

# Invariant Rooting Algorithm

April 25, 2015

## Score Computation :

The invariant penalty score computation involves only inequalities.

## 1 Analysis of output

We have analyzed the 10-taxon dataset and also the Avian dataset. First, we will discuss the results on the 10-taxon followed by the Avian dataset.

### 1.1 10-taxon dataset

We have analyzed 3 replicates on the dataset from higher to lower ILS. For each of the 3 replicates of the four model conditions we have performed two experiments :-

1. Fixed quintet - we have taken a fixed quintet  $[ '1', '3', '5', '7', '8' ]$  and have scored the edges which are induced in the subtree of the quintet.
2. Shortest Quintet - For each edge we have taken the shortest quintet (quintets topologically closer to the edge) such that edge is induced by the quintet.

### 1.2 Output Format of 5-taxon tree

It contains the taxons which are part of the quintet and the edges which are induced by the quintet (i.e. it also retains the nodes with out-degree 1).

1. For a leaf node, the node label is of the format  $v_1v_2$ , where  $v_1$  represents the taxon label and  $v_2$  denotes the score of the edge leading to that node.
2. For an internal node, the value represents the score of the edge leading to that node.

The **U** below each figure denotes the corresponding frequency of the gene tree topology.

Corresponding 5-taxon tree

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**Analysis:-**

```
***** Model Condition -model.10.540000.0.00000037/ Replicate -2/ *****
quintet ['1', '3', '5', '7', '8']
```

Analysis:-

```
***** Model Condition -model.10.5400000.0.000000037/ Replicate -3/ *****
quintet ['1', '3', '5', '7', '8']
```

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|

**Analysis:-**

```
***** Model Condition -model.10.1800000.0.000000111/ Replicate -1/ *****
quintet ['1', '3', '5', '7', '8']
```

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**Analysis:-**

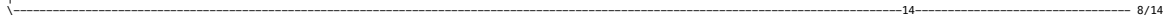
```
***** Model Condition -model.10.180000.0.00000111/ Replicate -2/ *****
quintet ['1', '3', '5', '7', '8']
```

[illegible]

**Analysis:-**

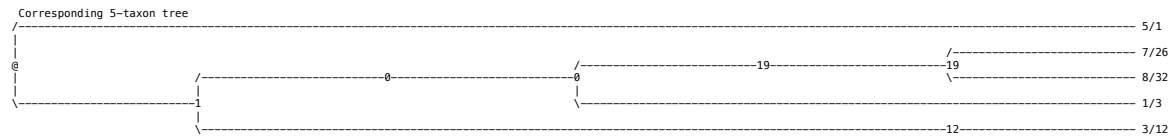
```
***** Model Condition -model.10.180000.0.000000111/ Replicate -3/ *****
```

Corresponding 5-taxon tree


$$U = [711,$$

2) # edges that have the best score - 3

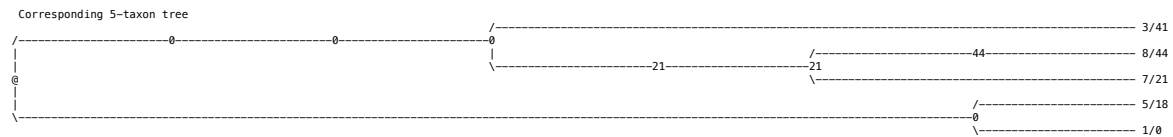
\*\*\*\*\* Model Condition -model.10.600000.0.00000333/ Replicate -1/ \*\*\*\*\*  
quintet ['1', '3', '5', '7', '8']



U = [362, 203, 202, 28, 24, 32, 10, 12, 28, 6, 10, 29, 38, 7, 9]

Analysis:-  
1) best score on the dataset - 0  
2) # edges that have the best score - 2

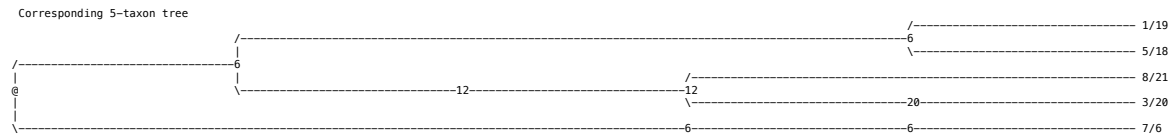
\*\*\*\*\* Model Condition -model.10.600000.0.00000333/ Replicate -2/ \*\*\*\*\*  
quintet ['1', '3', '5', '7', '8']



U = [470, 70, 85, 129, 28, 31, 0, 4, 26, 5, 1, 32, 111, 3, 5]

Analysis:-  
1) best score on the dataset - 0  
2) # edges that have the best score - 5

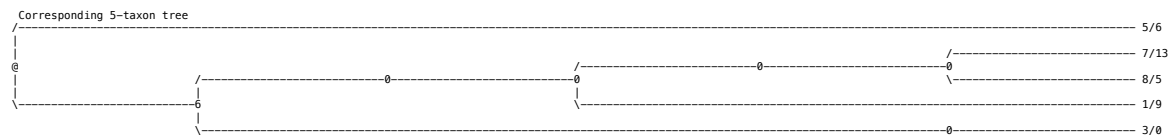
\*\*\*\*\* Model Condition -model.10.600000.0.00000333/ Replicate -3/ \*\*\*\*\*  
quintet ['1', '3', '5', '7', '8']



U = [94, 86, 145, 51, 47, 80, 51, 41, 71, 64, 39, 60, 54, 41, 76]

Analysis:-  
1) best score on the dataset - 6  
2) # edges that have the best score - 5

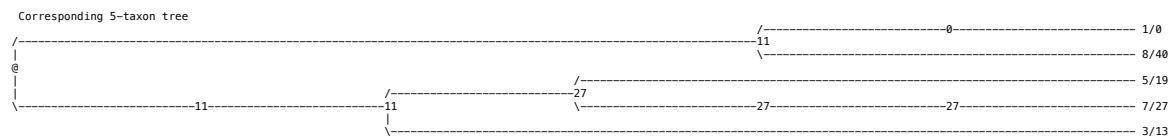
\*\*\*\*\* Model Condition -model.10.200000.0.00001000/ Replicate -1/ \*\*\*\*\*  
quintet ['1', '3', '5', '7', '8']



U = [182, 167, 161, 57, 43, 43, 30, 24, 43, 39, 48, 40, 48, 31, 44]

Analysis:-  
1) best score on the dataset - 0  
2) # edges that have the best score - 5

\*\*\*\*\* Model Condition -model.10.200000.0.00001000/ Replicate -2/ \*\*\*\*\*  
quintet ['1', '3', '5', '7', '8']

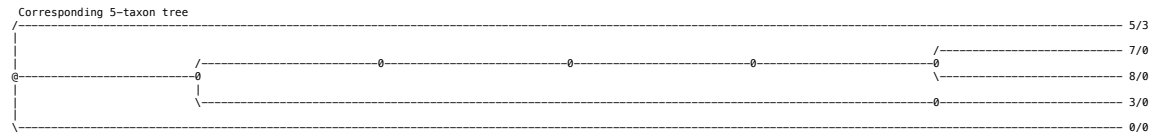


U = [152, 92, 91, 74, 85, 57, 41, 29, 72, 50, 37, 68, 67, 40, 45]

Analysis:-  
1) best score on the dataset - 0  
2) # edges that have the best score - 2

\*\*\*\*\* Quintet which includes the outgroup \*\*\*\*\*  
 Here we will be analyzing the above dataset with a different quintet which includes the outgroup

\*\*\*\*\* Model Condition -model.10.5400000.0.00000037/ Replicate -1/ \*\*\*\*\*  
 quintet ['0', '3', '5', '7', '8']

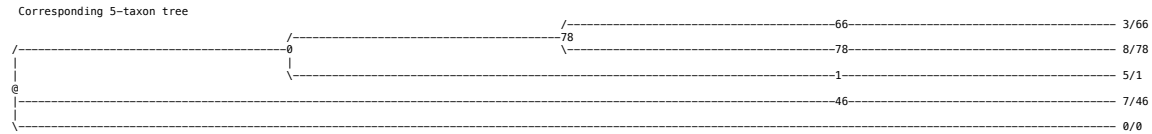


U = [499, 249, 252, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0]

Analysis:-

- 1) best score on the dataset - 0
- 2) # edges that have the best score - 10

\*\*\*\*\* Model Condition -model.10.5400000.0.00000037/ Replicate -2/ \*\*\*\*\*  
 quintet ['0', '3', '5', '7', '8']

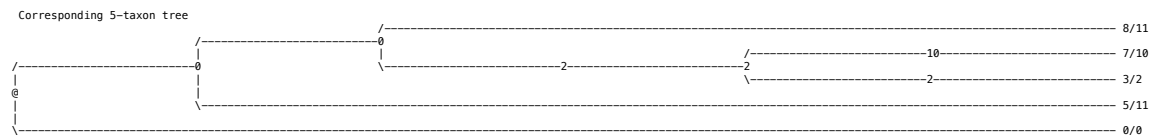


U = [149, 98, 127, 96, 63, 80, 22, 33, 93, 20, 22, 61, 95, 26, 15]

Analysis:-

- 1) best score on the dataset - 0
- 2) # edges that have the best score - 3

\*\*\*\*\* Model Condition -model.10.5400000.0.00000037/ Replicate -3/ \*\*\*\*\*  
 quintet ['0', '3', '5', '7', '8']

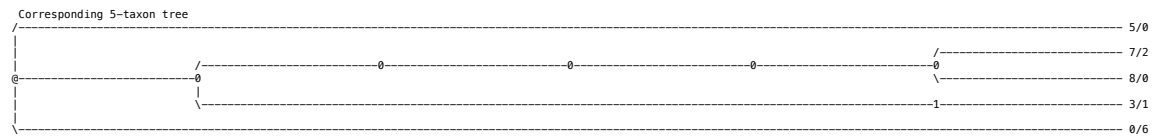


U = [799, 83, 92, 14, 0, 2, 0, 0, 2, 0, 0, 2, 6, 0, 0]

Analysis:-

- 1) best score on the dataset - 0
- 2) # edges that have the best score - 3

\*\*\*\*\* Model Condition -model.10.1800000.0.000000111/ Replicate -1/ \*\*\*\*\*  
 quintet ['0', '3', '5', '7', '8']

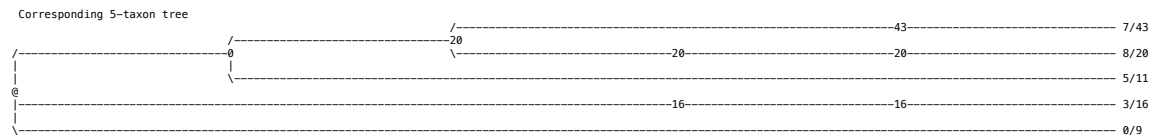


U = [399, 301, 295, 1, 1, 1, 1, 0, 0, 0, 1, 0, 0, 0, 0]

Analysis:-

- 1) best score on the dataset - 0
- 2) # edges that have the best score - 8

\*\*\*\*\* Model Condition -model.10.1800000.0.000000111/ Replicate -2/ \*\*\*\*\*  
 quintet ['0', '3', '5', '7', '8']

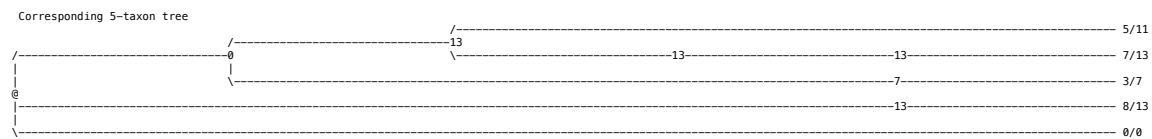


U = [534, 80, 71, 115, 16, 32, 0, 1, 20, 2, 0, 25, 104, 0, 0]

Analysis:-

- 1) best score on the dataset - 0
- 2) # edges that have the best score - 1

\*\*\*\*\* Model Condition -model.10.1800000.0.000000111/ Replicate -3/ \*\*\*\*\*  
 quintet ['0', '3', '5', '7', '8']

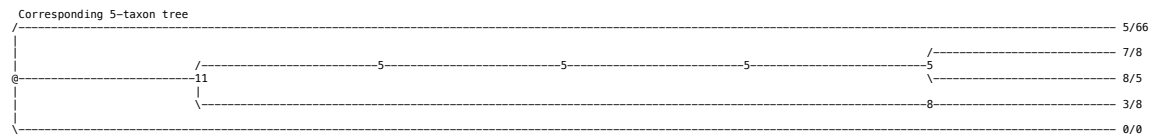


U = [592, 161, 172, 17, 6, 8, 2, 0, 14, 1, 0, 13, 13, 0, 1]

Analysis:-

- 1) best score on the dataset - 0
- 2) # edges that have the best score - 2

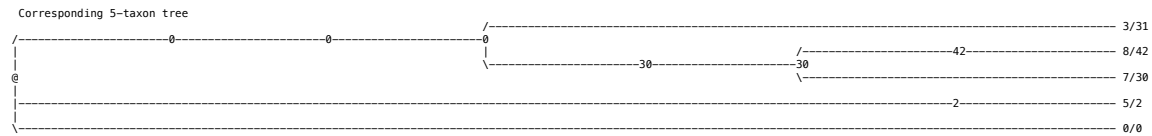
\*\*\*\*\* Model Condition -model.10.600000.0.000000333/ Replicate -1/ \*\*\*\*\*  
 quintet ['0', '3', '5', '7', '8']



U = [285, 244, 281, 19, 12, 30, 11, 11, 34, 10, 12, 15, 13, 10, 13]

Analysis:-  
 1)best score on the dataset - 0  
 2) # edges that have the best score - 1

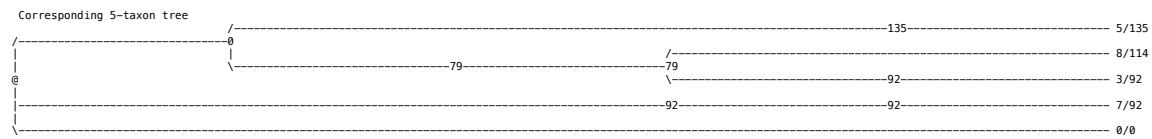
\*\*\*\*\* Model Condition -model.10.600000.0.000000333/ Replicate -2/ \*\*\*\*\*  
 quintet ['0', '3', '5', '7', '8']



U = [410, 107, 109, 99, 44, 44, 3, 3, 32, 7, 3, 36, 99, 2, 2]

Analysis:-  
 1)best score on the dataset - 0  
 2) # edges that have the best score - 4

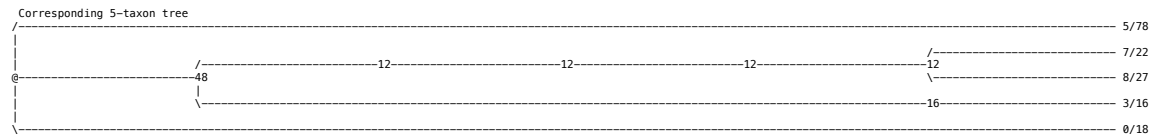
\*\*\*\*\* Model Condition -model.10.600000.0.000000333/ Replicate -3/ \*\*\*\*\*  
 quintet ['0', '3', '5', '7', '8']



U = [112, 93, 117, 82, 71, 108, 32, 28, 106, 19, 32, 69, 62, 37, 32]

Analysis:-  
 1)best score on the dataset - 0  
 2) # edges that have the best score - 2

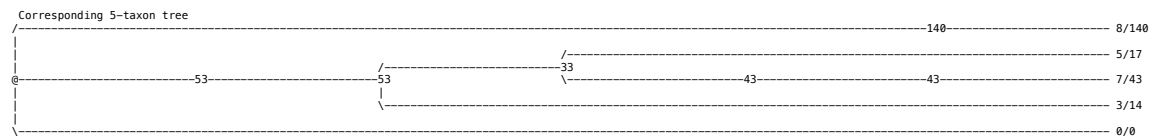
\*\*\*\*\* Model Condition -model.10.200000.0.000001000/ Replicate -1/ \*\*\*\*\*  
 quintet ['0', '3', '5', '7', '8']



U = [170, 179, 194, 29, 38, 53, 25, 35, 69, 38, 32, 35, 37, 32, 34]

Analysis:-  
 1)best score on the dataset - 12  
 2) # edges that have the best score - 4

\*\*\*\*\* Model Condition -model.10.200000.0.000001000/ Replicate -2/ \*\*\*\*\*  
 quintet ['0', '3', '5', '7', '8']



U = [123, 89, 132, 57, 57, 101, 40, 38, 76, 37, 32, 76, 64, 43, 35]

Analysis:-  
 1)best score on the dataset - 0