

# Embedding Methods for NLP

## Part 1: Unsupervised and Supervised Embeddings

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EMNLP tutorial – October 29, 2014

# What is a word embedding?

Suppose you have a dictionary of words.

The  $i^{th}$  word in the dictionary is represented by an embedding:

$$w_i \in \mathbb{R}^d$$

i.e. a  $d$ -dimensional vector, which is **learnt!**

- $d$  typically in the range 50 to 1000.
- Similar words should have similar embeddings (share latent features).
- Embeddings can also be applied to *symbols* as well as words (e.g. Freebase nodes and edges).
- Discuss later: can also have embeddings of phrases, sentences, documents, or even other modalities such as images.



## Main methods we highlight, ordered by date.

- Latent Semantic Indexing (Deerwester et al., '88).
- Neural Net Language Models (NN-LMs) (Bengio et al., '06)
- Convolutional Nets for tagging (SENNNA) (Collobert & Weston, '08).
- Supervised Semantic Indexing (Bai et al, '09).
- Wsabie (Weston et al., '10).
- Recurrent NN-LMs (Mikolov et al., '10).
- Recursive NNs (Socher et al., '11).
- Word2Vec (Mikolov et al., '13).
- Paragraph Vector (Le & Mikolov, '14).
- Overview of recent applications.

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## Ranking and Retrieval: The Goal

We want to learn to match a query (text) to a target (text).



Many classical supervised ranking methods use hand-coded features.



Methods like LSI that learn from words are unsupervised.

💡 Supervised Semantic Indexing (SSI) uses supervised learning from text only:

💡 *Bai et al, Learning to Rank with (a Lot of) Word Features. Journal of Information Retrieval, '09.*

💡 *Outperforms existing methods (on words) like TFIDF, LSI or a (supervised) margin ranking perceptron baseline.*

## Basic Bag-O'-Words



Bag-of-words + cosine similarity:

- Each doc.  $\{d_t\}_{t=1}^N \subset \mathbb{R}^D$  is a *normalized* bag-of-words.
- Similarity with query  $q$  is:  $f(q, d) = q^\top d$



Doesn't deal with synonyms: bag vectors can be orthogonal



No machine learning at all

# Latent semantic indexing (LSI)



Learn a linear embedding  $\phi(d_i) = Ud_i$  via a reconstruction objective.

- Rank with:  $f(q, d) = q^\top U^\top Ud = \phi(q)^\top \phi(d_i)$ <sup>1</sup>.



Uses “synonyms”: *low-dimensional latent “concepts”*.



Unsupervised machine learning: useful for goal?

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<sup>1</sup> $f(q, d) = q^\top (U^\top U + \alpha I)d$  gives better results.

Also, usually normalize this → cosine similarity.

# Supervised Semantic Indexing (SSI)

- Basic model: rank with

$$f(q, d) = q^\top Wd = \sum_{i,j=1}^{\mathcal{D}} q_i W_{ij} d_j$$

i.e. learn weights of polynomial terms between documents.

- Learn  $W \in \mathbb{R}^{\mathcal{D} \times \mathcal{D}}$  (huge!) with click-through data or other labels.



Uses “synonyms”



Supervised machine learning: targeted for goal



Too Big/Slow?! Solution = Constrain  $W$  :

**low rank** → embedding model!

## SSI: why is this a good model?

Classical bag-of-words doesn't work when there are few matching terms:

$$q = (\text{kitten}, \text{vet}, \text{nyc})$$

$$d = (\text{cat}, \text{veterinarian}, \text{new}, \text{york})$$



Method  $q^T Wd$  learns that e.g. kitten and cat are highly related.



E.g. if  $i$  is the index of kitten and  $j$  is the index of cat, then  $W_{ij} > 0$  after training.

## SSI: Why the Basic Model Sucks



$W$  is **big** : 3.4Gb if  $\mathcal{D} = 30000$ , 14.5Tb if  $\mathcal{D} = 2.5M$ .



**Slow:**  $q^T W d$  computation has  $mn$  computations  $q_j W_{ij} d_i$ , where  $q$  and  $d$  have  $m$  and  $n$  nonzero terms.



Or one computes  $v = q^T W$  once, and then  $vd$  for each document.  
Classical speed where query has  $\mathcal{D}$  terms, assuming  $W$  is dense →  
**still slow.**



One could minimize  $\|W\|_1$  and attempt to make  $W$  sparse. Then at most  $mp$  times slower than classical model (with  $p$  nonzeros in a column.)

## SSI Improved model: Low Rank $W$

💡 Constrain  $W$ :

$$W = U^\top V + I.$$

💡  $U$  and  $V$  are  $N \times D$  matrices  $\rightarrow$  smaller

💡 Low dimensional “latent concept” space like LSI (same speed).

💡 Differences: supervised, asymmetric, learns with  $I$ .

Variants:

- $W = I$ : bag-of-words again.
- $W = D$ , reweighted bag-of-words related to [Grangier and Bengio, 2005].
- $W = U^\top U + I$ : symmetric.

## SSI: Training via maximizing AUC

- Given a set of tuples  $\mathcal{R}$  with a query  $q$ , a related document  $d^+$  and an unrelated (or lower ranked) document  $d^-$ .
- We would like  $f(q, d^+) > f(q, d^-)$ .
- Minimize margin ranking loss [Herbrich et al., 2000]:

$$\sum_{(q, d^+, d^-) \in \mathcal{R}} \max(0, 1 - f(q, d^+) + f(q, d^-)).$$

Learning Algorithm Stochastic Gradient Descent: **Fast & scalable.**

Iterate | Sample a triplet  $(q, d^+, d^-)$ ,  
Update  $W \leftarrow W - \lambda \frac{\partial}{\partial W} \max(0, 1 - f(q, d^+) + f(q, d^-))$ .

Other options: batch gradient, parallel SGD (hogwild), Adagrad . . .

## Training: setting hyperparameters

The following hyperparameters can be tuned for training:

- The initial random weights of the embedding vectors:  
e.g. use (mean 0, variance  $\frac{1}{\sqrt{d}}$ ) .
- The learning rate (typically: 0.0001, 0.001, 0.01, 0.1, ...).
- The value of the margin (e.g.: 1, 0.5, 0.2, 0.1, ...).
- Restricting the norm of embeddings:  
 $||U_i|| \leq C, ||V_i|| \leq C$  (e.g.: C=1).

*All these parameters are relative to each other, e.g. a larger margin might need larger initial weights and learning rate.*

*Typically, we fix the initialization and norm, and try different values of margin and learning rate. This can make big differences in performance.*

## Prior Work: Summary of learning to Rank

- [Grangier & Bengio, '06] used similar methods to basic SSI for retrieving images.
- [Goel, Langord & Strehl, '08] used Hash Kernels (Vowpal Wabbit) for advert placement.
- Main difference: SSI uses low rank on  $W$ .
- SVM [Joachims, 2002] and NN ranking methods [Burges, 2005].  
Use hand-coded features: title, body, URL, search rankings,... (don't use words)  
(e.g. Burges uses 569 features in all).
- In contrast SSI uses only the words and trains on huge feature sets.
- Several works on optimizing different loss functions (MAP, ROC, NDCG):  
[Cao, 2008], [Yu, 2007], [Qin, 2006],...
- Lots of stuff for “metric learning” problem as well..



One could also add features + new loss to this method ..

# Experimental Comparison

- **Wikipedia**
  - 1,828,645 documents. 24,667,286 links.
  - Split into 70% train, 30% test.
- Pick random doc. as query, then rank other docs.
- Docs that are linked to it should be highly ranked.
- **Two setups:**
  - (i) whole document is used as query;
  - (ii) 5,10 or 20 words are picked to mimic keyword search.

## Wikipedia Experiments: Document Retrieval Performance

Experiments on Wikipedia, which contains 1.8M documents: retrieval task using the link structure and separated the data into 70% for training and 30% for test.

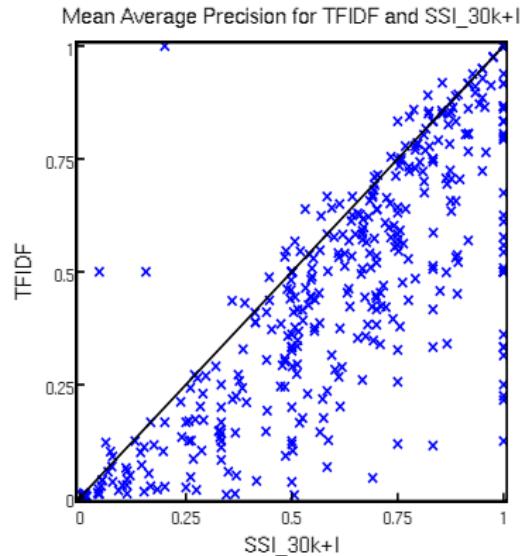
### Document based retrieval:

Algorithm	Rank-Loss	MAP	P10
TFIDF	0.842%	0.432±0.012	0.193
$\alpha$ LSI + $(1 - \alpha)$ TFIDF	0.721%	0.433	0.193
Linear SVM Ranker	0.410%	0.477	0.212
Hash Kernels + $\alpha$ I	0.322%	0.492	0.215
SSI	0.158%	0.547±0.012	0.239±0.008

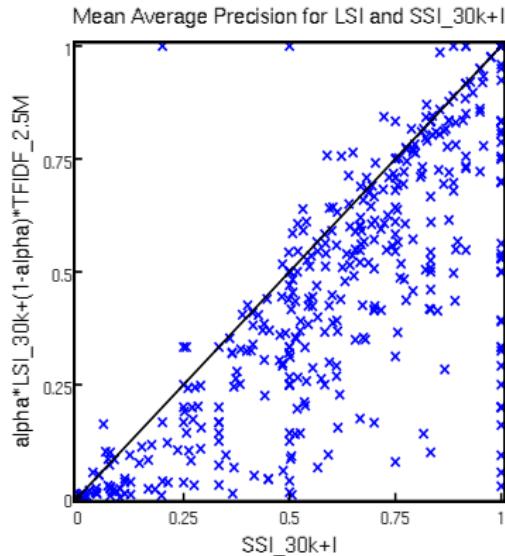
### k-keywords based retrieval:

$k = 5$ : Algorithm	Params	Rank	MAP	P@10
TFIDF	0	21.6%	0.047	0.023
$\alpha$ LSI + $(1 - \alpha)$ TFIDF	$200\mathcal{D}+1$	14.2%	0.049	0.023
SSI	$400\mathcal{D}$	<b>4.37%</b>	<b>0.166</b>	<b>0.083</b>

## Scatter Plots: SSI vs. TFIDF and LSI



(a)



(b)

Figure : Scatter plots of Average Precision for 500 documents:  
(a) SSI vs. TFIDF, (b) SSI vs.  $\alpha$ LSI +  $(1 - \alpha)$  TFIDF.

## Experiments: Cross-Language Retrieval

Retrieval experiments using a query document in Japanese, where the task is to retrieve documents in English (using link structure as ground truth).

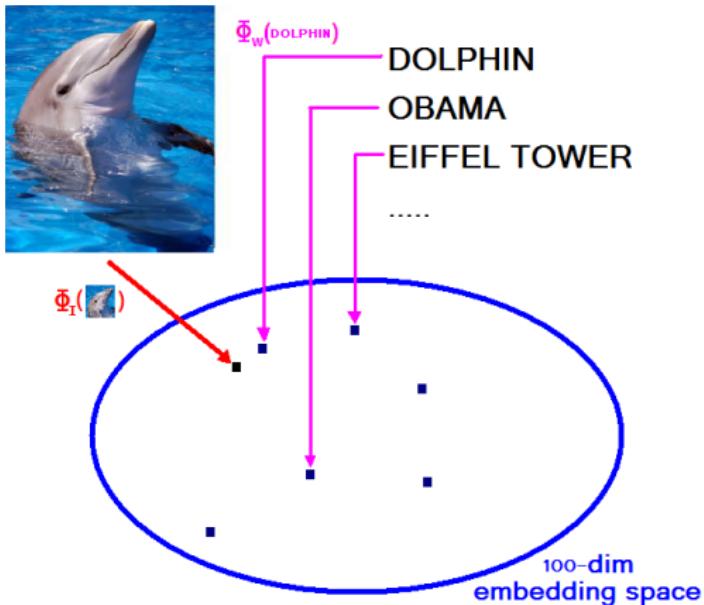
SSI can do this without doing a translation step first as it learns to map the two languages together in the embedding space.

Algorithm	Rank-Loss	MAP	P10
$\text{TFIDF}_{\text{EngEng}}$ (Google translated queries)	4.78%	0.319	0.259
$\alpha \text{LSI}_{\text{EngEng}} + (1 - \alpha) \text{TFIDF}_{\text{EngEng}}$	3.71%	0.300	0.253
$\alpha \text{CL-LSI}_{\text{JapEng}} + (1 - \alpha) \text{TFIDF}_{\text{EngEng}}$	3.31%	0.275	0.212
$\text{SSI}_{\text{EngEng}}$	1.72%	0.399	0.325
$\text{SSI}_{\text{JapEng}}$	0.96%	0.438	0.351
$\alpha \text{SSI}_{\text{JapEng}} + (1 - \alpha) \text{TFIDF}_{\text{EngEng}}$	0.75%	0.493	0.377
$\alpha \text{SSI}_{\text{JapEng}} + (1 - \alpha) \text{SSI}_{\text{EngEng}}$	<b>0.63%</b>	<b>0.524</b>	<b>0.386</b>

Some recent related translation-based embeddings:  
(Hermann & Blunsom, ICLR '14) and (Mikolov et al., '13).

## Wsabie (Weston, Bengio & Usunier, '10)

- Extension to SSI, also embeds objects other than text, e.g. images.
- WARP loss function that optimizes precision@k.



Learn  $\Phi_I(\cdot)$  and  $\Phi_W(\cdot)$  to optimize precision@k.

## Joint Item-Item Embedding Model

L.H.S: Image, query string or user profile (depending on the task)

$$\Phi_{LHS}(x) = U\Phi_x(x) : \mathbb{R}^{d_x} \rightarrow \mathbb{R}^{100}.$$

R.H.S: document, image, video or annotation (depending on the task)

$$\Phi_{RHS}(y) = V\Phi_y(y) : \mathbb{R}^{d_y} \rightarrow \mathbb{R}^{100}.$$

This model again compares the degree of match between the L.H.S and R.H.S in the embedding space:

$$f_y(x) = \text{sim}(\Phi_{LHS}(x), \Phi_{RHS}(y)) = \Phi_x(x)^\top U^\top V\Phi_y(y)$$

*Also constrain the weights (regularize):*

$$\|U_i\|_2 \leq C, \quad i = 1, \dots, d_x, \quad \|V_i\|_2 \leq C, \quad i = 1, \dots, d_y.$$

## Ranking Annotations: AUC is Suboptimal

Classical approach to learning to rank is maximize AUC by minimizing:

$$\sum_x \sum_y \sum_{\bar{y} \neq y} \max(0, 1 + f_{\bar{y}}(x) - f_y(x))$$

**Problem:** All pairwise errors are considered the same, it counts the number of ranking violations.

**Example:**

Function 1: true annotations ranked 1st and 101st.

Function 2: true annotations ranked 50th and 52nd.

AUC prefers these *equally* as both have 100 “violations”.

We want to optimize the top of the ranked list!

## Rank Weighted Loss [Usunier et al. '09]

Replace classical AUC optimization:

$$\sum_x \sum_y \sum_{\bar{y} \neq y} \max(0, 1 + f_{\bar{y}}(x) - f_y(x))$$

With weighted version:

$$\sum_x \sum_y \sum_{\bar{y} \neq y} L(\text{rank}_y(x)) \max(0, 1 + f_{\bar{y}}(x) - f_y(x))$$

where  $\text{rank}_y(f(x))$  is the rank of the true label:

$$\text{rank}_y(f(x)) = \sum_{\bar{y} \neq y} I(f_{\bar{y}}(x) \geq f_y(x))$$

and  $L(\eta)$  converts the rank to a weight, e.g.  $L(\eta) = \sum_{i=1}^{\eta} 1/\eta$ .

## Weighted Approximate-Rank Pairwise (WARP) Loss

**Problem:** we would like to apply SGD:

$$\text{Weighting } L(\text{rank}_y(f(x))), \quad \text{rank}_y(f(x)) = \sum_{\bar{y} \neq y} I(f_{\bar{y}}(x) + 1 \geq f_y(x))$$

... too expensive to compute per  $(x, y)$  sample as  $y \in \mathcal{Y}$  is large.

**Solution:** approximate by sampling  $f_i(x)$  until we find a violating label  $\bar{y}$

$$\text{rank}_y(f(x)) \approx \left\lfloor \frac{|\mathcal{Y}| - 1}{N} \right\rfloor$$

where  $N$  is the number of trials in the sampling step.

# Online WARP Loss

**Input:** labeled data  $(x_i, y_i)$ ,  $y_i \in \{1, \dots, Y\}$ .

**repeat**

Pick a random labeled example  $(x_i, y_i)$

Set  $N = 0$ .

**repeat**

Pick a random annotation  $\bar{y} \in \{1, \dots, Y\} \setminus y_i$ .

$N = N + 1$ .

**until**  $f_{\bar{y}}(x) > f_{y_i}(x) - 1$  or  $N > Y - 1$

**if**  $f_{\bar{y}}(x) > f_{y_i}(x) - 1$  **then**

Make a **gradient step** to minimize:

$$L(\lfloor \frac{Y-1}{N} \rfloor) |1 - f_y(x) + f_{\bar{y}}(x)|_+$$

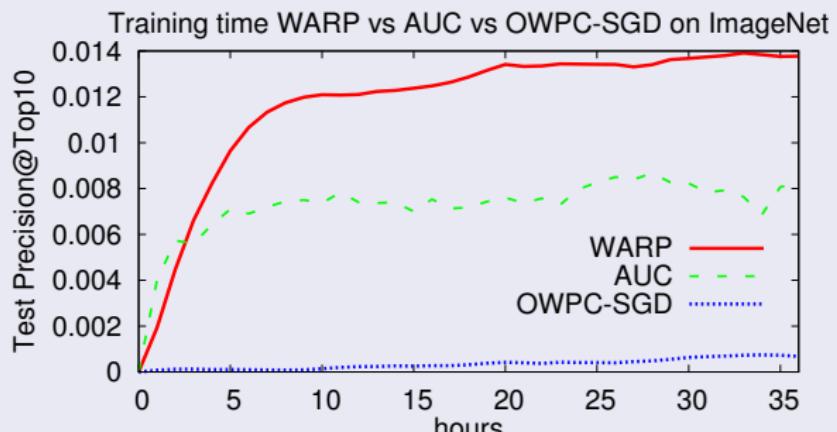
**end if**

**until** validation error does not improve.

## Image Annotation Performance

Algorithm	16k ImageNet	22k ImageNet	97k Web Data
Nearest Means	4.4%	2.7%	2.3%
One-vs-all SVMs 1+:1-	4.1%	3.5%	1.6%
One-vs-all SVMs	9.4%	8.2%	6.8%
AUC SVM Ranker	4.7%	5.1%	3.1%
Wsabie	11.9%	10.5%	8.3%

## Training time: WARP vs. OWPC-SGD & AUC



## Learned Annotation Embedding (on Web Data)

Annotation	Neighboring Annotations
barack obama david beckham santa	<i>barak obama, obama, barack, barrack obama, bow wow beckham, david beckam, alessandro del piero, del piero santa claus, papa noel, pere noel, santa clause, joyeux noel</i>
dolphin cows	delphin, dauphin, <i>whale, delfin, delfini, baleine, blue whale cattle, shire, dairy cows, kuh, horse, cow, shire horse, kone</i>
rose pine tree	rosen, <i>hibiscus, rose flower, rosa, roze, pink rose, red rose abies alba, abies, araucaria, pine, neem tree, oak tree</i>
mount fuji eiffel tower	mt fuji, fuji, fujisan, fujiyama, <i>mountain, zugspitze eiffel, tour eiffel, la tour eiffel, big ben, paris, blue mosque</i>
ipod f18	i pod, <i>ipod nano, apple ipod, ipod apple, new ipod f 18, eurofighter, f14, fighter jet, tomcat, mig 21, f 16</i>

# Summary

## Conclusion



Powerful: supervised methods for ranking.

- Outperform classical methods



Efficient low-rank models → learn hidden representations.



Embeddings good for generalization, but can “blur” too much e.g. for exact word matches.

## Extensions

- Nonlinear extensions – e.g. convolutional net instead.  
e.g. DeViSE (Frome et al., NIPS '13)

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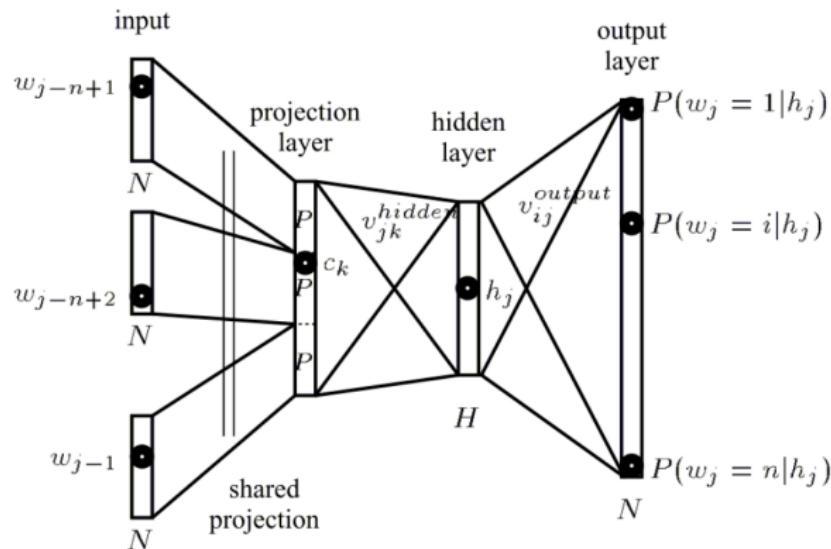
# Language Modeling

Task: given a sequence of words, predict the next word.

the cat sat on the ??

- $n$ -gram models are a strong baseline on this task.
- A variety of embedding models have been tried, they can improve results.
- The embeddings learnt from this unsupervised task can also be used to transfer to and improve a supervised task.

# Neural Network Language Models



Bengio, Y., Schwenk, H., Sencal, J. S., Morin, F., & Gauvain, J. L. (2006). Neural probabilistic language models. In Innovations in Machine Learning (pp. 137-186). Springer Berlin Heidelberg.

# Neural Network Language Models: Hierarchical Soft Max Trick (Morin & Bengio '05)

Predicting the probability of each next word is slow in NNLMs because the output layer of the network is the size of the dictionary.

Can predict via a tree instead:

- ① Cluster the dictionary either according to semantics (similar words in the same cluster) or frequency (common words in the same cluster).  
*This gives a two-layer tree, but a binary tree is another possibility.*
- ② The internal nodes explicitly model the probability of its child nodes.
- ③ The cost of predicting the probability of the true word is now: traversal to the child, plus normalization via the internal nodes and children in the same node.

This idea is used in Word2Vec and RNN models as well.

# Recurrent Neural Network Language Models

**Key idea:** *input to predict next word is current word plus context fed-back from previous word (i.e. remembers the past with recurrent connection).*

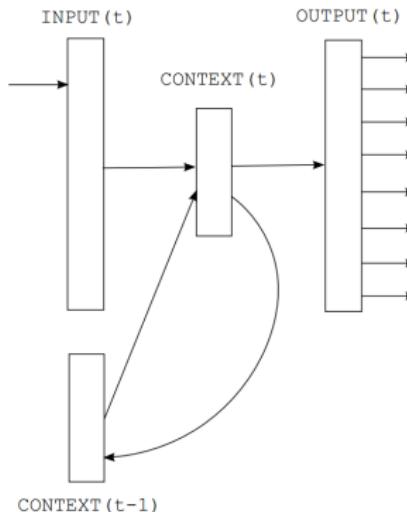


Figure: Recurrent neural network based LM

Recurrent neural network based language model. Mikolov et al., Interspeech, '10.

## NNLMS vs. RNNS: Penn Treebank Results (Mikolov)

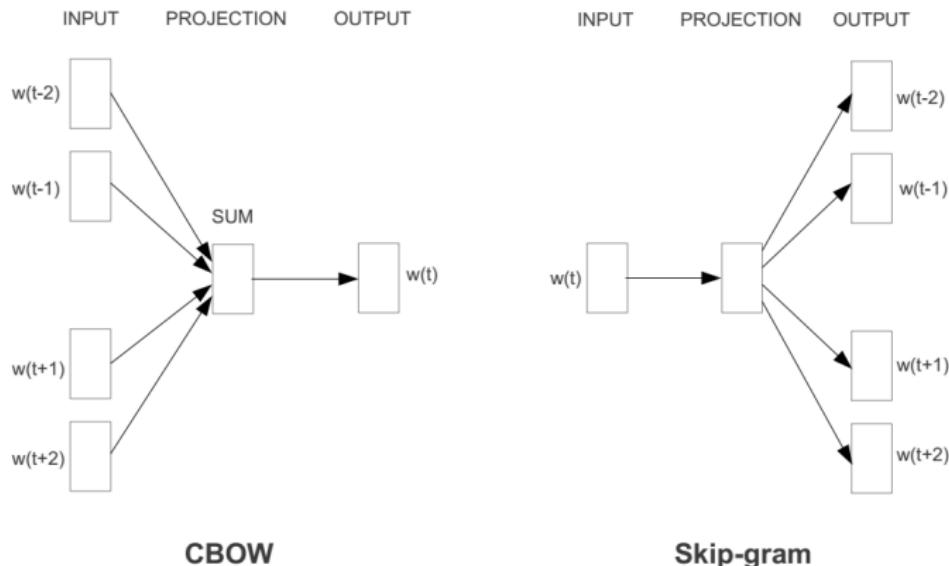
Model	Weight	PPL
3-gram with Good-Turing smoothing (GT3)	0	165.2
5-gram with Kneser-Ney smoothing (KN5)	0	141.2
5-gram with Kneser-Ney smoothing + cache	0.0792	125.7
Maximum entropy model	0	142.1
Random clusterings LM	0	170.1
Random forest LM	0.1057	131.9
Structured LM	0.0196	146.1
Within and across sentence boundary LM	0.0838	116.6
Log-bilinear LM	0	144.5
Feedforward NNLM	0	140.2
Syntactical NNLM	0.0828	131.3
Combination of static RNNLMs	0.3231	102.1
Combination of adaptive RNNLMs	0.3058	101.0
ALL	1	<b>83.5</b>

*Recent uses of NNLMs and RNNs to improve machine translation:*

Fast and Robust NN Joint Models for Machine Translation, Devlin et al, ACL '14.

Also (Kalchbrenner '13), (Sutskever et al., '14), (Cho et al., '14).

# Word2Vec : very simple LM, works well



Tomas Mikolov, Ilya Sutskever, Kai Chen, Greg Corrado, and Jeffrey Dean.  
Distributed Representations of Words and Phrases and their Compositionality.  
NIPS, 2013.

## Word2Vec: compositionality

Table 7: Comparison and combination of models on the Microsoft Sentence Completion Challenge.

Architecture	Accuracy [%]
4-gram [32]	39
Average LSA similarity [32]	49
Log-bilinear model [24]	54.8
RNNLMs [19]	55.4
Skip-gram	48.0
Skip-gram + RNNLMs	<b>58.9</b>

Czech + currency	Vietnam + capital	German + airlines	Russian + river	French + actress
koruna	Hanoi	airline Lufthansa	Moscow	Juliette Binoche
Check crown	Ho Chi Minh City	carrier Lufthansa	Volga River	Vanessa Paradis
Polish zolty	Viet Nam	flag carrier Lufthansa	upriver	Charlotte Gainsbourg
CTK	Vietnamese	Lufthansa	Russia	Cecile De

Table 5: Vector compositionality using element-wise addition. Four closest tokens to the sum of two vectors are shown, using the best Skip-gram model.

Code: <https://code.google.com/p/word2vec/>

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# NLP Tasks

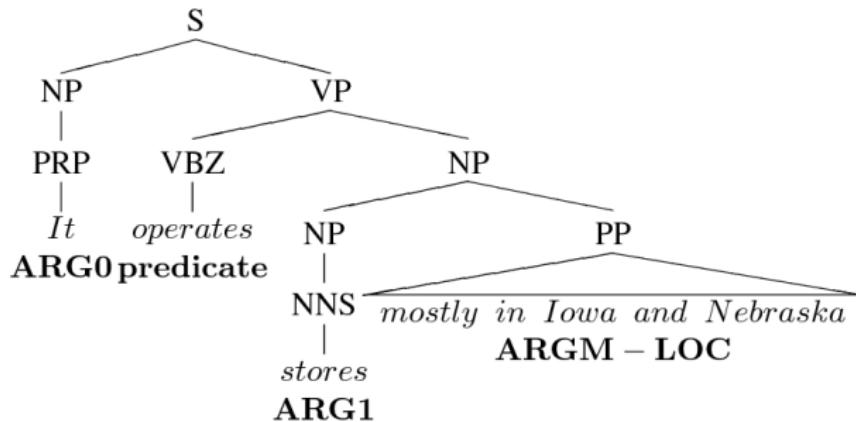
- Part-Of-Speech Tagging (POS): syntactic roles (noun, adverb...)
- Chunking: syntactic constituents (noun phrase, verb phrase...)
- Name Entity Recognition (NER): person/company/location...
- Semantic Role Labeling (SRL):

[John]**ARG0** [ate]**REL** [the apple]**ARG1** [in the garden]**ARGM-LOC**

## Complex Systems

- Two extreme choices to get a **complex system**
  - ★ **Large Scale Engineering:** design a lot of **complex features**, use a fast existing linear machine learning algorithm
  - ★ **Large Scale Machine Learning:** use simple features, design a **complex model** which will **implicitly learn** the right features

# The Large Scale Feature Engineering Way



- Extract **hand-made features** e.g. from the parse tree
- Disjoint: all tasks trained separately, Cascade features
- Feed these features to a shallow classifier like SVM

# ASSERT: many hand built features for SRL (Pradhan et al, '04)

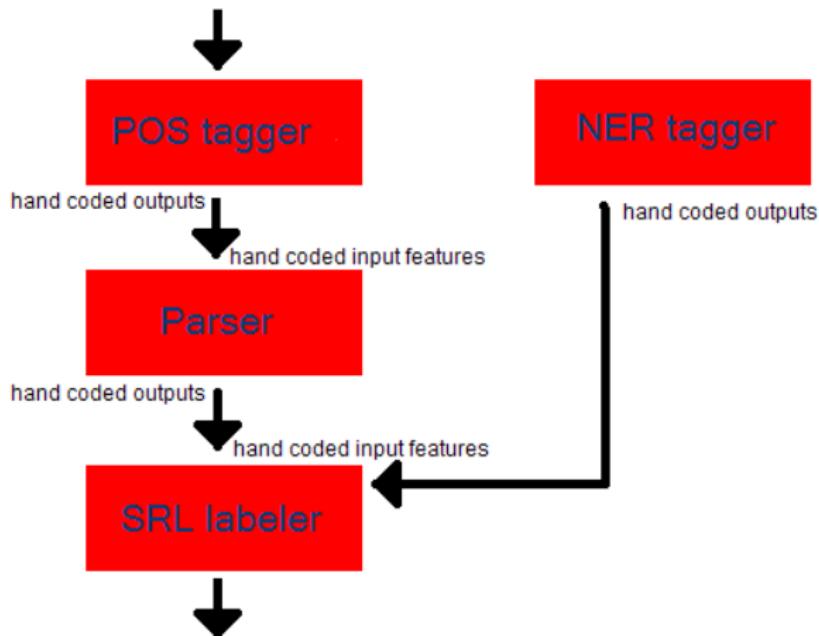
Problems:

- 1) Features rely on other solutions (parsing, named entity, word-sense)
  - 2) Technology task-transfer is difficult
- Choose some **good hand-crafted features**

Predicate and POS tag of predicate Phrase type: adverbial phrase, prepositional phrase, ... Head word and POS tag of the head word Path: traversal from predicate to constituent Word-sense disambiguation of the verb Length of the target constituent (number of words) Partial Path: lowest common ancestor in path First and last words and POS in constituents Constituent tree distance Dynamic class context: previous node labels Constituent relative features: head word Constituent relative features: siblings	Voice: active or passive (hand-built rules) Governing category: Parent node's phrase type(s) Position: left or right of verb Predicted named entity class Verb clustering NEG feature: whether the verb chunk has a "not" Head word replacement in prepositional phrases Ordinal position from predicate + constituent type Temporal cue words (hand-built rules) Constituent relative features: phrase type Constituent relative features: head word POS Number of pirates existing in the world...
---	---

- Feed them to a **shallow classifier** like SVM

# The Suboptimal (?) Cascade



*(Or, the opposing view is the above is a smart use of prior knowledge..)*

# NLP: Large Scale Machine Learning

## Goals

- Task-specific engineering limits NLP scope
- Can we find unified hidden representations?
- Can we build unified NLP architecture?

## Means

- Start from scratch: forget (most of) NLP knowledge
- Compare against classical NLP benchmarks
- Our dogma: avoid task-specific engineering

## NLP Benchmarks

- Datasets:

- ★ POS, CHUNK, SRL: [WSJ](#) ( $\approx$  up to 1M labeled words)
- ★ NER: [Reuters](#) ( $\approx$  200K labeled words)

System	Accuracy
Shen, 2007	97.33%
<b>Toutanova, 2003</b>	<b>97.24%</b>
Gimenez, 2004	97.16%

(a) **POS**: As in (Toutanova, 2003)

System	F1
<b>Ando, 2005</b>	<b>89.31%</b>
Florian, 2003	88.76%
Kudoh, 2001	88.31%

(c) **NER**: CoNLL 2003

System	F1
Shen, 2005	95.23%
<b>Sha, 2003</b>	<b>94.29%</b>
Kudoh, 2001	93.91%

(b) **CHUNK**: CoNLL 2000

System	F1
<b>Koomen, 2005</b>	<b>77.92%</b>
Pradhan, 2005	77.30%
Haghghi, 2005	77.04%

(d) **SRL**: CoNLL 2005

- We chose as [benchmark systems](#):

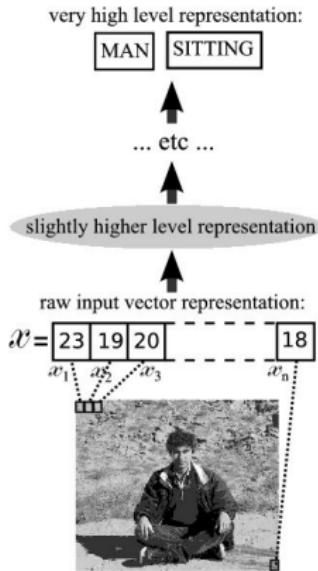
- ★ [Well-established](#) systems
- ★ Systems avoiding [external labeled](#) data

- Notes:

- ★ [Ando, 2005](#) uses external [unlabeled](#) data
- ★ [Koomen, 2005](#) uses 4 parse trees not provided by the challenge

# The “Deep Learning” Way

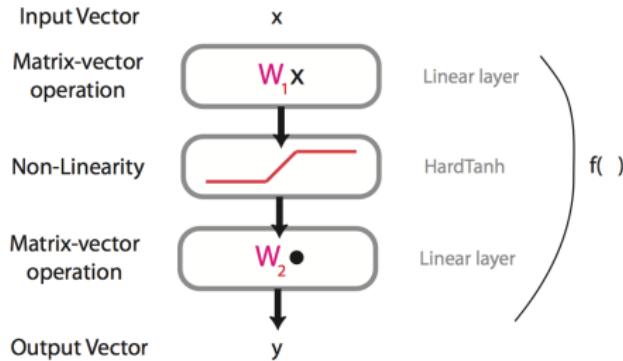
Neural nets attempt to propose a radically? different **end-to-end** approach:



- Avoid building a **parse tree**. Humans don't need this to talk.
- Try to avoid all **hand-built features** → **monolithic systems**.

# Neural Networks

- Stack several layers together



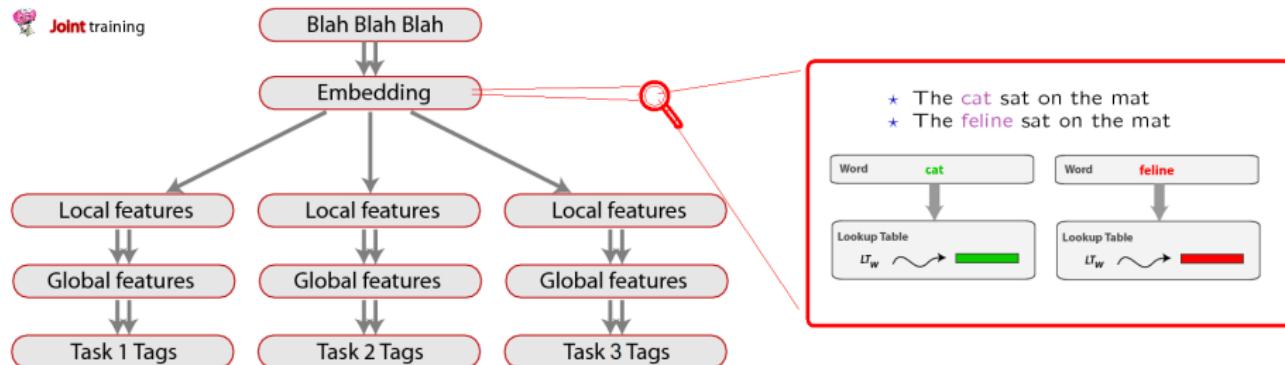
- Increasing level of abstraction at each layer
- Requires simpler features than “shallow” classifiers
- The “weights”  $W_i$  are trained by gradient descent
- How can we feed words?

# The Big Picture

A unified architecture for all NLP (labeling) tasks:

Sentence:	<i>Felix</i>	<i>sat</i>	<i>on</i>	<i>the</i>	<i>mat</i>	.
POS:	NNP	VBD	IN	DT	NN	.
CHUNK:	NP	VP	PP	NP	NP-I	.
NER:	PER	-	-	-	-	-
SRL:	ARG1	REL	ARG2	ARG2-I	ARG2-I	-

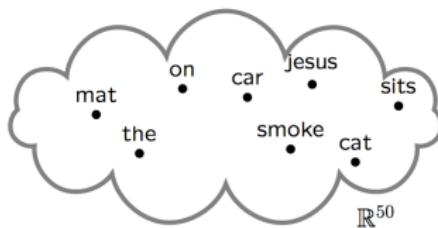
Joint training



## Words into Vectors

### Idea

- Words are **embed** in a **vector** space



- Embeddings are **trained**

### Implementation

- A word  $w$  is an **index** in a dictionary  $\mathcal{D} \in \mathbb{N}$
- Use a **lookup-table** ( $W \sim \text{feature size} \times \text{dictionary size}$ )

$$LT_W(w) = W_{\bullet w}$$

### Remarks

- Applicable to any **discrete feature** (words, caps, stems...)
- See (Bengio et al, 2001)

## The Lookup Tables

Each word/element in dictionary maps to a vector in  $\mathbb{R}^d$ .

- We learn these vectors.
- LookupTable: input of  $i^{th}$  word is

$$x = (0, 0, \dots, 1, 0, \dots, 0) \quad 1 \text{ at position } i$$

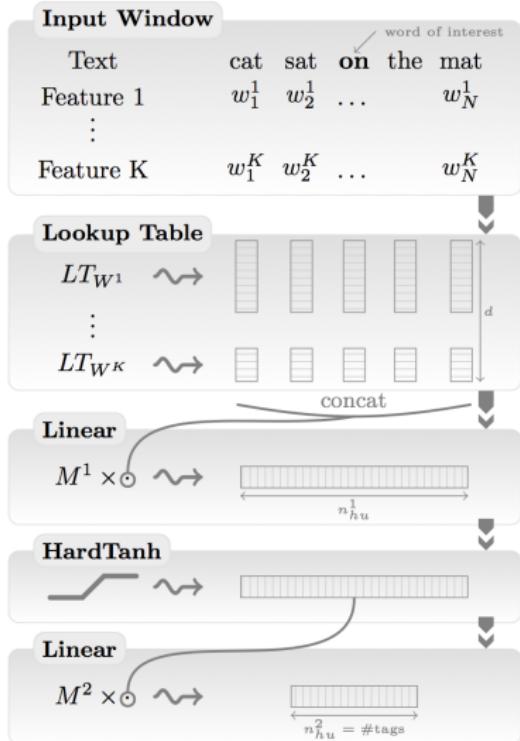
*In the original space words are orthogonal.*

$$\text{cat} = (0, 0, 0, 0, 0, 0, 0, 0, 1, 0, 0, 0, 0, \dots)$$

$$\text{kitten} = (0, 0, 1, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, \dots)$$

To get the  $\mathbb{R}^d$  embedding vector for the word we multiply  $Wx$  where  $W$  is a  $d \times N$  vector with  $N$  words in the dictionary.

## Window Approach



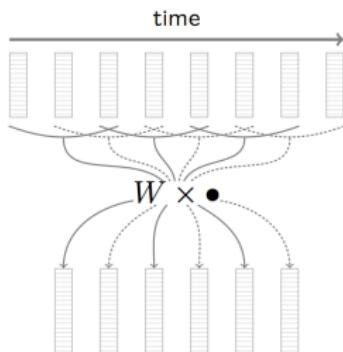
- Tags **one word** at the time
- Feed a **fixed-size window** of text around **each word** to tag
- Works fine for most tasks
- How do deal with **long-range dependencies?**

E.g. in **SRL**, the **verb** of interest might be **outside** the **window!**

## Sentence Approach

(1/2)

- Feed the **whole sentence** to the network
- Tag one word at the time: add extra **position** features
- **Convolutions** to handle variable-length inputs



See (Bottou, 1989)  
or (LeCun, 1989).

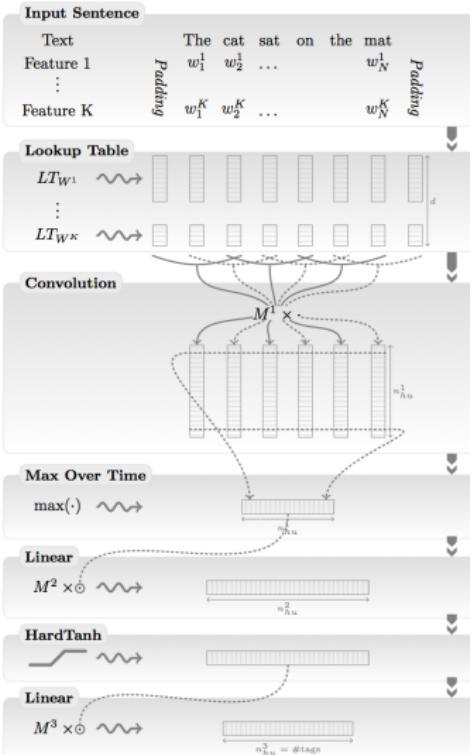
- Produces **local** features with higher level of abstraction
- **Max over time** to capture most relevant features



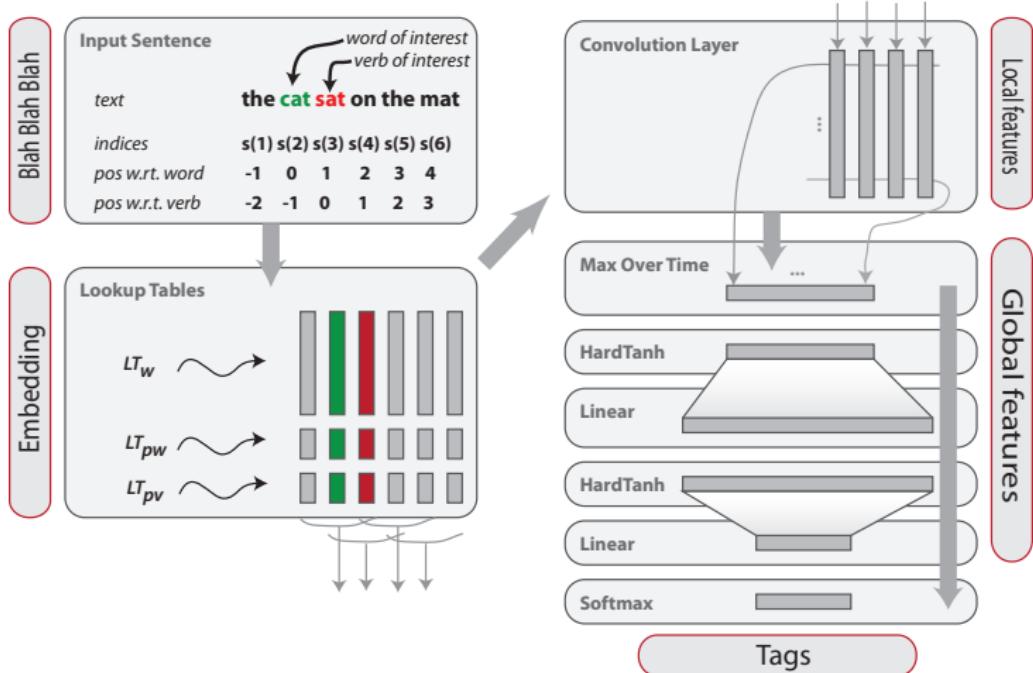
Outputs a **fixed-sized** feature vector

# Sentence Approach

(2/2)

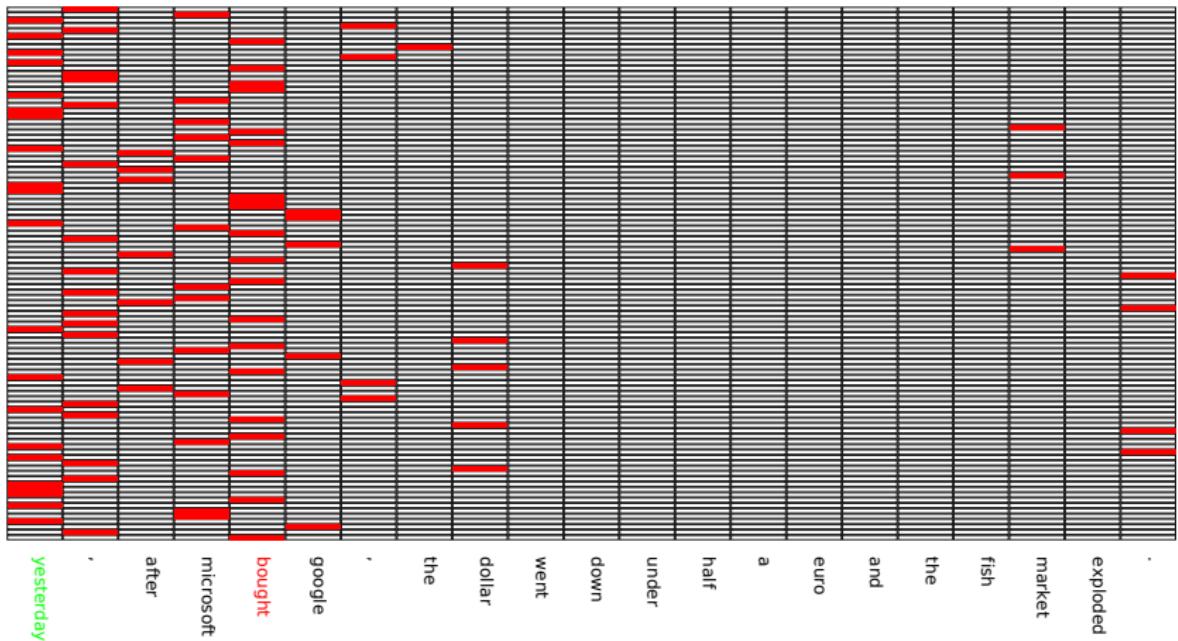


# Deep SRL

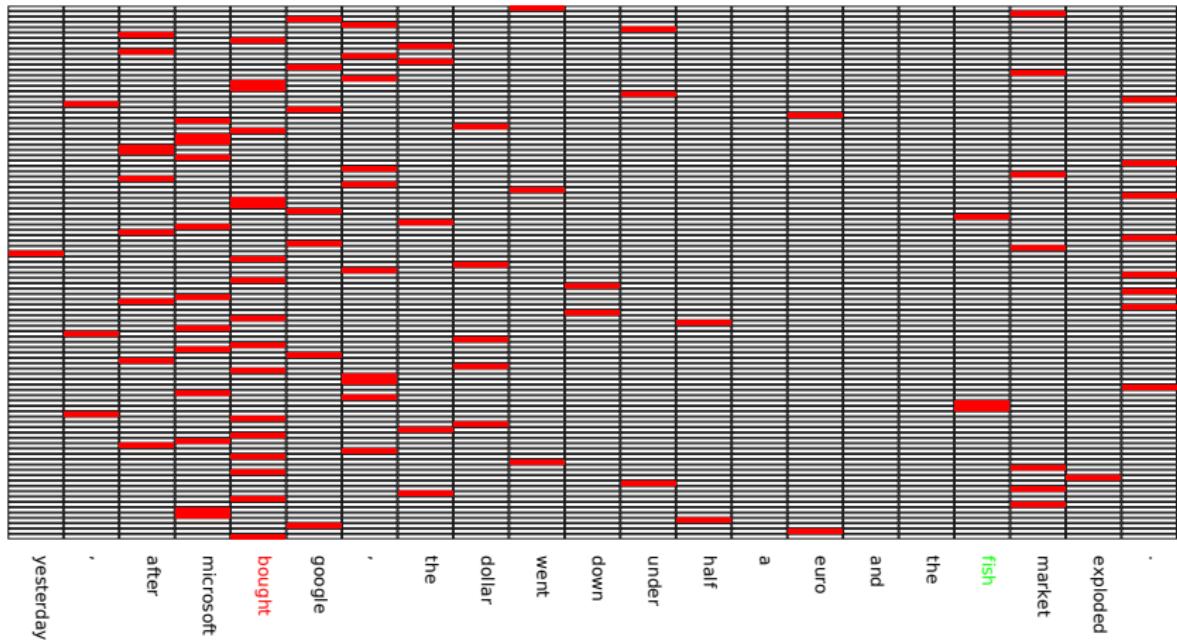


This is the network for a single window. We train/test predicting the entire sentence of tags ("structured outputs") using viterbi approach, similar to other NLP methods.

# Removing The Time Dimension (1/2)



## Removing The Time Dimension (2/2)



## Word Tag Likelihood (WTL)

- The network has one output  $f(\mathbf{x}, i, \theta)$  per tag  $i$
- Interpreted as a probability with a softmax over all tags

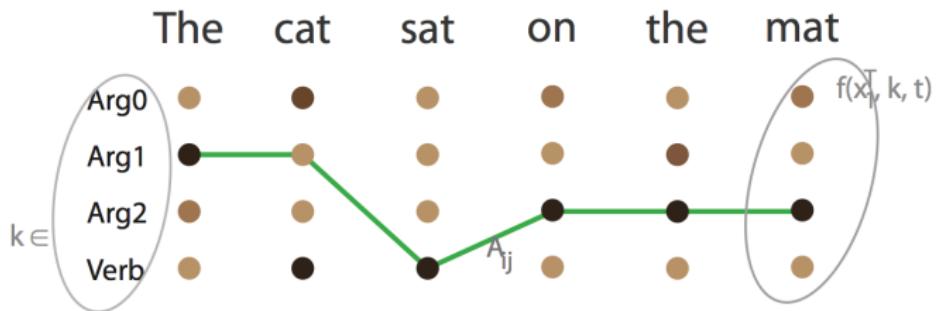
$$p(i | \mathbf{x}, \theta) = \frac{e^{f(\mathbf{x}, i, \theta)}}{\sum_j e^{f(\mathbf{x}, j, \theta)}}$$

.. we can train directly for that (word tag likelihood) or we could train in a structured way by predicting the entire sentence's tags.

That should be useful because tags are not independent.

## Sentence Tag Likelihood (STL)

- The network score for tag  $k$  at the  $t^{\text{th}}$  word is  $f([\mathbf{x}]_1^T, k, t, \boldsymbol{\theta})$
- $A_{kl}$  transition score to jump from tag  $k$  to tag  $l$



- Sentence score for a tag path  $[i]_1^T$

$$s([\mathbf{x}]_1^T, [i]_1^T, \tilde{\boldsymbol{\theta}}) = \sum_{t=1}^T \left( A_{[i]_{t-1}[i]_t} + f([\mathbf{x}]_1^T, [i]_t, t, \boldsymbol{\theta}) \right)$$

## Supervised Benchmark Results

- Network architectures:
  - ★ Window (5) approach for POS, CHUNK & NER (300HU)
  - ★ Convolutional (3) for SRL (300+500HU)
  - ★ Word Tag Likelihood (WTL) and Sentence Tag Likelihood (STL)
- Network features: lower case words (size 50), capital letters (size 5)  
dictionary size 100,000 words

Approach	POS (PWA)	Chunking (F1)	NER (F1)	SRL (F1)
<b>Benchmark Systems</b>	<b>97.24</b>	<b>94.29</b>	<b>89.31</b>	<b>77.92</b>
NN+WTL	96.31	89.13	79.53	55.40
NN+STL	96.37	90.33	81.47	70.99

- STL helps, but... fair performance.
- Capacity mainly in words features... are we training it right?

## Supervised Word Embeddings

- Sentences with **similar words** should be **tagged in the same way**:
  - The **cat** sat on the mat
  - The **feline** sat on the mat

france	jesus	xbox	reddish	scratched	megabits
454	1973	6909	11724	29869	87025
persuade	thickets	decadent	widescreen	odd	ppa
faw	savary	divo	antica	anchietsa	uddin
blackstock	sympathetic	verus	shabby	emigration	biologically
giorgi	jfk	oxide	awe	marking	kayak
shaheed	khwarazm	urbina	thud	heuer	mclarens
rumelia	stationery	epos	occupant	sambhaji	gladwin
planum	ilias	eglington	revised	worshippers	centrally
goa'uld	gsNUMBER	edging	leavened	ritsuko	indonesia
collation	operator	frg	pandionidae	lifeless	moneo
bacha	w.j.	namsos	shirt	mahan	nilgiris

- About **1M** of words in WSJ
- 15% of most frequent words** in the dictionary are seen **90% of the time**
- Cannot expect words to be trained properly!**

# Improving Word Embedding

- Rare words are not trained properly
- Sentences with similar words should be tagged in the same way:
  - The cat sat on the mat
  - The feline sat on the mat



Only 1M WSJ not enough – let's use lots of unsupervised data!

## Semi-supervised: MTL with Unlabeled Text

- Language Model: “*is a sentence actually english or not?*”  
Implicitly captures: \* syntax \* semantics
- Bengio & Ducharme (2001) Probability of next word given previous words. Overcomplicated – we do not need probabilities here
- English sentence windows: Wikipedia ( $\sim 631M$  words)  
Non-english sentence windows: middle word randomly replaced
  - the champion federer wins wimbledon
  - vs. the champion saucepan wins wimbledon
- Multi-class margin cost:

$$\sum_{s \in \mathcal{S}} \sum_{w \in \mathcal{D}} \max(0, 1 - f(s, w_s^*) + f(s, w))$$

$\mathcal{S}$ : sentence windows  $\mathcal{D}$ : dictionary

$w_s^*$ : true middle word in  $s$

$f(s, w)$ : network score for sentence  $s$  and middle word  $w$

# Language Model: Embedding

Nearest neighbors in 100-dim. embedding space:

FRANCE 454	JESUS 1973	XBOX 6909	REDDISH 11724	SCRATCHED 29869
SPAIN	CHRIST	PLAYSTATION	YELLOWISH	SMASHED
ITALY	GOD	DREAMCAST	GREENISH	RIPPED
RUSSIA	RESURRECTION	PSNUMBER	BROWNISH	BRUSHED
POLAND	PRAYER	SNES	BLUISH	HURLED
ENGLAND	YAHWEH	WII	CREAMY	GRABBED
DENMARK	JOSEPHUS	NES	WHITISH	TOSSED
GERMANY	MOSES	NINTENDO	BLACKISH	SQUEEZED
PORTUGAL	SIN	GAMECUBE	SILVERY	BLASTED
SWEDEN	HEAVEN	PSP	GREYISH	TANGLED
AUSTRIA	SALVATION	AMIGA	PALER	SLASHED

(Even fairly rare words are embedded well.)

## Results

Algorithm	POS (PWA)	CHUNK (F1)	NER (F1)	SRL (F1)
Baselines	97.24 [Toutanova '03]	94.29 [Sha '03]	89.31 [Ando '05]	77.92 [Koomen '05]
NN + WTL	96.31	89.13	79.53	55.40
NN + STL	96.37	90.33	81.47	70.99
NN + LM + STL	97.22	94.10	88.67	74.15
NN + ... + tricks	97.29 [+suffix]	94.32 [+POS]	89.95 [+gazetteer]	76.03 [+Parse Trees]

### NOTES:

- Didn't compare to benchmarks that used external labeled data.
- [Ando '05] uses external unlabeled data.
- [Koomen '05] uses 4 parse trees not provided by the challenge. Using only 1 tree it gets 74.76.

# Software

Code for tagging with POS, NER, CHUNK, SRL + parse trees:

<http://ml.nec-labs.com/senna/>

System	RAM (Mb)	Time (s)
Toutanova, 2003	1100	1065
Shen, 2007	2200	833
SENNNA	32	4

(a) POS

System	RAM (Mb)	Time (s)
Koomen, 2005	3400	6253
SENNNA	124	52

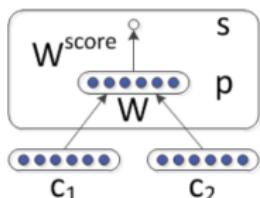
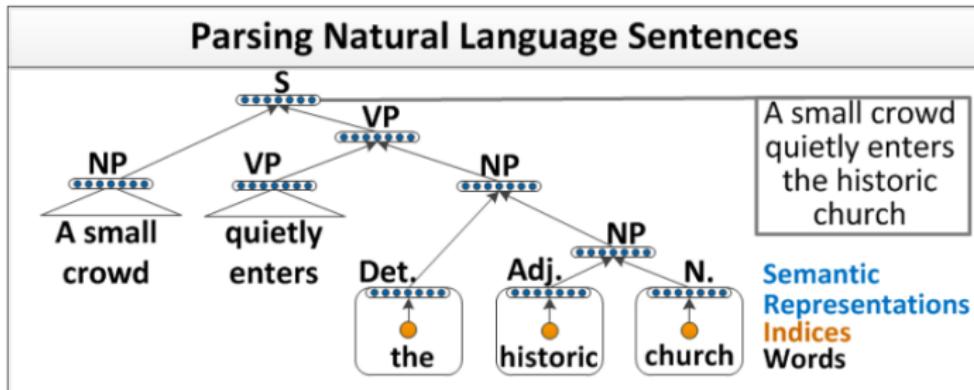
(b) SRL

See also Torch: <http://www.torch.ch>

# Recursive NNs for Parsing, Sentiment, ... and more!

(Socher et al., ICML '13), (Socher et al., EMNLP, '13))

Build sentence representations using the parse tree to compose embeddings via a nonlinear function taking pairs ( $c_1, c_2$ ) and output  $p$ .

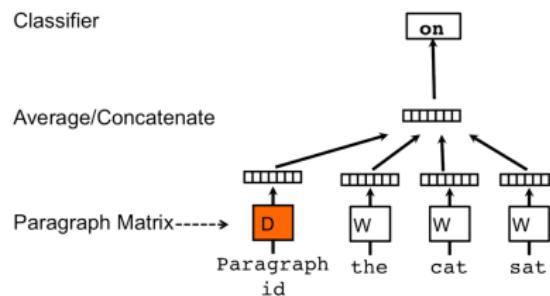
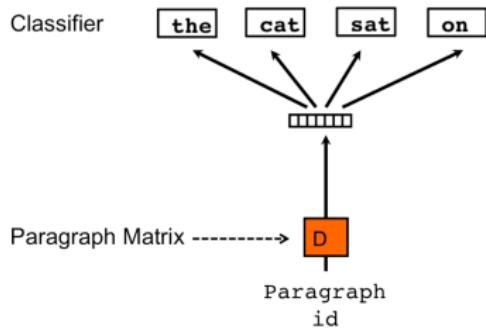


# Paragraph Vector

(Le & Mikolov, '14)

A Paragraph Vector (*a vector that represents a paragraph/doc*) learned by:

- 1) Predicting the words in a doc;
- 2) predict  $n$ -grams in the doc:



At test time, for a new document, one needs to learn its vector, this can encode word order via the  $n$ -gram prediction approach.

# Comparison of CNN, RNN & PV (Kim '14)

Model	MR	SST-1	SST-2	Subj	TREC	CR	MPQA
CNN-rand	76.1	45.0	82.7	89.6	91.2	79.8	83.4
CNN-static	81.0	45.5	86.8	93.0	92.8	84.7	<b>89.6</b>
CNN-non-static	<b>81.5</b>	48.0	87.2	93.4	93.6	84.3	89.5
CNN-multichannel	81.1	47.4	<b>88.1</b>	93.2	92.2	<b>85.0</b>	89.4
RAE (Socher et al., 2011)	77.7	43.2	82.4	—	—	—	86.4
MV-RNN (Socher et al., 2012)	79.0	44.4	82.9	—	—	—	—
RNTN (Socher et al., 2013)	—	45.7	85.4	—	—	—	—
DCNN (Kalchbrenner et al., 2014)	—	48.5	86.8	—	93.0	—	—
Paragraph-Vec (Le and Mikolov, 2014)	—	<b>48.7</b>	87.8	—	—	—	—
CCAE (Hermann and Blunsom, 2013)	77.8	—	—	—	—	—	87.2
Sent-Parser (Dong et al., 2014)	79.5	—	—	—	—	—	86.3
NBSVM (Wang and Manning, 2012)	79.4	—	—	93.2	—	81.8	86.3
MNB (Wang and Manning, 2012)	79.0	—	—	<b>93.6</b>	—	80.0	86.3
G-Dropout (Wang and Manning, 2013)	79.0	—	—	93.4	—	82.1	86.1
F-Dropout (Wang and Manning, 2013)	79.1	—	—	<b>93.6</b>	—	81.9	86.3
Tree-CRF (Nakagawa et al., 2010)	77.3	—	—	—	—	81.4	86.1
CRF-PR (Yang and Cardie, 2014)	—	—	—	—	—	82.7	—
SVM <sub>S</sub> (Silva et al., 2011)	—	—	—	—	<b>95.0</b>	—	—

Table 2: Results of our CNN models against other methods. **RAE**: Recursive Autoencoders with pre-trained word vectors from Wikipedia (Socher et al., 2011). **MV-RNN**: Matrix-Vector Recursive Neural Network with parse trees (Socher et al., 2012). **RNTN**: Recursive Neural Tensor Network with tensor-based feature function and parse trees (Socher et al., 2013). **DCNN**: Dynamic Convolutional Neural Network with k-max pooling (Kalchbrenner et al., 2014). **Paragraph-Vec**: Logistic regression on top of paragraph vectors (Le and Mikolov, 2014). **CCAE**: Combinatorial Category Autoencoders with combinatorial category grammar operators (Hermann and Blunsom, 2013). **Sent-Parser**: Sentiment analysis-specific parser (Dong et al., 2014). **NBSVM, MNB**: Naive Bayes SVM and Multinomial Naive Bayes with uni-bigrams from Wang and Manning (2012). **G-Dropout, F-Dropout**: Gaussian Dropout and Fast Dropout from Wang and Manning (2013). **Tree-CRF**: Dependency tree

## Some More Recent Work

- Compositionality approaches by Marco Baroni's group:  
**Words are combined with linear matrices dependent on the P.O.S.:**  
G. Dinu and M. Baroni. How to make words with vectors: Phrase generation in distributional semantics. ACL '14.
- Document representation by Phil Blunsom's group:  
**Variants of convolutional networks for text:**  
Kalchbrenner et al. A Convolutional Neural Network for Modelling Sentences. ACL '14

Good tutorial slides from these teams covering multiple topics:

New Directions in Vector Space Models of Meaning

<http://www.cs.ox.ac.uk/files/6605/aclVectorTutorial.pdf>

# Summary

- Generic end-to-end deep learning system for NLP tasks.
- Word embeddings combined to form sentence or document embeddings can perform well on supervised tasks.
- Previous common belief in NLP: engineering syntactic features necessary for semantic tasks.  
*One can do well by engineering a model/algorithm rather than features.*

Attitude is changing in recent years... let's see what happens!

# Embedding Methods for NLP

## Part 2: Embeddings for Multi-relational Data

Antoine Bordes & Jason Weston

Facebook AI Research

EMNLP tutorial – October 29, 2014

# Menu – Part 2

## 1 Embeddings for multi-relational data

- Multi-relational data
- Link Prediction in KBs
- Embeddings for information extraction
- Question Answering

## 2 Pros and cons of embedding models

## 3 Future of embedding models

## 4 Resources

# Menu – Part 2

## 1 Embeddings for multi-relational data

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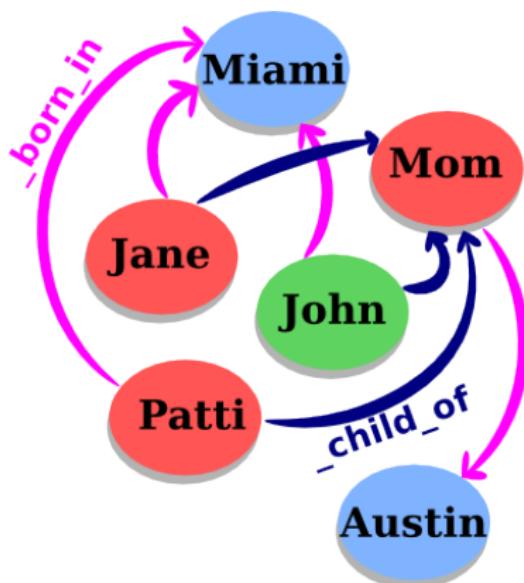
## 2 Pros and cons of embedding models

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# Multi-relational data

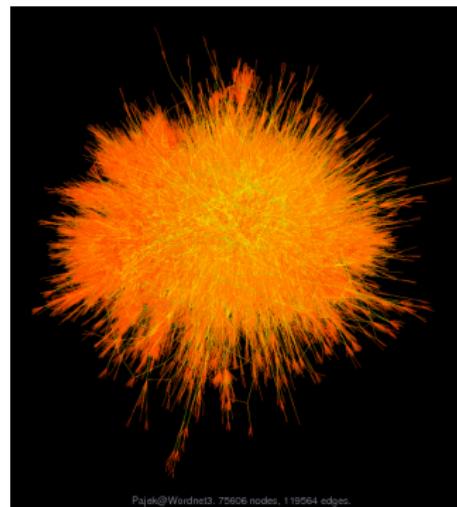
- Data is structured as a graph
- Each node = an entity
- Each edge = a relation/fact
- A relation = (*sub*, *rel*, *obj*):
  - *sub* = subject,
  - *rel* = relation type,
  - *obj* = object.
- Nodes w/o features.



In this talk, we focus on Knowledge Bases (KBs).

# Example of KB: WordNet

- WordNet: dictionary where each entity is a sense (synset).
- Popular in NLP.
- Statistics:
  - 117k entities;
  - 20 relation types;
  - 500k facts.
- Examples:
  - (car\_NN\_1, \_has\_part, \_wheel\_NN\_1)
  - (score\_NN\_1, \_is\_a, \_rating\_NN\_1)
  - (score\_NN\_2, \_is\_a, \_sheet\_music\_NN\_1)



# Example of KB: Freebase

- **Freebase:** huge collaborative (hence noisy) KB.
- Part of the Google Knowledge Graph.
- Statistics:
  - 80M of entities;
  - 20k relation types;
  - 1.2B facts.
- Examples:
  - (Barack Obama, \_place\_of\_birth, Hawaii)
  - (Albert Einstein, \_follows\_diet, Veganism)
  - (San Francisco, \_contains, Telegraph Hill)



# Modeling Knowledge Bases

- **Why KBs?**

- **KBs:** Semantic search, connect people and things
- **KBs ← Text:** Information extraction
- **KBs → Text:** Text interpretation, summary, Q&A

- **Main issue: KBs are hard to manipulate**

- **Large dimensions:**  $10^5/10^8$  entities,  $10^4/10^6$  rel. types
- **Sparse:** few valid links
- **Noisy/incomplete:** missing/wrong relations/entities

- **How?**

- ① **Encode KBs into low-dimensional vector spaces**
- ② **Use these representations:**
  - to complete/visualize KBs
  - as KB data in text applications

# Menu – Part 2

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## 2 Pros and cons of embedding models

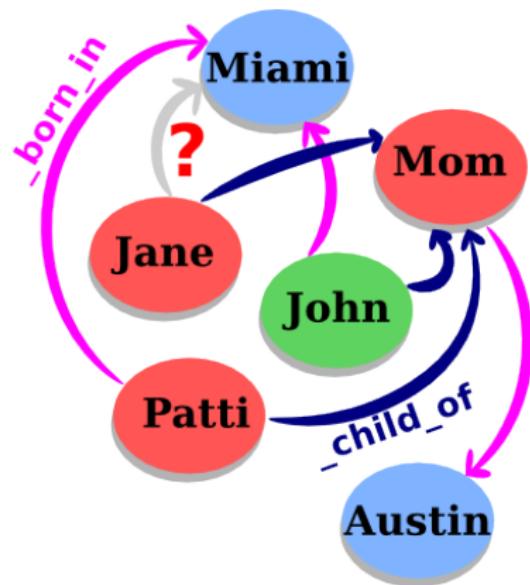
## 3 Future of embedding models

## 4 Resources

# Link Prediction

Add new facts [without requiring extra knowledge](#)

From known information, assess the validity of an unknown fact

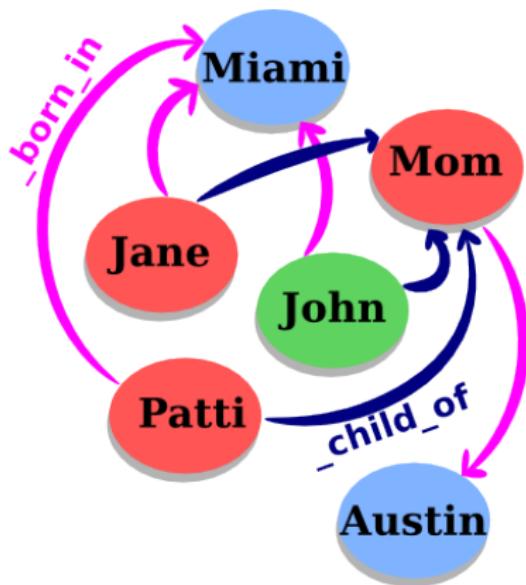


# Link Prediction

Add new facts [without requiring extra knowledge](#)

From known information, assess the validity of an unknown fact

- *collective classification*
- *reasoning in embedding spaces*



# Statistical Relational Learning

- **Framework:**

- $n_s$  subjects  $\{sub_i\}_{i \in [1; n_s]}$
  - $n_r$  relation types  $\{rel_k\}_{k \in [1; n_r]}$
  - $n_o$  objects  $\{obj_j\}_{j \in [1; n_o]}$
- For us,  $n_s = n_o = n_e$  and  $\forall i \in [1; n_e], sub_i = obj_i$ .

- A fact exists for  $(sub_i, rel_k, obj_j)$  if  $rel_k(sub_i, obj_j) = 1$

- **Goal:** We want to model, from data,

$$\mathbb{P}[rel_k(sub_i, obj_j) = 1]$$

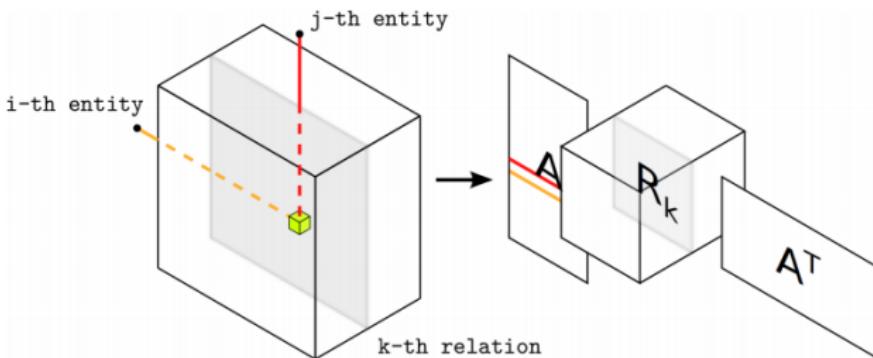
(eq. to approximate the binary tensor  $\mathbf{X} \in \{0, 1\}^{n_s \times n_o \times n_r}$ )

# Previous Work

- Tensor factorization (Harshman et al., '94)
- Probabilistic Relational Learning (Friedman et al., '99)
- Relational Markov Networks (Taskar et al., '02)
- Markov-logic Networks (Kok et al., '07)
- Extension of SBMs (Kemp et al., '06) (Sutskever et al., '10)
- Spectral clustering (undirected graphs) (Dong et al., '12)
- Ranking of random walks (Lao et al., '11)
- Collective matrix factorization (Nickel et al., '11)
- **Embedding models** (Bordes et al., '11, '13) (Jenatton et al., '12)  
(Socher et al., '13) (Wang et al., '14) (García-Durán et al., '14)

# Collective Matrix Factorization (Nickel et al., '11)

- **RESCAL**:  $\forall k \in [1; n_r], \mathbf{R}_k \in \mathbb{R}^{d \times d}$  and  $\mathbf{A} \in \mathbb{R}^{n_e \times d}$   
 (close from DEDICOM (Harshman, '78)).



- **A & R** learned by reconstruction (alternating least-squares):

$$\min_{\mathbf{A}, \mathbf{R}} \frac{1}{2} \left( \sum_k \|\mathbf{X}_k - \mathbf{A}\mathbf{R}_k\mathbf{A}^\top\|_F^2 \right) + \lambda_A \|\mathbf{A}\|_F^2 + \lambda_R \sum_k \|\mathbf{R}_k\|_F^2$$

# Scalability

Method	Nb of parameters	on Freebase15k
RESCAL	$O(n_e d + n_r d^2)$	88M ( $d = 250$ )

Freebase15k:  $n_e = 15k$ ,  $n_r = 1.3k$ .

- RESCAL involves many parameters.
- Bad scalability w.r.t.  $n_r$ .
- Reconstruction criterion does not fit well for binary data..

# Embedding Models

Two main ideas:

- ① Models based on low-dimensional continuous vector embeddings for entities and relation types, directly trained to define a similarity criterion.
- ② Stochastic training based on ranking loss with sub-sampling of unknown relations.

# Embedding Models for KBs

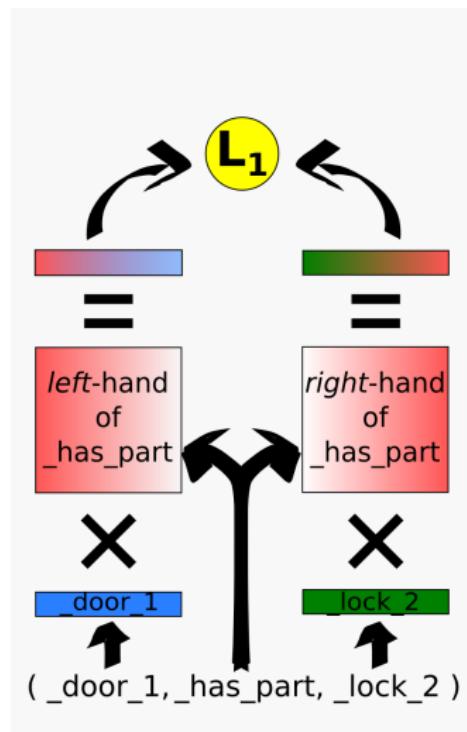
- Subjects and objects are represented by vectors in  $\mathbb{R}^d$ .
  - $\{\text{sub}_i\}_{i \in [1; n_s]} \rightarrow [\mathbf{s}^1, \dots, \mathbf{s}^{n_s}] \in \mathbb{R}^{d \times n_s}$
  - $\{\text{obj}_j\}_{j \in [1; n_o]} \rightarrow [\mathbf{o}^1, \dots, \mathbf{o}^{n_o}] \in \mathbb{R}^{d \times n_o}$
- For us,  $n_s = n_o = n_e$  and  $\forall i \in [1; n_e], \mathbf{s}_i = \mathbf{o}_i$ .
- Rel. types = similarity operators between subj/obj.
  - $\{\text{rel}_k\}_{k \in [1; n_r]} \rightarrow \text{operators } \{\mathbf{R}_k\}_{k \in [1; n_r]}$
- Learning similarities depending on  $\text{rel} \rightarrow d(\text{sub}, \text{rel}, \text{obj})$ , parameterized by  $\mathbf{s}$ ,  $\mathbf{R}$  and  $\mathbf{o}$ .

# Structured Embeddings (Bordes et al., '11)

**Intuition:** *sub* and *obj* are projected using *rel* in a space where they are similar

$$d(\text{sub}, \text{rel}, \text{obj}) = -\|\mathbf{R}^{\text{left}} \mathbf{s}^\top - \mathbf{R}^{\text{right}} \mathbf{o}^\top\|_1$$

- Entities:  $\mathbf{s}$  and  $\mathbf{o} \in \mathbb{R}^d$
- Projection:  $\mathbf{R}^{\text{left}}$  and  $\mathbf{R}^{\text{right}} \in \mathbb{R}^{d \times d}$
- $\mathbf{R}^{\text{left}} \neq \mathbf{R}^{\text{right}}$  because of asymmetry
- Similarity: L1 distance



# Stochastic Training

- Learning by **stochastic gradient descent**: one training fact after the other
- For each relation from the training set:
  - ① **sub-sample unobserved facts** (false?)
  - ② check if the similarity of the true fact is lower
  - ③ **if not**, update parameters of the considered facts
- **Stopping criterion**: performance on a validation set

# Scalability

Method	Nb of parameters	on Freebase15k
RESCAL	$O(n_e d + n_r d^2)$	88M ( $d = 250$ )
SE	$O(n_e d + 2n_r d^2)$	8M ( $d = 50$ )

Freebase15k:  $n_e = 15k$ ,  $n_r = 1.3k$ .

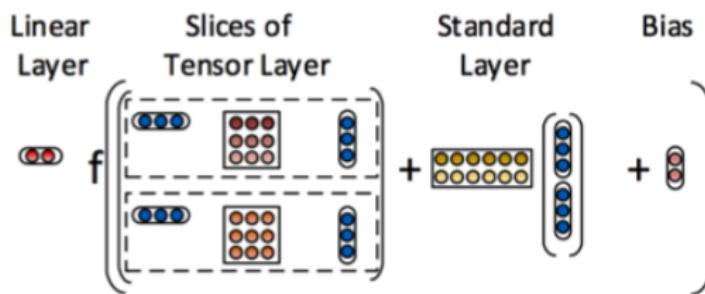
- SE also involves many parameters.
- Bad scalability w.r.t.  $n_r$ .
- Potential training problems for SE (overfitting).

# Neural Tensor Networks (Socher et al., '13)

- In NTN, a relationship is represented by a tensor, 2 matrices and 2 vectors + a non-linearity ( $\tanh$ ).

$$d(\text{sub}, \text{rel}, \text{obj}) = \mathbf{u}_r^\top \tanh (\mathbf{h}^\top \mathcal{W}_r \mathbf{t} + \mathbf{V}_r^1 \mathbf{h} + \mathbf{V}_r^2 \mathbf{t} + \mathbf{b}_r)$$

- Neural Tensor layer:



- Very powerful model with high capacity for each relation.

# Scalability

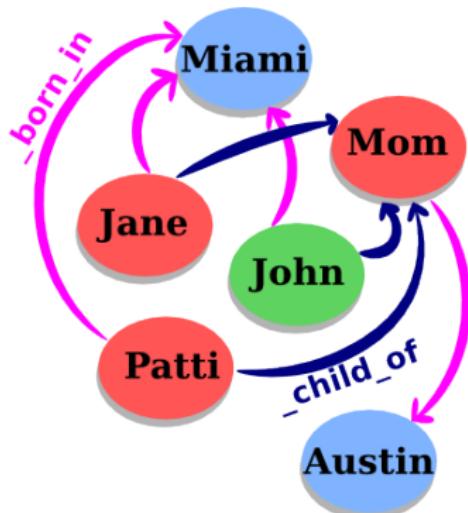
Method	Nb of parameters	on Freebase15k
RESCAL	$O(n_e d + n_r d^2)$	88M ( $d = 250$ )
SE	$O(n_e d + 2n_r d^2)$	8M ( $d = 50$ )
NTN	$O(n_e d + n_r d^3)$	165M ( $d = 50$ )

Freebase15k:  $n_e = 15k$ ,  $n_r = 1.3k$ .

- Very high modeling capacity.
- Involves many parameters.
- Bad scalability w.r.t.  $n_r$  (overfitting if few triples).

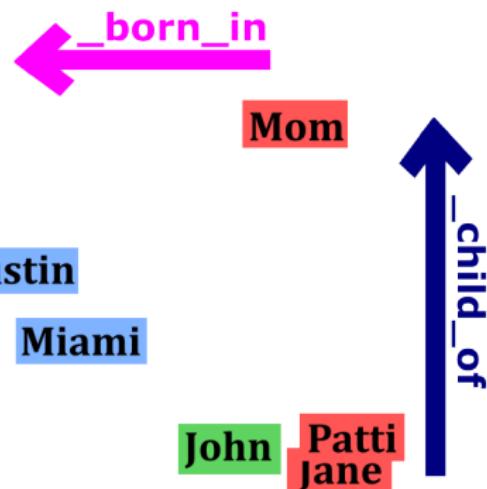
# Modeling Relations as Translations (Bordes et al. '13)

**Intuition:** we want  $s + r \approx o$ .



# Modeling Relations as Translations (NIPS13)

**Intuition:** we would like that  $s + r \approx o$ .



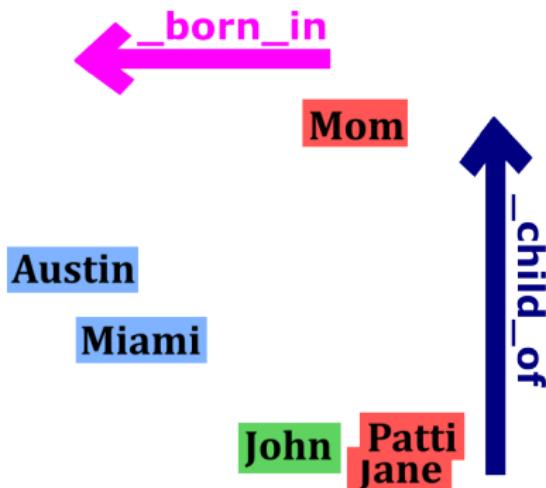
# Modeling Relations as Translations (Bordes et al. '13)

**Intuition:** we want  $\mathbf{s} + \mathbf{r} \approx \mathbf{o}$ .

The similarity measure is defined as:

$$d(\text{sub}, \text{rel}, \text{obj}) = \|\mathbf{s} + \mathbf{r} - \mathbf{o}\|_2^2$$

$\mathbf{s}, \mathbf{r}$  and  $\mathbf{o}$  are learned to verify that.



# Learning TransE

For training, a margin ranking criterion is minimized:

$$\sum_{pos} \sum_{neg \in S'} [\gamma + \|\mathbf{s} + \mathbf{r} - \mathbf{o}\|_2^2 - \|\mathbf{s}' + \mathbf{r} - \mathbf{o}'\|_2^2]_+$$

where  $[x]_+$  is the positive part of  $x$ ,  $\gamma > 0$  is a margin, and:

$$S' = \{(\text{sub}', \text{rel}, \text{obj}) | \text{sub}' \in \mathcal{E}\} \cup \{(\text{sub}, \text{rel}, \text{obj}') | \text{obj}' \in \mathcal{E}\}$$

# Learning TransE

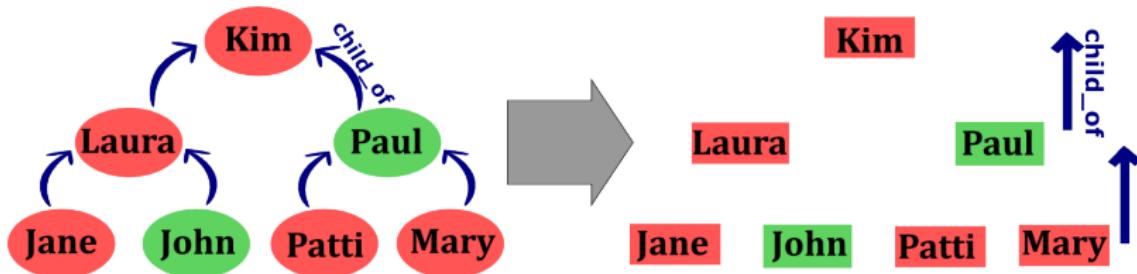
```

1: input: Training set  $S = \{(sub, rel, obj)\}$ , margin  $\gamma$ , learning rate  $\lambda$ 
2: initialize  $\mathbf{r} \leftarrow \text{uniform}\left(-\frac{6}{\sqrt{k}}, \frac{6}{\sqrt{k}}\right)$  for each rel
3:  $\mathbf{r} \leftarrow \ell / \|\ell\|$  for each  $\ell$ 
4:  $\mathbf{e} \leftarrow \text{uniform}\left(-\frac{6}{\sqrt{j}}, \frac{6}{\sqrt{k}}\right)$  for each entity ent(sub or obj)
5: loop
6:  $\mathbf{e} \leftarrow \mathbf{e} / \|\mathbf{e}\|$  for each entity ent
7:  $S_{batch} \leftarrow \text{sample}(S, b)$  //sample minibatch of size  $b$ 
8:  $T_{batch} \leftarrow \emptyset$  //initialize set of pairs
9: for  $(sub, rel, obj) \in S_{batch}$  do
10:    $(sub', rel, obj') \leftarrow \text{sample}(S'(\text{sub}, \text{rel}, \text{obj}))$  //sample negative triplet
11:    $T_{batch} \leftarrow T_{batch} \cup \{(sub, rel, obj), (sub', rel, obj')\}$ 
12: end for
13: Update embeddings w.r.t.  $\sum_{T_{batch}} \nabla [\gamma + \|\mathbf{s} + \mathbf{r} - \mathbf{o}\|_2^2 - \|\mathbf{s}' + \mathbf{r} - \mathbf{o}'\|_2^2]_+$ 
14: end loop

```

# Motivations of a Translation-based Model

- Natural representation for hierarchical relationships.



- Recent work on word embeddings (Mikolov et al., '13): there may exist embedding spaces in which relationships among concepts are represented by translations.

# Scalability

Method	Nb of parameters	on Freebase15k
RESCAL	$O(n_e d + n_r d^2)$	88M ( $d = 250$ )
SE	$O(n_e d + 2n_r d^2)$	8M ( $d = 50$ )
NTN	$O(n_e d + n_r d^3)$	165M ( $d = 50$ )
TransE	$O(n_e d + n_r d)$	0.8M ( $d = 50$ )

Freebase15k:  $n_e = 15k$ ,  $n_r = 1.3k$ .

- TransE is a special case of SE and NTN.
- TransE obtains better training errors: **less overfitting**.
- Much better **scalability**.

# Chunks of Freebase

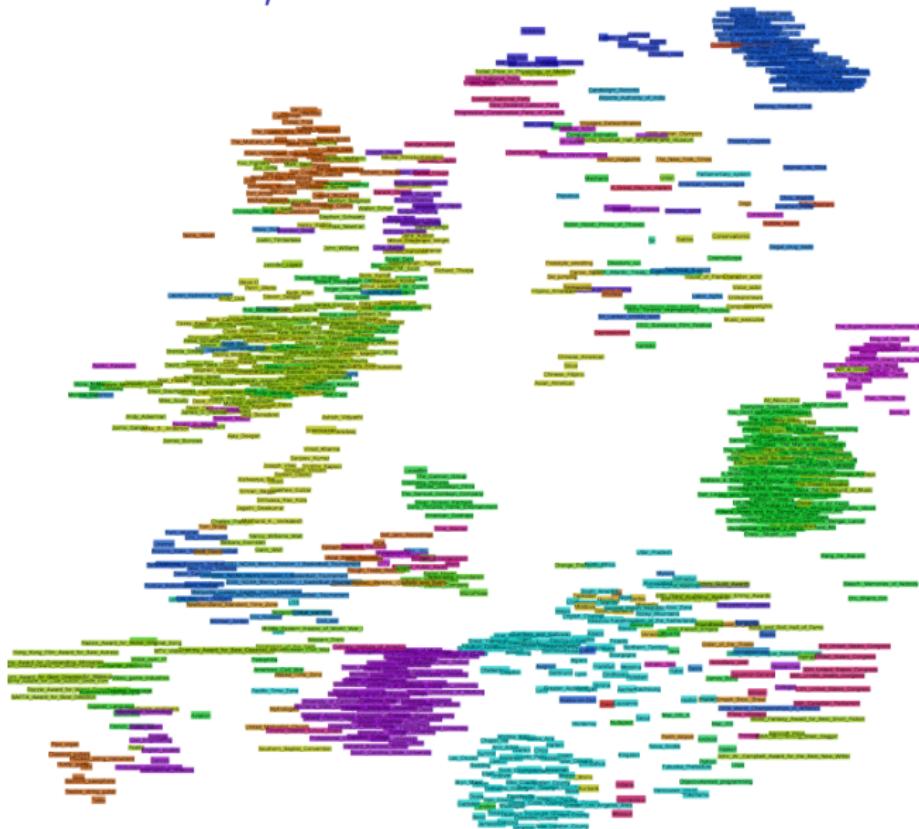
- **Data statistics:**

	Entities ( $n_e$ )	Rel. ( $n_r$ )	Train. Ex.	Valid. Ex.	Test Ex.
FB13	75,043	13	316,232	5,908	23,733
FB15k	14,951	1,345	483,142	50,000	59,071
FB1M	$1 \times 10^6$	23,382	$17.5 \times 10^6$	50,000	177,404

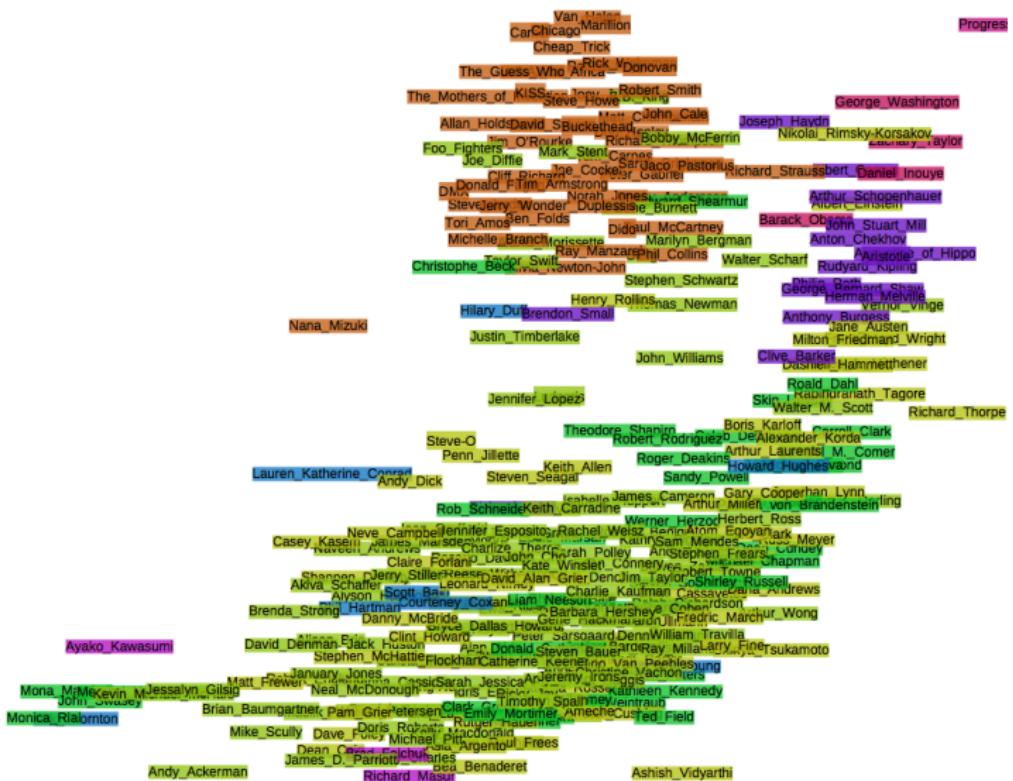
- **Training times for TransE:**

- Embedding dimension: 50.
- Training time:
  - on Freebase15k:  $\approx 2\text{h}$  (on 1 core),
  - on Freebase1M:  $\approx 1\text{d}$  (on 16 cores).

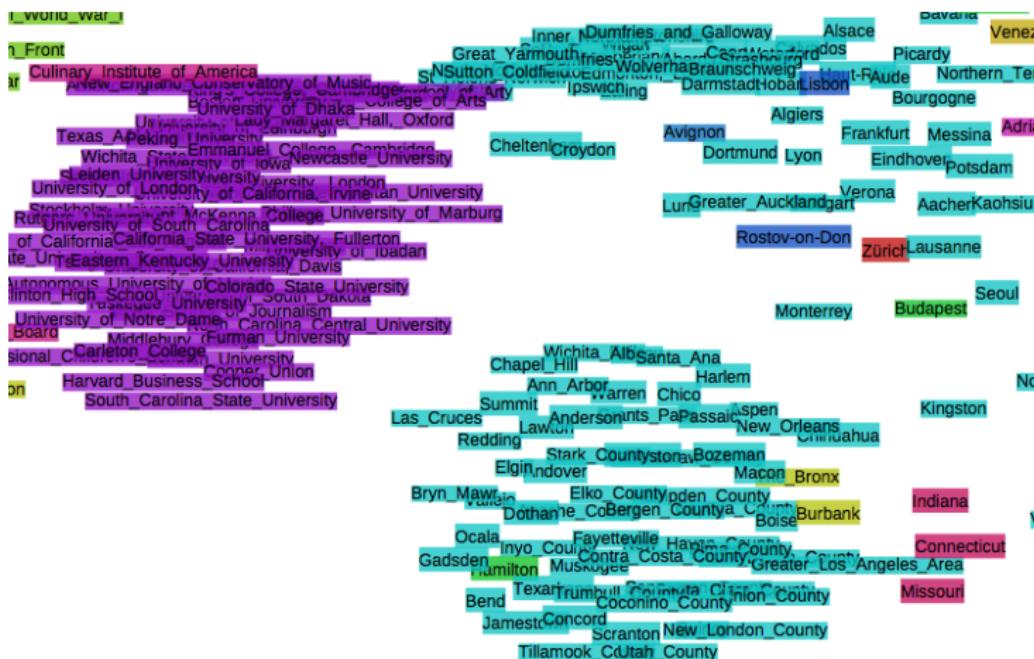
# Visualization of 1,000 Entities



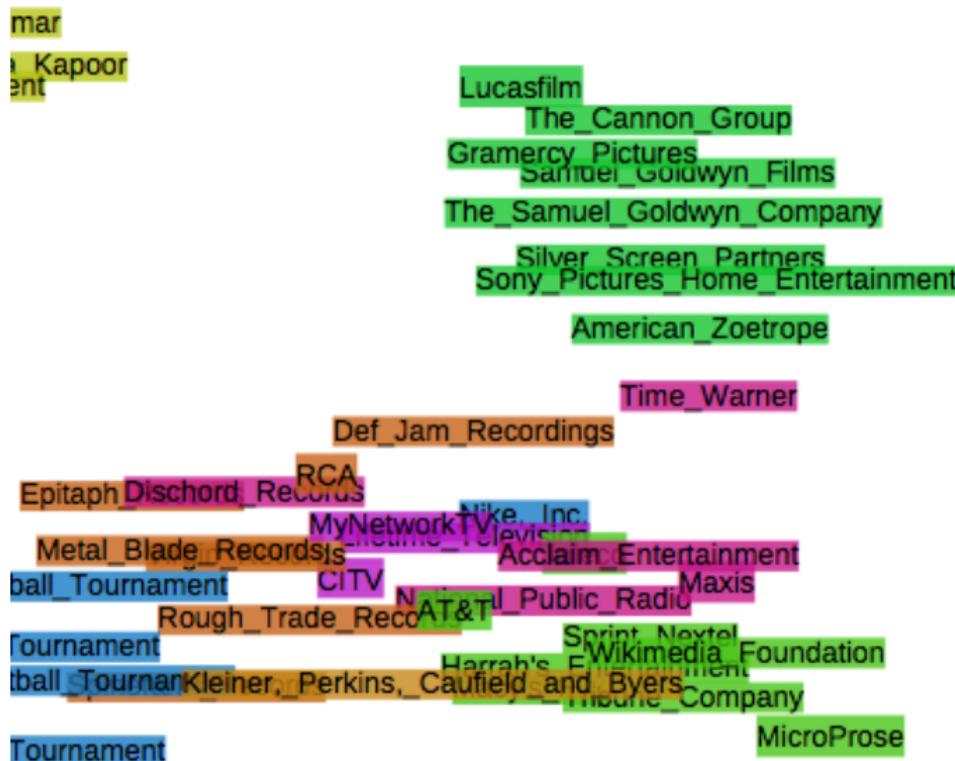
# Visualization of 1,000 Entities - Zoom 1



# Visualization of 1,000 Entities - Zoom 2



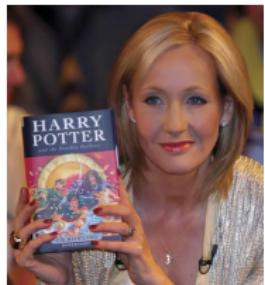
# Visualization of 1,000 Entities - Zoom 3



# Example

"Who influenced J.K. Rowling?"

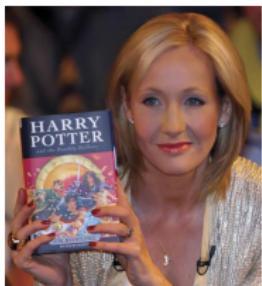
J. K. Rowling \_influenced\_by ?



# Example

"Who influenced J.K. Rowling?"

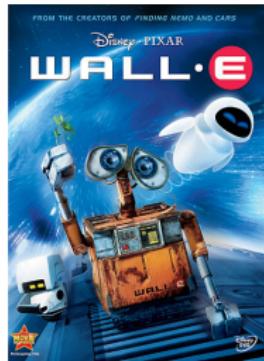
J. K. Rowling    `_influenced_by`    G. K. Chesterton  
J. R. R. Tolkien  
C. S. Lewis  
Lloyd Alexander  
Terry Pratchett  
Roald Dahl  
Jorge Luis Borges  
Stephen King  
Ian Fleming



# Example

"Which genre is the movie WALL-E?"

WALL-E      has\_genre ?



# Example

"Which genre is the movie WALL-E?"

WALL-E

\_has\_genre

Animation

Computer animation

Comedy film

Adventure film

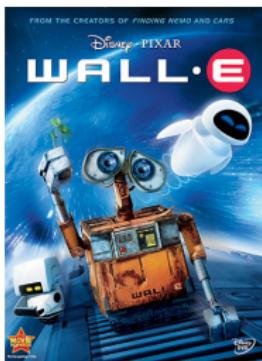
Science Fiction

Fantasy

Stop motion

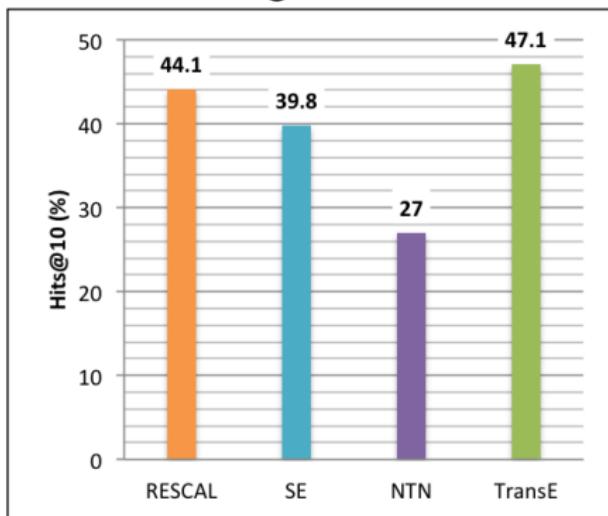
Satire

Drama

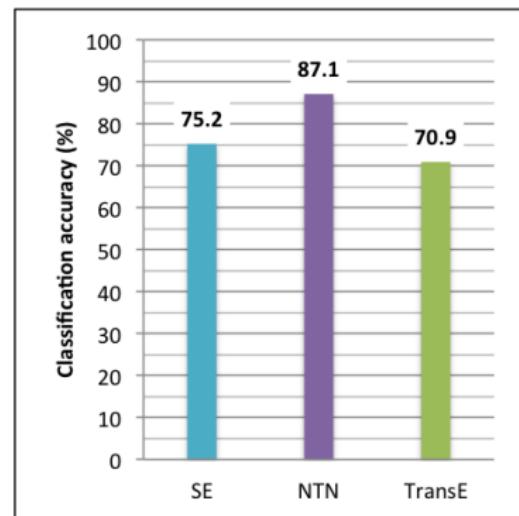


# Benchmarking

Ranking on FB15k



Classification on FB13



On FB1M, TransE predicts 34% in the Top-10 (SE only 17.5%).  
Results extracted from (Bordes et al., '13) and (Wang et al., '14)

# Refining TransE

- **TATEC** (García-Durán et al., '14) supplements TransE with a **trigram term** for encoding complex relationships:

$$d(\text{sub}, \text{rel}, \text{obj}) = \underbrace{\mathbf{s}_1^\top \mathbf{R} \mathbf{o}_1}_{\text{trigram}} + \underbrace{\mathbf{s}_2^\top \mathbf{r} + \mathbf{o}_2^\top \mathbf{r}' + \mathbf{s}_2^\top \mathbf{D} \mathbf{o}_2}_{\text{bigrams} \approx \text{TransE}},$$

with  $\mathbf{s}_1 \neq \mathbf{s}_2$  and  $\mathbf{o}_1 \neq \mathbf{o}_2$ .

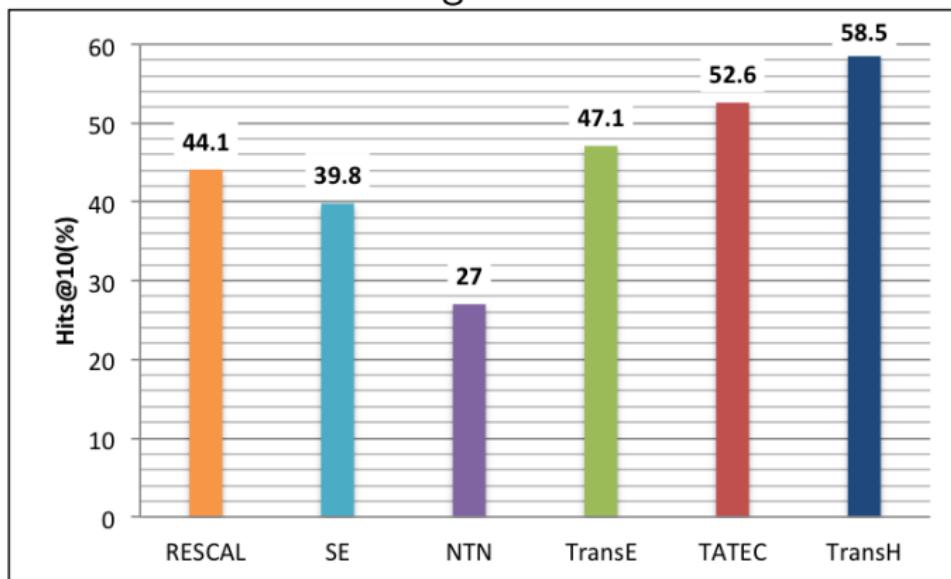
- **TransH** (Wang et al., '14) adds an **orthogonal projection** to the translation of TransE:

$$d(\text{sub}, \text{rel}, \text{obj}) = \|(\mathbf{s} - \mathbf{r}_p^\top \mathbf{s} \mathbf{r}_p) + \mathbf{r}_t - (\mathbf{o} - \mathbf{r}_p^\top \mathbf{o} \mathbf{r}_p)\|_2^2,$$

with  $\mathbf{r}_p \perp \mathbf{r}_t$ .

# Benchmarking

Ranking on FB15k



Results extracted from (García-Durán et al., '14) and (Wang et al., '14)

# Menu – Part 2

## 1 Embeddings for multi-relational data

- Multi-relational data
- Link Prediction in KBs
- Embeddings for information extraction
- Question Answering

## 2 Pros and cons of embedding models

## 3 Future of embedding models

## 4 Resources

# Information Extraction

- Information extraction: populate KBs with new facts using text
- Usually **two steps**:
  - **Entity linking**: identify mentions of entities in text
  - **Relation extraction**: extract facts about them
- Previous works include rule-based models, classifiers with features from parsers, graphical models, etc.
- Embedding models exist for both steps.

# Entity Linking as WSD

Word Sense Disambiguation  $\leftrightarrow$  WordNet entity linking

Towards open-text semantic parsing:

``A musical score accompanies a television program .''

 **Semantic Role Labeling**

(``A musical score'', ``accompanies'', ``a television program'')

 **Preprocessing (POS, Chunking, ...)**

((musical\_JJ score\_NN ), accompany\_VB , television\_program\_NN )

 **Word-sense Disambiguation**

((musical\_JJ\_1 score\_NN\_2), accompany\_VB\_1, television\_program\_NN\_1)

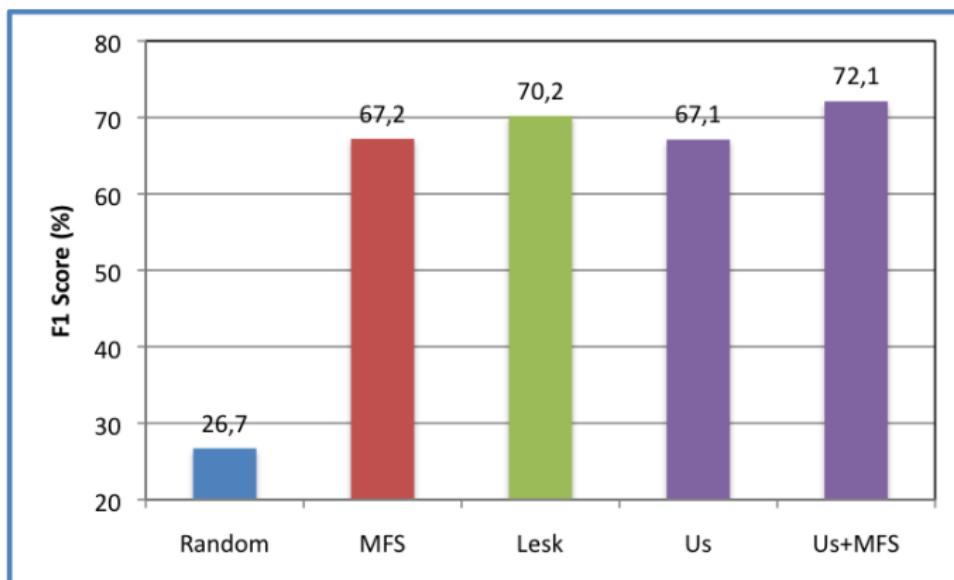
# Embeddings of Text and WordNet (Bordes et al., '12)

- Text is converted into relations (*sub,rel,obj*).
- Joint learning of embeddings for all symbols: words, entities and relation types from WordNet.
- This system can label 37,141 words with 40,943 synsets.

	Train. Ex.	Test Ex.	Labeled?	Symbol
WordNet	146,442	5,000	No	synsets
Wikipedia	2,146,131	10,000	No	words
ConceptNet	11,332	0	Non	words
Ext. WordNet	42,957	5,000	Yes	words+synsets
Unamb. Wikip.	981,841	0	Yes	words+synsets
<b>TOTAL</b>	<b>3,328,703</b>	<b>20,000</b>	-	-

# Benchmarking on Extended WordNet

F1-score on 5,000 test sentences to disambiguate.



Results extracted from (Bordes et al., '12)

# WordNet is enriched through text

Similarities among senses [beyond WordNet](#)

"what does an army attack?"

army\_NN\_1    attack\_VB\_1    ?

# WordNet is enriched through text

Similarities among senses **beyond** original WordNet data

"what does an army attack?"

army\_NN\_1   attack\_VB\_1   troop\_NN\_4  
armed\_service\_NN\_1  
ship\_NN\_1  
territory\_NN\_1  
military\_unit\_NN\_1

# WordNet is enriched through text

Similarities among senses **beyond WordNet**

"Who or what earns money"

? earn\_VB\_1 money\_NN\_1

# WordNet is enriched through text

Similarities among senses **beyond** original WordNet data

"Who or what earns money"

person\_NN\_1      earn\_VB\_1    money\_NN\_1

business\_firm\_NN\_1

family\_NN\_1

payoff\_NN\_3

card\_game\_NN\_1

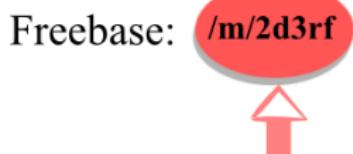
# Relation Extraction

Given a bunch of sentences.

Text: **"Alfred Hitchcock , who wrote and directed, The Birds"**  
**"M. Hitchcock , on the set of the movie The Birds"**  
**"Sir A. Hitchcock , the famous director of The Birds"**

# Relation Extraction

Given a bunch of sentences concerning the same pair of entities.



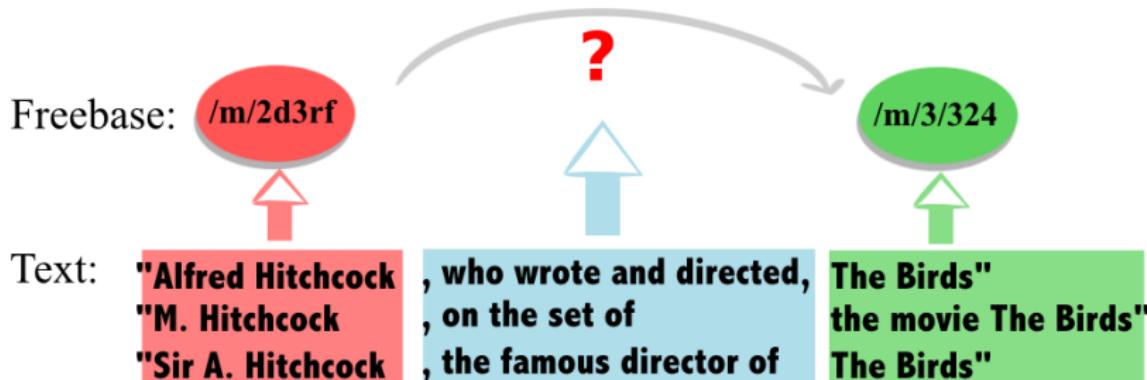
Text: **"Alfred Hitchcock"**, who wrote and directed,  
**"M. Hitchcock"**, on the set of  
**"Sir A. Hitchcock"**, the famous director of



**"The Birds"**  
**the movie The Birds"**  
**The Birds"**

# Relation Extraction

**Goal:** identify if there is a relation between them to add to the KB.



# Relation Extraction

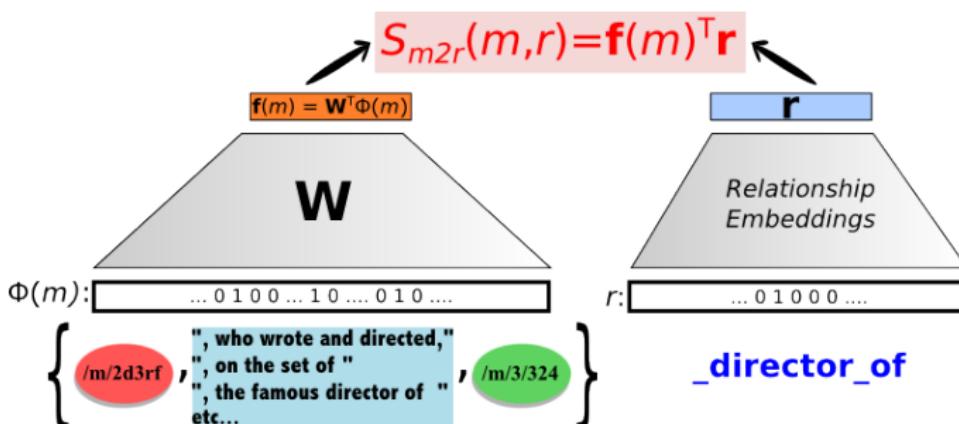
And from which type, to enrich an existing KB.



# Embeddings of Text and Freebase (Weston et al., '13)

- **Standard Method:** an embedding-based classifier is trained to predict the relation type, given text mentions  $\mathcal{M}$  and  $(sub, obj)$ :

$$r(m, sub, obj) = \arg \max_{rel'} \sum_{m \in \mathcal{M}} S_{m2r}(m, rel')$$



Classifier based on WSABIE (Weston et al., '11).

# Embeddings of Text and Freebase (Weston et al., '13)

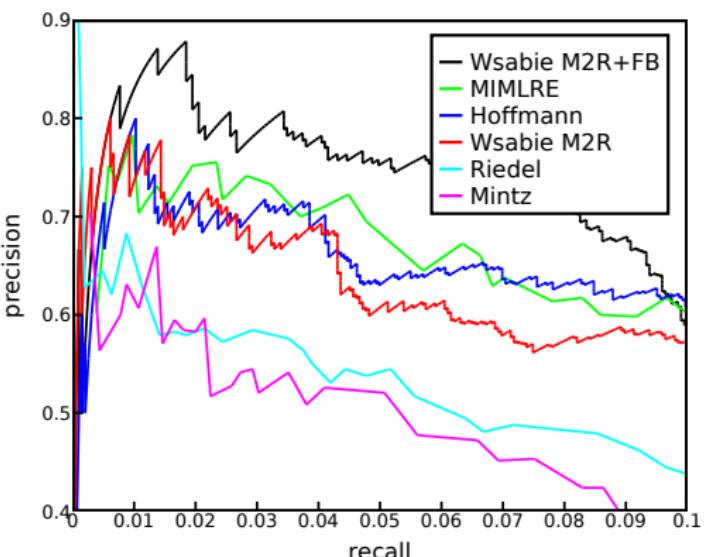
- **Idea:** improve extraction by using both text + available knowledge (= current KB).
- A model of the KB is used in a re-ranking setting to force extracted relations to agree with it:

$$r'(m, sub, obj) = \arg \max_{rel'} \left( \sum_{m \in \mathcal{M}} S_{m2r}(m, rel') - d_{KB}(sub, rel', obj) \right)$$

with  $d_{KB}(sub, rel', obj) = \|\mathbf{s} + \mathbf{r}' - \mathbf{o}\|_2^2$  (trained separately)

# Benchmarking on NYT+Freebase

Exp. on NY Times papers linked with Freebase (Riedel et al., '10)

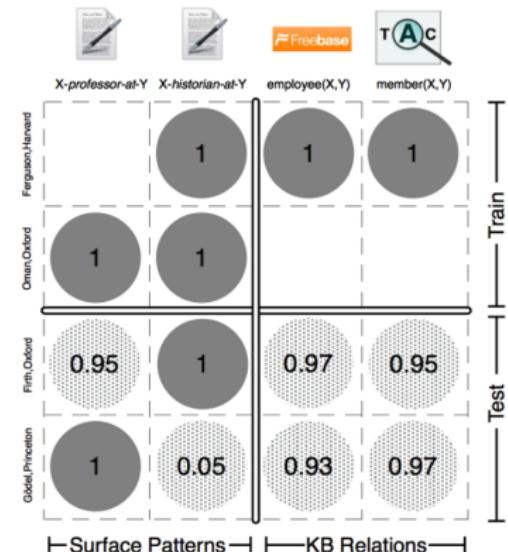


Precision/recall curve for predicting relations

Results extracted from (Weston et al., '13)

# Universal Schemas (Riedel et al., '13)

- Join in a single learning problem:
  - relation extraction
  - link prediction
- The same model score triples:
  - made of text mentions
  - from a KB



# Universal Schemas (Riedel et al., '13)

- Relation prediction using the score:

$$r'(m, sub, obj) = \arg \max_{rel'} \left( \sum_{m \in \mathcal{M}} S_{m2r}(m, rel') + S_{KB}(sub, rel', obj) + S_{neighbors}(sub, rel', obj) \right)$$

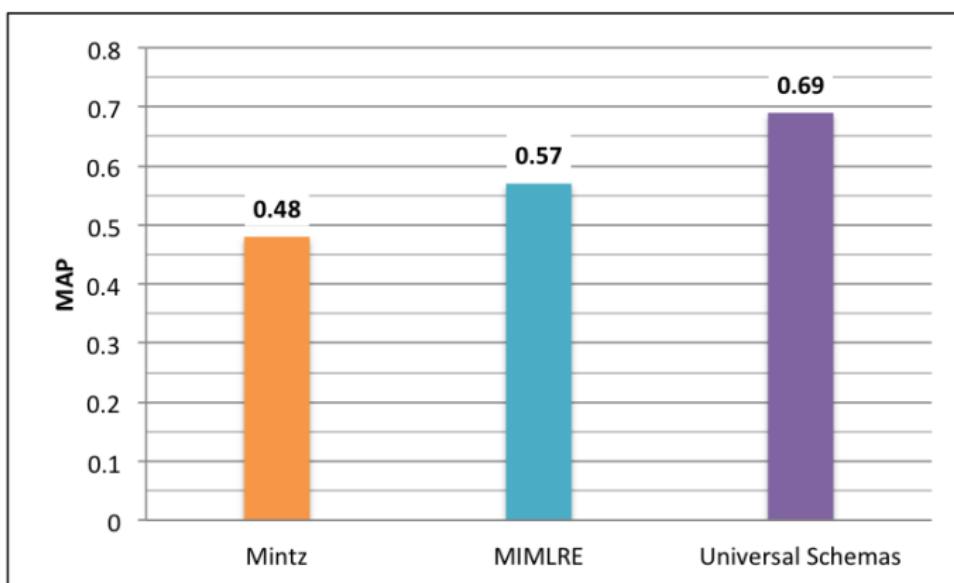
- All scores are defined using **embeddings**:

- $S_{m2r}(m, rel') = \mathbf{f}(m)^\top \mathbf{r}'$
- $S_{kb}(sub, rel', obj) = \mathbf{s}^\top \mathbf{r}'_s + \mathbf{o}^\top \mathbf{r}'_o$
- $S_{neighbors}(sub, rel', obj) = \sum_{\substack{(sub, rel'', obj) \\ rel'' \neq rel'}} w_{rel''}^{rel'}$

- Training by **ranking observed facts versus other** and updating using SGD.

# Benchmarking on NYT+Freebase

Exp. on NY Times papers linked with Freebase (Riedel et al., '10)



Mean Averaged Precision for predicting relations

Results extracted from (Riedel et al., '13)

# Menu – Part 2

## 1 Embeddings for multi-relational data

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- Embeddings for information extraction
- Question Answering

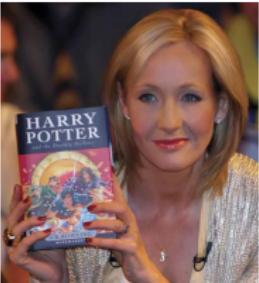
## 2 Pros and cons of embedding models

## 3 Future of embedding models

## 4 Resources

# Link Prediction as Q&A

"Who influenced J.K. Rowling?"

J. K. Rowling	_influenced_by	G. K. Chesterton
		J. R. R. Tolkien
		C. S. Lewis
		Lloyd Alexander
		Terry Pratchett
		Roald Dahl
		Jorge Luis Borges

Can we go beyond such rigid structure?

# Open-domain Question Answering

- **Open-domain Q&A:** answer question on any topic  
→ query a KB with natural language

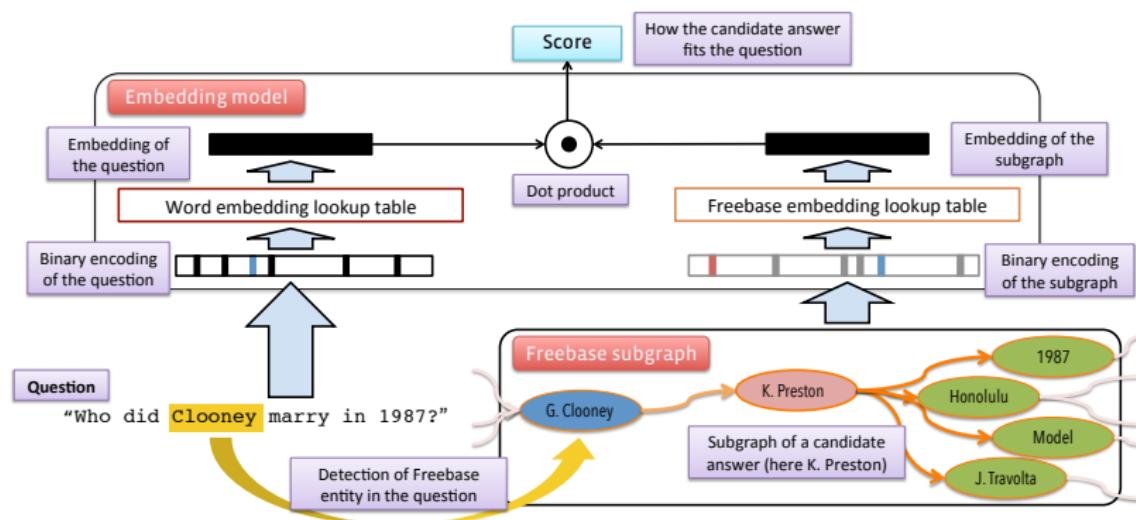
## Examples

“What is <code>cher</code> 's son's name ?”	<code>elijah_blue_allman</code>
“What are <code>dollars</code> called in <code>spain</code> ?”	<code>peseta</code>
“What is <code>henry_clay</code> known for ?”	<code>lawyer</code>
“Who did <code>georges_clooney</code> marry in <code>1987</code> ?”	<code>kelly_preston</code>

- Recent effort with **semantic parsing** (Kwiatkowski et al. '13) (Berant et al. '13, '14) (Fader et al., '13, '14) (Reddy et al., '14)
- Models with **embeddings** as well (Bordes et al., '14)

# Subgraph Embeddings (Bordes et al., '14)

- Model learns **embeddings of questions** and (candidate) answers
- Answers are represented by entity and its neighboring subgraph



# Training data

- Freebase is automatically converted into Q&A pairs
- Closer to expected language structure than triples

## Examples of Freebase data

(sikkim, location.in\_state.judicial\_capital, gangtok)  
what is the judicial capital of the in state sikkim ? – gangtok

(brighouse, location.location.people\_born\_here, edward\_barber)  
who is born in the location brighouse ? – edward\_barber

(sepsis, medicine.disease.symptoms, skin\_discoloration)  
what are the symptoms of the disease sepsis ? – skin\_discoloration

# Training data

- All Freebase questions have rigid and similar structures
- Supplemented by pairs from clusters of paraphrase questions
- Multitask training: similar questions  $\leftrightarrow$  similar embeddings

## Examples of paraphrase clusters

what are two reason to get a 404 ?

what is error 404 ?

how do you correct error 404 ?

what is the term for a teacher of islamic law ?

what is the name of the religious book islam use ?

who is chief of islamic religious authority ?

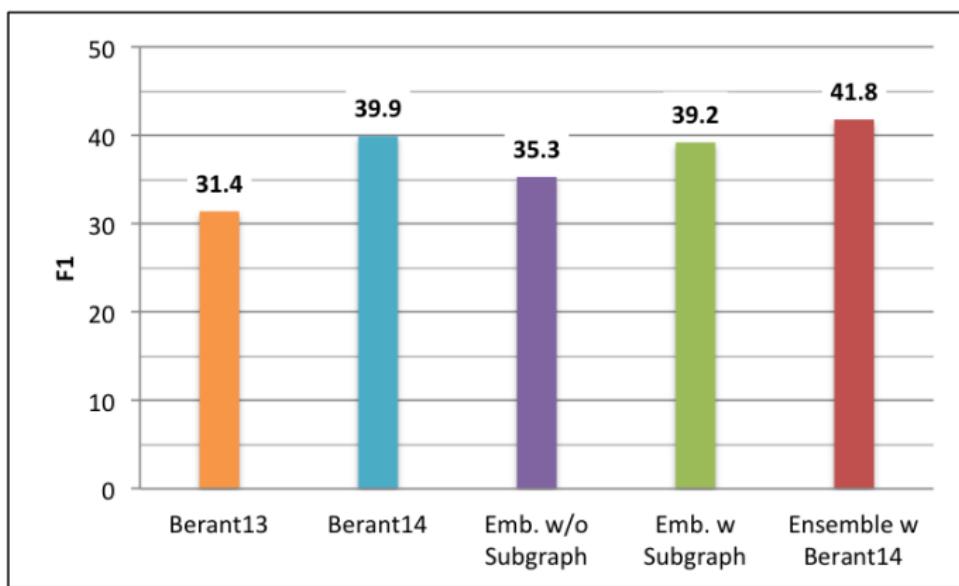
what country is bueno aire in ?

what countrie is buenos aires in ?

what country is bueno are in ?

# Benchmarking on WebQuestions

Experiments on WebQuestions (Berant et al., '13)



F1-score for answering test questions

Results extracted from (Berant et al., '14) and (Bordes et al., '14)

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## 2 Pros and cons of embedding models

## 3 Future of embedding models

## 4 Resources

# Advantages

- Efficient features for many tasks in practice
- Training with SGD scales & parallelizable (Niu et al., '11)
- Flexible to various tasks: multi-task learning of embeddings
- Supervised or unsupervised training
- Allow to use extra-knowledge in other applications

# Issues

- Must train all embeddings together (no parallel 1-vs-rest)
- Low-dimensional vector → compression, blurring
- Sequential models suffer from long-term memory
- Embeddings need quite some updates to be good – not 1-shot
- Negative example sampling can be inefficient

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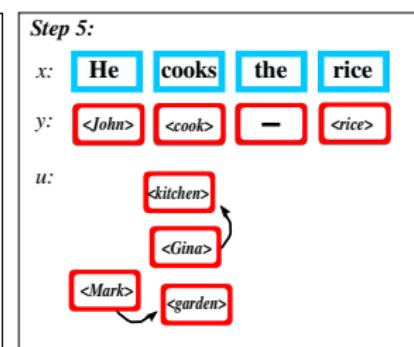
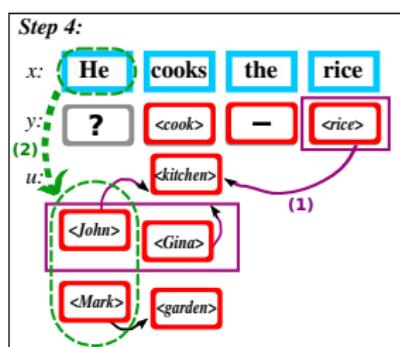
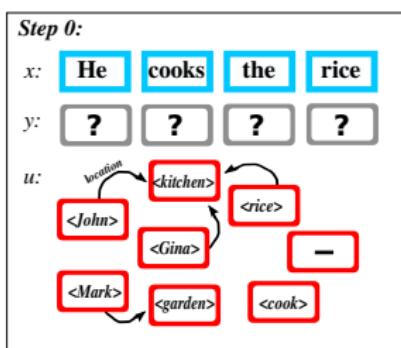
## 4 Resources

# Fix current limitations

- **Compression**: improve the memory capacity of embeddings and allows for one-shot learning of new symbols
- **Long-term memory**: encode longer dependencies in sequential models like RNNs
- **Training**: faster and better sampling of examples
- **Beyond linear**: most supervised labeling problems are well tackled by simple linear models. Non-linearity should help more.

# Explore new directions

- Compositionality (Baroni et al. '10) (Grefenstette, 13)
- Multimodality (Bruni et al., 12) (Kiros et al., '14)
- Grounding language into actions (Bordes et al., 10)



# At EMNLP

Modeling Interestingness with Deep Neural Networks

Jianfeng Gao, Patrick Pantel, Michael Gamon, Xiaodong He and Li Deng

Translation Modeling with Bidirectional Recurrent Neural Networks

Martin Sundermeyer, Tamer Alkhouri, Joern Wuebker and Hermann Ney

Learning Image Embeddings using Convolutional Neural Networks for Improved Multi-Modal Semantics

Douwe Kiela and Léon Bottou

Learning Abstract Concept Embeddings from Multi-Modal Data: Since You Probably Can't See What I Mean

Felix Hill and Anna Korhonen

Incorporating Vector Space Similarity in Random Walk Inference over Knowledge Bases

Matt Gardner, Partha Talukdar, Jayant Krishnamurthy and Tom Mitchell

Composition of Word Representations Improves Semantic Role Labelling

Michael Roth and Kristian Woodsen

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[A Neural Network for Factoid Question Answering over Paragraphs](#)

Mohit Iyyer, Jordan Boyd-Graber, Leonardo Claudino, Richard Socher and Hal Daumé III

[Joint Relational Embeddings for Knowledge-based Question Answering](#)

Min-Chul Yang, Nan Duan, Ming Zhou and Hae-Chang Rim

[Evaluating Neural Word Representations in Tensor-Based Compositional Settings](#)

Dmitrijs Milajevs, Dimitri Kartsaklis, Mehrnoosh Sadrzadeh and Matthew Purver

[Opinion Mining with Deep Recurrent Neural Networks](#)

Ozan Irsoy and Claire Cardie

[The Inside-Outside Recursive Neural Network model for Dependency Parsing](#)

Phong Le and Willem Zuidema

[A Fast and Accurate Dependency Parser using Neural Networks](#)

Danqi Chen and Christopher Manning

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[Reducing Dimensions of Tensors in Type-Driven Distributional Semantics](#)

Tamara Polajnar, Luana Fagarasan and Stephen Clark

[Word Semantic Representations using Bayesian Probabilistic Tensor Factorization](#)

Jingwei Zhang, Jeremy Salwen, Michael Glass and Alfio Gliozzo

[Glove: Global Vectors for Word Representation](#)

Jeffrey Pennington, Richard Socher and Christopher Manning

[Jointly Learning Word Representations and Composition Functions Using Predicate-Argument Structures](#)

Kazuma Hashimoto, Pontus Stenetorp, Makoto Miwa and Yoshimasa Tsuruoka

[Typed Tensor Decomposition of Knowledge Bases for Relation Extraction](#)

Kai-Wei Chang, Wen-tau Yih, Bishan Yang and Christopher Meek

[Knowledge Graph and Text Jointly Embedding](#)

Zhen Wang, Jianwen Zhang, Jianlin Feng and Zheng Chen

# At EMNLP

[Question Answering with Subgraph Embeddings](#)

Antoine Bordes, Sumit Chopra and Jason Weston

[Word Translation Prediction for Morphologically Rich Languages with Bilingual Neural Networks](#)

Ke M. Tran, Arianna Bisazza and Christof Monz

[Learning Phrase Representations using RNN Encoder–Decoder for Statistical Machine Translation](#)

Kyunghyun Cho, Bart van Merriënboer, Caglar Gulcehre, Dzmitry Bahdanau, Fethi Bougares, Holger Schwenk and Yoshua Bengio

[Convolutional Neural Networks for Sentence Classification](#)

Yoon Kim

[#TagSpace: Semantic Embeddings from Hashtags](#)

Jason Weston, Sumit Chopra and Keith Adams

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# Code

- Torch: [www.torch.ch](http://www.torch.ch)
- SENNA: [ronan.collobert.com/senna](http://ronan.collobert.com/senna)
- RNNLM: [www.fit.vutbr.cz/~imikolov/rnnlm](http://www.fit.vutbr.cz/~imikolov/rnnlm)
- Word2vec: [code.google.com/p/word2vec](http://code.google.com/p/word2vec)
- Recursive NN: [nlp.stanford.edu/sentiment](http://nlp.stanford.edu/sentiment)
- SME (multi-relational data): [github.com/glorotxa/sme](https://github.com/glorotxa/sme)

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