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Program Structures & Algorithms

Fall 2021

Assignment No. 3 (WQUPC)

◉ Tasks performed

- i. Implemented below methods in UF_HWQUPC.java
 - find(int p)
 - mergeComponents(int i, int j)
 - doPathCompression(int i)
- ii. Ran unit tests and verified successful execution for
 - UF_HWQUPC_Test.java
- iii. Developed UF (“union-find”) client to determine number of random pairs that are required to be generated to connect all the sites. Implemented a static count method to that takes number of sites as input and returns the number of random pairs required to be generated to connect all sites.
- iv. The main method initially took an integer input n (number of “sites”) from command line, however I modified the code further for benchmarking using doubling method to determine relation between in n and number of pairs.
- v. Ran the Java code – HWQUPC_Solution for various values of n (number of “sites”) and analyzed output.
- vi. Plotted a graph to understand the and analyze results.

Relationship Conclusion:

A standard plot graph i.e. n (number of sites) vs number of pairs generated was plotted based on the evidences, below are the observations and conclusions:

1. The graph is a **linearithmic** graph and hence the relation between **N and number of pairs is linear**.
2. Based on the benchmarking evidences, below is the approximate relation that I could derive

N	No of pairs
16	34
32	62.4
64	158.5
128	354.8
256	830
512	1708.2
1024	3937.6
2048	8958.4
4096	19688.7
8192	38417.1
16384	83712.8
32768	190141
65536	378940.8
131072	815444.6
262144	1728704.3

From the graph and above observations, it is evident that as N doubles, the number of pairs also doubles. So, it is a direct proportion.

Considering above highlighted values to derivation

$$N = 65536 = 2^{16}$$

$$\text{Number of pairs} = 378940.8$$

$$\log_2 378940 = 18.5 \approx N + 2$$

$$N = 131072 = 2^{17}$$

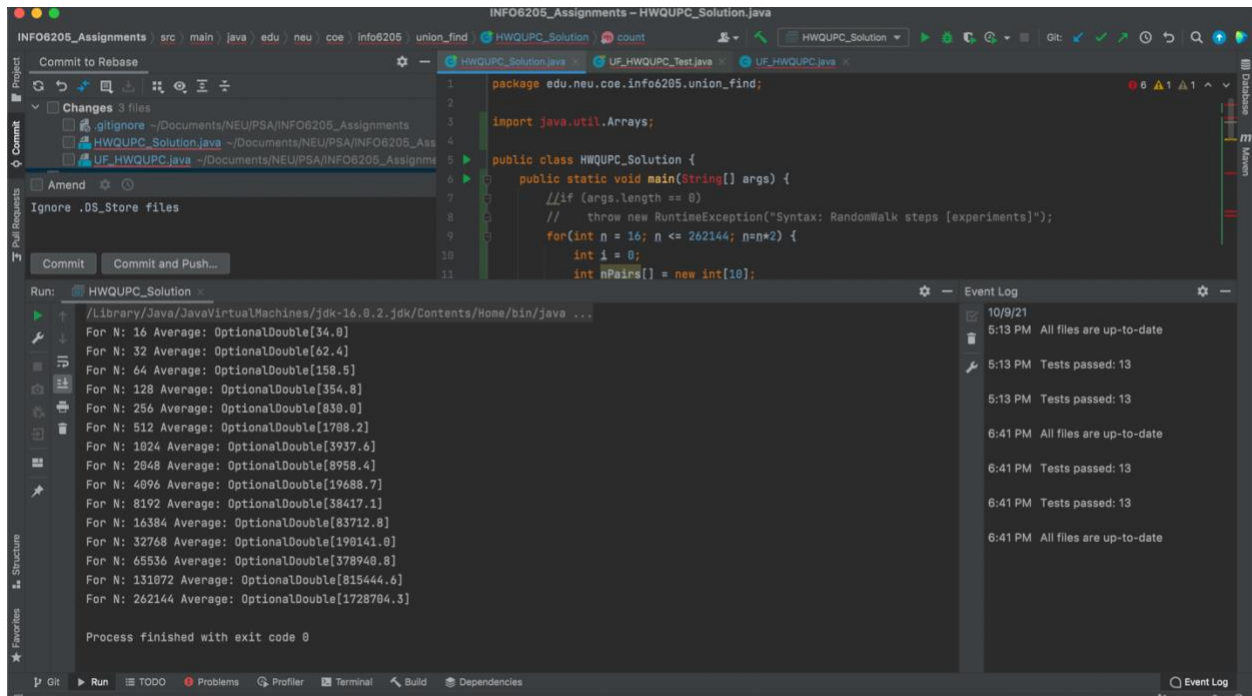
$$\text{Number of pairs} = 815444.6$$

$$\log_2 815444.6 = 19.6 \approx N + 2$$

From above I can conclude logarithmic relation is definitely there however with some other factor. With some trial and errors and comparing with graphs of $k \cdot N \log(N)$, I could come to the conclusion that this is a linearithmic relation.

◉ Evidence to support the conclusion:

1. Output (Snapshot of Code output in the terminal)



The screenshot shows an IDE with a Java file named `HWQUPC_Solution.java`. The code defines a class `HWQUPC_Solution` with a `main` method that runs a loop for `n` from 16 to 262144 in increments of 16. For each `n`, it calculates an average and prints it. The terminal output shows the results of these calculations, with the average values increasing as `n` increases. The process finished with exit code 0.

```
package edu.neu.coe.info6205.union_find;

import java.util.Arrays;

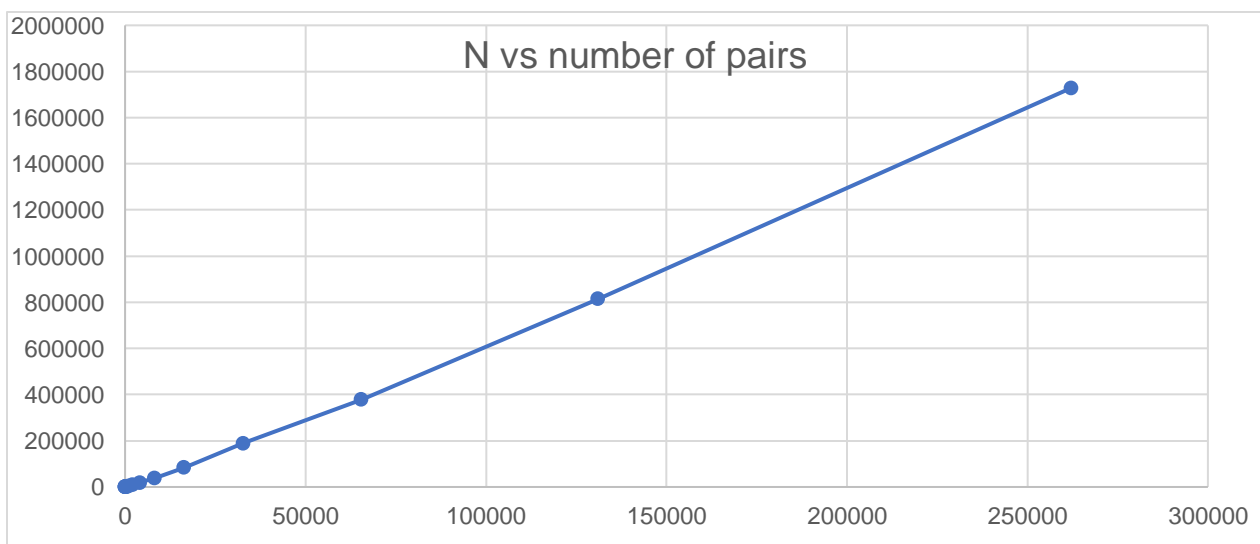
public class HWQUPC_Solution {
    public static void main(String[] args) {
        //if (args.length == 0)
        //    throw new RuntimeException("Syntax: RandomWalk steps [experiments]");
        for(int n = 16; n <= 262144; n+=16) {
            int i = 0;
            int nPairs[] = new int[10];
```

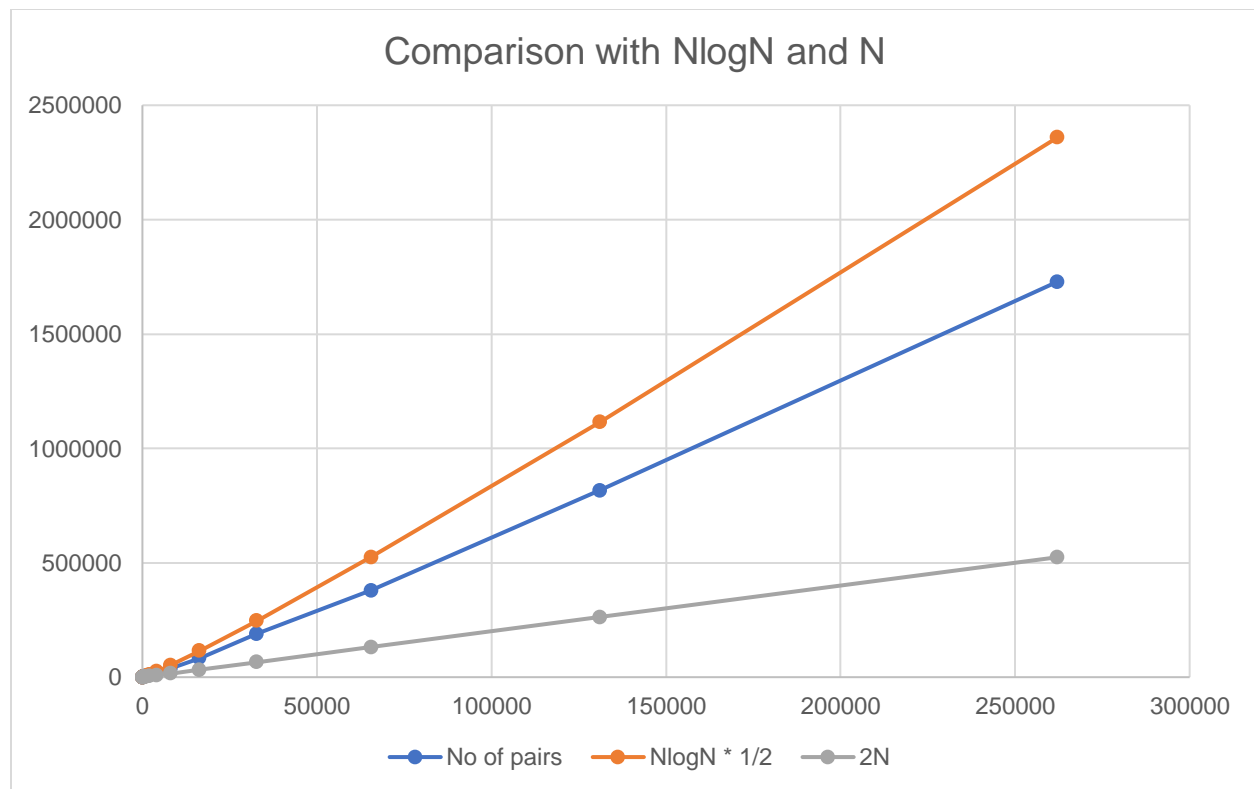
Run: HWQUPC_Solution -

```
/Library/Java/JavaVirtualMachines/jdk-16.0.2.jdk/Contents/Home/bin/java ...
For N: 16 Average: OptionalDouble[34.0]
For N: 32 Average: OptionalDouble[62.4]
For N: 64 Average: OptionalDouble[158.5]
For N: 128 Average: OptionalDouble[354.8]
For N: 256 Average: OptionalDouble[838.0]
For N: 512 Average: OptionalDouble[1788.2]
For N: 1024 Average: OptionalDouble[3937.6]
For N: 2048 Average: OptionalDouble[8958.4]
For N: 4096 Average: OptionalDouble[19688.7]
For N: 8192 Average: OptionalDouble[38417.1]
For N: 16384 Average: OptionalDouble[83712.8]
For N: 32768 Average: OptionalDouble[198141.0]
For N: 65536 Average: OptionalDouble[378948.8]
For N: 131072 Average: OptionalDouble[815444.6]
For N: 262144 Average: OptionalDouble[1728784.3]

Process finished with exit code 0
```

2. Graphical Representation(Observations from experiments should be tabulated and analyzed by plotting graphs(usually in excel) to arrive on the relationship conclusion)





◉ **Unit tests result:(Snapshot of successful unit test run)**

UF_HWQUPC_Test.java

