#### Predictive Hebbian Learning

### Computational Models of Neural Systems Lecture 5.2

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Based on slides by Mirella Lapata

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#### **Outline**

- Clasical conditioning in honeybees
  - identification of VUMmx1
  - properties of VUMmx1
- Bee foraging in uncertain environments
  - model of bee foraging
  - theory of predictive hebbian learning
- Dopamine neurons in the macaque monkey
  - activity of dopamine neurons
  - generalized theory of predictive hebbian learning
  - modeling predictions

#### Questions

- What are the cellular mechanisms responsible for classical conditioning?
- How is information about the unconditioned stimulus (US) represented at the neuronal level?
- What are the properties of neurons mediating the US?
  - Response to US
  - Convergence with the conditioned stimulus (CS) pathway
  - Reinforcement in conditioning
- How to identify such neurons?

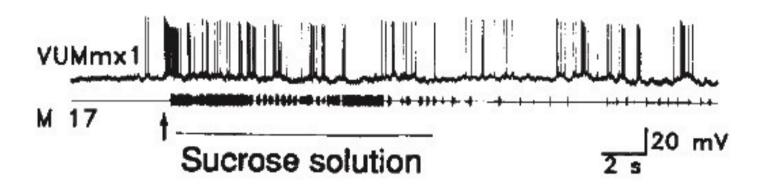
#### **Experiments on Honeybees**

- Bees fixed by waxing dorsal thorax to small metal table.
- Odors were presented in a gentle air stream.
- Sucrose solution applied briefly to antenna and proboscis.
- Proboscis extension was seen after a single pairing of the odor (CS) with sucrose (US).



#### Measuring Responses

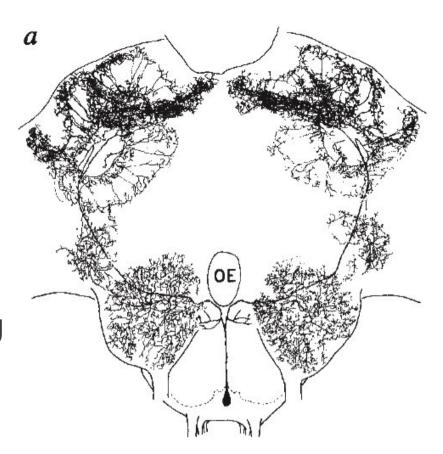
- Proboscis extension reflex (PER) was recorded as an electromyogram from the M17 muscle involved in the reflex.
- Neurons were tested for responsiveness to the US.

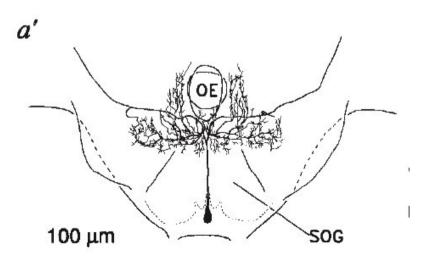


#### VUMmx1 Responds to US

- Unique morphology: arborizes in the suboesophageal ganglion (SOG) and projects widely in regions involved in odor (CS) processing
- Responds to sucrose with a long burst of action potentials which outlasts the sucrose US.
- Neurotransmitter is octopamine: related to dopamine.

OE = Oesophagus





#### Anatomy of the Bee Brain

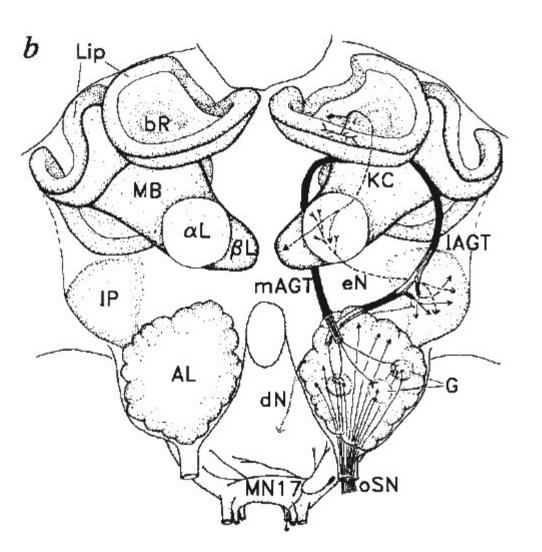
MB: Mushroom body

AL: Antenna lobe

KC: Kenyon cells

 oSN: Olfactory sensory neurons

 MN17: motor neuron involved in PER

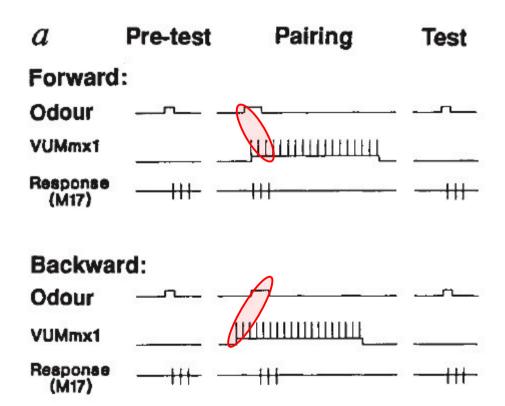


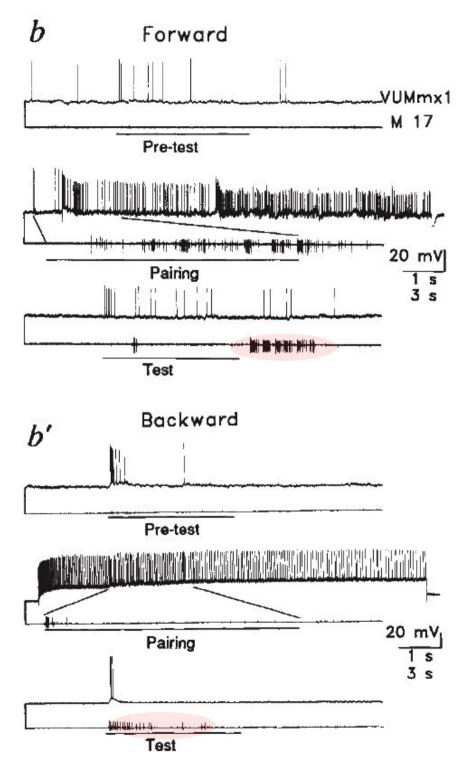
# Where is memory located in the honey bee brain? ant

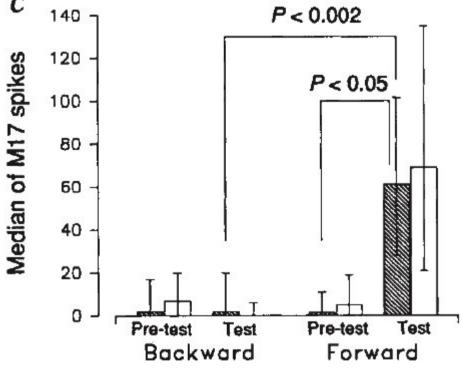
http://web.neurobio.arizona.edu/gronenberg/nrsc581

#### Stimulating VUMmx1 Simulates a US

- Introduce CS then inject depolarizing current into VUMmx1 in lieu of applying sucrose.
- Try both forward and backward conditioning paradigms.





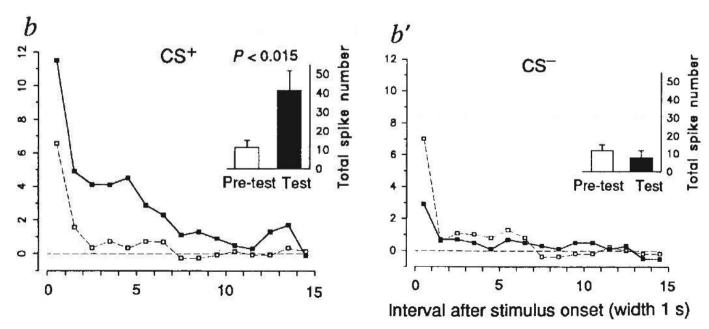


Open bars: sucrose US

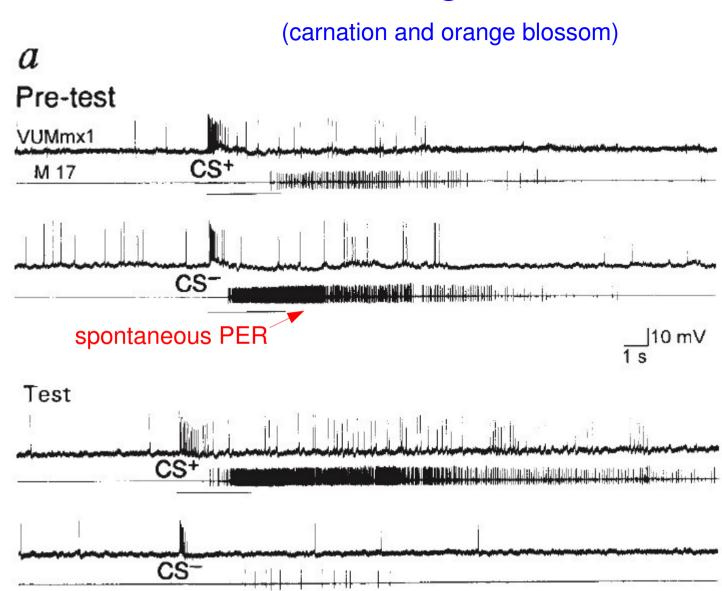
Shaded bars: VUMmx1 stimulation

#### Learning Effects of VUMmx1 Stimulation

- After learning, the odor alone stimulates VUMmx1 activity.
- Temporal contiguity effect: forward pairing causes a larger increase in spiking than backward pairing.
- Differential conditioning effect:
  - Differentially conditioned bees respond strongly to an odor (CS+) specifically paired with the US, and significantly less to an unpaired odor (CS-).



#### Differential Conditioning of Two Odors



#### **Discussion**

#### Main claims:

- VUMmx1 mediates the US in associative learning
- A learned CS also activates VUMmx1.
- Physiology is compatible with structures involved in complex forms of learning.

#### Questions:

- Is VUMmx1 the only neuron mediating the US?
  - Serial homologue of VUMmx1 has almost identical branching pattern.
  - Response to electrical stimulation is less than response to sucrose, so perhaps other neurons also contribute to the US signal.
- Can VUMmx1 mediate other conditioning phenomena, e.g., blocking, overshadowing, extinction?
- Do different stimuli induce similar responses?

#### Bee Foraging

#### Real's (1991) experiment:

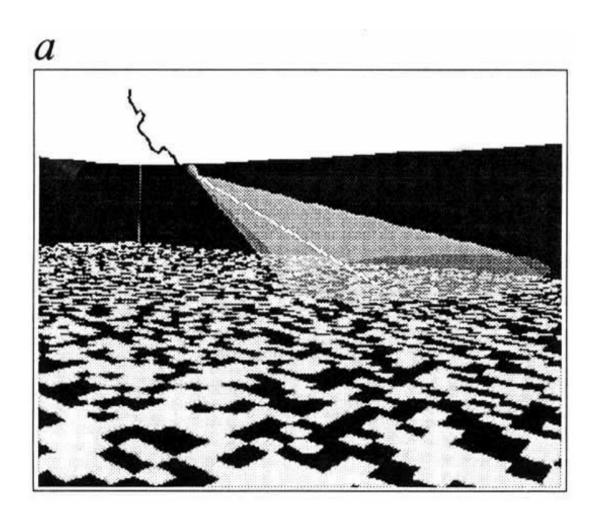
- Bumblebees foraged on artificial blue and yellow flowers.
- Blue flowers contained 2 μl of nectar.
- Yellow flowers contained 6  $\mu$ l in one third of the flowers and no nectar in the remaining two thirds.
- Blue and yellow flowers contained the same average amount of nectar.

#### Results:

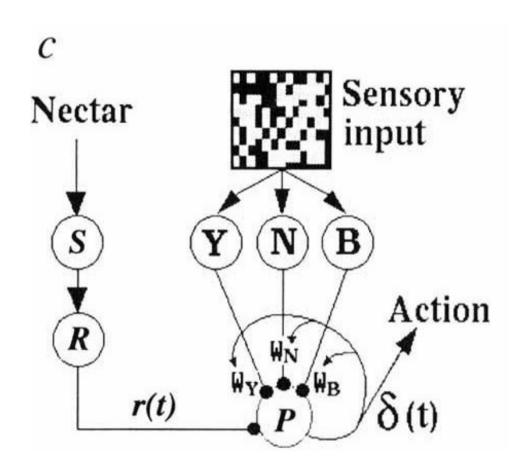
- Bees favored the constant blue over the variable yellow flowers even though the mean reward was the same.
- Bees forage equally from both flower types if the mean reward from yellow is made sufficiently large.

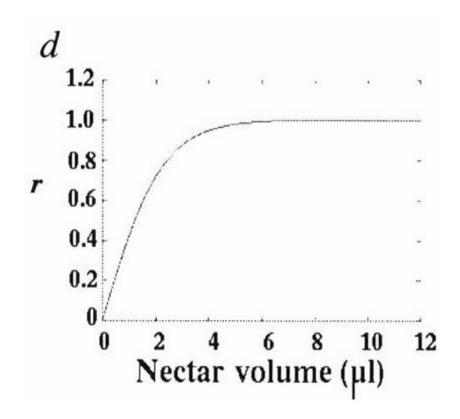
#### Montague, Dayan, and Sejnowski (1995)

- Model of bee foraging behavior based on VUMmx1.
- Bee decides at each time step whether to randomly reorient.



#### **Neural Network Model**





S: sucrose sensitive neuron; R: reward neuron;

P: reward predicting neuron;  $\delta$ : prediction error signal

#### **TD Equations**

$$\delta(t) = r(t) + \gamma V(t) - V(t-1)$$
  
Let  $\gamma = 1$ : no discounting

$$\delta(t) = r(t) + V(t) - V(t-1)$$
$$= r(t) + \dot{V}(t)$$

$$V(t) = \sum_{i} w_{i} x_{i}(t)$$

$$\dot{V}(t) = \sum_{i} w_{i} [x_{i}(t) - x_{i}(t-1)]$$

$$= \sum_{i} w_{i} \dot{x}_{i}(t)$$

$$\delta(t) = r(t) + \sum_{i} w_{i} \dot{x}_{i}(t)$$

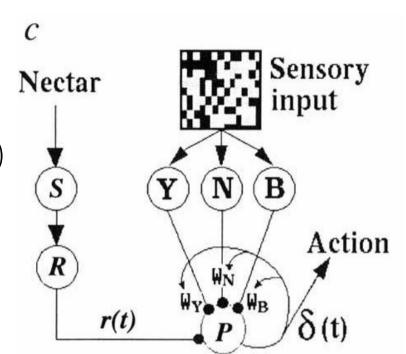
#### **Bee Foraging Model**

 $x_Y, x_B, x_N$  encode <u>change</u> in scene

$$\dot{V}(t) = w_b x_b(t) + w_y x_y(t) + w_n x_n(t)$$

$$\delta(t) = r(t) + \dot{V}(t)$$

$$\Delta w_i(t) = \lambda x_i(t-1) \cdot \delta(t)$$



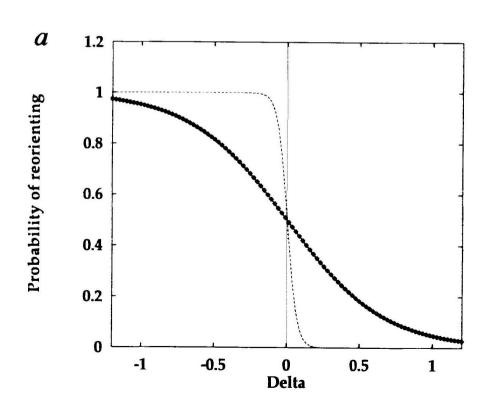
#### **Parameters**

 $w_B$  and  $w_Y$  are adaptable;  $w_N$  fixed at -0.5

Probability of reorienting:  $P_r(\delta(t)) = \frac{1}{1 + \exp(mx + b)}$ 

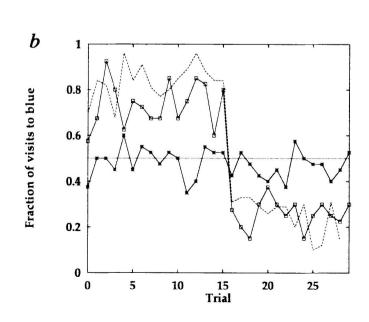
Learning rate  $\lambda = 0.9$ 

Volume of nectar reward determined by empirically derived utility curve.



#### Theoretical Idea

- Unit P is analogous to VUMmx1.
- Nectar r(t) represents the reward, which can vary over time.
- At each time t,  $\delta(t)$  determines the bee's next action: continue on present heading, or reorient.
- Weights are adjusted on encounters with flowers: they are updated according to the nectar reward.
- Model best matches the bee when  $\lambda = 0.9$ .
- Graph shows bee response to switch in contingencies on trial 15.



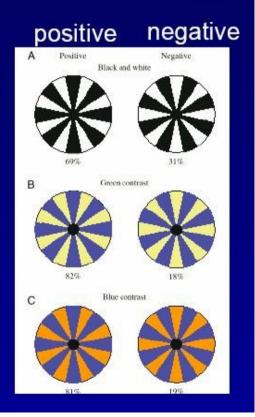
#### An Aside: Honeybee Operant Learning

## Honey bees can learn visual cues associated with nectar rewards

Colors

- Shapes

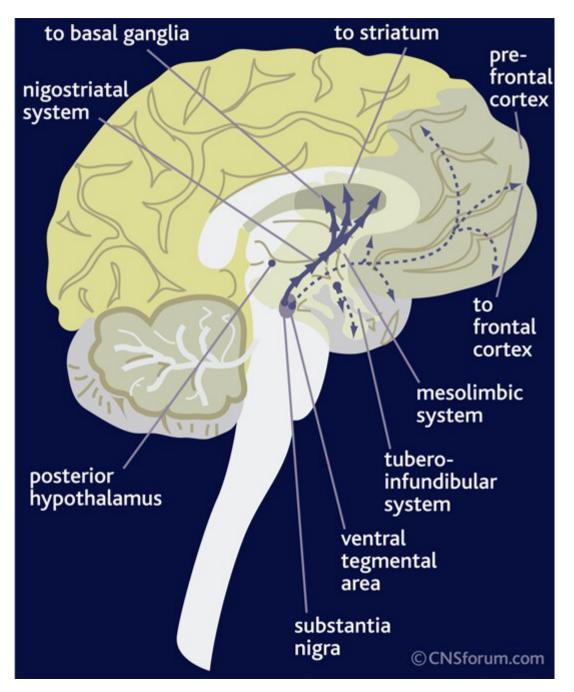
- Symmetry
- Complex patterns



http://web.neurobio.arizona.edu/gronenberg/nrsc581

#### Dopamine

- Involved in:
  - Addiction
  - Self-stimulation
  - Learning
  - Motor actions
  - Rewarding situations

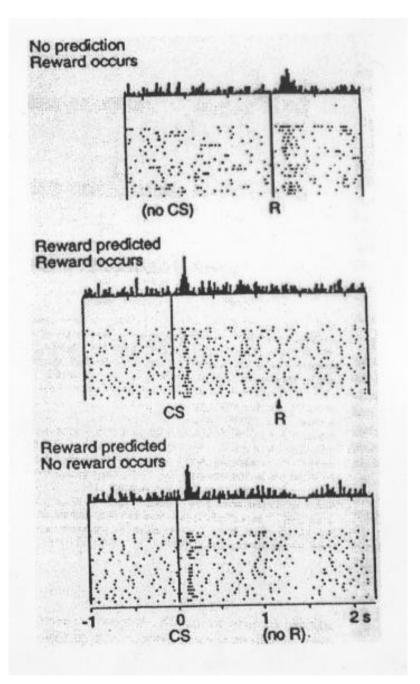


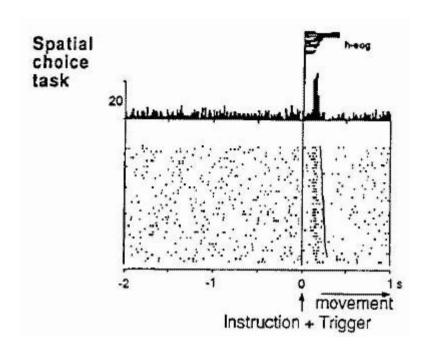
#### Responses of Dopamine Neurons in Macaques

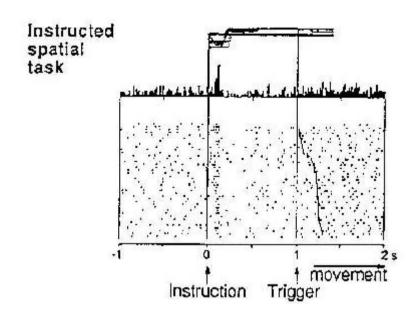
 Burst for unexpected reward

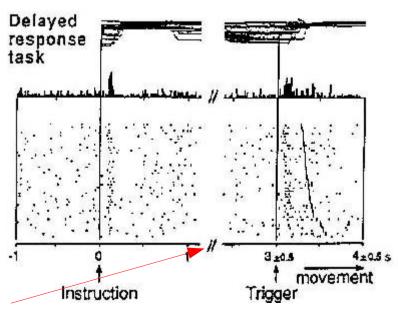
 Response transfers to reward predictors

Pause at time of missed reward



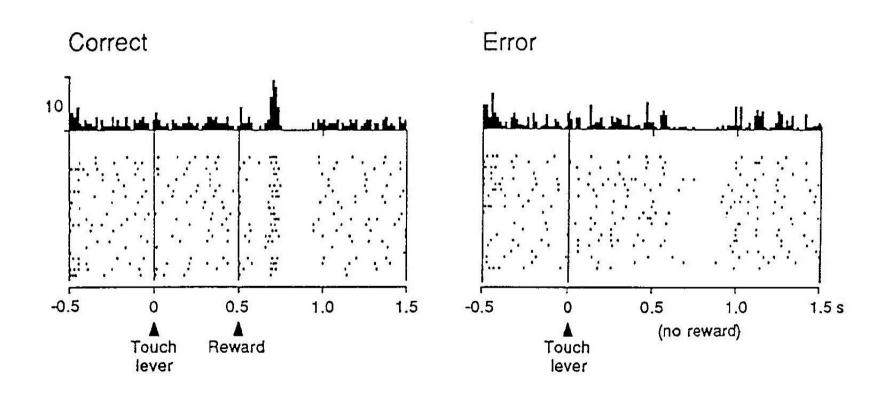




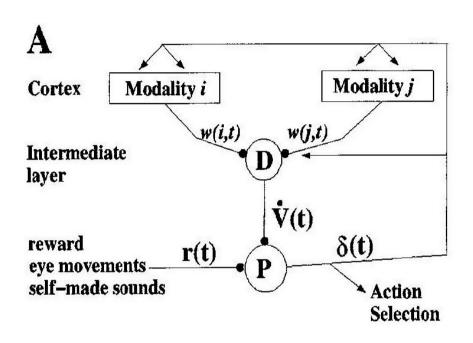


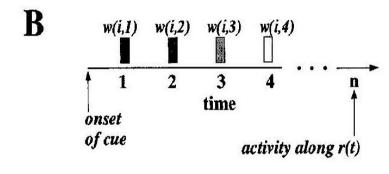
1.5 to 3.5 second delay

#### **Correct and Error Trials**

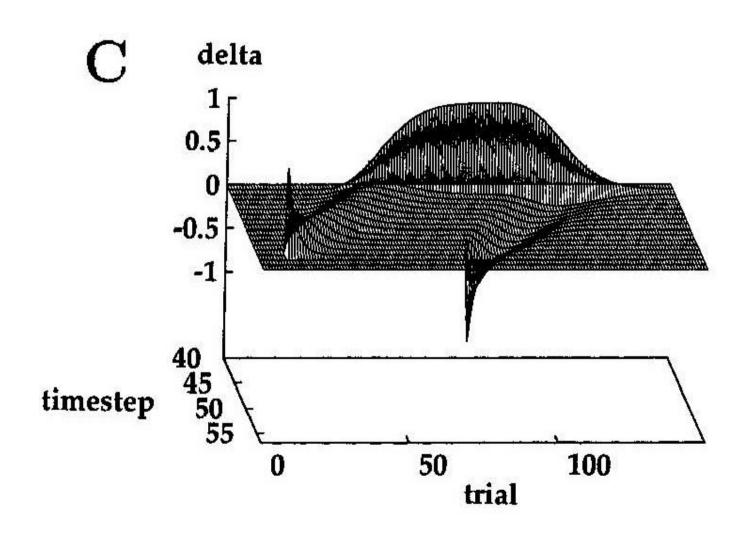


#### Predictive Hebbian Learning Model

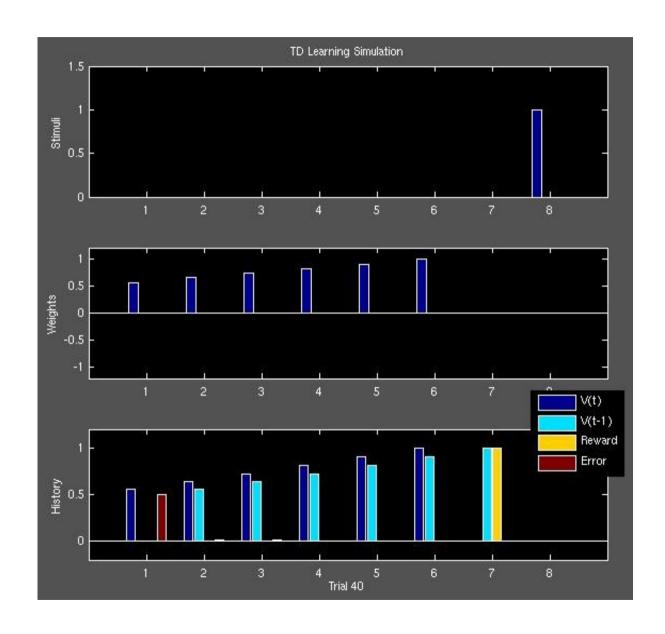




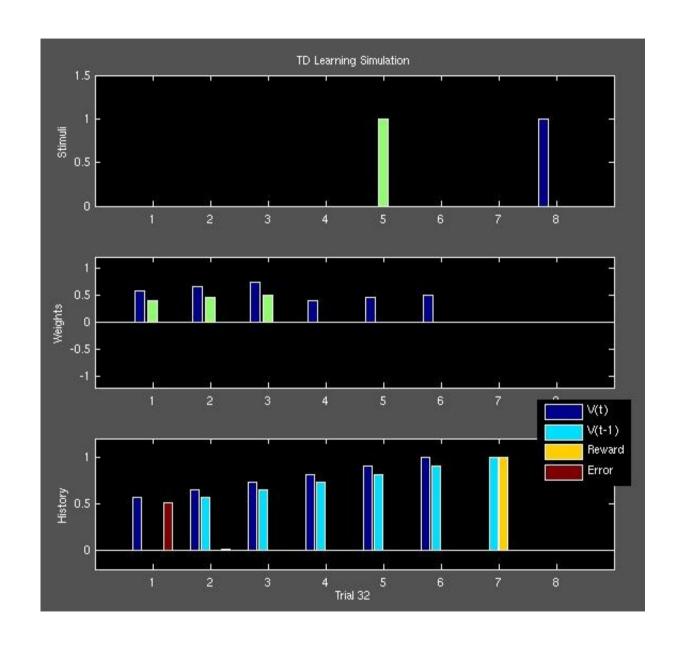
#### **Model Behavior**

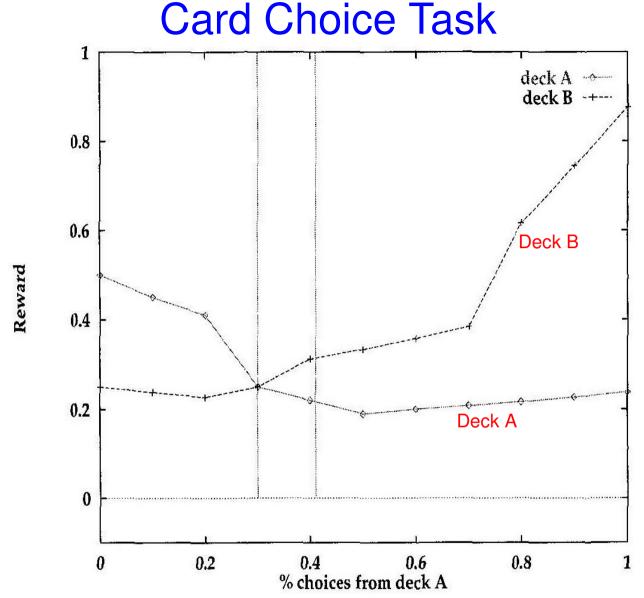


#### **TD Simulation 1**



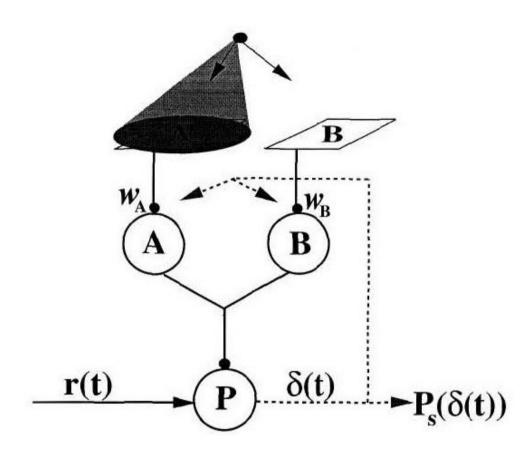
#### TD Simulation 2





Magnitude of reward is a function of the % choices from deck A in the last 40 draws. Optimal strategy lies to the right of the crossover point, but human subjects generally get stuck around the crossover point

#### **Card Choice Model**



"Attention" alternates between decks A and B. Change in predicted reward determines  $P_s$ , the probability of selecting the current deck. The model tends to get stuck at the crossover point, as humans do.

#### Conclusions

- Specific neurons distribute a signal that represents information about future expected reward (VUMmx1; dopamine neurons).
- These neurons have access to the precise time at which a reward will be delivered.
  - Serial compound stimulus makes this possible.
- Fluctuations in activity levels of these neurons represent errors in predictions about future reward.
- Montague et al. (1996) present a model of how such errors could be computed in a real brain.
- The theory makes predictions about human choice behaviors in simple decision-making tasks.