

- **Complementation**: If $X \twoheadrightarrow Y$, then $X \twoheadrightarrow R - (X \cup Y)$
- **Augmentation**: If $X \twoheadrightarrow Y$ and $Z \subseteq W$, then $XW \twoheadrightarrow YZ$
- **Transitive**: If $X \twoheadrightarrow Y$ and $Y \twoheadrightarrow Z$, then $X \twoheadrightarrow Z - Y$
- **Replication**: If $X \rightarrow Y$, then $X \twoheadrightarrow Y$
- **Coalescence**: If $X \twoheadrightarrow Y$ and $\exists W$ s.t. $W \cap Y = \Phi$, $W \rightarrow Z$, and $Z \subseteq Y$, then $X \rightarrow Z$

Fourth normal form (4NF)

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- Consider (course, teacher, book) with MVD: $\text{course} \twoheadrightarrow \text{book}$
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- After 4NF normalization,
 - (course, book) with trivial MVD: $(\text{course}) \twoheadrightarrow (\text{book})$
 - (course, teacher) with trivial MVD: $(\text{course}) \twoheadrightarrow (\text{teacher})$
- Decompose R with $X \twoheadrightarrow Y$ into (X, Y) and $(X, R - Y - X)$

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 - (course, teacher) with trivial MVD: $(\text{course}) \twoheadrightarrow (\text{teacher})$
- Decompose R with $X \twoheadrightarrow Y$ into (X, Y) and $(X, R - Y - X)$
- Good design ensures that every relation is in 3NF or BCNF

Join dependency (JD)

- General way of decomposing a relation into multi-way joins
- A **join dependency (JD)** (R_1, \dots, R_n) holds for a relation schema R if for all *legal* relations $r(R)$, $\bowtie_{i=1}^n (\Pi_{R_i}(r)) = r$
- A JD is **trivial** if one of R_i is R itself

Salesman	Brand	Product
J	A	V
J	A	B
W	R	P
W	R	V
W	R	B
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- Suppose, the following rule holds: If S sells products of brand B and if S sells product type P, then S *must* sell product type P of brand B (assuming B makes P)
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- A MVD is a special case of JD with $n = 2$

Fifth normal form (5NF) or Project-Join normal form (PJNF)

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- Consider that J starts selling brand R's products
- Insertion anomaly since multiple tuples need to be inserted
- Better design if broken into three relations (B,P), (S,B), and (P,S)

Brand	Product	Salesman	Brand	Product	Salesman
A	V			V	J
A	B	J	A	B	J
R	P	W	R	P	W
R	V	W	A	V	W
R	B			B	W

- Now, insertion requires only one tuple (J, R) in (Salesman, Brand)

Domain-Key normal form (DKNF)

- A relation schema is in **domain-key normal form (DKNF)** if all constraints and relations that should hold can be enforced simply by domain constraints and key constraints
- *Ideal* normal form
- Mostly theoretical
- Once a relation is in DKNF, there is no anomaly and FDs and MVDs need not be checked any more